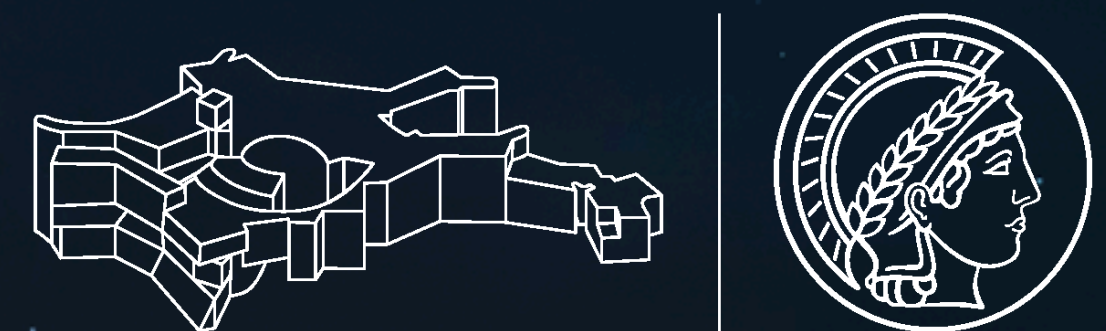


# Revealing systematics in strong lens substructure detection with CNNs

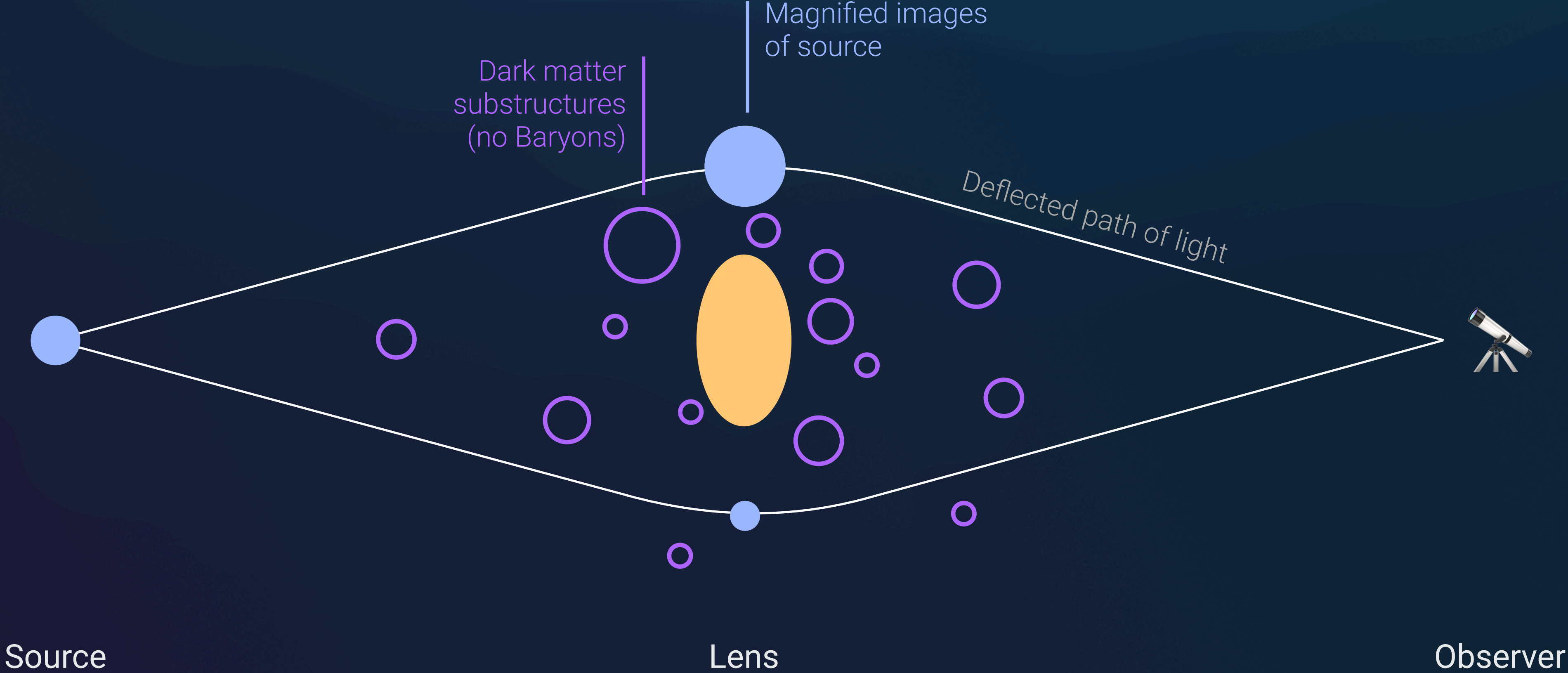
**Conor O’Riordan**, Simona Vegetti, SHARP collaboration  
*Dark Matter Group, MPA*

ML-IAP 2 | 30.11.23



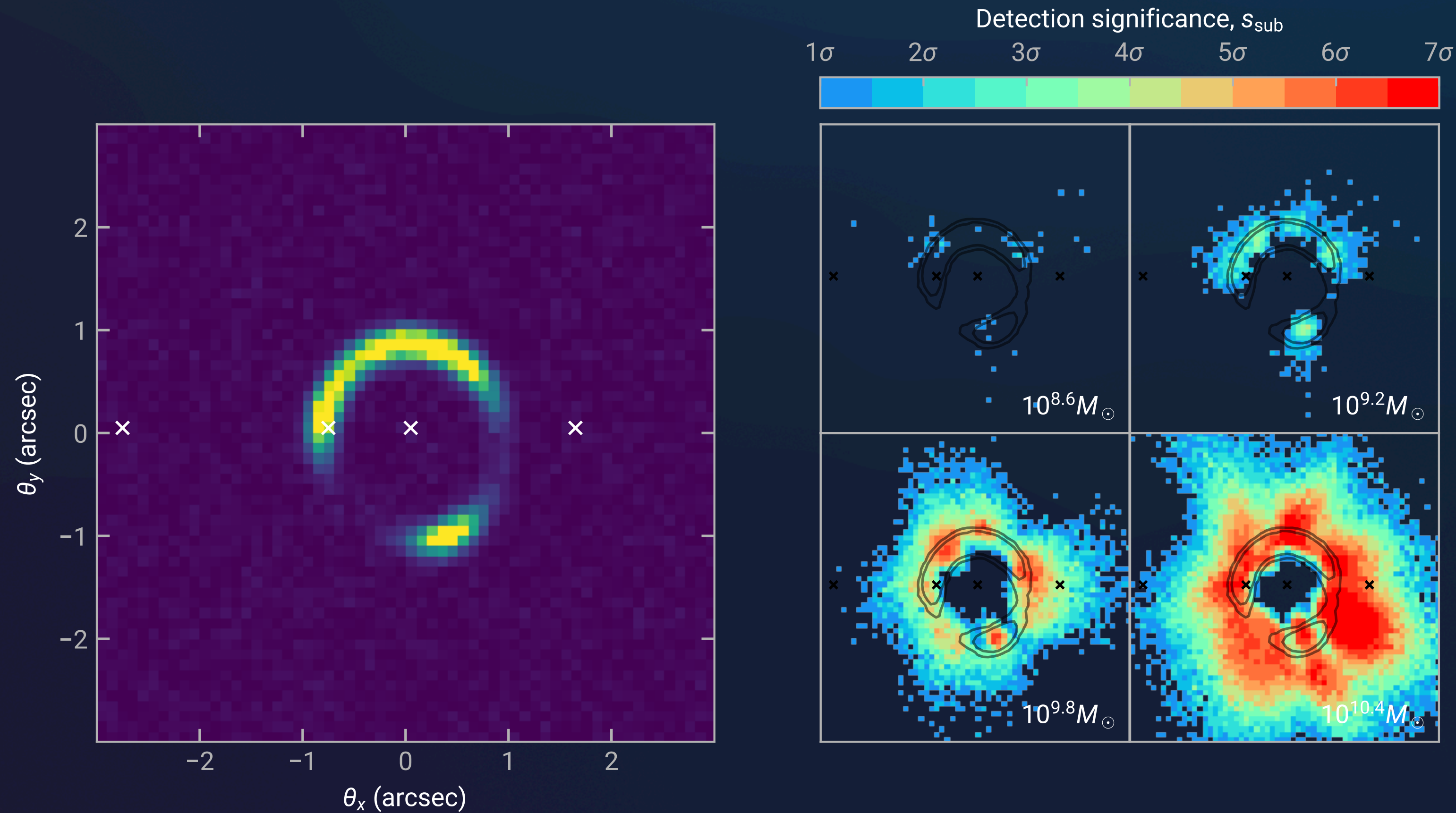
**MAX PLANCK INSTITUTE**  
FOR ASTROPHYSICS

