

# Cosmology with *Galaxy Photometry Alone*











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## Cosmology with One Galaxy?

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### Abstract

Galaxies can be characterized by many internal properties such as stellar mass, gas metallicity, and star formation rate. We quantify the amount of cosmological and astrophysical information that the internal properties of individual galaxies and their host dark matter halos contain. We train neural networks using hundreds of thousands of galaxies from 2000 state-of-the-art hydrodynamic simulations with different cosmologies and astrophysical models of the CAMELS project to perform likelihood-free inference on the value of the cosmological and astrophysical parameters. We find that knowing the internal properties of a single galaxy allows our models to infer the value of  $\Omega_m$ , at fixed  $\Omega_b$ , with a  $\sim 10\%$  precision, while no constraint can be placed on  $\sigma_8$ . Our results hold for any type of galaxy, central or satellite, massive or dwarf, at all considered redshifts,  $z \leq 3$ , and they incorporate uncertainties in astrophysics as modeled in CAMELS. However, our models are not robust to changes in subgrid physics due to the large intrinsic differences the two considered models imprint on galaxy properties. We find that the stellar mass, stellar metallicity, and maximum circular velocity are among the most important galaxy properties to determine the value of  $\Omega_m$ . We believe that our results can be explained by considering that changes in the value of  $\Omega_m$ , or potentially  $\Omega_b/\Omega_m$ , affect the dark matter content of galaxies, which leaves a signature in galaxy properties distinct from the one induced by galactic processes. Our results suggest that the low-dimensional manifold hosting galaxy properties provides a tight direct link between cosmology and astrophysics.

*Unified Astronomy Thesaurus concepts:* [Galaxy formation \(595\)](#); [Cosmological models \(337\)](#); [Astrostatistics \(1882\)](#); [Hydrodynamical simulations \(767\)](#)

cosmology with *one galaxy*? trained using **CAMELS**

$$p(\Omega | \theta_g)$$

cosmology with *one galaxy*? trained using **CAMELS**

$$p(\Omega \mid \theta_g)$$

*cosmological parameters*

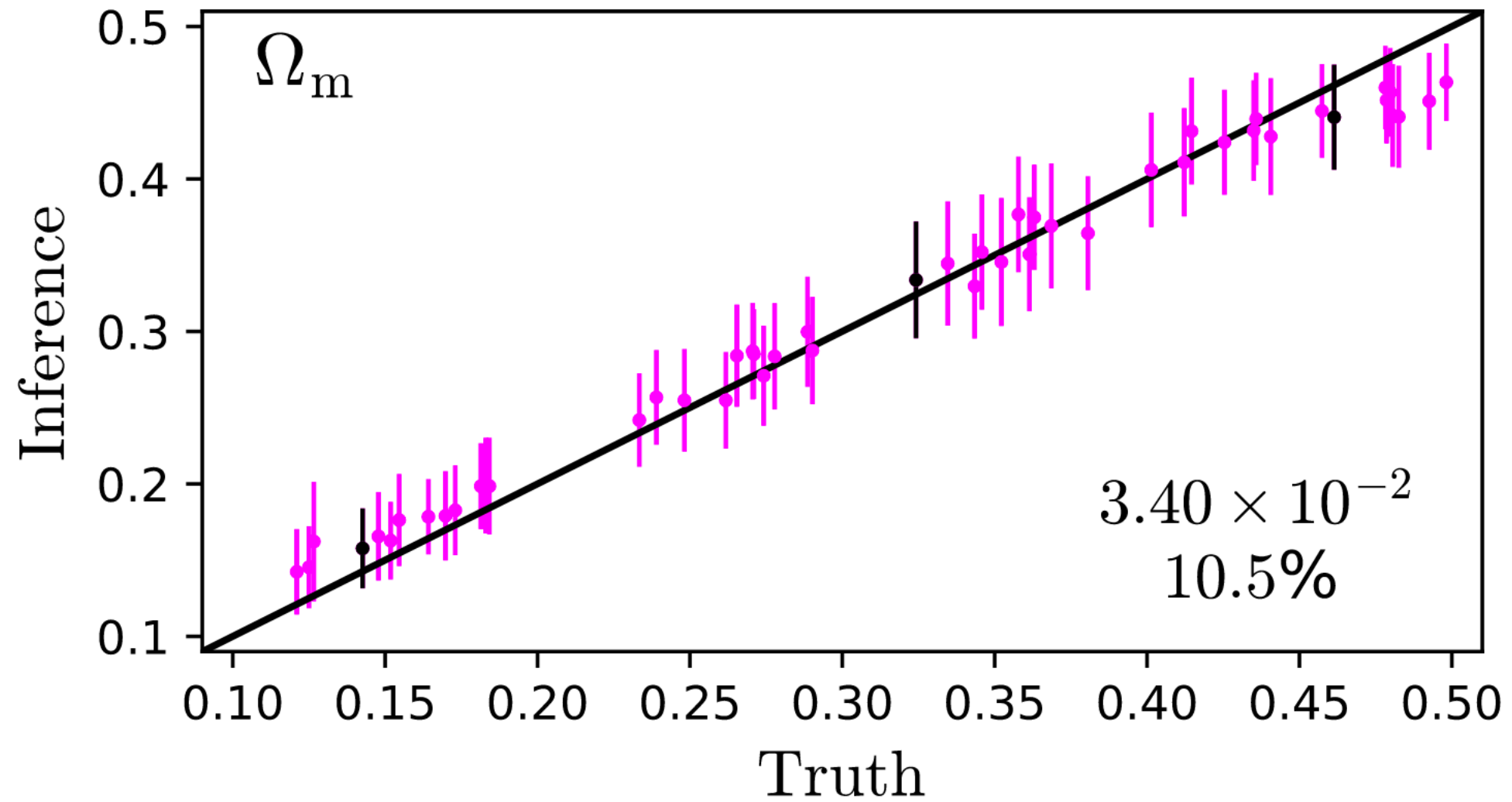
*galaxy properties*

$$\Omega_m, \sigma_8$$

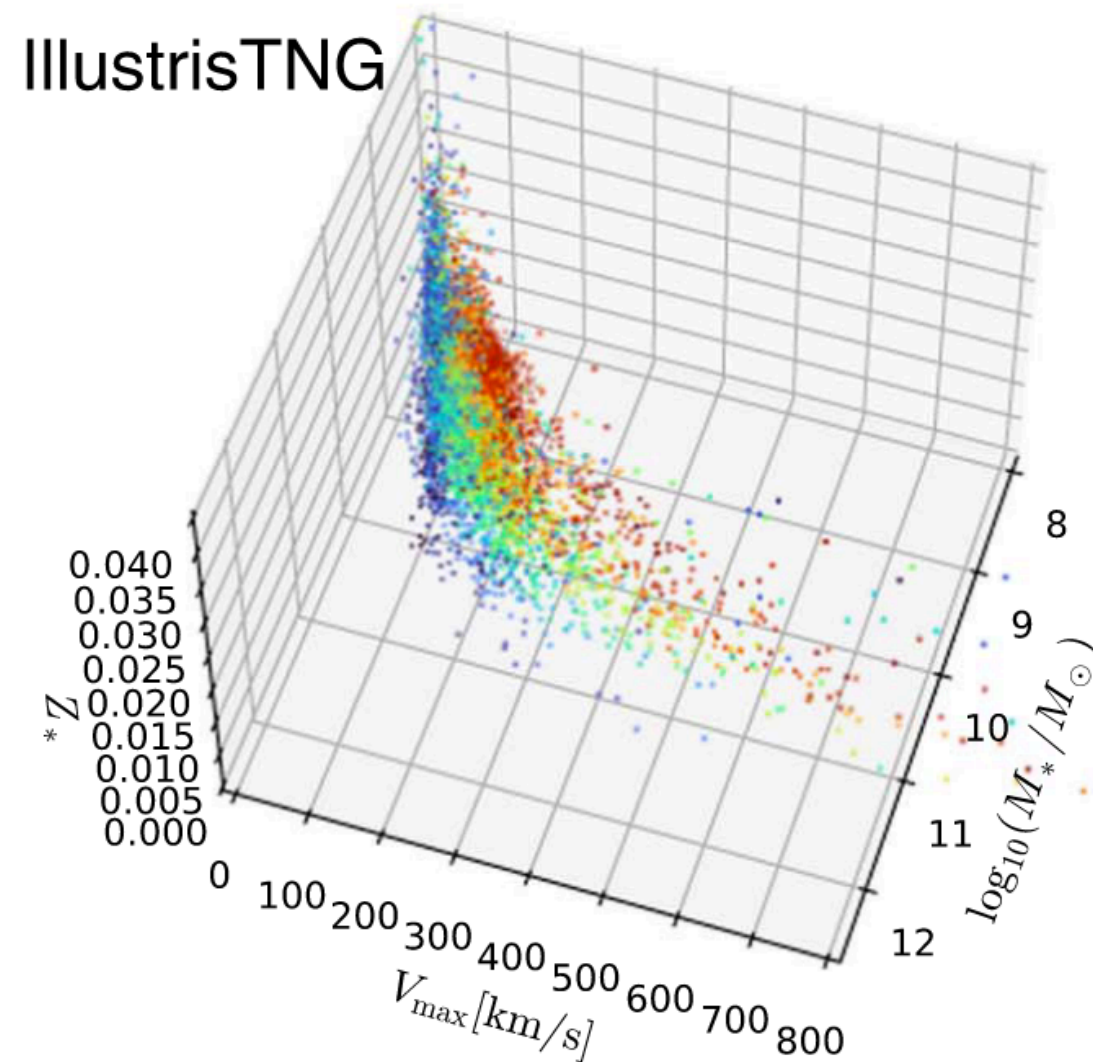
$$V_{\max}, M_*, M_{\text{gas}}, Z_*, R_* \dots$$



cosmology with *one galaxy*?



cosmology with *one galaxy*?



some low-dimensional manifold hosting  $\theta_g$ ?

cosmology with *one galaxy*?

$$\frac{\Omega_m}{\Omega_b} \approx \frac{M_{\text{tot}}}{M_b}$$

cosmology with *one galaxy*?

$$\frac{\Omega_m}{\Omega_b} \approx \frac{M_{\text{tot}}}{M_b} = \frac{M_{\text{tot}}(V_{\text{max}} \dots)}{M_* / \epsilon_*(M_*, M_{\text{gas}}, Z_* \dots)}$$

star formation efficiency

cosmology with *one galaxy*? — similar approach as *White et al. (1993)*

ARTICLES

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# **The baryon content of galaxy clusters: a challenge to cosmological orthodoxy**

**Simon D. M. White<sup>\*</sup>, Julio F. Navarro<sup>†</sup>, August E. Evrard<sup>‡</sup>  
& Carlos S. Frenk<sup>†</sup>**

<sup>\*</sup> Institute of Astronomy, Madingley Road, Cambridge CB3 0HA, UK

<sup>†</sup> Department of Physics, University of Durham, Durham DH1 3LE, UK

<sup>‡</sup> Department of Physics, University of Michigan, Ann Arbor, Michigan 48109, USA

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**Baryonic matter constitutes a larger fraction of the total mass of rich galaxy clusters than is predicted by a combination of cosmic nucleosynthesis considerations (light-element formation during the Big Bang) and standard inflationary cosmology. This cannot be accounted for by gravitational and dissipative effects during cluster formation. Either the density of the Universe is less than that required for closure, or there is an error in the standard interpretation of element abundances.**

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$$p(\Omega | \theta_g)$$

$\theta_g = \{ V_{\max}, M_*, M_{\text{gas}}, Z_*, R_* \dots \}$  are ***not* observables**

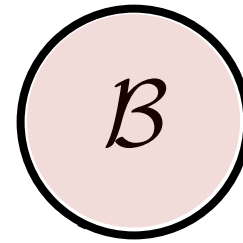
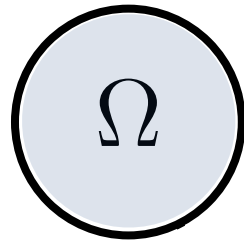


$$p(\Omega | X_i) ?$$

cosmology with the  $X_i =$  **observables** of *one galaxy*?

