

Today's Universe

The Early Universe

# Tensions in Cosmology

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*Les Houches summer school  
July, 28th & 29th 2025*



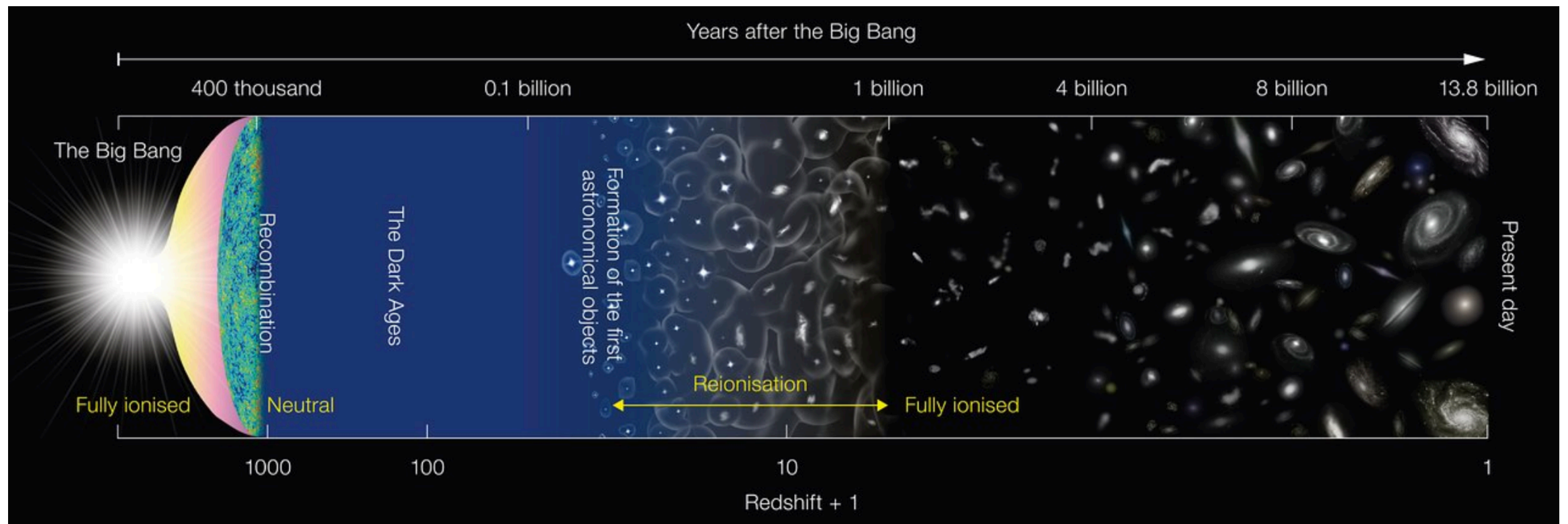
European Research Council  
Established by the European Commission



# The Era of Precision Cosmology

## Astonishing success of $\Lambda$ CDM Cosmology: GR+ Cosmological Principle

$$\omega \equiv \Omega h^2, \quad H_0 = 100h \text{ km/s/Mpc} \quad \{H_0, \omega_b, \omega_{\text{cdm}}, A_s, n_s, \tau_{\text{reio}}\} \quad \Omega_\Lambda = 1 - \Omega_m$$





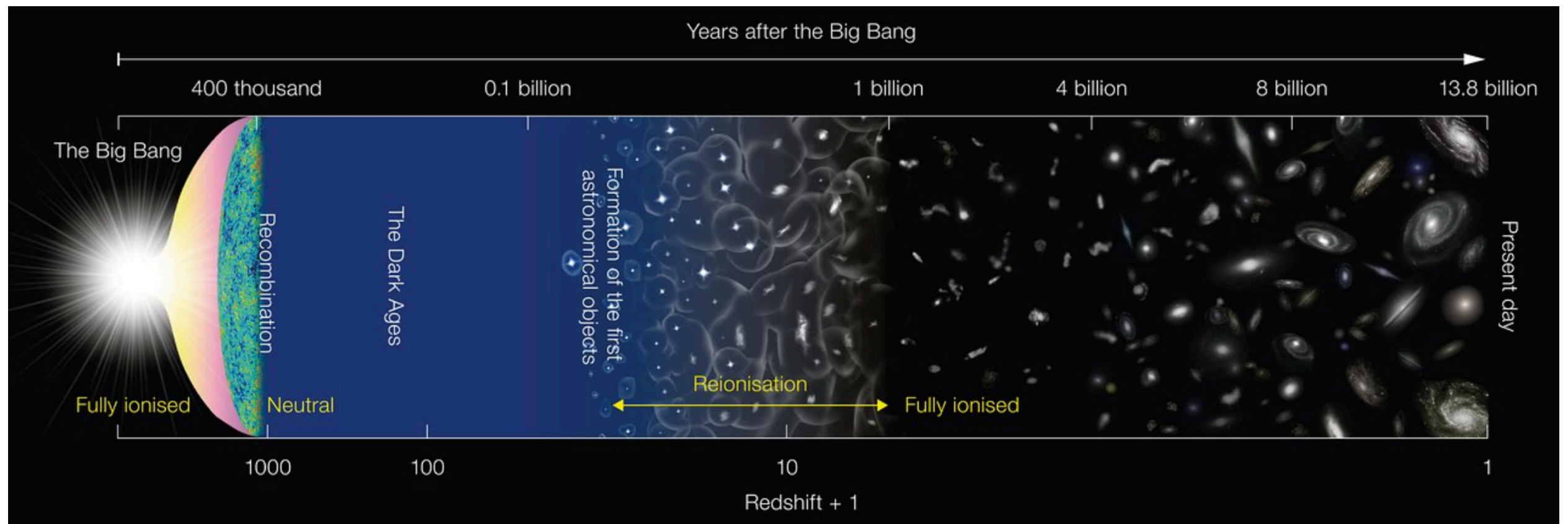
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Expansion/Energy  
content