Background:  
**Strong lensing**

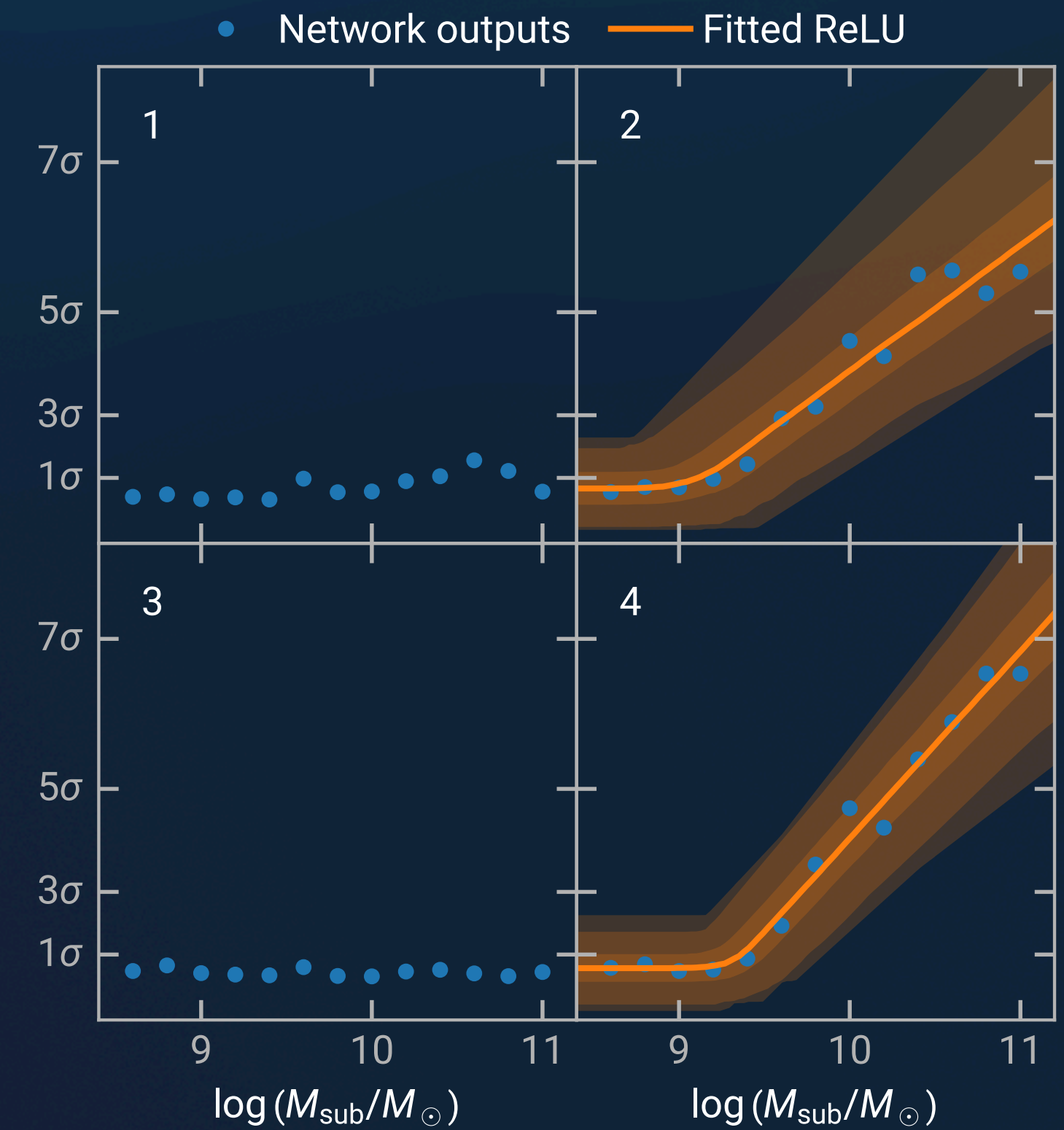


Background:

# Estimating sensitivity with ML



O’Riordan et al (2023)



Ray trace realisations  
of system

Get detection significance in  
every pixel and every mass

Find mass at significance  
threshold by fitting

Method:

# Training data

Galaxy isophotes and simulations show that <1% perturbations are very common.

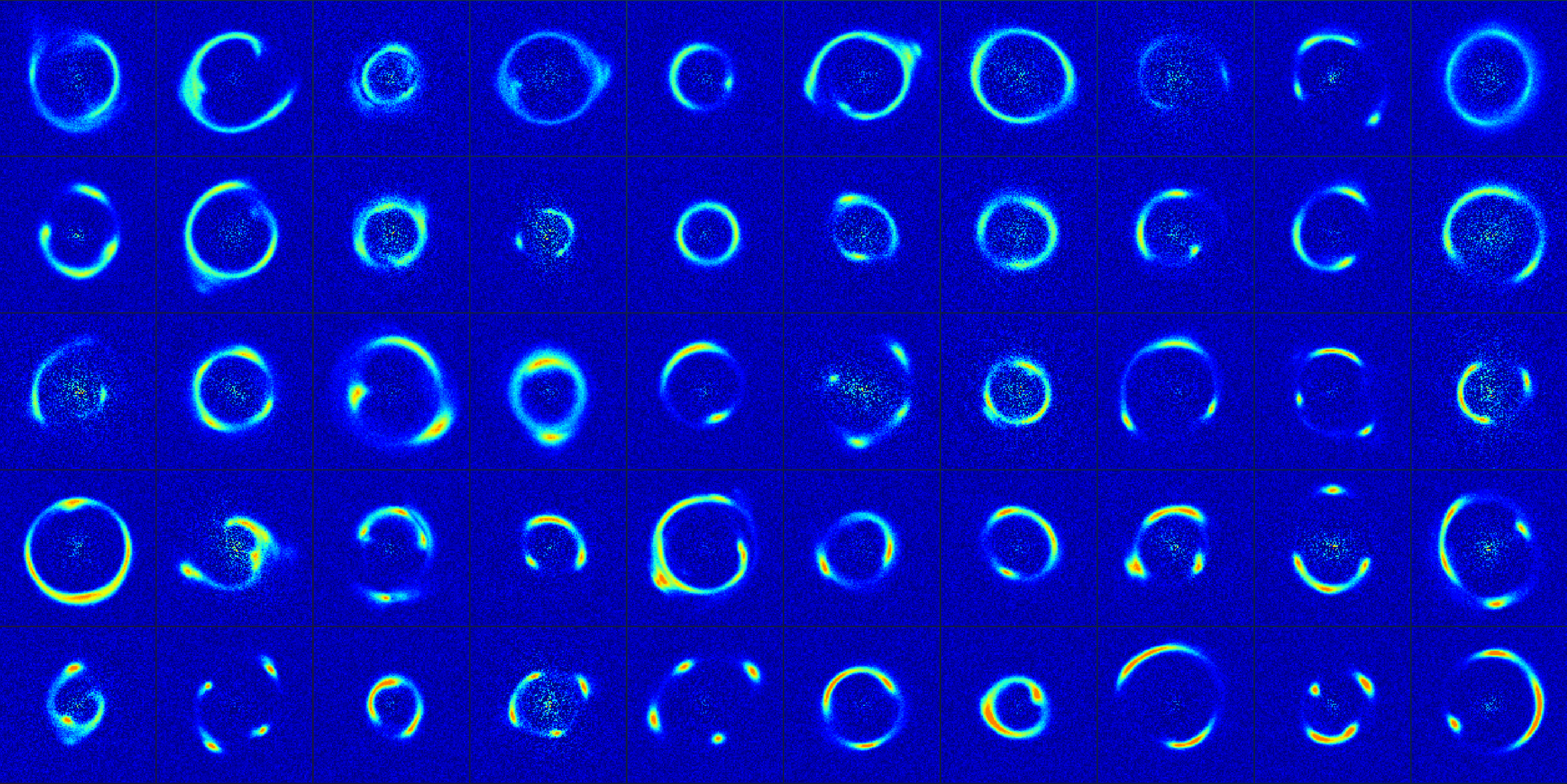
Order 4 is more common than 3, as it fits boxy/discy isophotes.

This informs our model choice: a reasonable prior of <1%, and a more extreme version with <3%

See Naab & Burkert (2003), Hao et al, (2006), Chaware et al (2014) Mitsuda et al (2017)

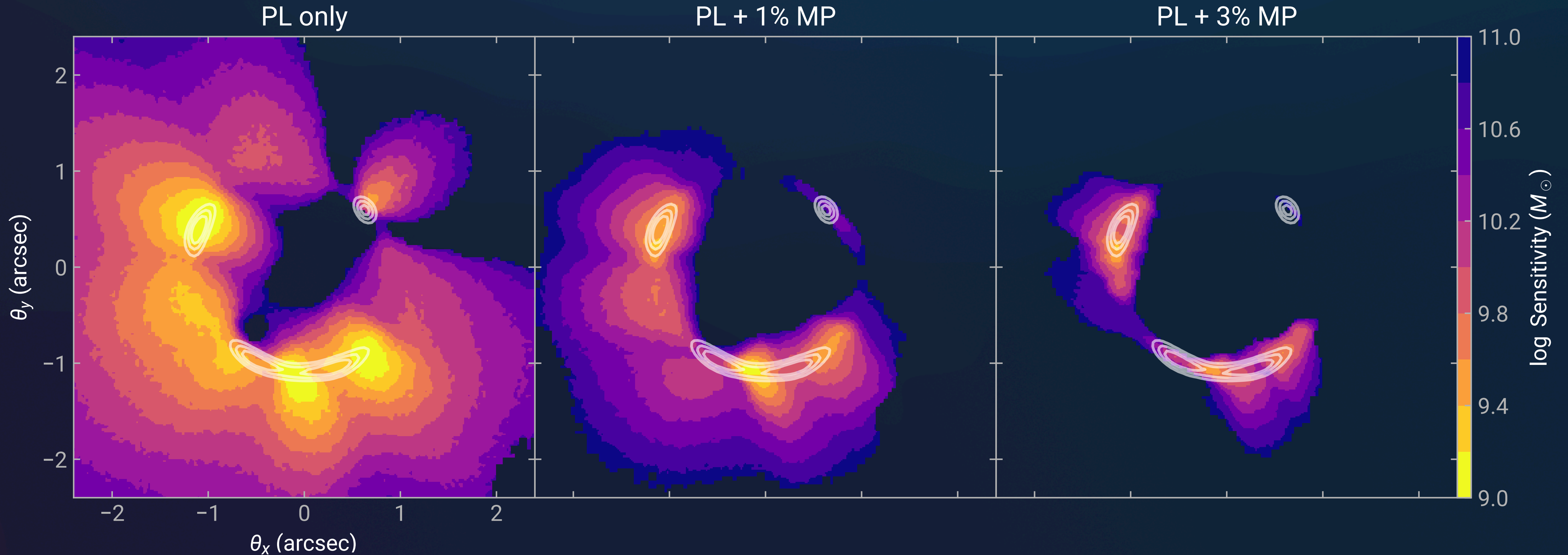
	Lensing components	Observation	Subhaloes
PL + $\gamma_{\text{ext}}$	Hubble deep field sources	S/N from $10^1$ to $10^3$	$v_{\text{max}} - r_{\text{max}}$ to set concentration
	Elliptical power-law mass	HST pixel scale and PSF	$M_{\text{max}}$ from $10^{7.6}$ to $10^{11}$
	External shear	Poisson limited lens subtraction	Zero or 1-4, randomly placed
+ MP (<1%)	Order 1, 3, 4 MPs <1%		
+ MP (<3%)	Order 1, 3, 4 MPs <3%		