*cosmological parameters*

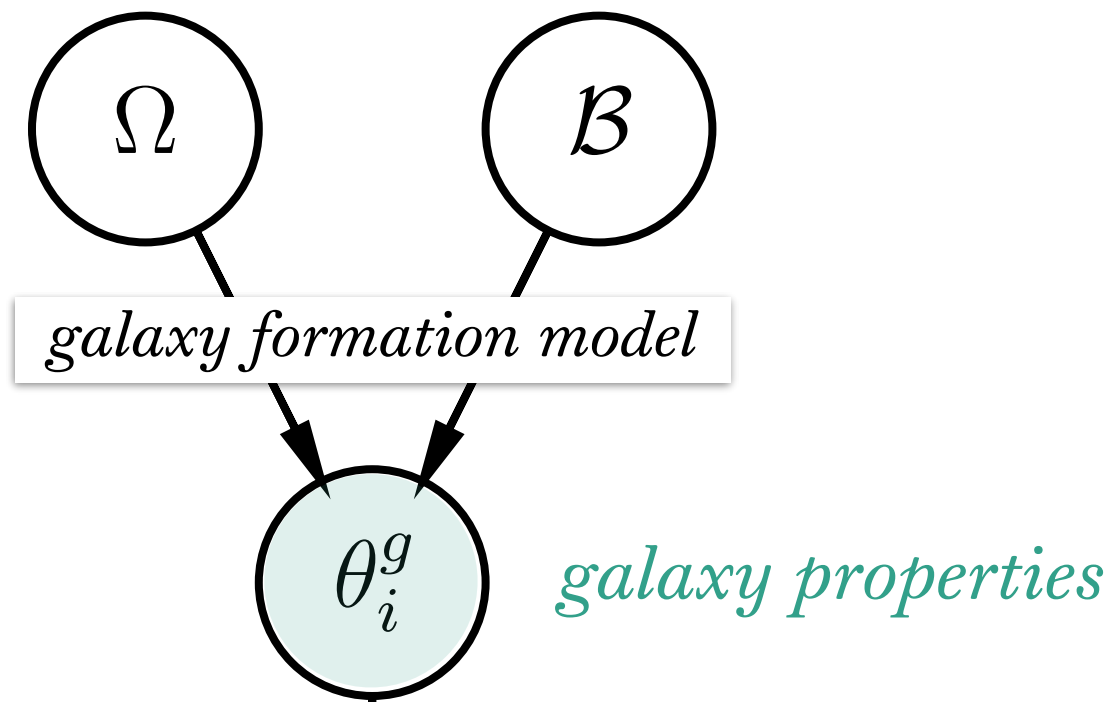
$\Omega_m, \sigma_8$

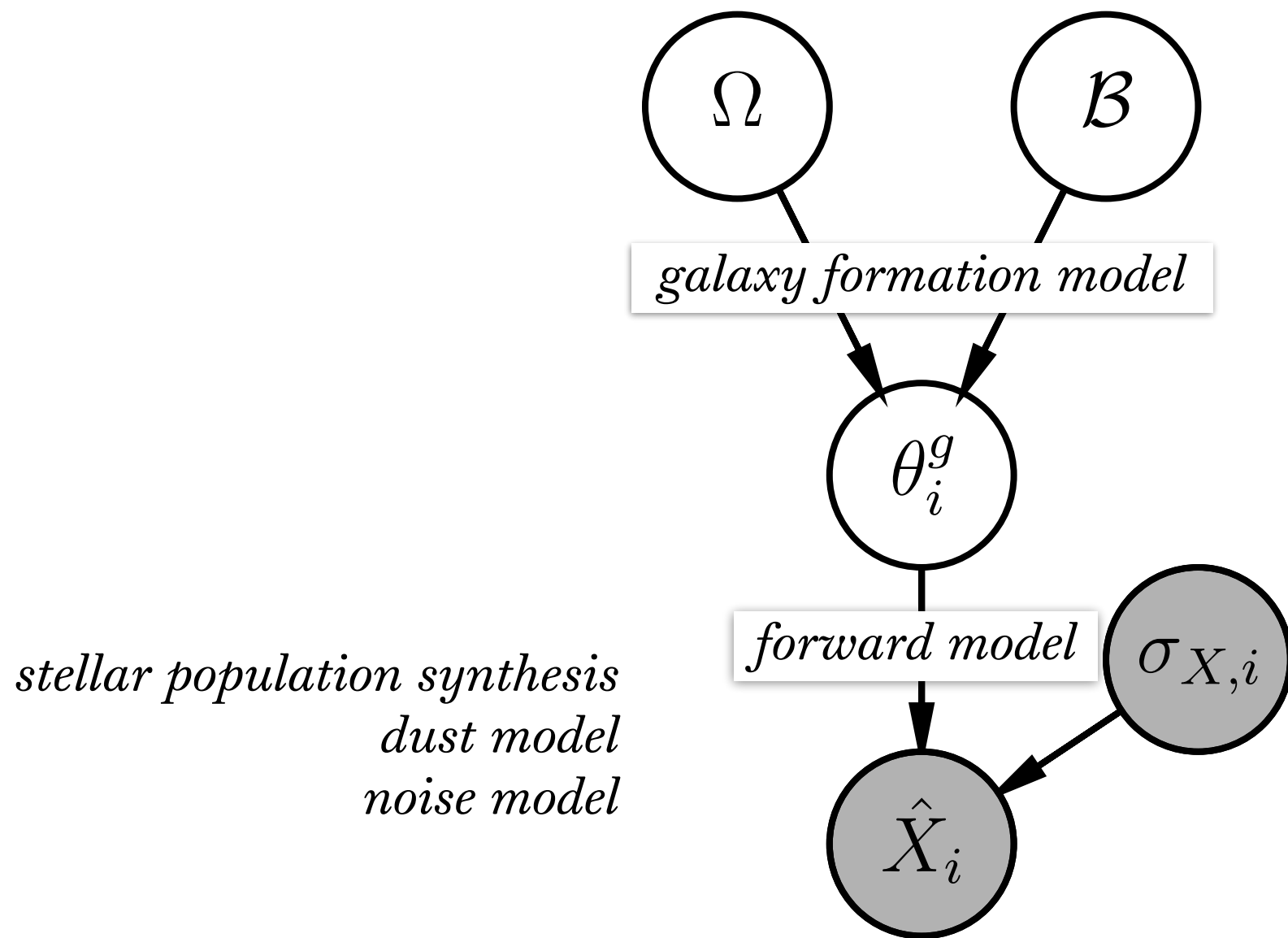


*hydro parameters*

$A_{SN1}, A_{SN2}, A_{AGN1}, A_{AGN2},$

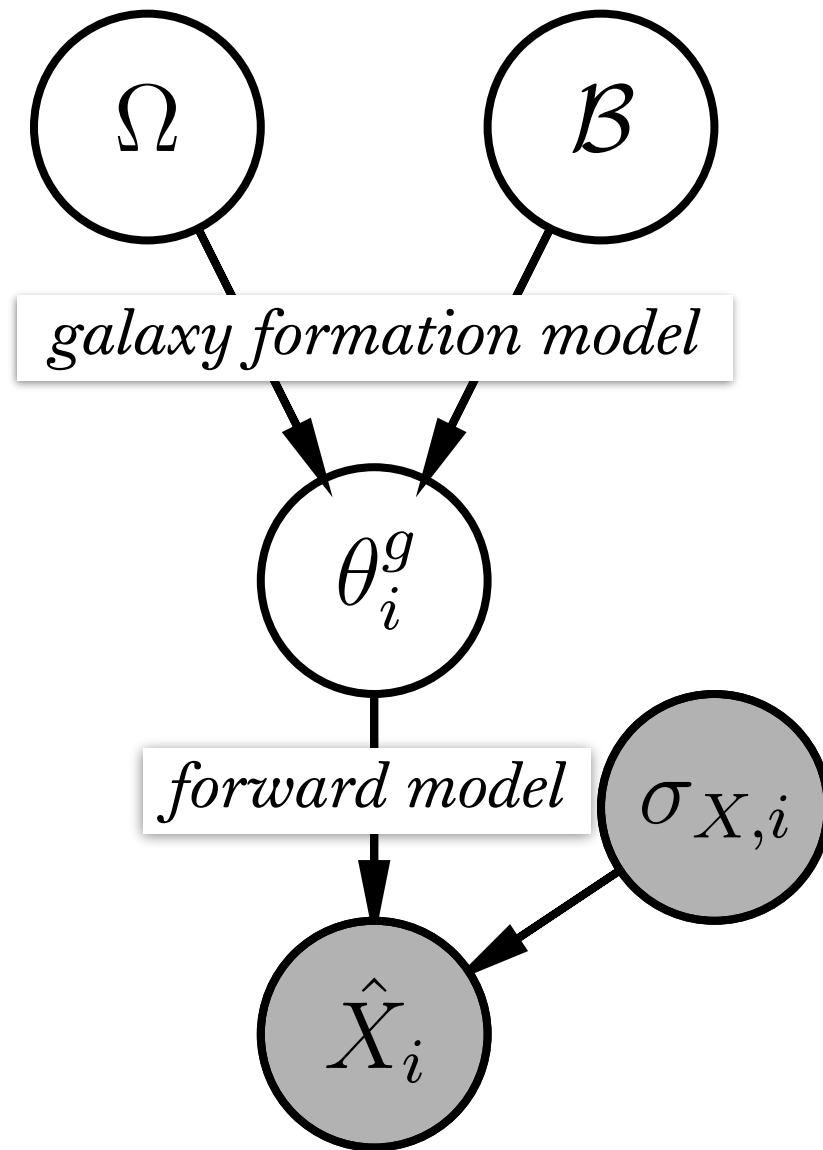
*e.g. TNG, SIMBA*





$$p(\theta_i^g \mid \Omega, \mathcal{B})$$

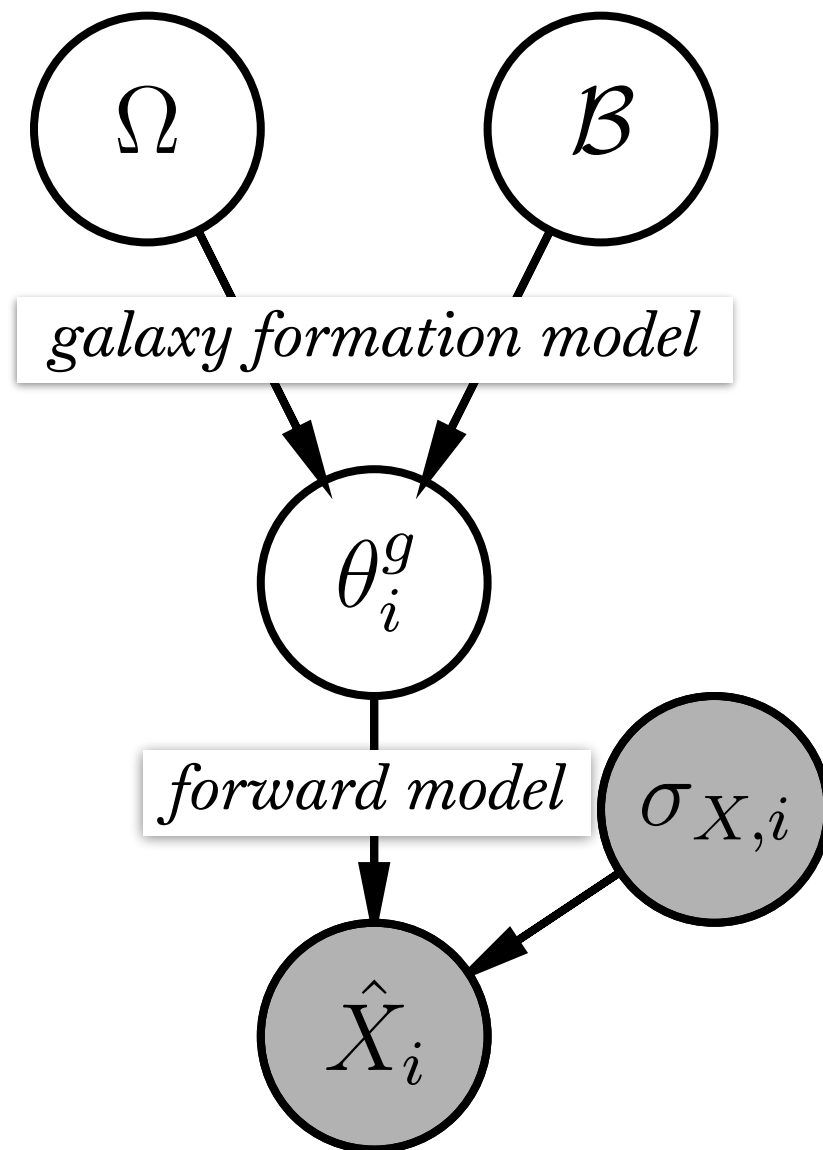
$$p(X_i \mid \theta_i^g)$$



$$p(\theta_i^g \mid \Omega, \mathcal{B})$$

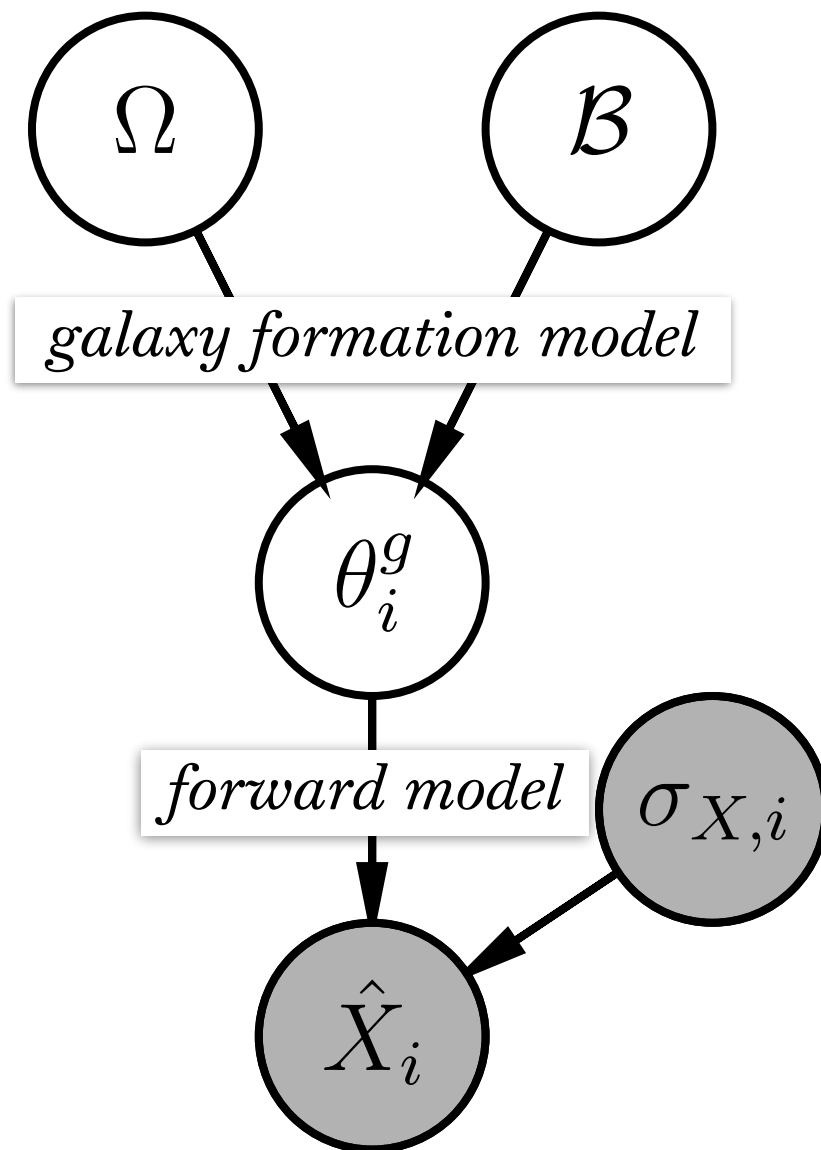
$$p(X_i \mid \theta_i^g)$$

$$p(\Omega, \mathcal{B} \mid X_i)$$





$$p(\theta_i^g \mid \Omega, \mathcal{B})$$



$$p(X_i \mid \theta_i^g)$$

$$p(\Omega, \mathcal{B} \mid X_i) = \int p(\Omega, \mathcal{B} \mid \theta_i^g) p(\theta_i^g \mid X_i) d\theta_i^g$$

$$p(\Omega, \mathcal{B} | X_i) = \int p(\Omega, \mathcal{B} | \theta_i^g) p(\theta_i^g | X_i) d\theta_i^g$$