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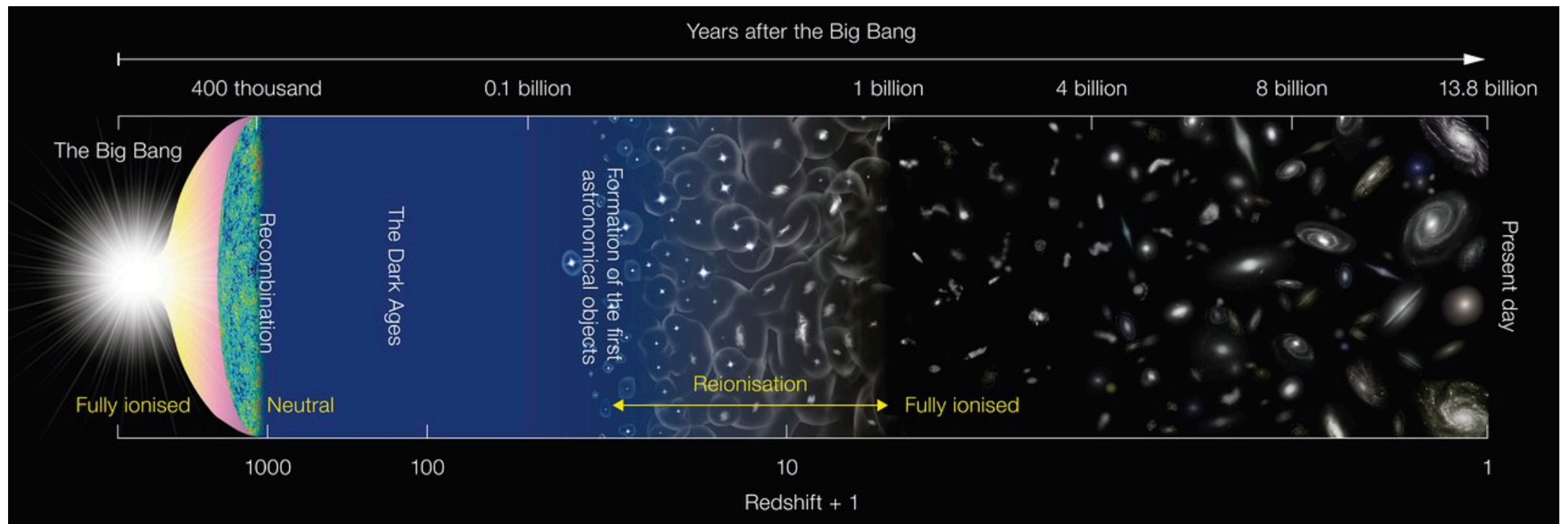
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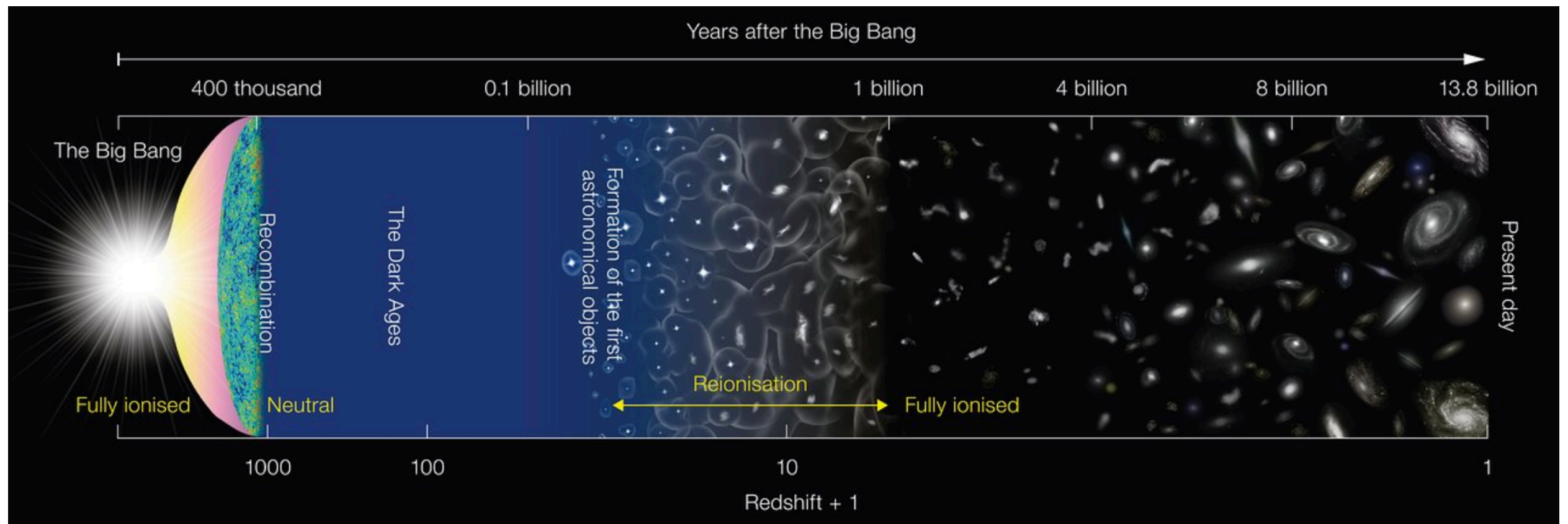
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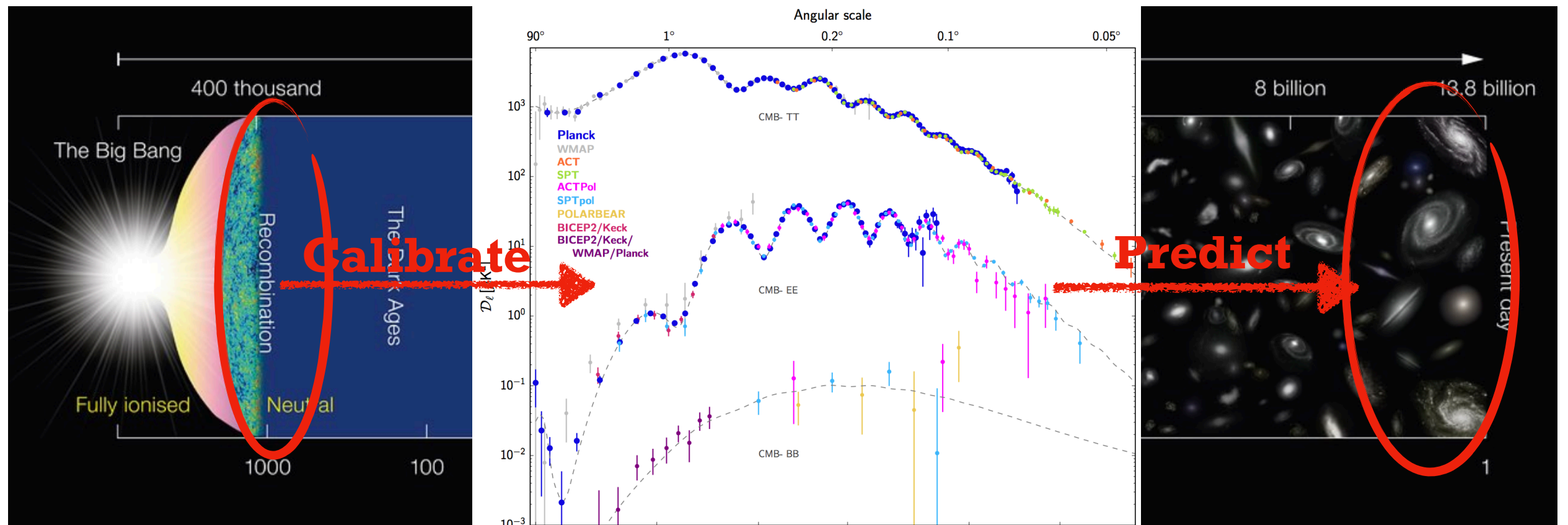
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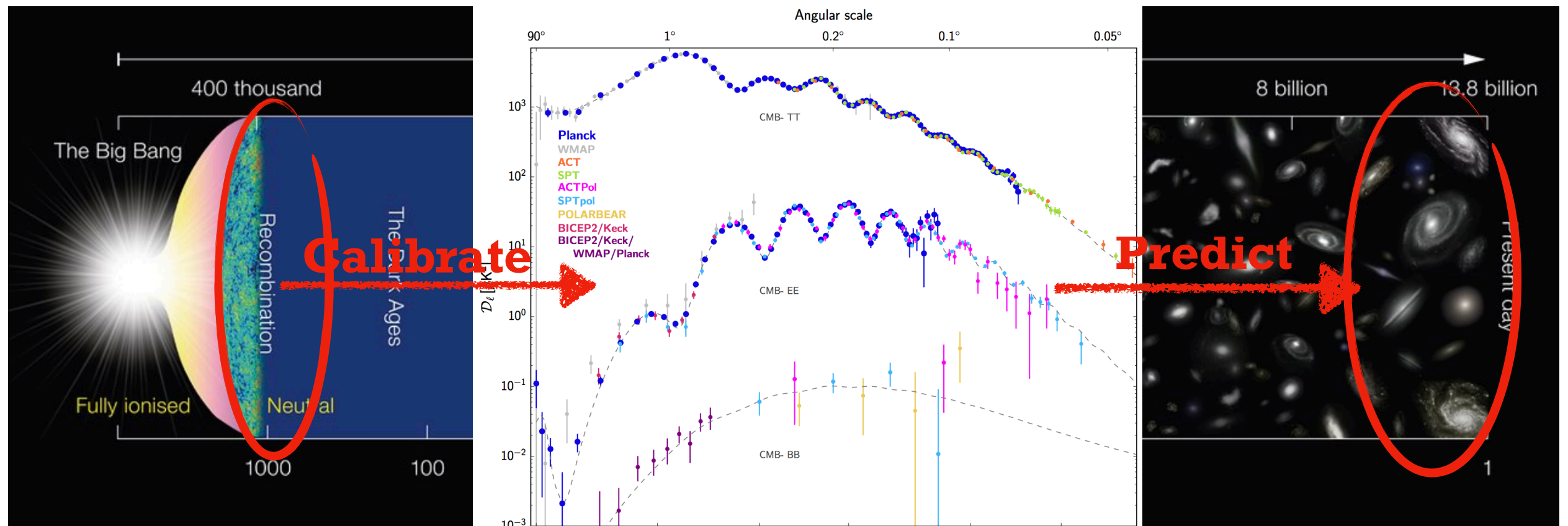
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95% of the energy budget today is unknown! 70% Dark Energy, 25% Dark Matter.