Results: HST mock images



Results:

# Sensitivity mapping with multipoles

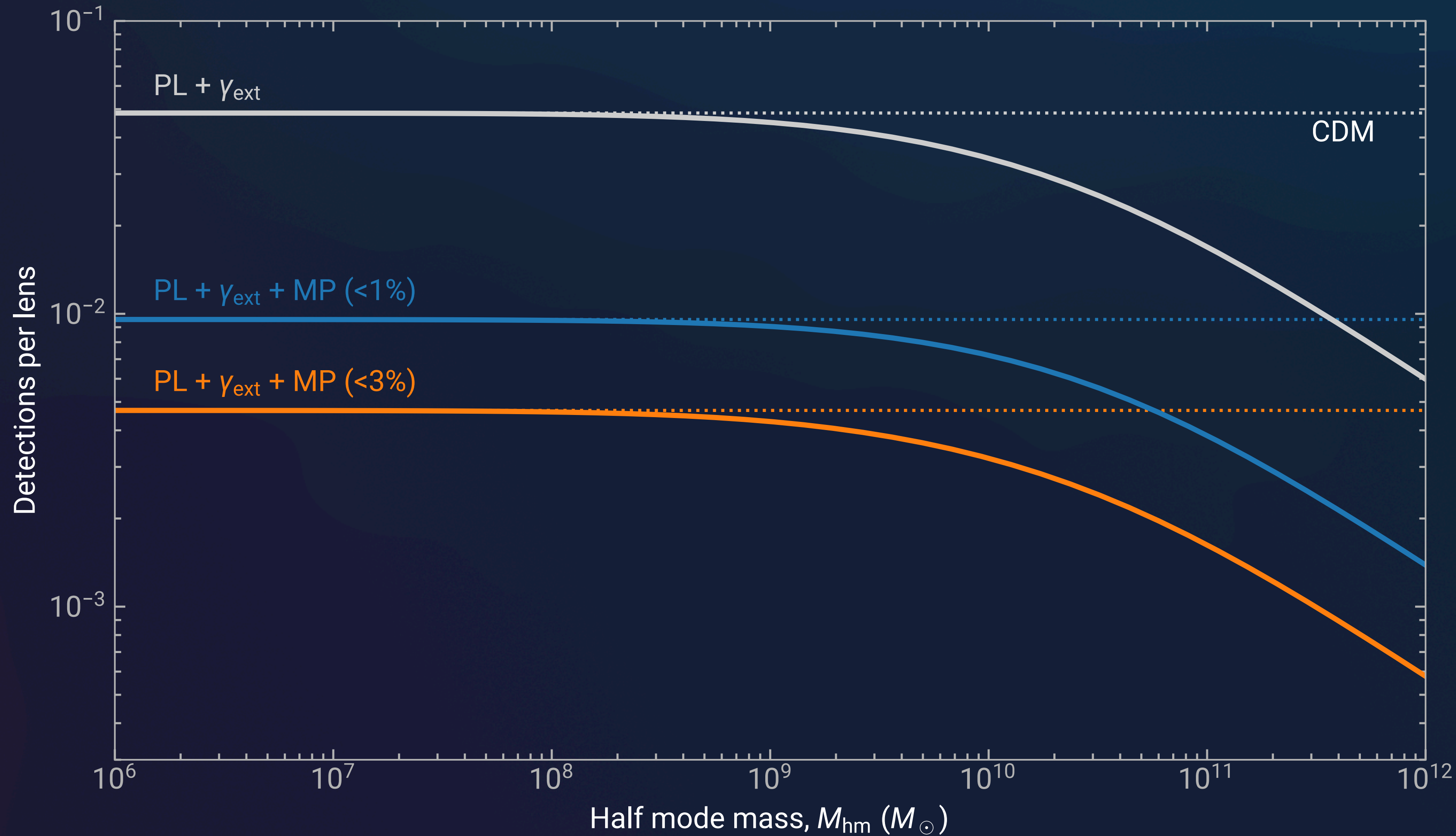


Including multipoles in the macro-model removes sensitivity away from the arc

Sensitivity in and close to the arc remains similar, especially when going from modest to extreme multipoles

Results:

# Expected detections with multipoles



With a smaller sensitive area, the number of expected detections drops by a factor of 4 for the 1% case.

But with only a small change in depth, the number of detections deviate from CDM at similar HM masses.

# Conclusions

We tested the effect of angular structure on the sensitivity maps of 100 mock HST lenses. For multipoles up to 1% amplitude we find...

**20%** False positive  
detection rate

**61%** Loss in  
sensitivity area

**0.28** Orders of magnitude  
loss in depth

Substructure detection efforts must allow for angular structure in the lens to remain reliable.

*But*, the constraining power on the underlying DM model should not drastically change.

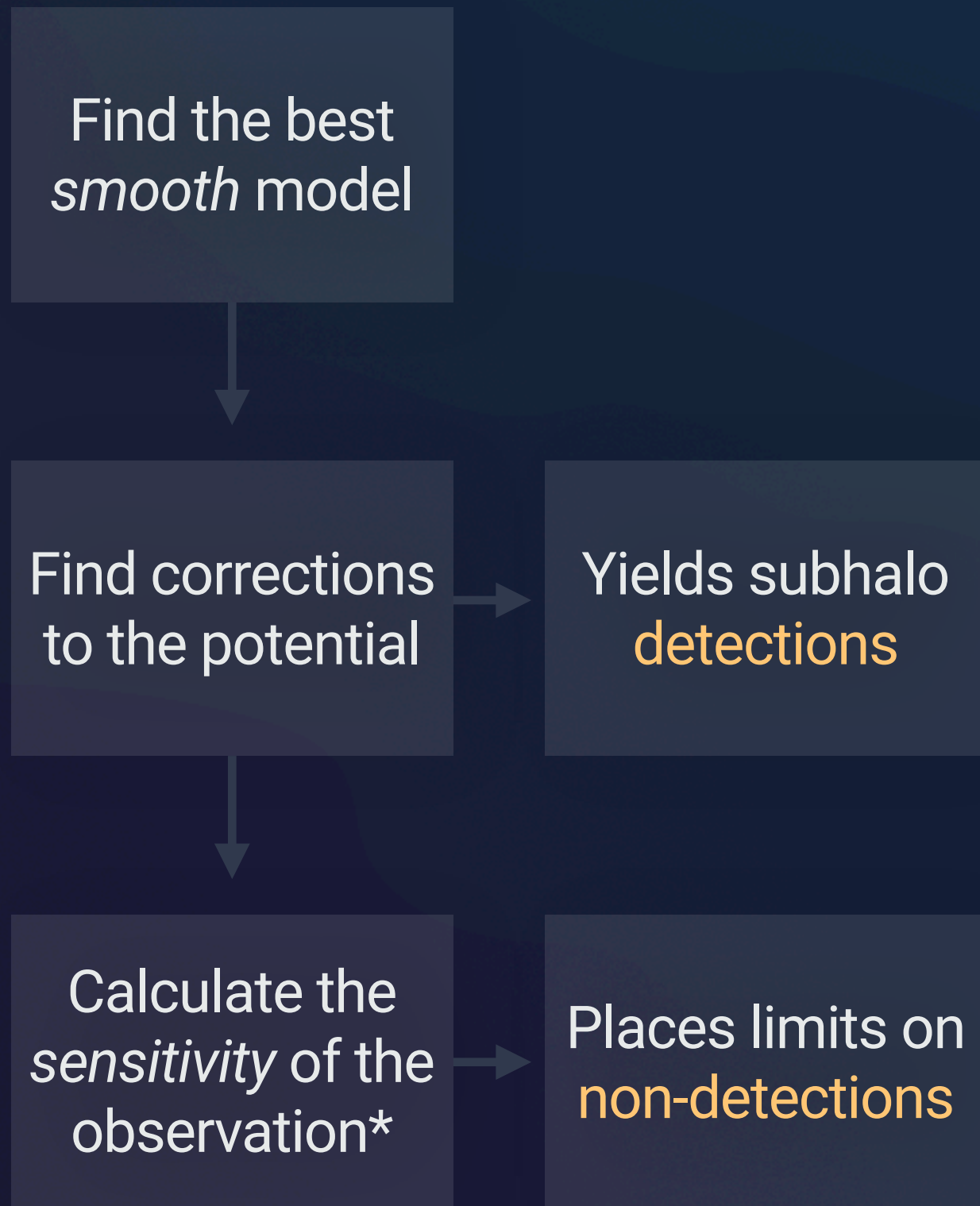
[conor@mpa-garching.mpg.de](mailto:conor@mpa-garching.mpg.de)