*cosmology with one galaxy*    *SED modeling*

$$p(\Omega, \mathcal{B} | X_i) = \int p(\Omega, \mathcal{B} | \theta_i^g) p(\theta_i^g | X_i) d\theta_i^g$$

with **CAMELS** and *neural density estimation*, we can directly estimate flexible model  $q$  with hyperparameters  $\phi$

$$\approx q_\phi(\Omega, \mathcal{B} | X_i)$$

$$p(\Omega, \mathcal{B} | X_i) = \int p(\Omega, \mathcal{B} | \theta_i^g) p(\theta_i^g | X_i) d\theta_i^g$$

with **CAMELS** and *neural density estimation*, we can directly estimate flexible model  $q$  with hyperparameters  $\phi$

$$\approx q_\phi(\Omega, \mathcal{B} | X_i)$$

$$\min_{\phi} D_{\text{KL}}(p \parallel q_\phi) = \min_{\phi} \int p \log \left( \frac{p}{q_\phi} \right)$$

$$p(\Omega, \mathcal{B} | X_i) = \int p(\Omega, \mathcal{B} | \theta_i^g) p(\theta_i^g | X_i) d\theta_i^g$$

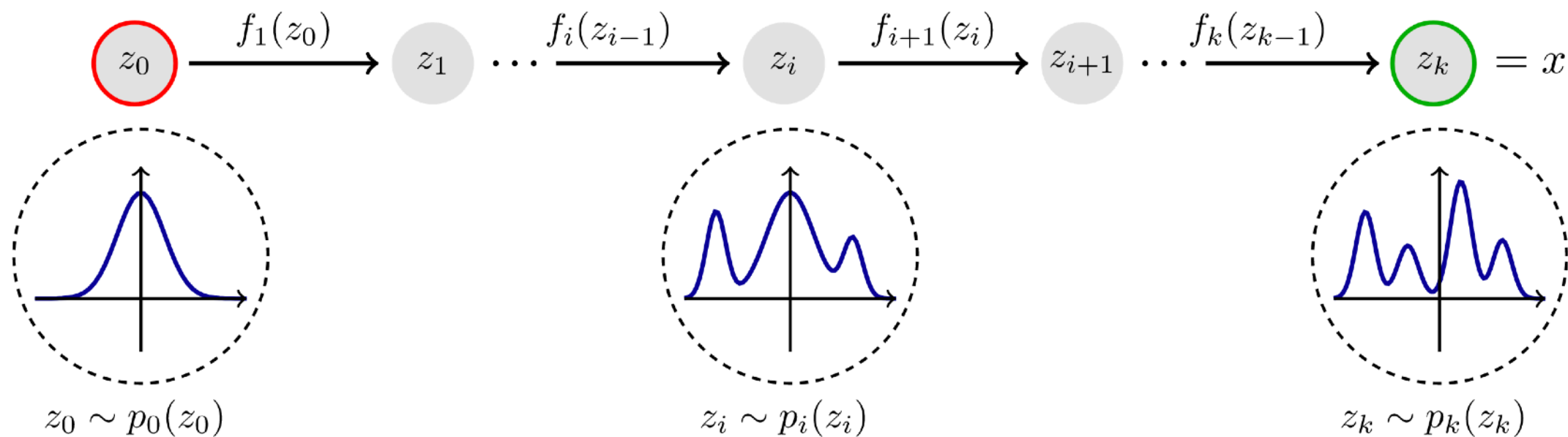
with **CAMELS** and *neural density estimation*, we can directly estimate flexible model  $q$  with hyperparameters  $\phi$

$$\approx q_\phi(\Omega, \mathcal{B} | X_i)$$

$$\min_{\phi} D_{\text{KL}}(p \parallel q_\phi) = \min_{\phi} \int p \log \left( \frac{p}{q_\phi} \right) \approx \max_{\phi} \sum_i \log q_\phi(\Omega_i, \mathcal{B}_i | X_i)$$

*galaxies in CAMELS forward model*  
 $\{(\Omega', \mathcal{B}', X')\} \sim p(\Omega, \mathcal{B}, X)$

$q_\phi$  — **normalizing flows** are easy to evaluate and flexibly expressive

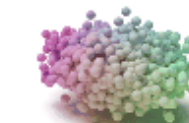
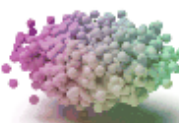
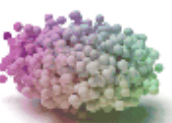
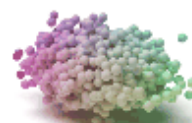
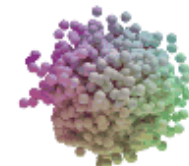
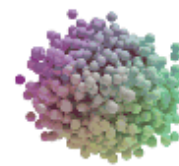
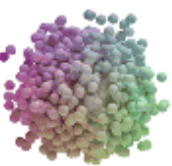
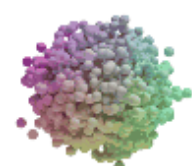
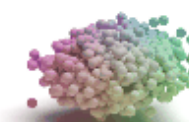
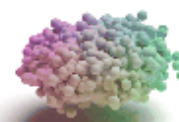
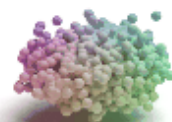
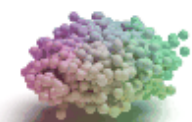


$z_i = f_i(z_{i-1})$  are *invertible* and *differentiable* transformations

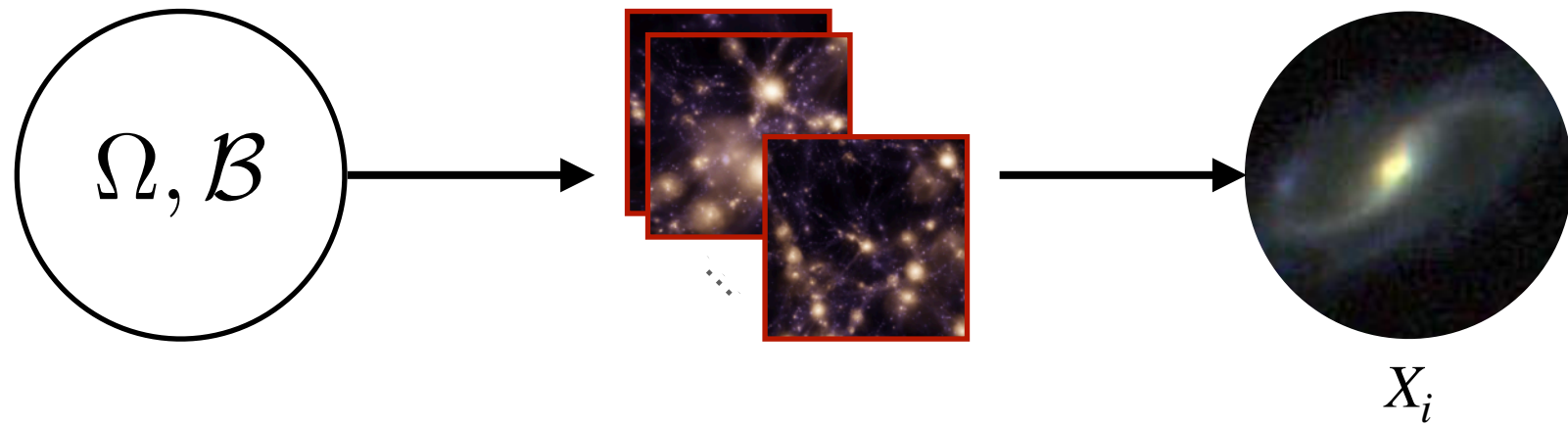
$$p(z_i) = p(z_{i-1}) \left| \det \left( \frac{\partial f_i^{-1}}{\partial z_i} \right) \right|$$



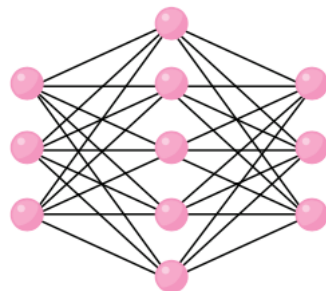
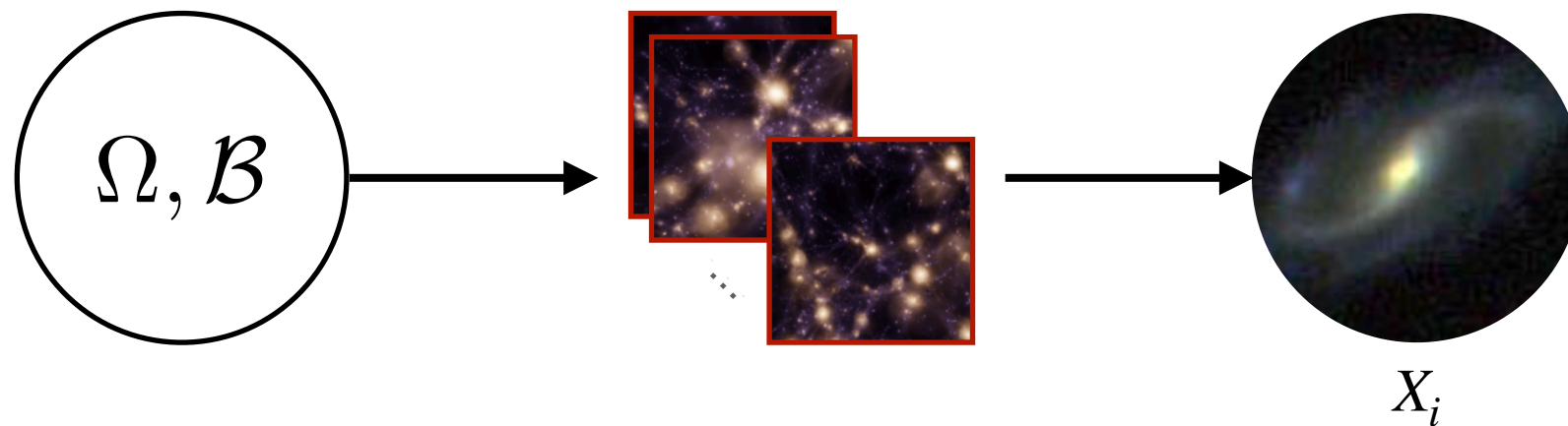
$q_\phi$  — **normalizing flows** are easy to evaluate and flexibly expressive