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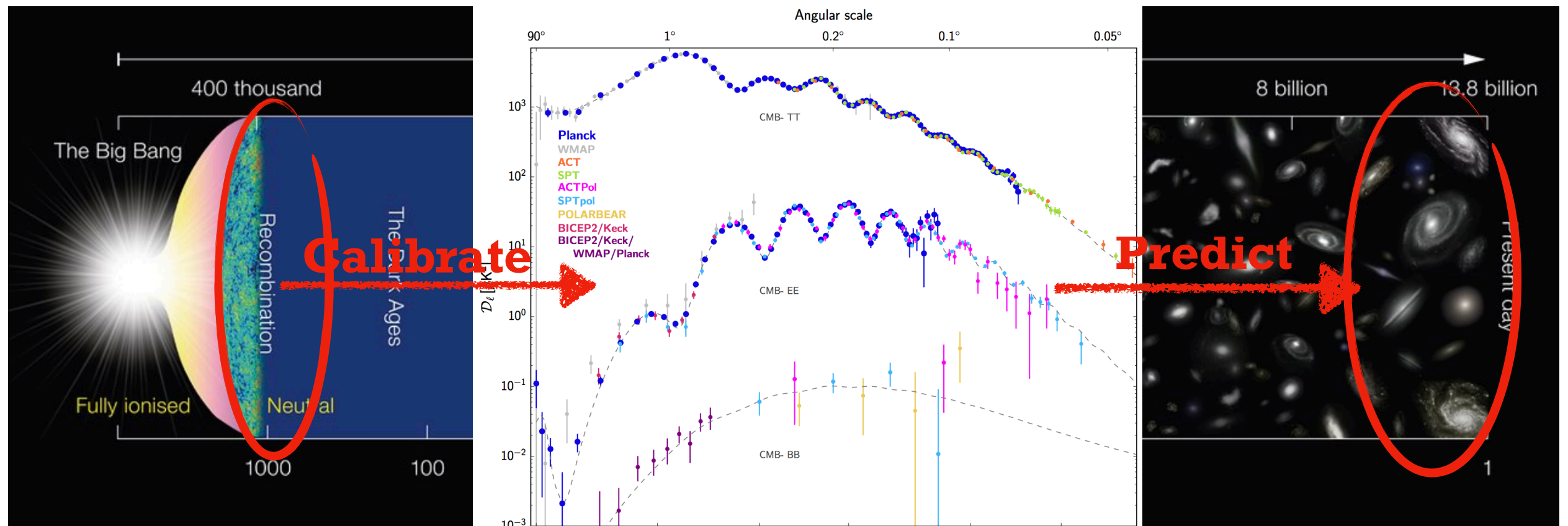
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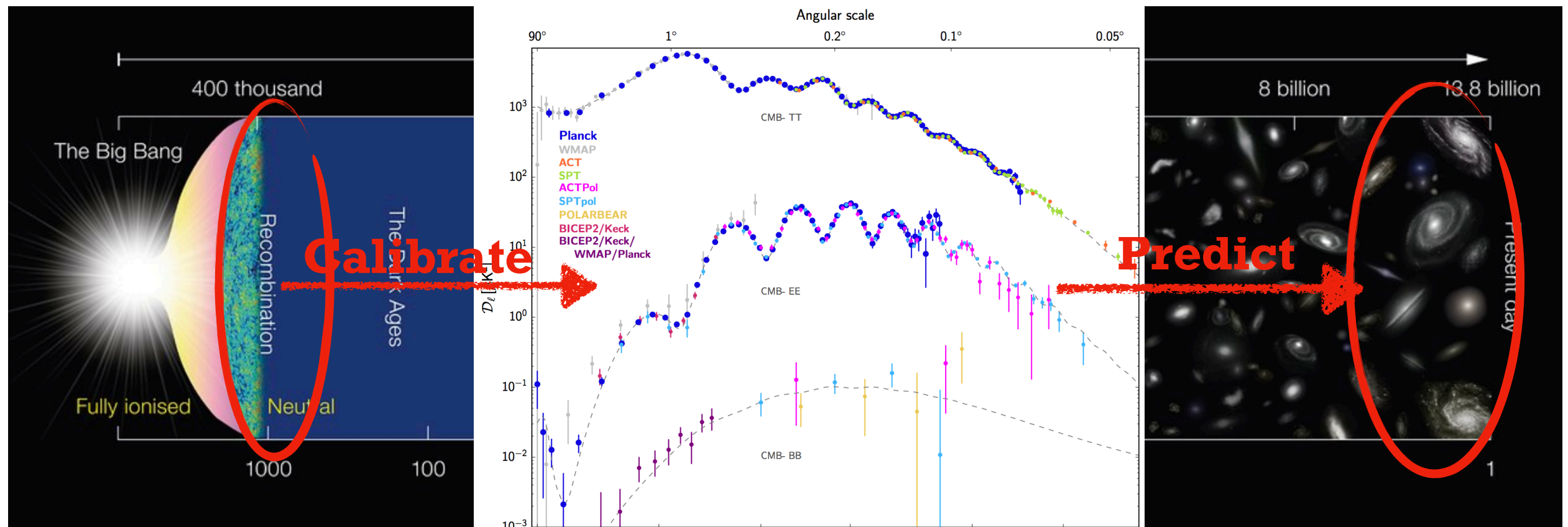
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95% of the energy budget today is unknown! 70% Dark Energy, 25% Dark Matter.