**Extra slides**

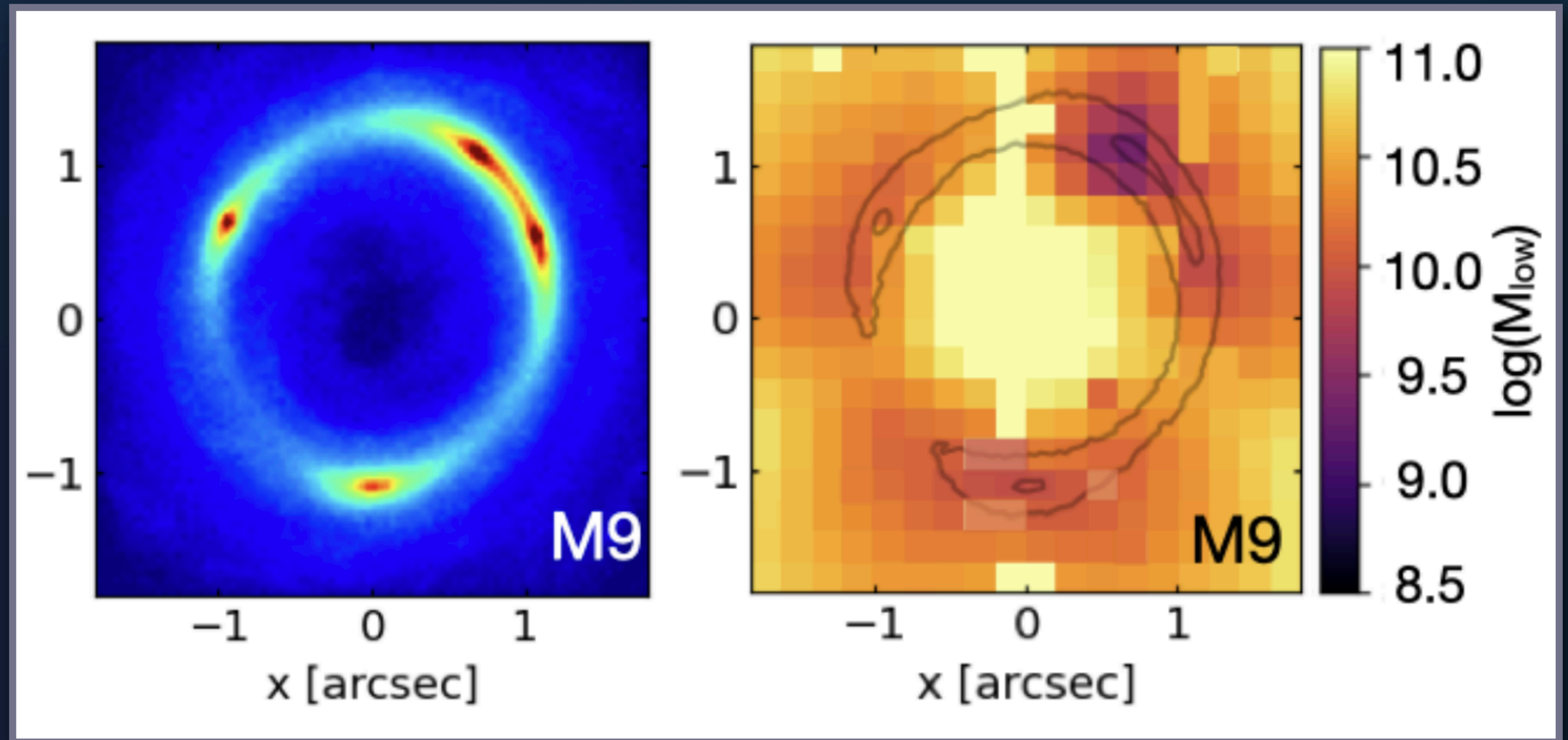
Background:

# Sensitivity function



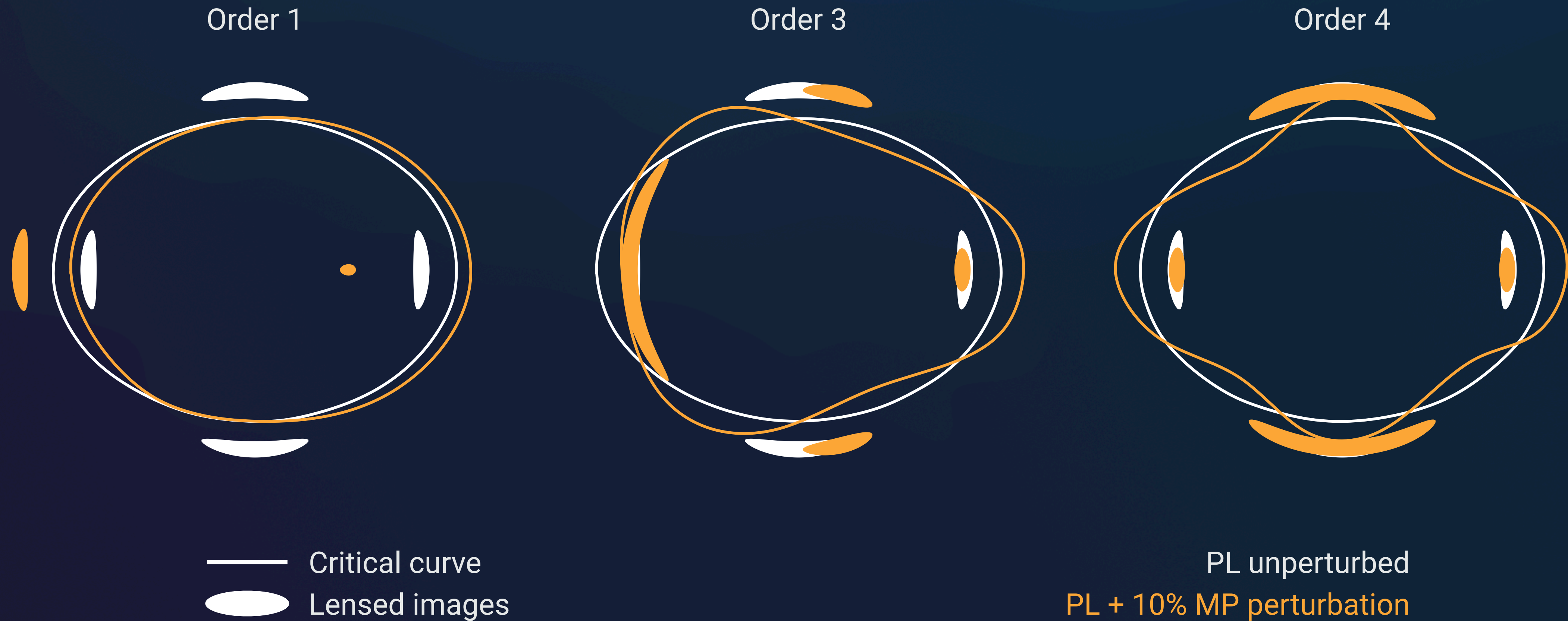
*\*expensive!*

*Despali et al (2021)*



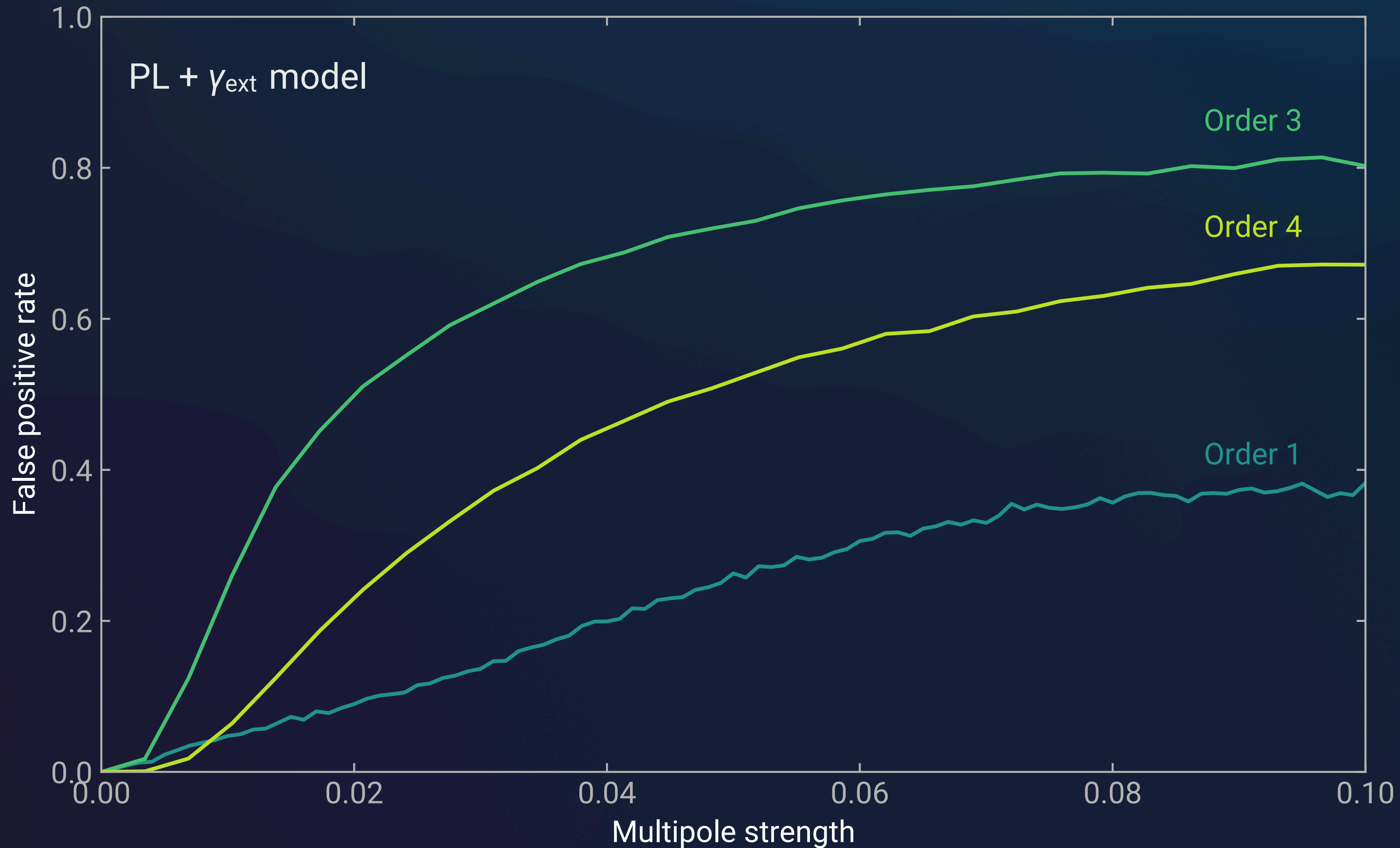
Method:

# Modelling angular structure



Results:

# Substructure false positives



We add multipoles to our mock HST data and run the images through our PL-only model.

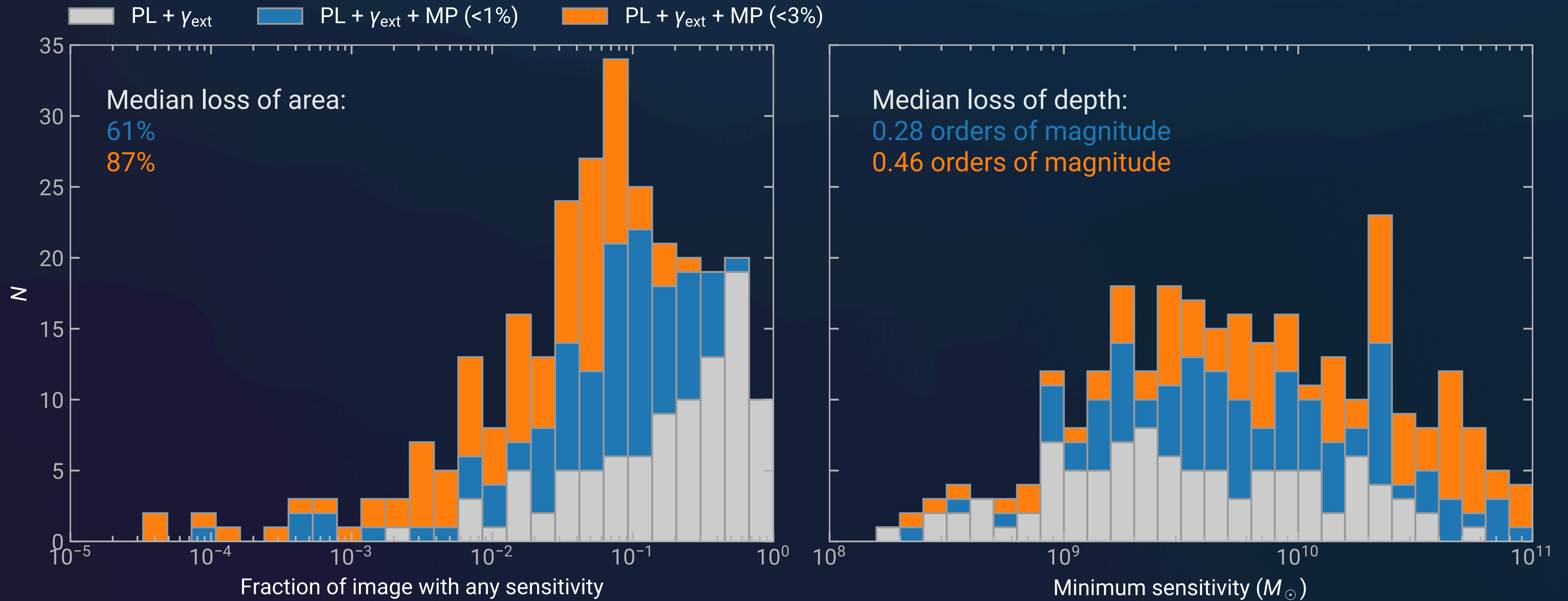
Substructure is detected very often for even modest multipole strengths.

Order 3 multipoles have the strongest degeneracy, followed closely by order 4.

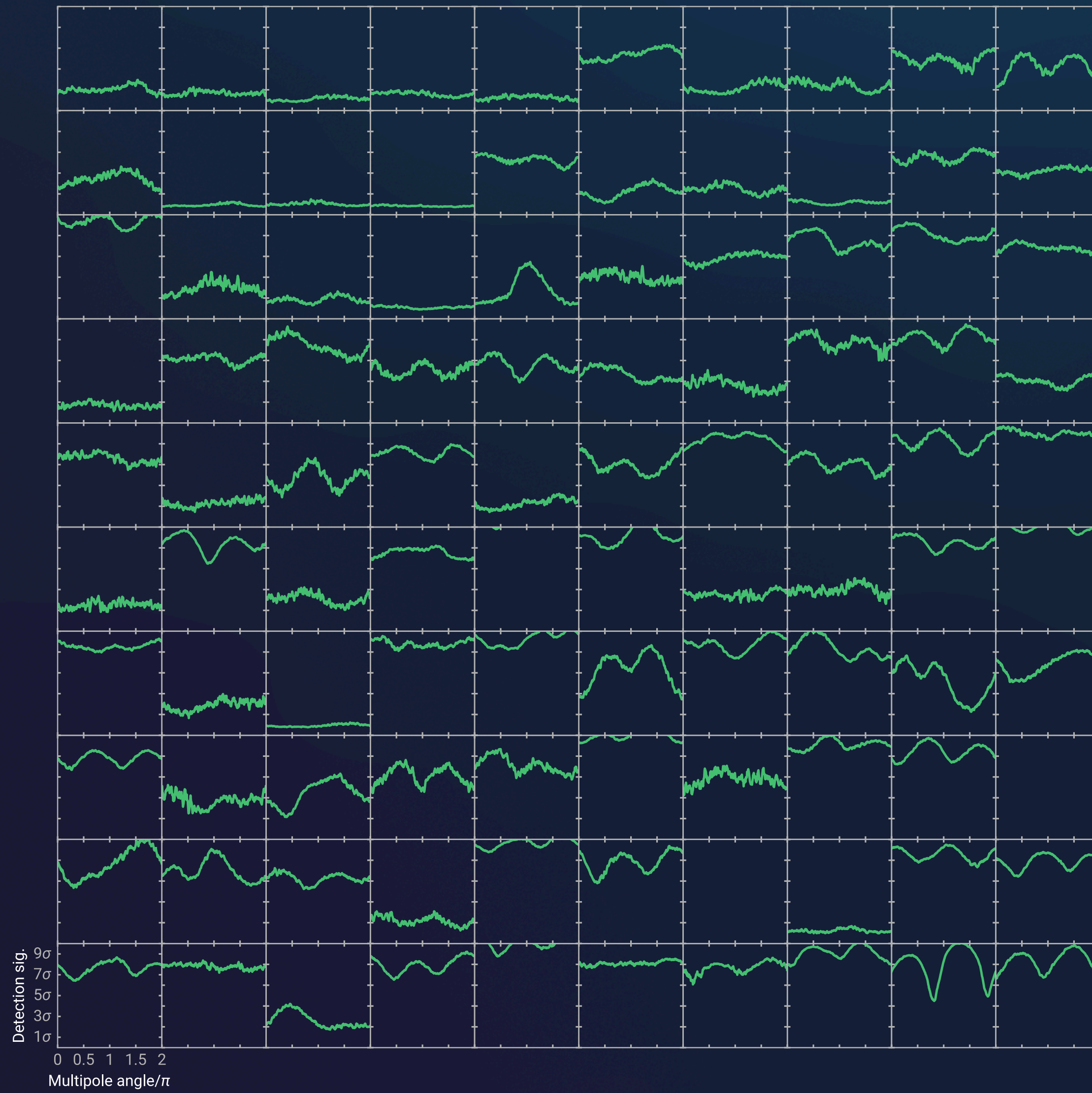
Models with 1% and 3% MPs have zero false positives in their prior ranges

Results:

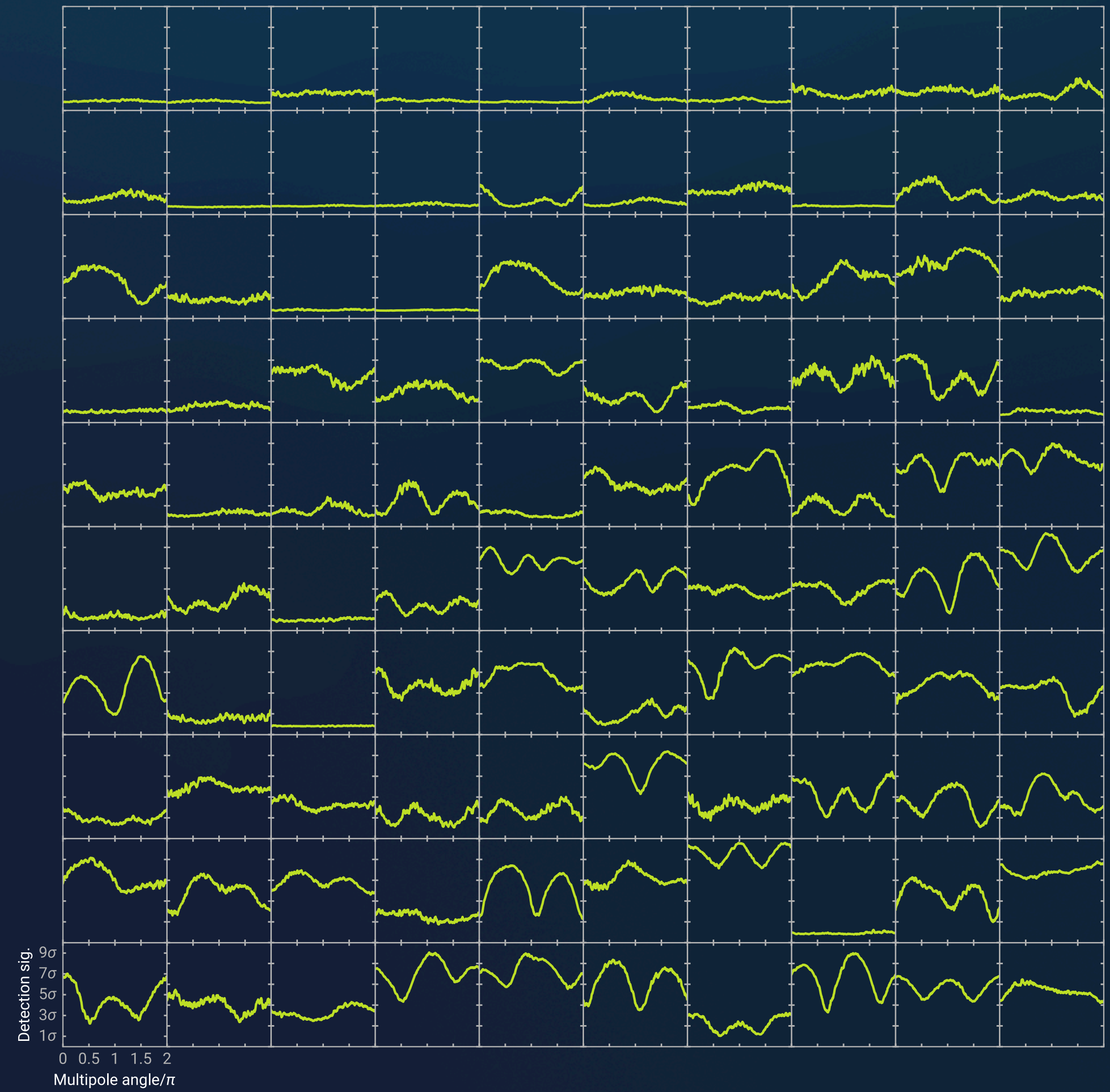
# Sensitivity mapping with multipoles



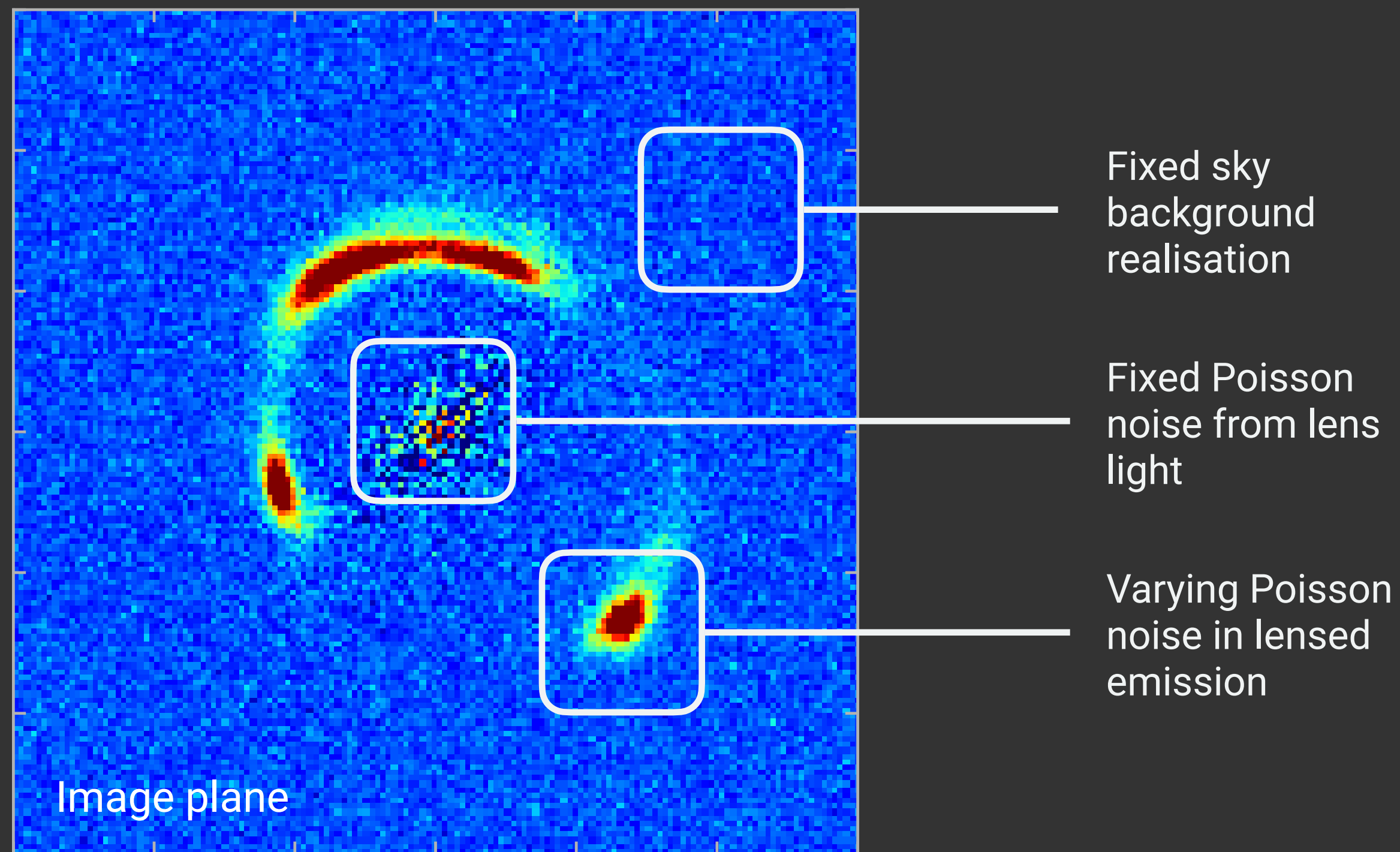
Order 3



Order 4



# Sensitivity map uncertainty



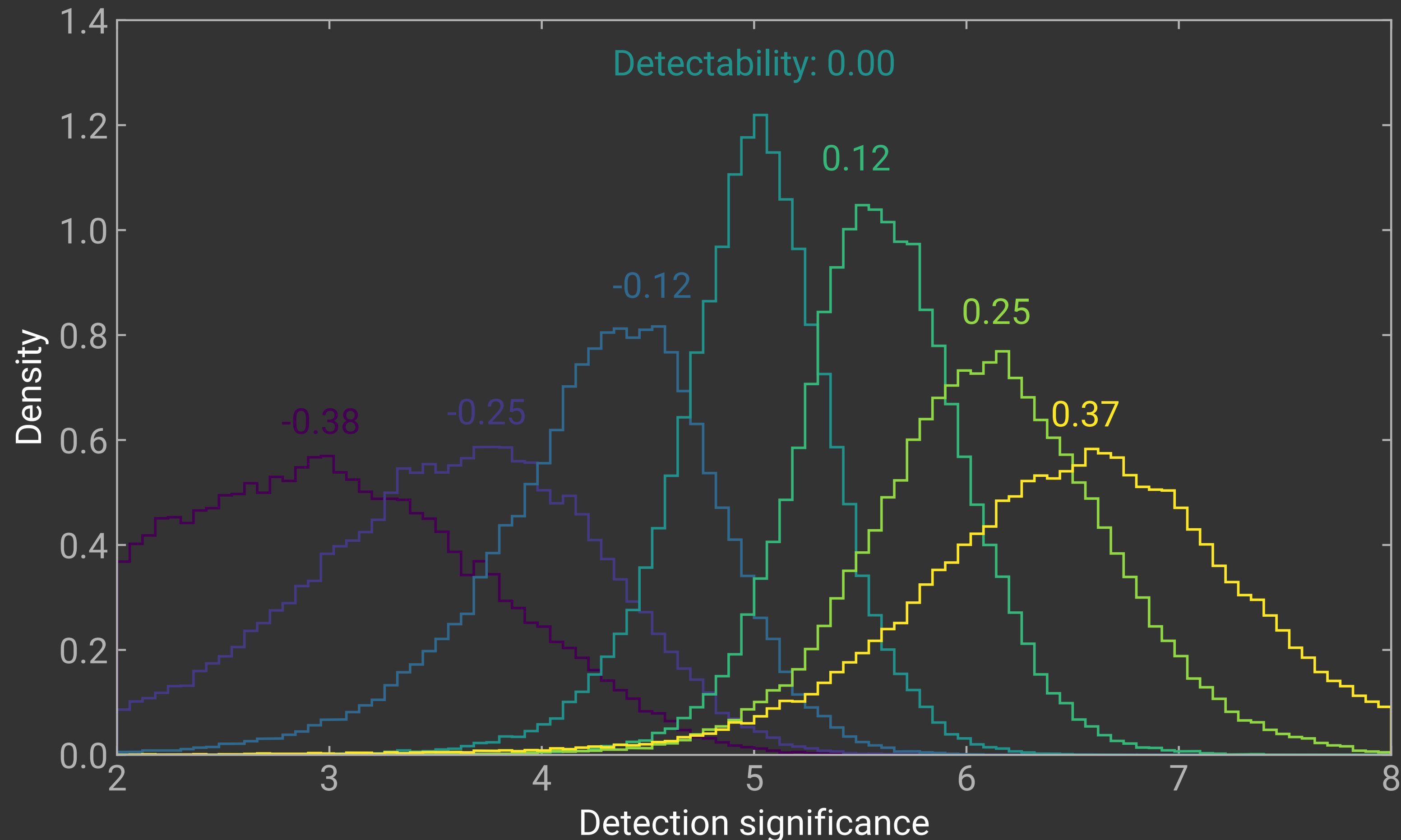
Some of the noise in the image changes between making the sensitivity map and running the subhalo detections