**CAMELS**  $\{(\Omega', \mathcal{B}', X')\} \sim p(\Omega, \mathcal{B}, X)$

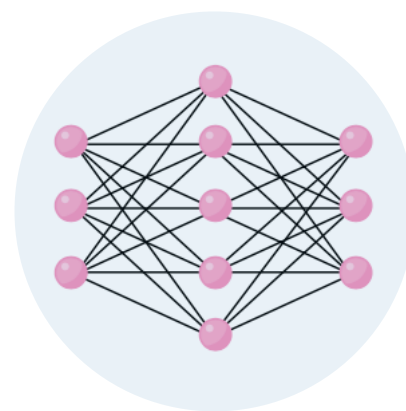
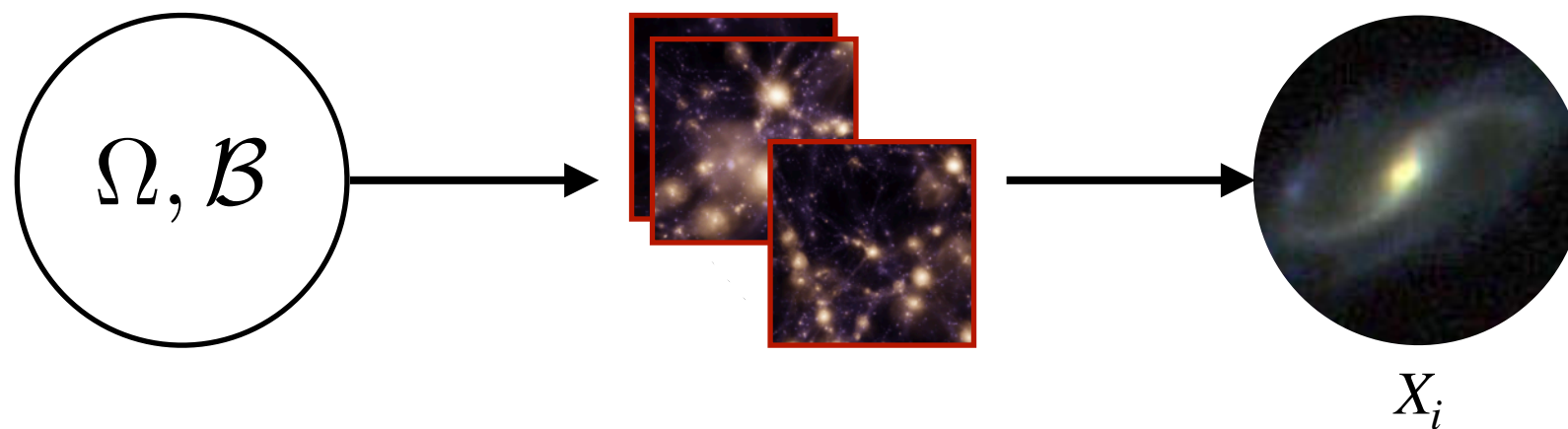


**CAMELS**  $\{(\Omega', \mathcal{B}', X')\} \sim p(\Omega, \mathcal{B}, X)$



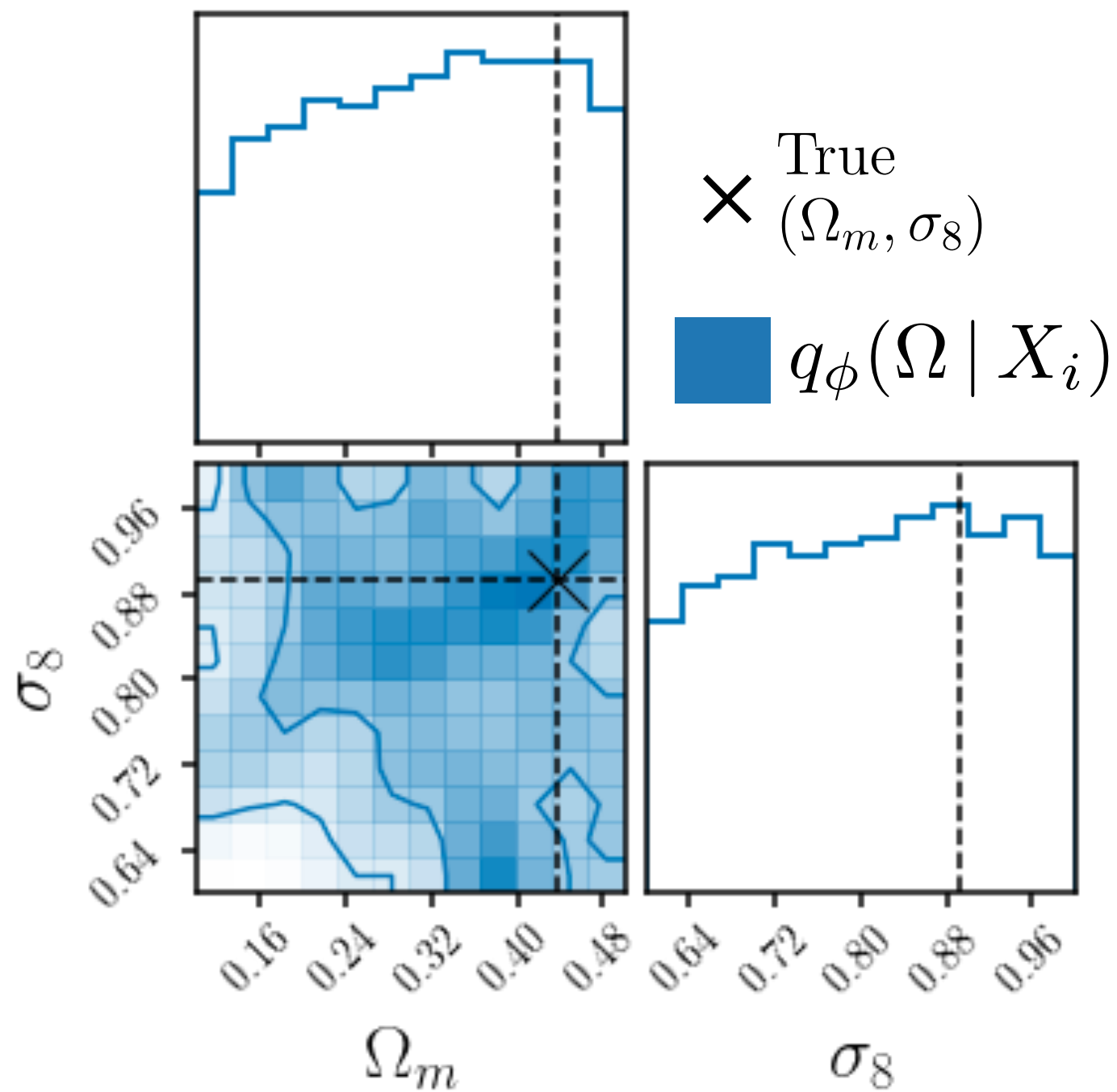
*training  
normalizing flow  
 $q_\phi(\Omega, \mathcal{B} | X)$*