The mechanism behind initial conditions is unknown.

How star formation happened and re-ionized the universe is unknown.



# Precision Cosmology or Cosmic Discordance?

## The $\Lambda$ CDM Cosmology is under extreme pressure

- Cosmic dipole anomaly? **The universe is not isotropic?**

*Colin++ 1703.09376, 1808.04597, Secrest++ 2009.14826, Alari++ 2207.05765, Guandalin++ 2212.04925*

- Cosmic void? **The universe is not locally homogeneous?**

*Wu&Huterer 1706.09723, Kenworthy++ 1901.08681, Cai++ 2012.08292, Camarena++ 2205.05422*

- **Tensions** in cosmological parameters?

*Abdalla++ 2203.06142*

- Anomalies in CMB data? **Evidence for a curved universe?**

*Di Valentino++ 1911.02087, Calderón++ 2302.14300*

- Hints of **dynamical dark energy and negative neutrino masses?**

*Union3 2311.12098, DES 2401.02929, DESI 2404.03002*

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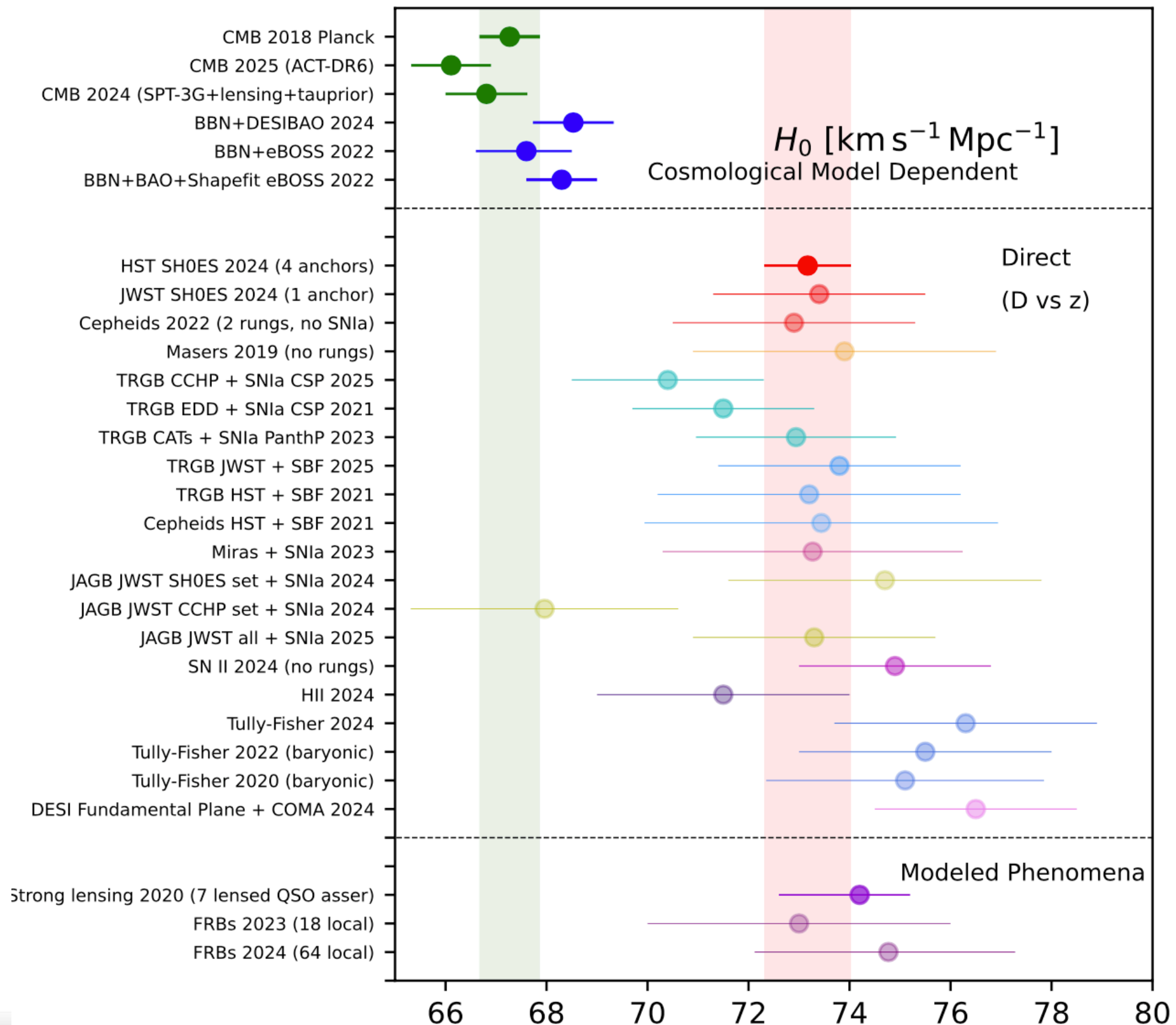
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**Is this a sign of a break down in the cosmological principle or GR?**