This introduces uncertainty - what was detectable at  $5\sigma$  in the SM realisation, might not be when we run the detections, and vice versa

Accounting for uncertainty will always boost the number of expected detections because the mass function is steep.

# Sensitivity map uncertainty

Here I define the detectability of a subhalo:  $\log \left( M_{\max} / M_{\text{map}} \right)$



Running many realisations of the same single subhalo through the detector gives a distribution of detection significances, as a function of how detectable the subhalo is.

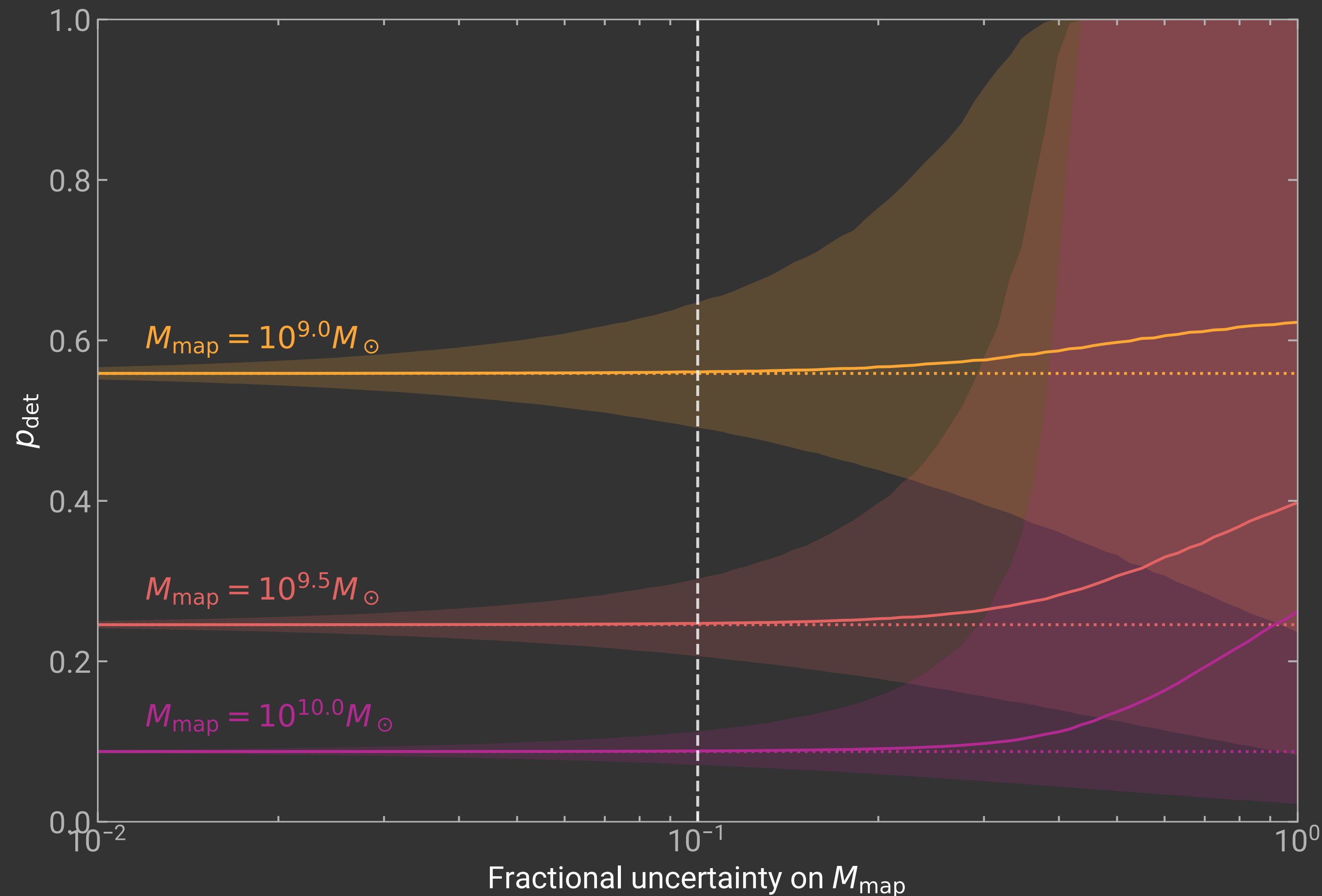
Repeating for many lenses and masses we can estimate the uncertainty as a function of mass

At all masses,  $\sigma_{M_{\text{map}}} / M_{\text{map}} < 10^{-1}$



# Sensitivity map uncertainty

Here I define the detectability of a subhalo:  $\log \left( M_{\text{max}} / M_{\text{map}} \right)$



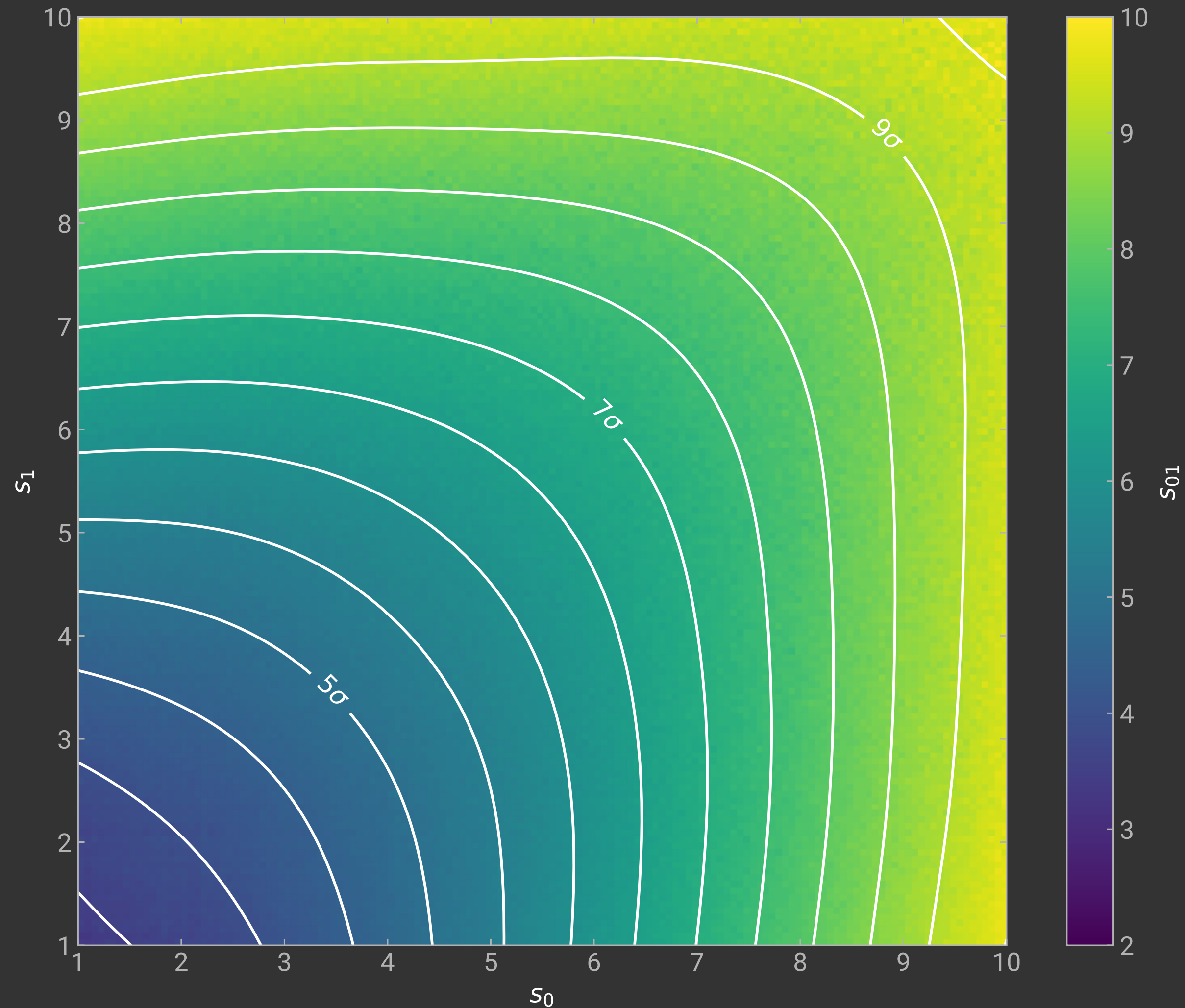
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At all masses,  $\sigma_{M_{\text{map}}} / M_{\text{map}} < 10^{-1}$

Sensitivity map uncertainty is too small to fully explain the boost.