**CAMELS**  $\{(\Omega', \mathcal{B}', X')\} \sim p(\Omega, \mathcal{B}, X)$

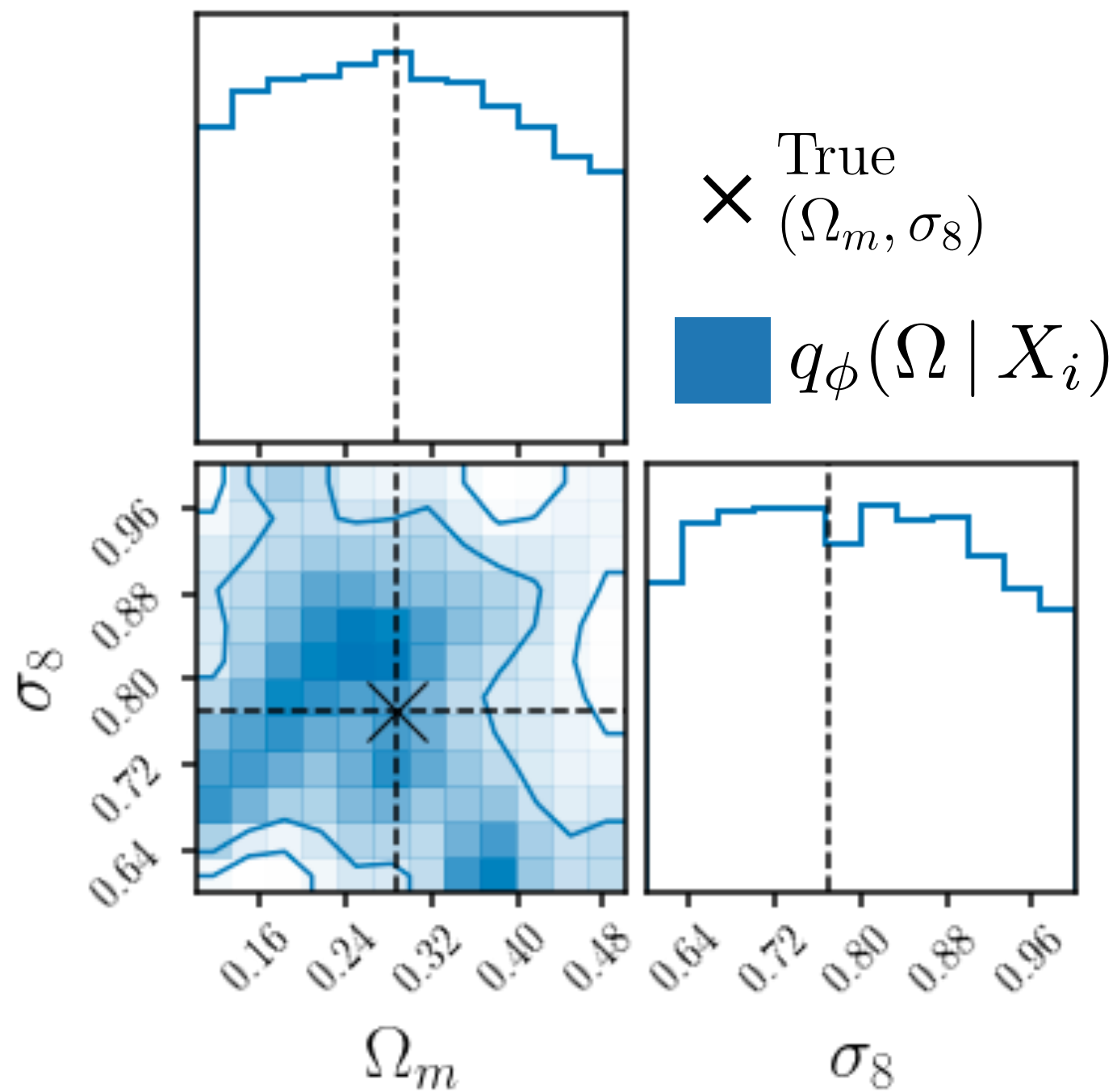


*trained  
normalizing flow  $q_\phi$*

$$p(\Omega | X_i) \approx q_\phi(\Omega | X_i) \text{ validation}$$

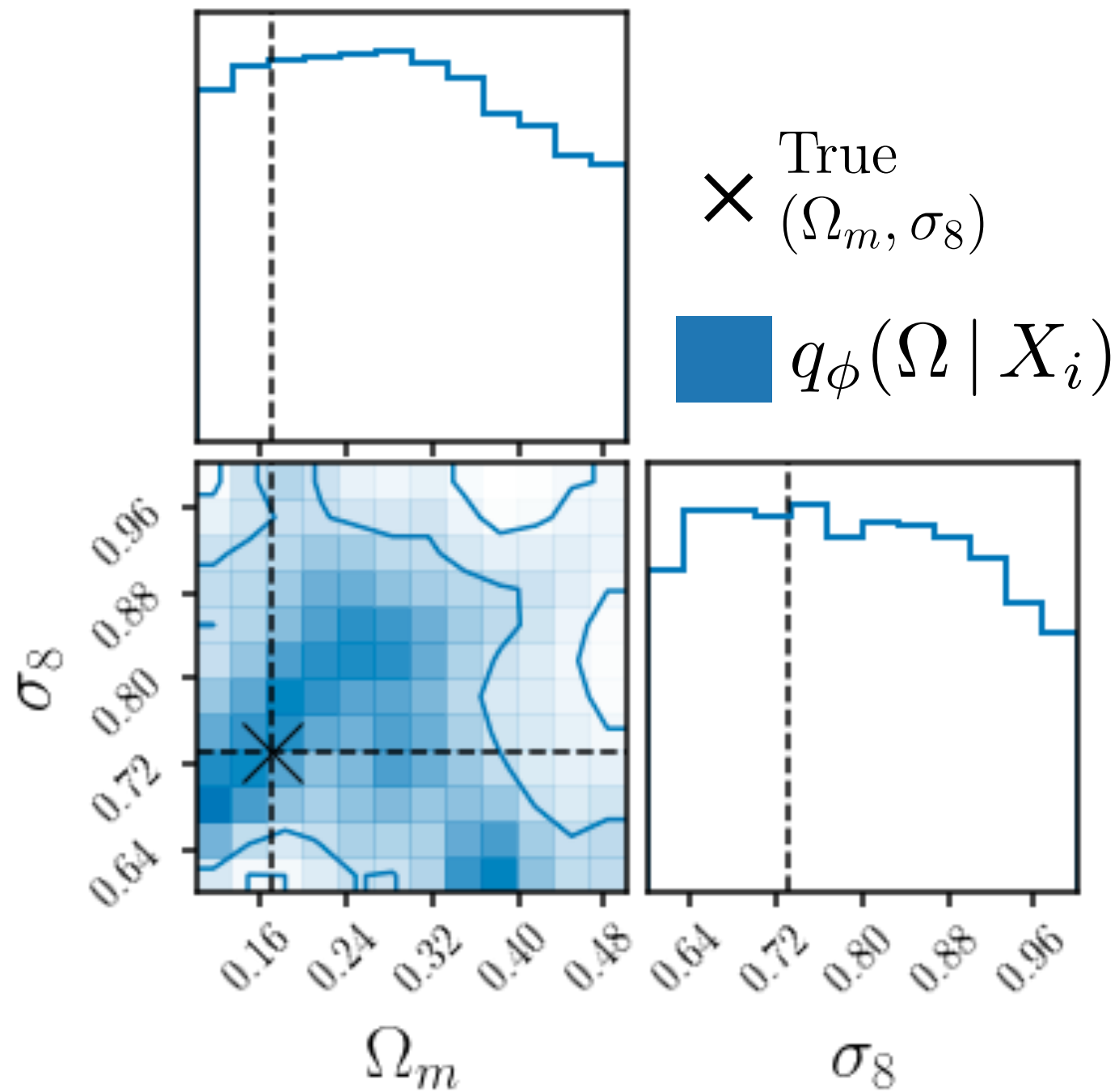


$$p(\Omega | X_i) \approx q_\phi(\Omega | X_i) \text{ validation}$$

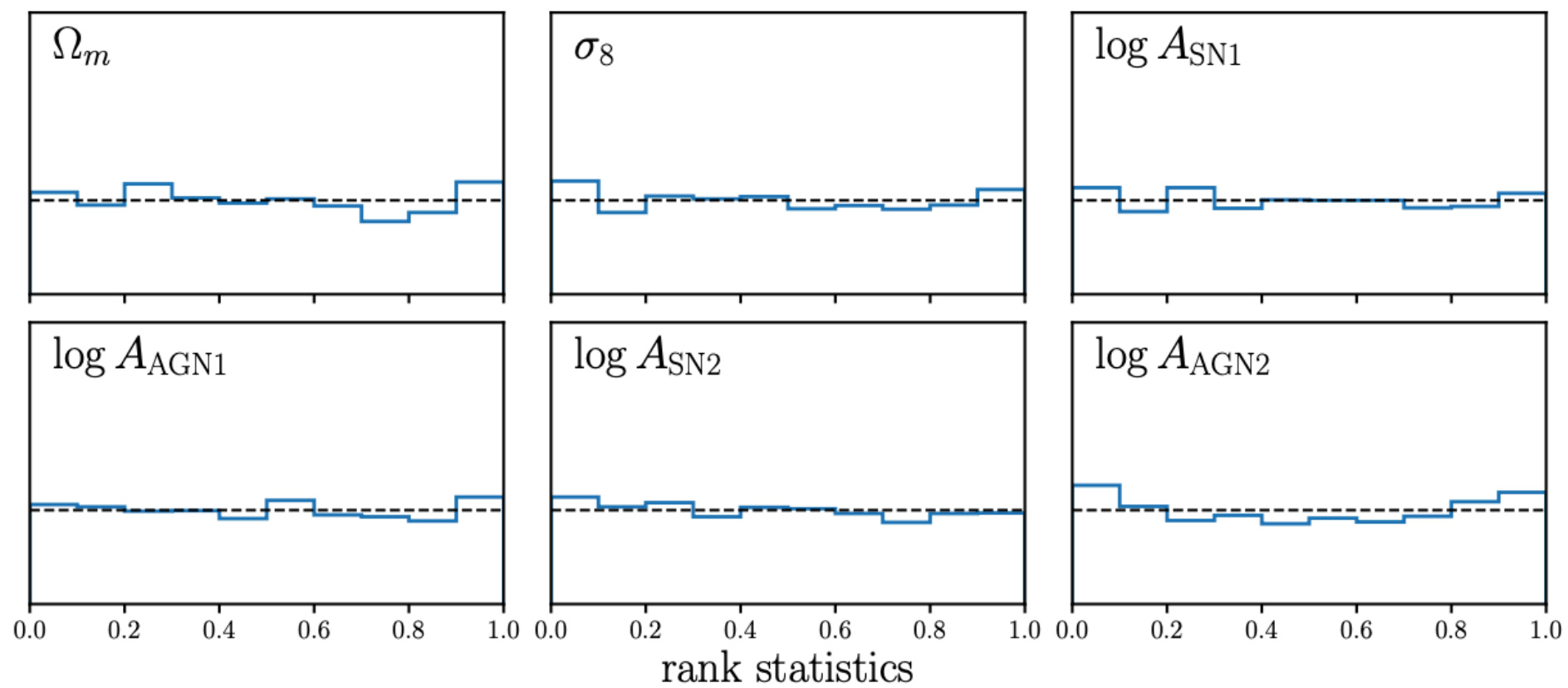




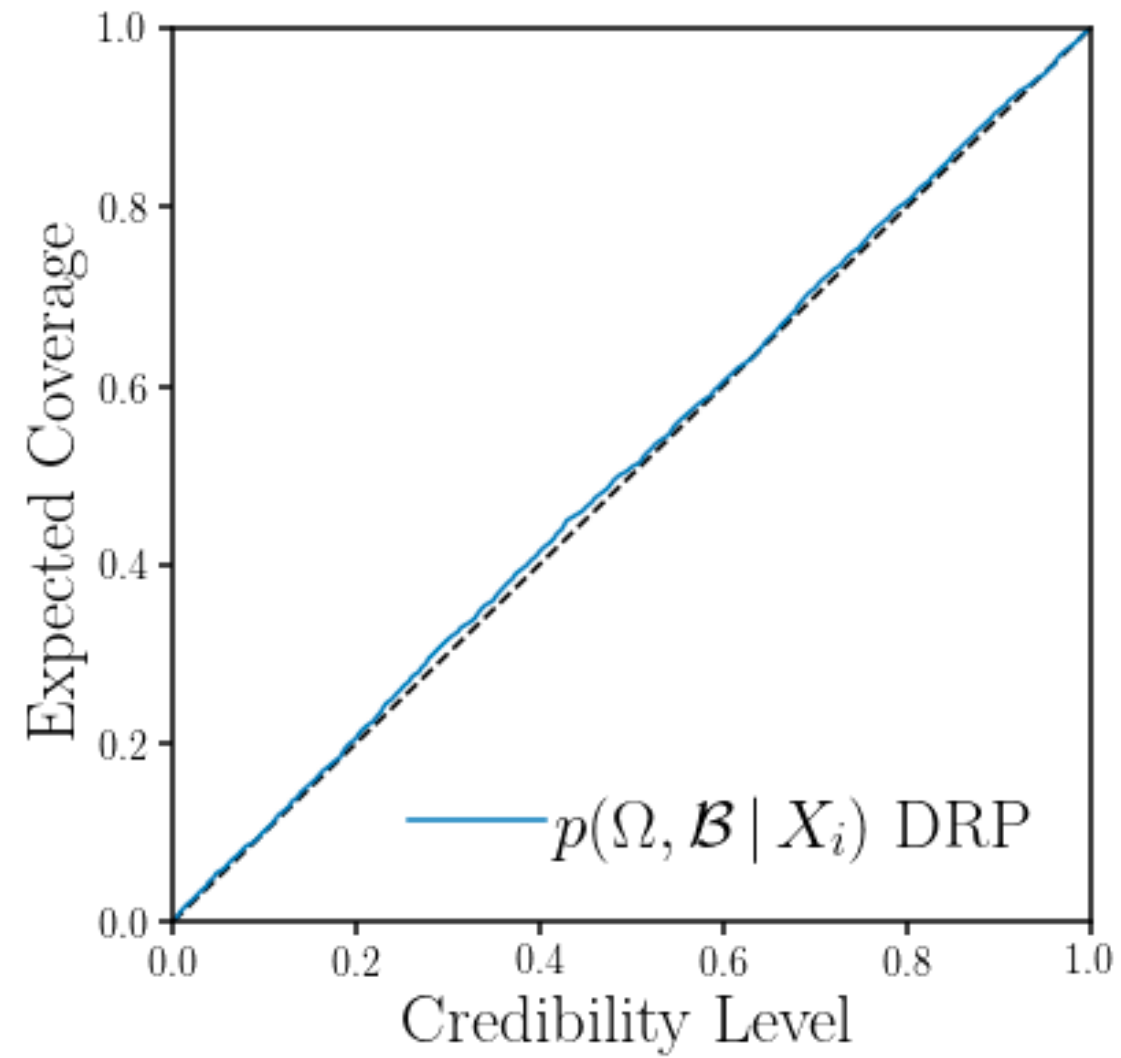
$$p(\Omega | X_i) \approx q_\phi(\Omega | X_i) \text{ validation}$$



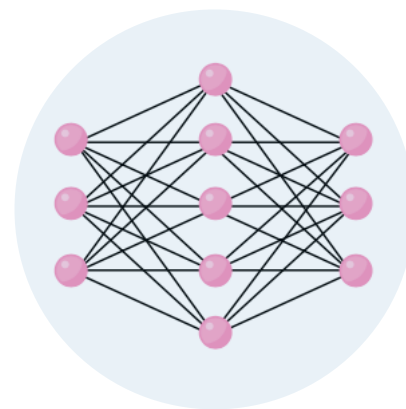
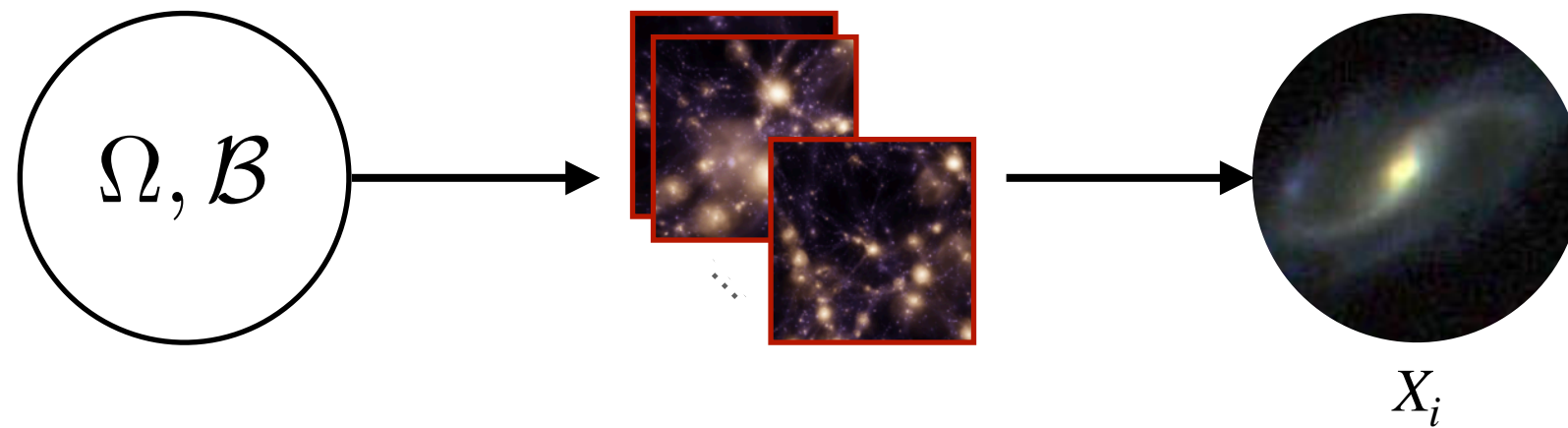
$p(\Omega | X_i) \approx q_\phi(\Omega | X_i)$  validation: **coverage tests**



$p(\Omega | X_i) \approx q_\phi(\Omega | X_i)$  validation: **coverage tests**

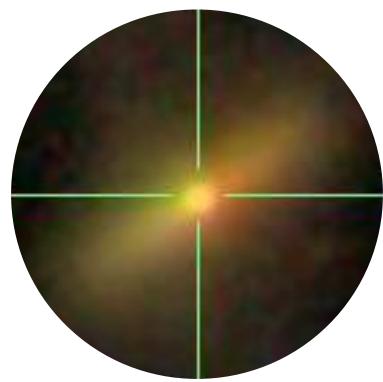
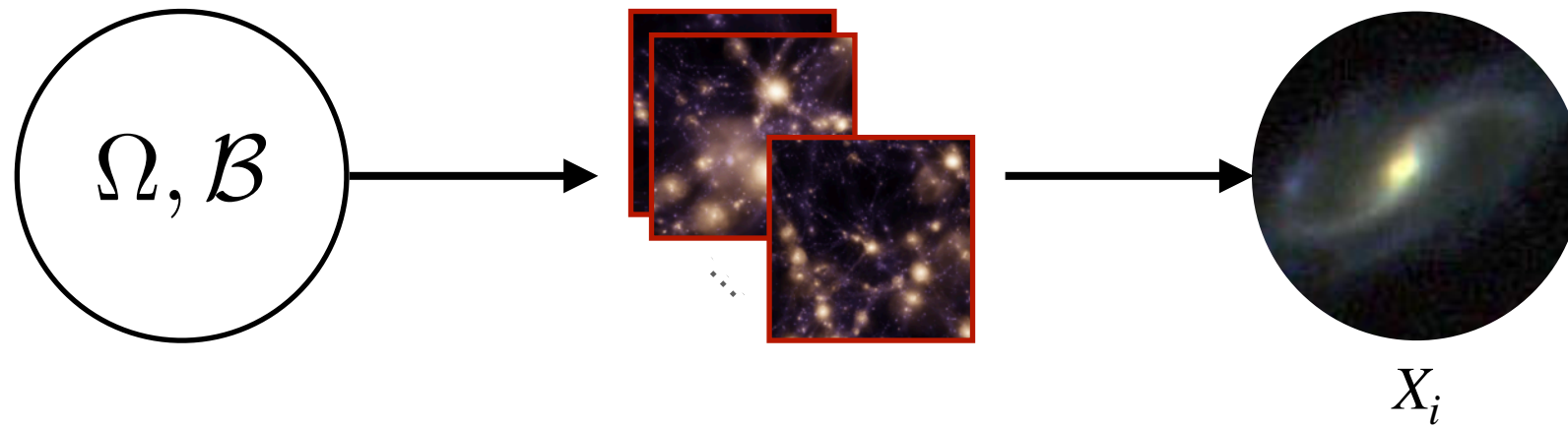