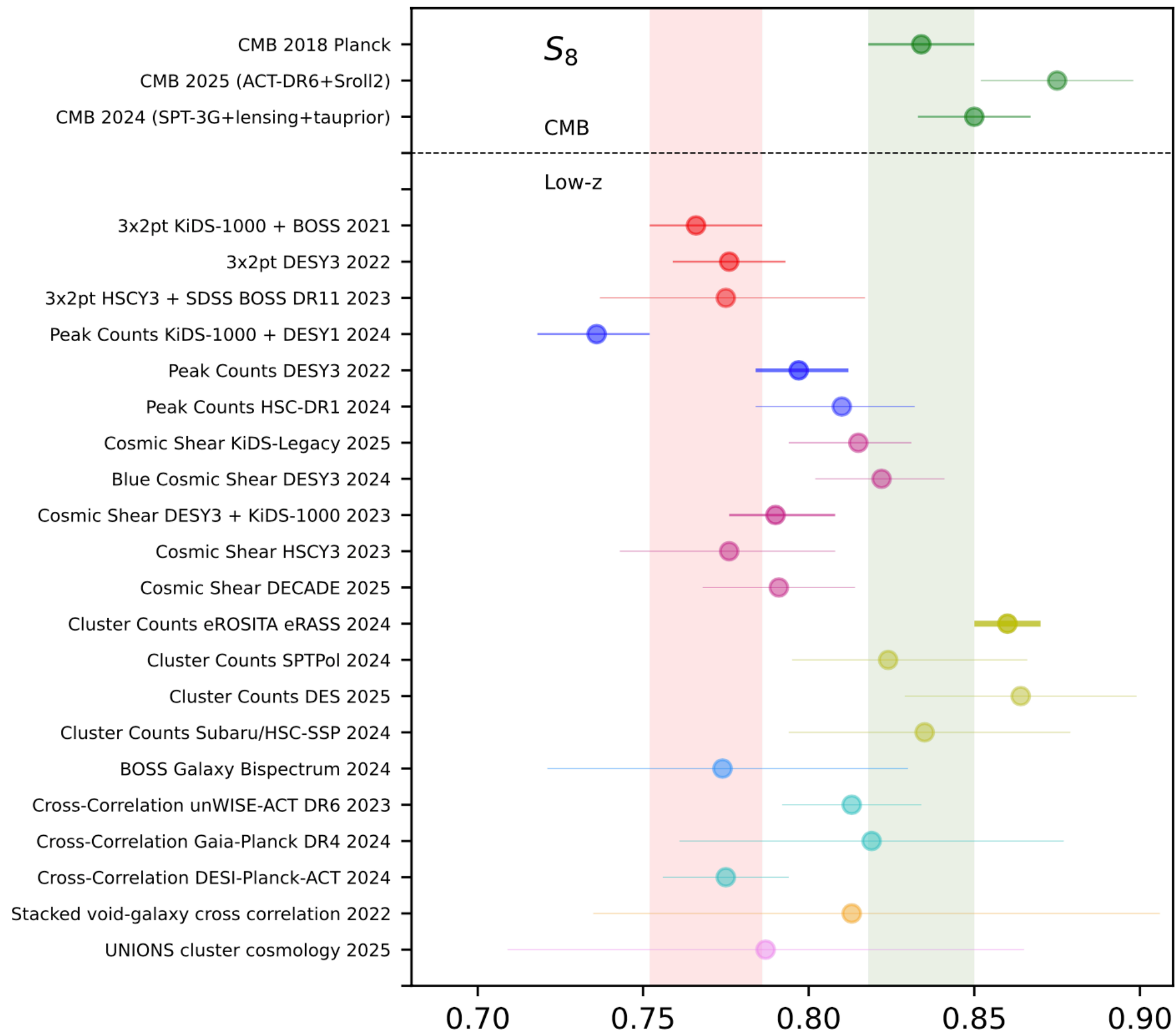
**Are these the first signs of the true nature of DM and DE?**