# Multiple object detections



We draw pairs of substructures and record:

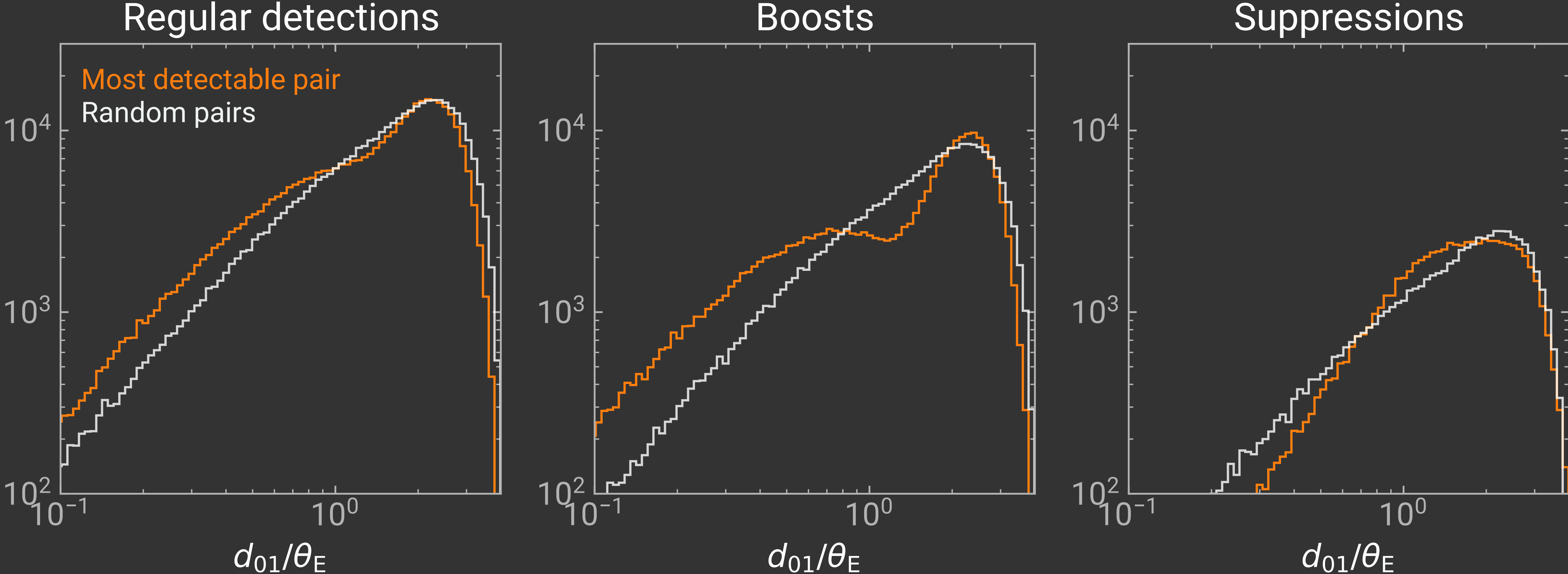
- Individual isolated detection significances  $s_0$  and  $s_1$
- Joint detection significance  $s_{01}$

We already compute  $s_0$  and  $s_1$  for all positions and masses when we produce the sensitivity maps.

We can map the substructures in the realisations to those in the map data and compute  $s_{01}$  for the two largest subhaloes in each realisation.

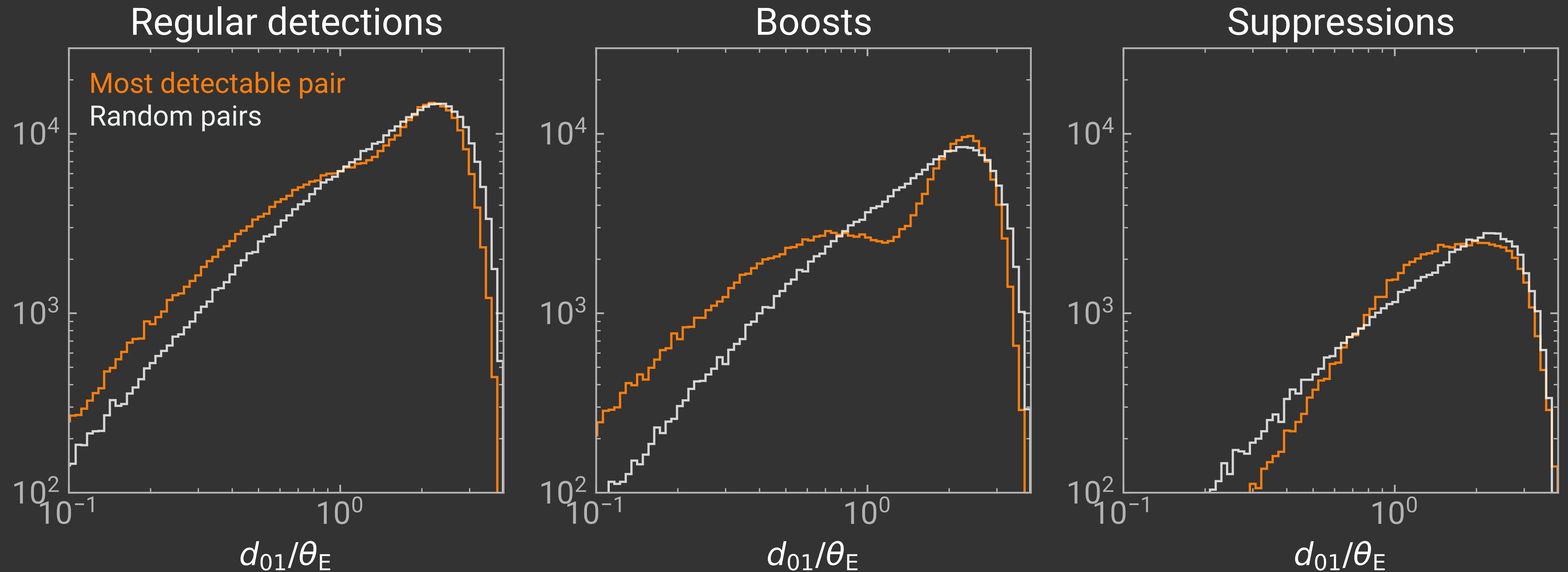
Accounting for the situation with two large but not quite detectable subhaloes in this way, we gain more expected detections...

# Interactions between substructures



$d_{01}$  is the separation between the two most detectable substructures in each realisation

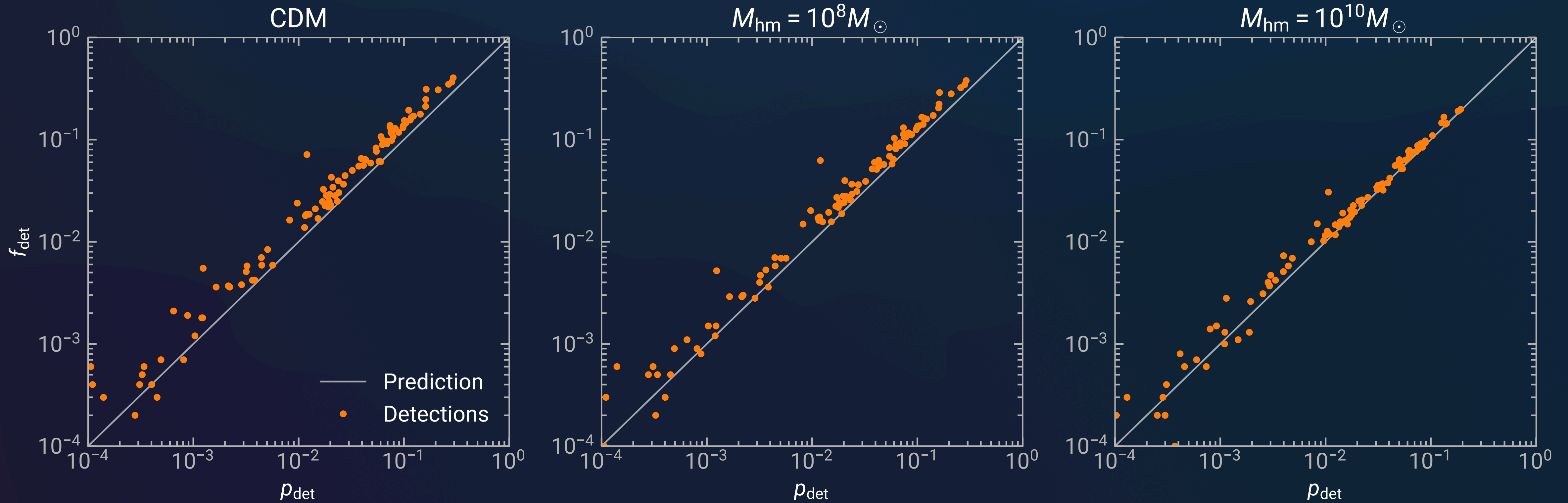
# Interactions between substructures



In realisations where we did not expect a detection, the largest substructures were on average closer than in the rest of the population

Results:

# Detections from subhalo populations



In warmer DM models, the excess of detections seen in CDM disappears.