**CAMELS**  $\{(\Omega', \mathcal{B}', X')\} \sim p(\Omega, \mathcal{B}, X)$

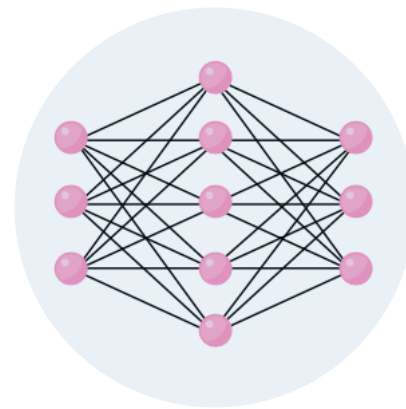


*validated  
normalizing flow  $q_\phi$*

**CAMELS**  $\{(\Omega', \mathcal{B}', X')\} \sim p(\Omega, \mathcal{B}, X)$

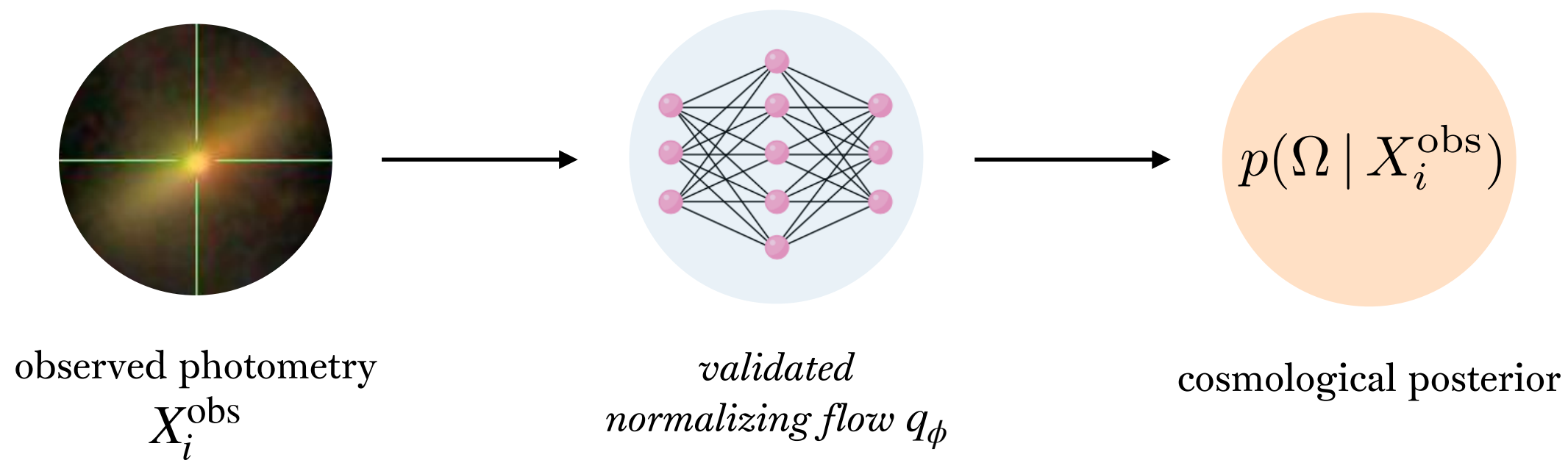
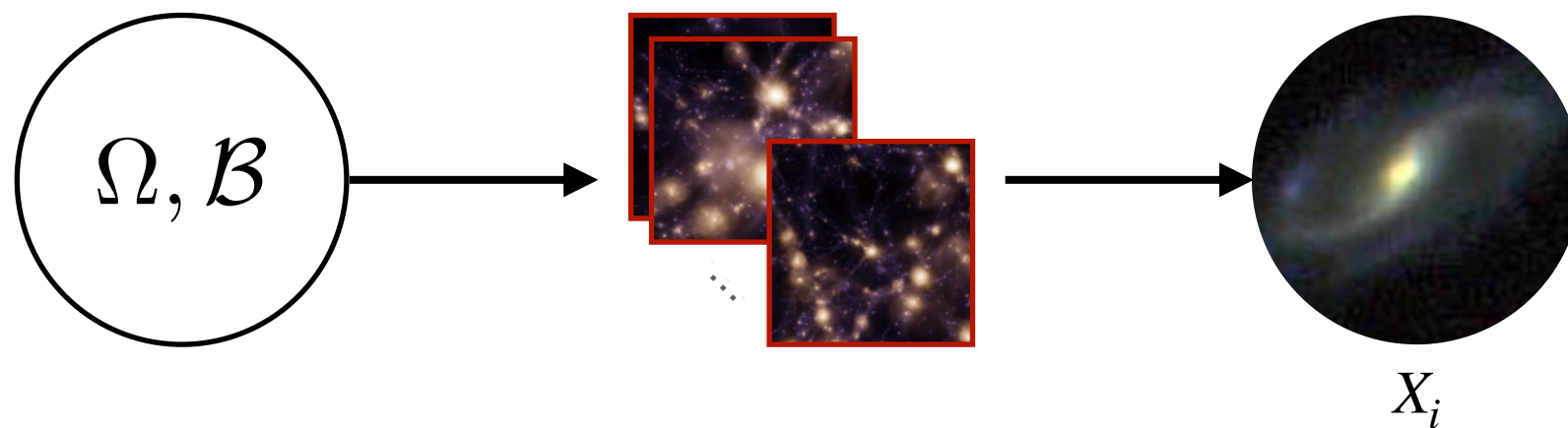


observed photometry  
 $X_i^{\text{obs}}$

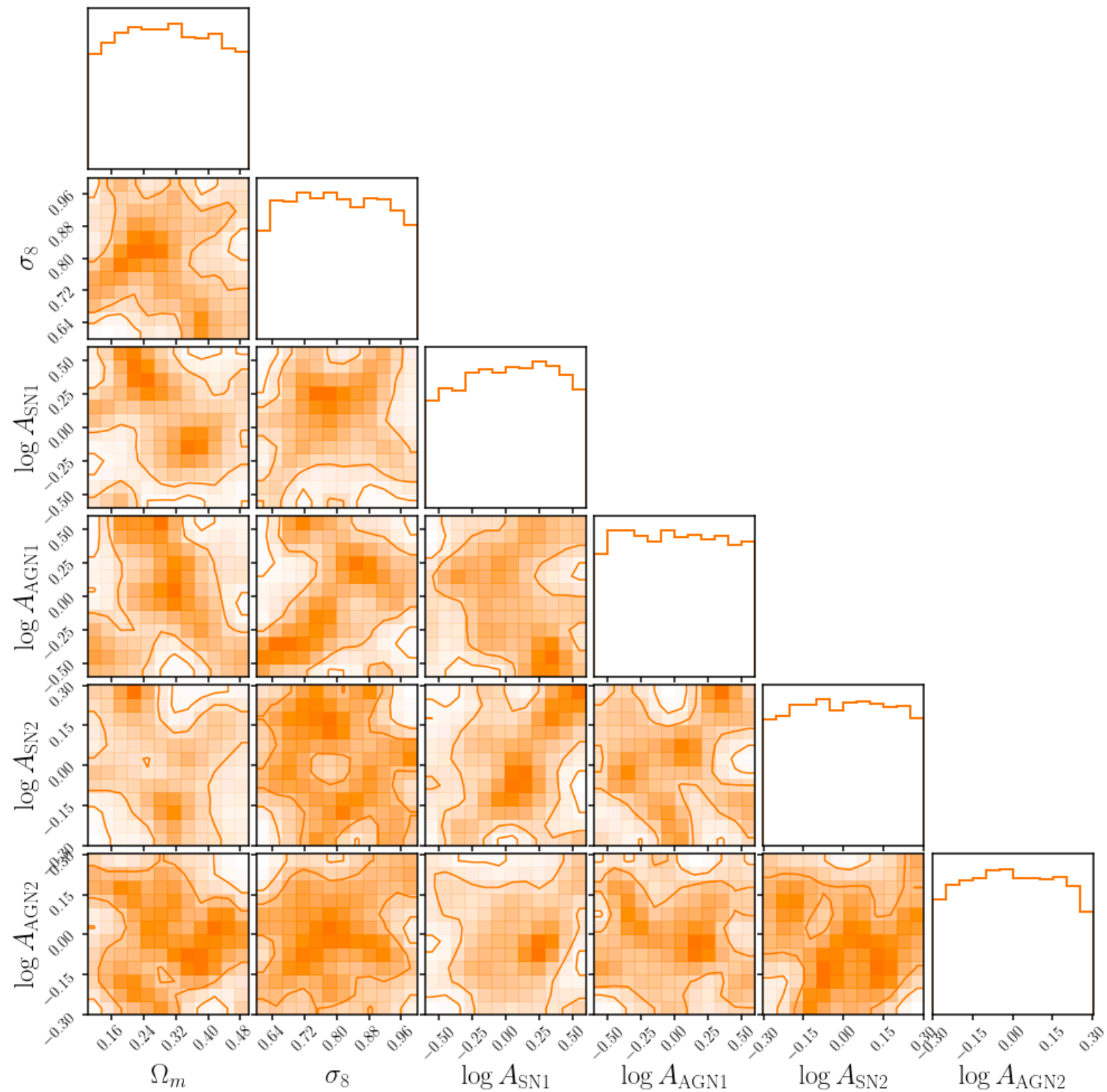


*validated*  
*normalizing flow*  $q_\phi$

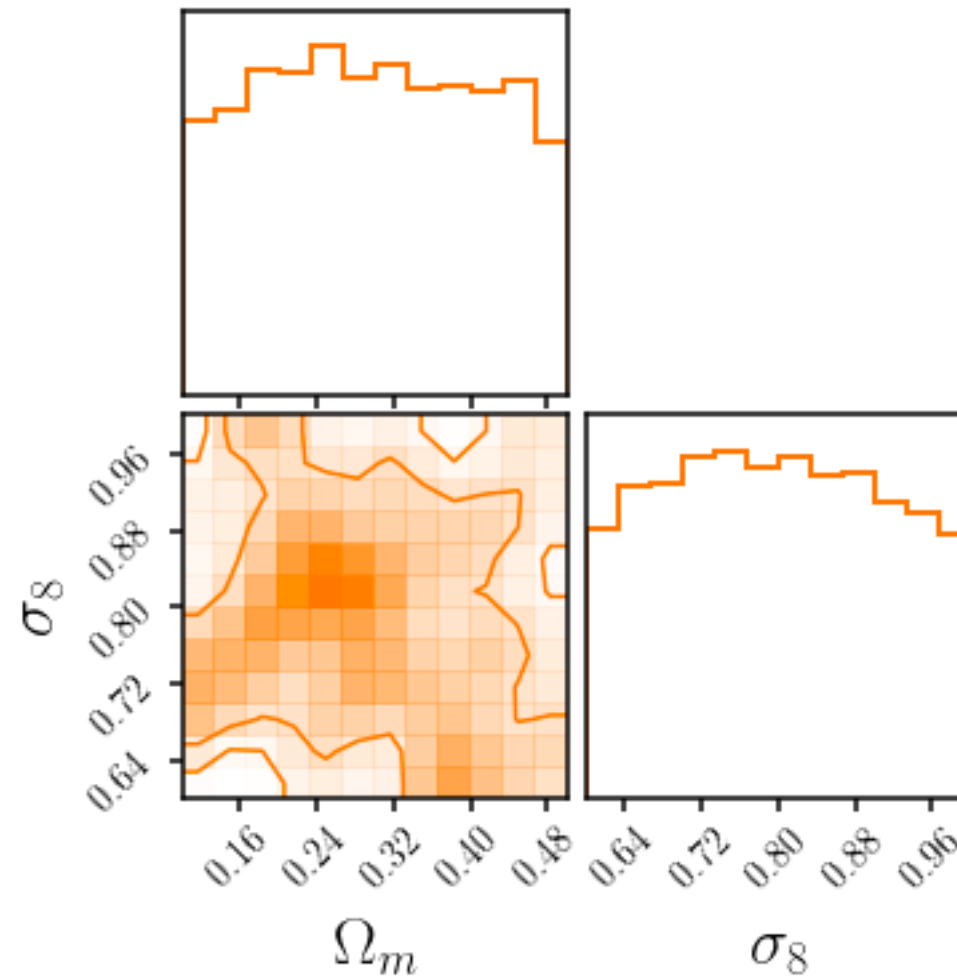
**CAMELS**  $\{(\Omega', \mathcal{B}', X')\} \sim p(\Omega, \mathcal{B}, X)$



$p(\Omega, \mathcal{B} | X_i) \approx q_\phi(\Omega, \mathcal{B} | X_i)$  from *griz* optical photometry of a **single SDSS galaxy**