# The Hubble tension



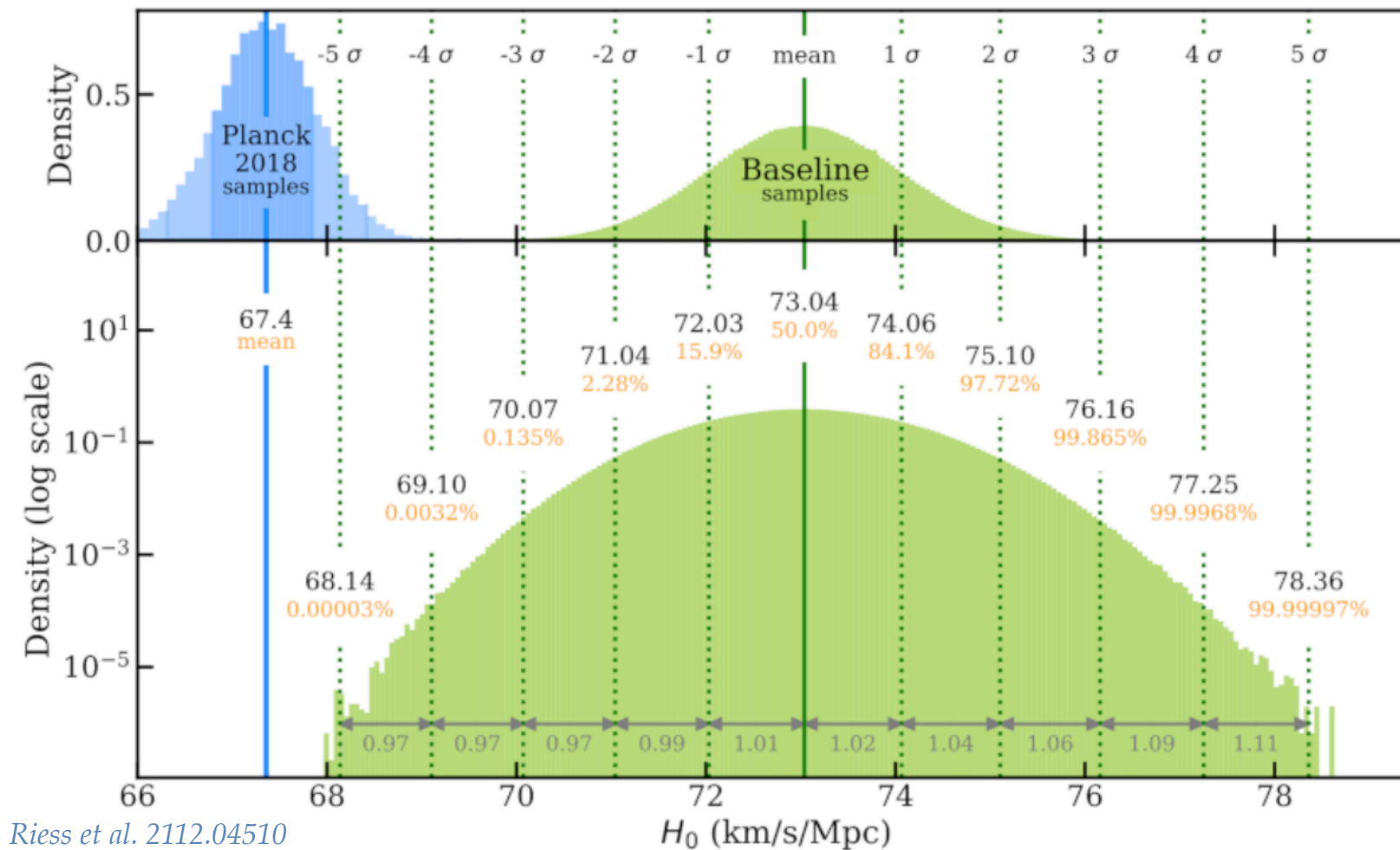
# The S8 tension





# The Hubble tension between SH0ES & *Planck*

There is a  $5\sigma$  discrepancy between the SH0ES and *Planck* determination of the Hubble parameter

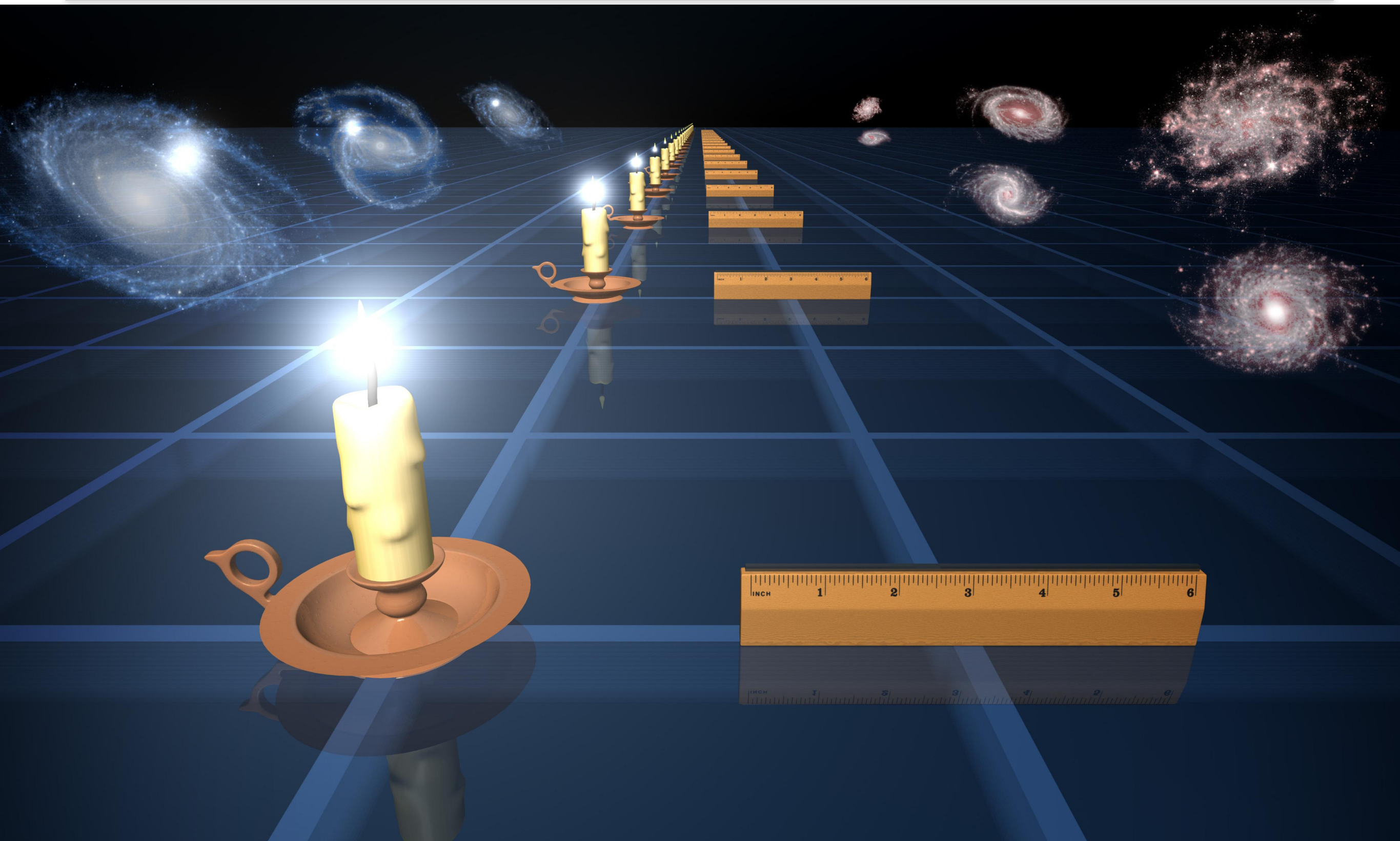


$$H_0(\Lambda\text{CDM}/\text{Planck}) = 67.4 \pm 0.5 \text{ km/s/Mpc}$$

$$H_0(\text{SH0ES}) = 73.04 \pm 1.04 \text{ km/s/Mpc}$$

Is this first sign of a crack in  $\Lambda\text{CDM}$ ?