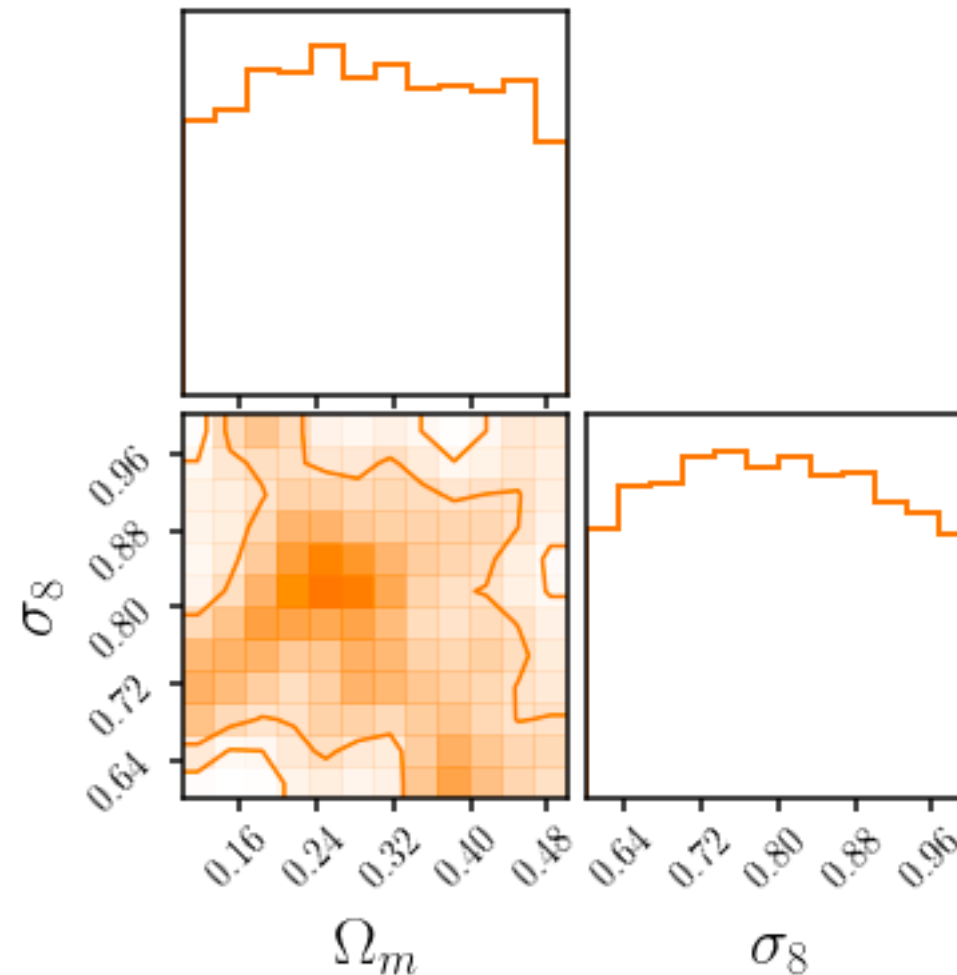
$p(\Omega, \mathcal{B} | X_i) \approx q_\phi(\Omega, \mathcal{B} | X_i)$  from *griz* optical photometry of a **single SDSS galaxy**



photometry of a single galaxy contains *limited* cosmological information

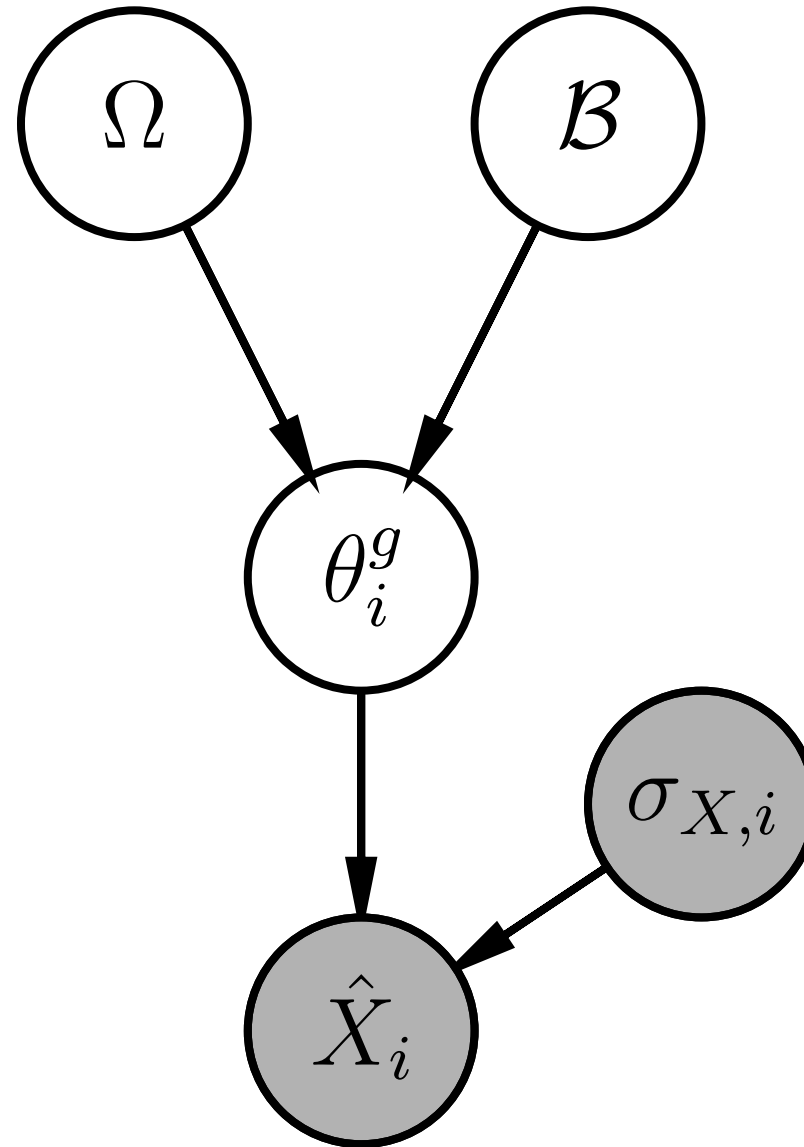


$p(\Omega, \mathcal{B} | X_i) \approx q_\phi(\Omega, \mathcal{B} | X_i)$  from *griz* optical photometry of a **single SDSS galaxy**

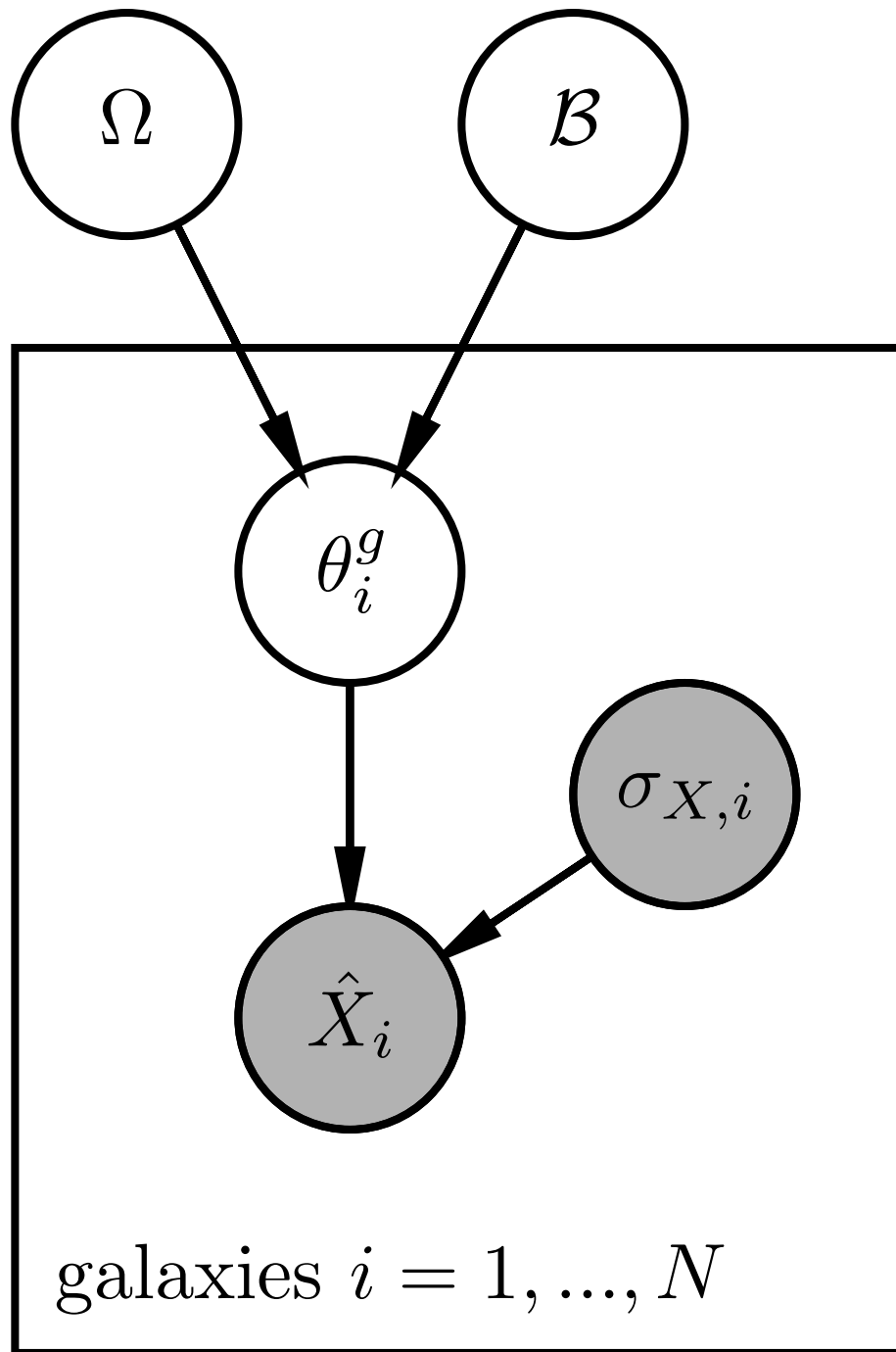


photometry of a single galaxy contains *limited* cosmological information

*but not zero...*

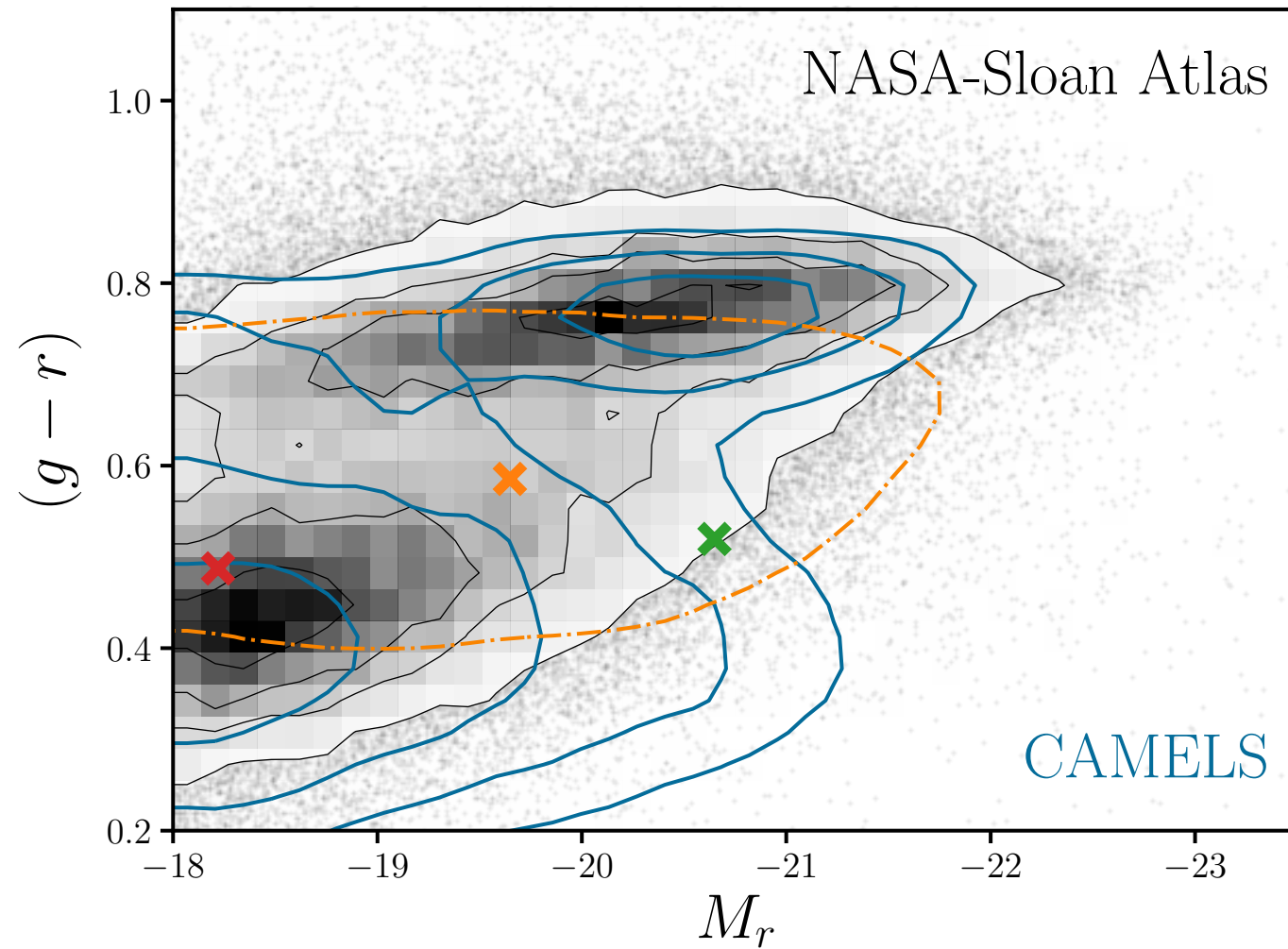


but we can combine the constraining power of *many* galaxies using **hierarchical population inference**