# Measuring distances in Cosmology





# A tension between luminosity and angular distance

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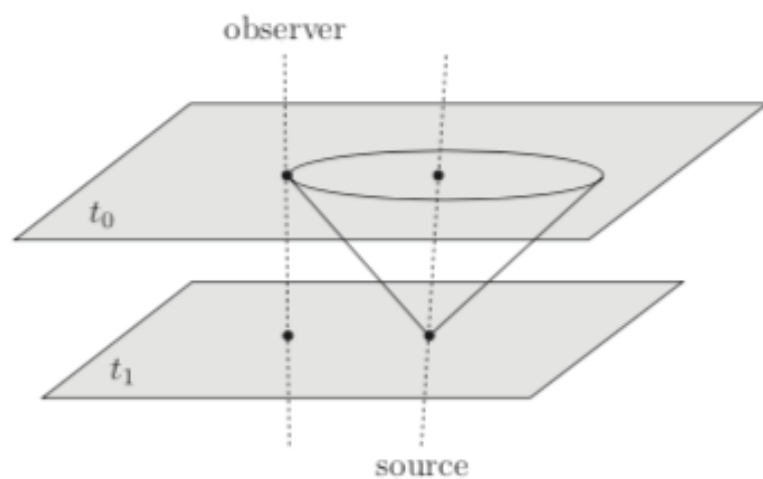
- The **comoving distance**  $\chi = \int_{t_e}^{t_0} \frac{dt}{a(t)} = \int_0^z \frac{dz}{H(z)}$  from imposing  $ds^2 = dt^2 - a^2 d\chi^2 = 0$

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- The **luminosity distance** to a source of known flux and luminosity

$$F = \frac{L}{4\pi d_L(a)^2} \quad d_L = \frac{\chi(a)}{a} = \chi(z)(1+z)$$



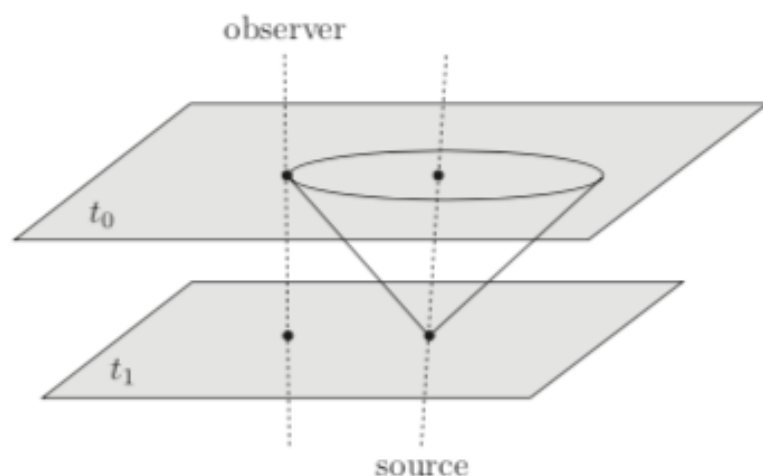


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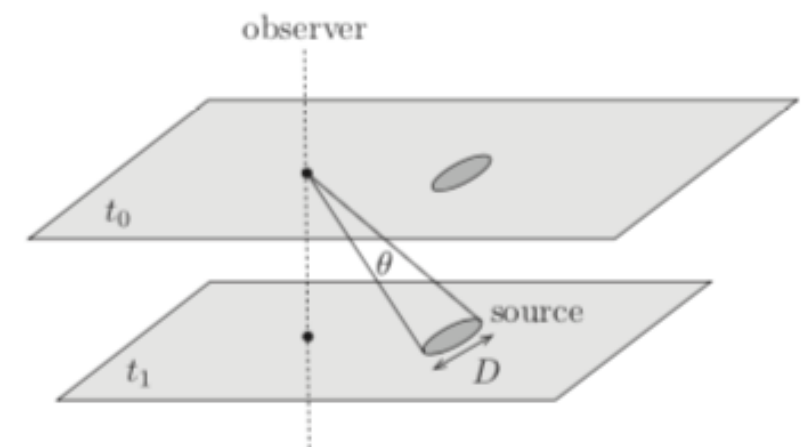
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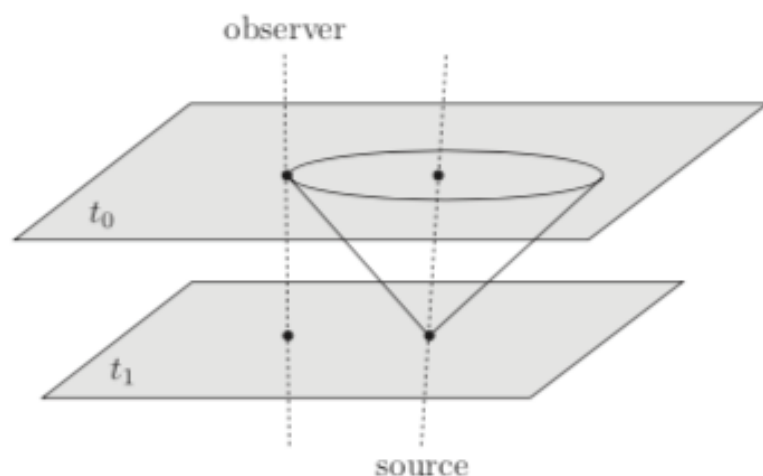


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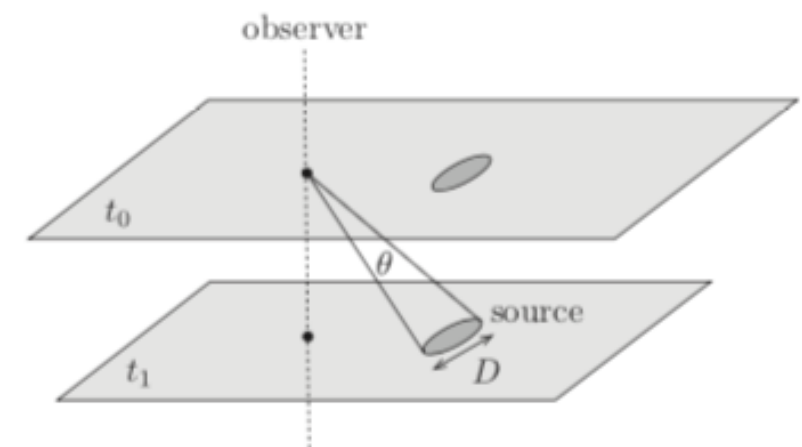
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$$d_A = d_L / (1+z)^2$$