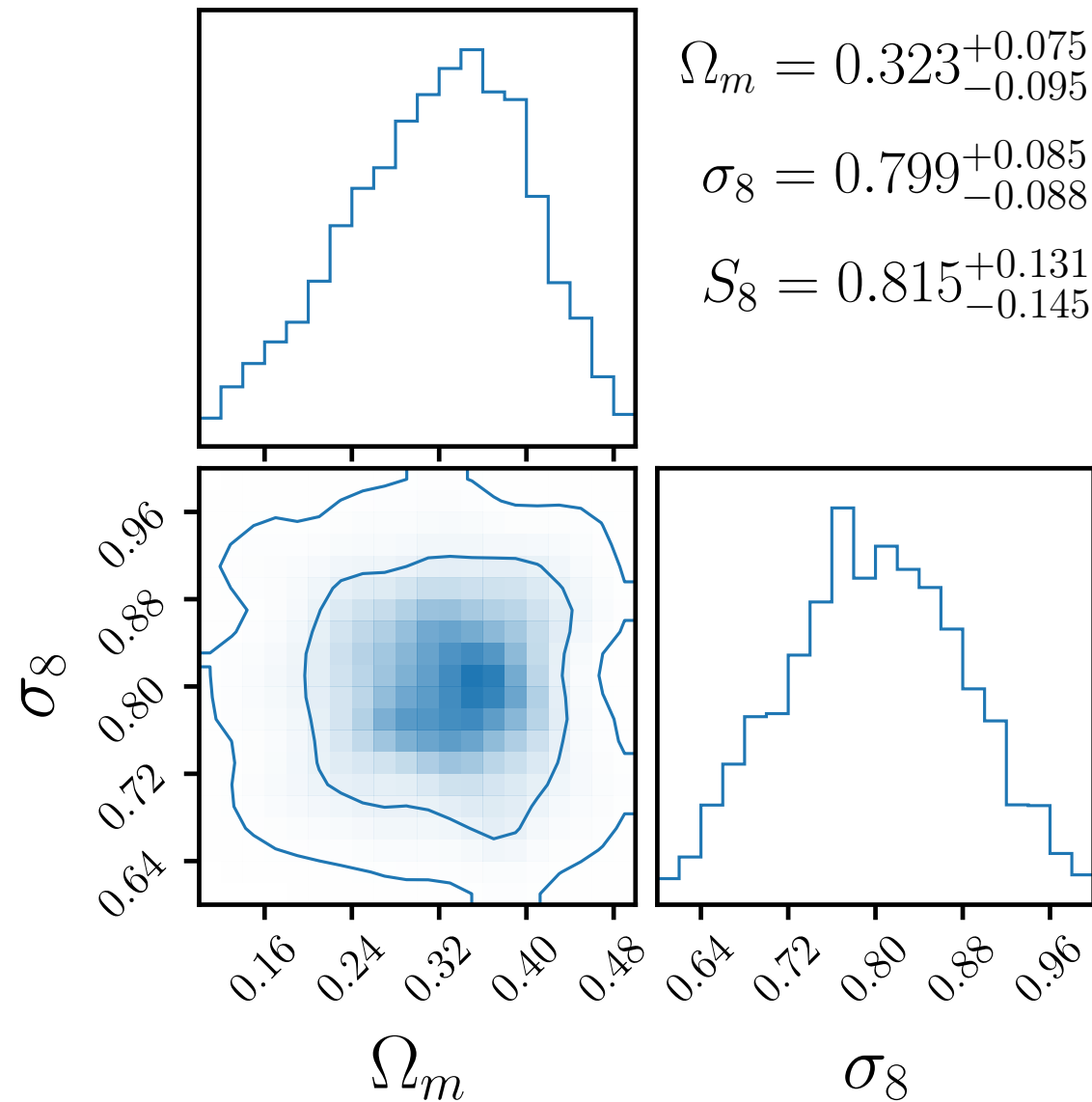


$$p(\Omega, \mathcal{B} \mid \{X_i\}) = p(\Omega, \mathcal{B})^{-(N-1)} \prod_{i=1}^N p(\Omega, \mathcal{B} \mid X_i)$$

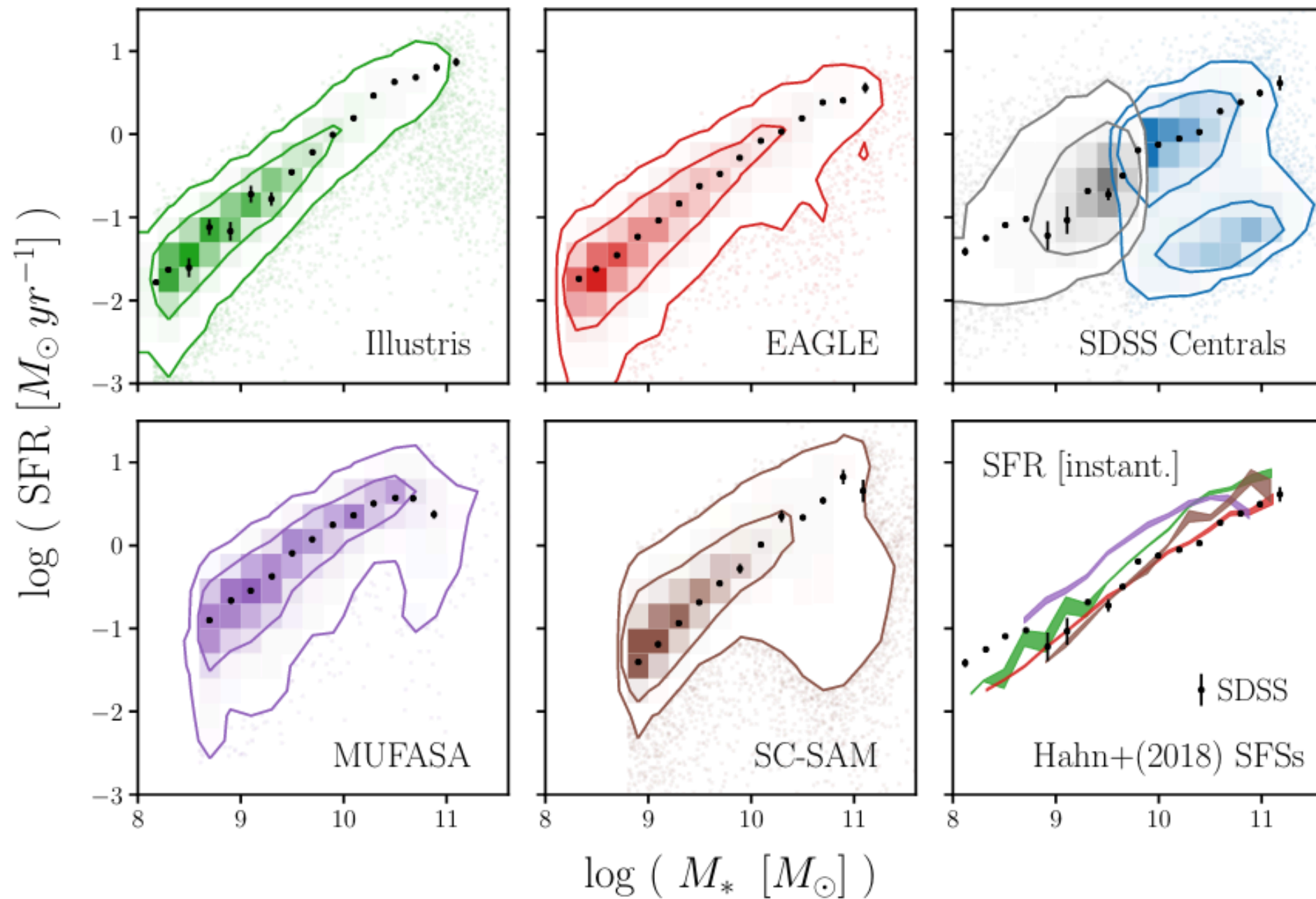
$N = 22,338$  galaxies from the NASA-Sloan Atlas



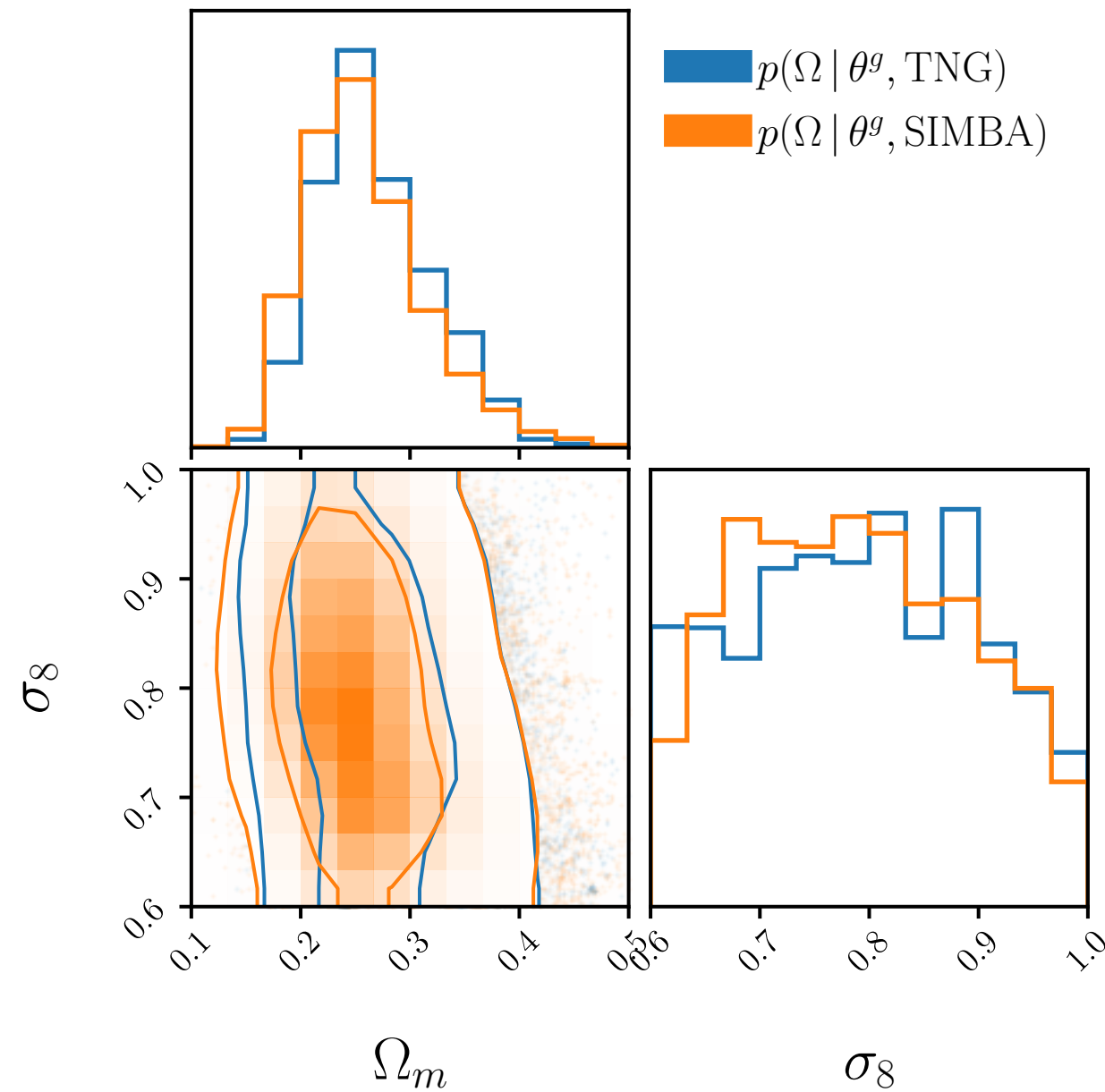
cosmological constraints from *only* the observed photometry of  
22,338 NASA-Sloan Atlas galaxies



*caveat:* we assume a **galaxy formation model** (TNG) and an SED model



control regions: we can choose galaxy populations most *robust* to galaxy formation models — e.g. star-forming galaxy with  $M_* \sim 10^{9.5} M_\odot$



*caveat:* we assume a galaxy formation model (TNG) and an **SED model**

$$f_{\lambda} = \int_{t'=0}^{t'=t} \text{SFR}(t') f_{\text{SSP}}(t', Z(t')) e^{-\tau_{\text{dust}}(t')} dt'$$



control regions: we can choose galaxy populations most *robust* to SED models

$$f_{\lambda} = \int_{t'=0}^{t'=t} \text{SFR}(t') \underbrace{f_{\text{SSP}}(t', Z(t'))}_{\substack{\text{stellar evolution theory} + \\ \text{stellar spectral libraries} + \\ \text{initial mass function}}} e^{-\tau_{\text{dust}}(t')} dt'$$

focus on galaxies with *well-established IMF*

control regions: we can choose galaxy populations most *robust* to SED models

$$f_{\lambda} = \int_{t'=0}^{t'=t} \text{SFR}(t') f_{\text{SSP}}(t', Z(t')) \underline{e^{-\tau_{\text{dust}}(t')}} dt'$$

*dust attenuation curve,  
star-to-dust geometry*

focus on galaxies with *well-established IMF, with low WISE IR emission*

*we can be picky!* — DESI and PFS will observe >40 million galaxies

**DESI Bright Galaxy Survey** (*Hahn et al. 2023c*):  
a  $r < 19.5$  magnitude-limited sample of >10 million galaxies



## summary

the photometry of a single galaxy contains *some* cosmological information

with *neural density estimation, hierarchical population inference, and CAMELS*  
we can exploit this information from *thousands of galaxies*

*control regions*: we can target galaxy populations most ***robust*** to galaxy and SED modeling

**DESI Bright Galaxy Survey** will soon observe a diverse magnitude-limited sample of *>10 million galaxies* to choose from