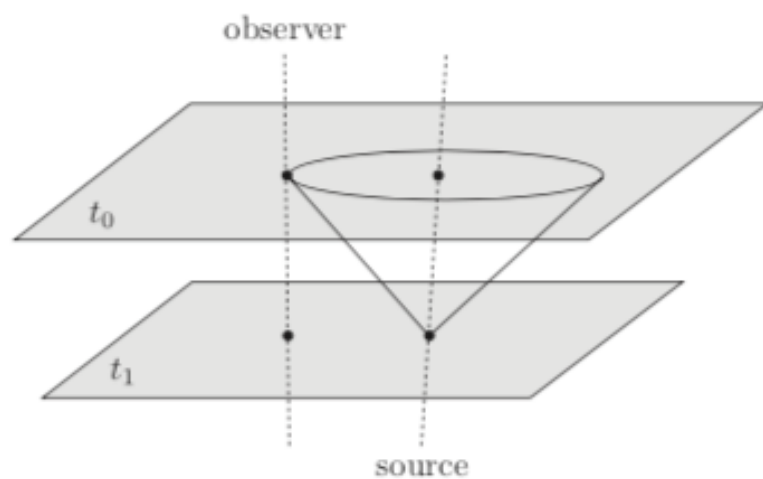
$$d_A = \frac{1}{1+z} \int_0^z \frac{dz}{H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_r(1+z)^4 + \Omega_\Lambda}}$$

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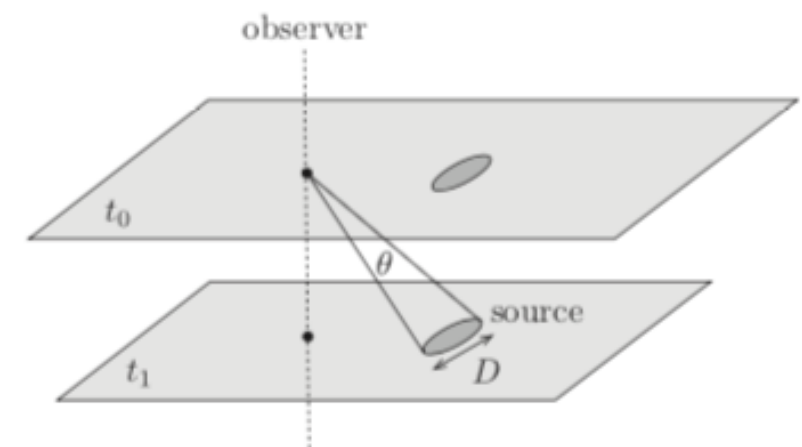
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Measuring  $H_0$  == measuring distances

Mismatch in  $H_0$  == wrong distance!



# The cosmic distance ladder

- **Standard candle:** Object of **known luminosity  $L$**

$$F = \frac{L}{4\pi D_L^2}$$

$$m \equiv -2.5 \log F + \text{const.}$$

$$M \equiv -2.5 \log F(10 \text{ pc}) + \text{const.}$$

$$m - M = 5 \log D_L [\text{Mpc}] + 25$$

$$*1 \text{ Mpc} = 3.2 \times 10^6 \text{ l.y.}$$

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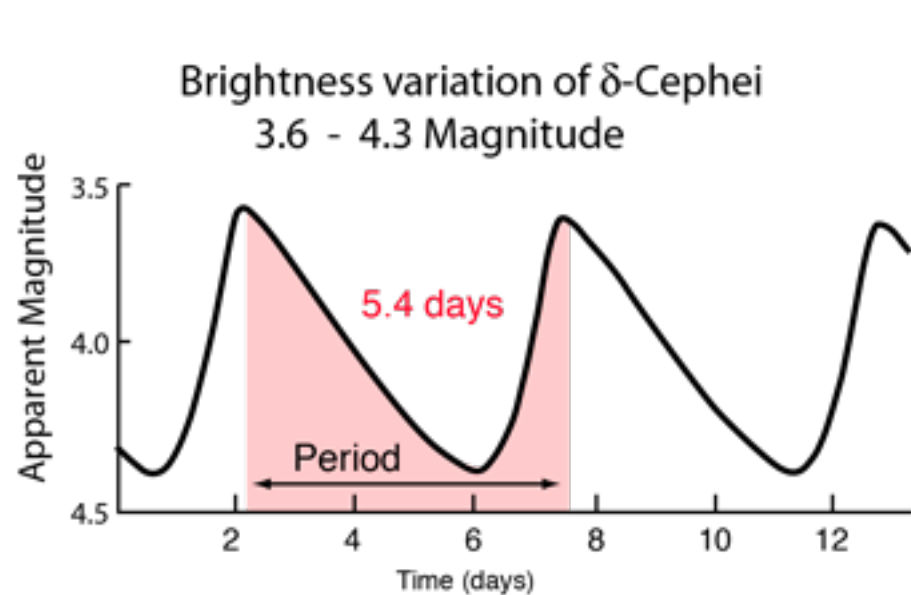
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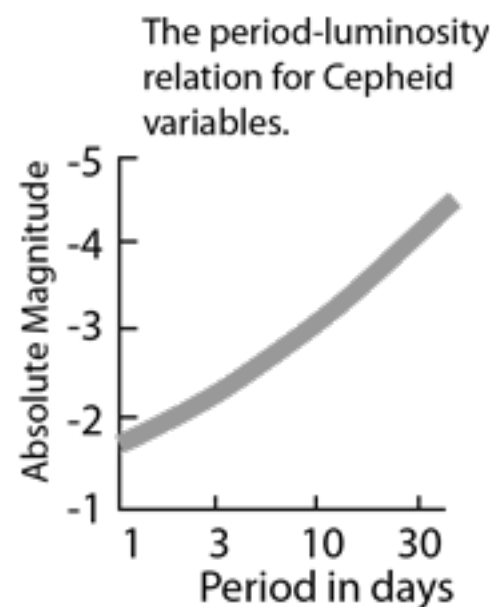
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## Cepheid stars

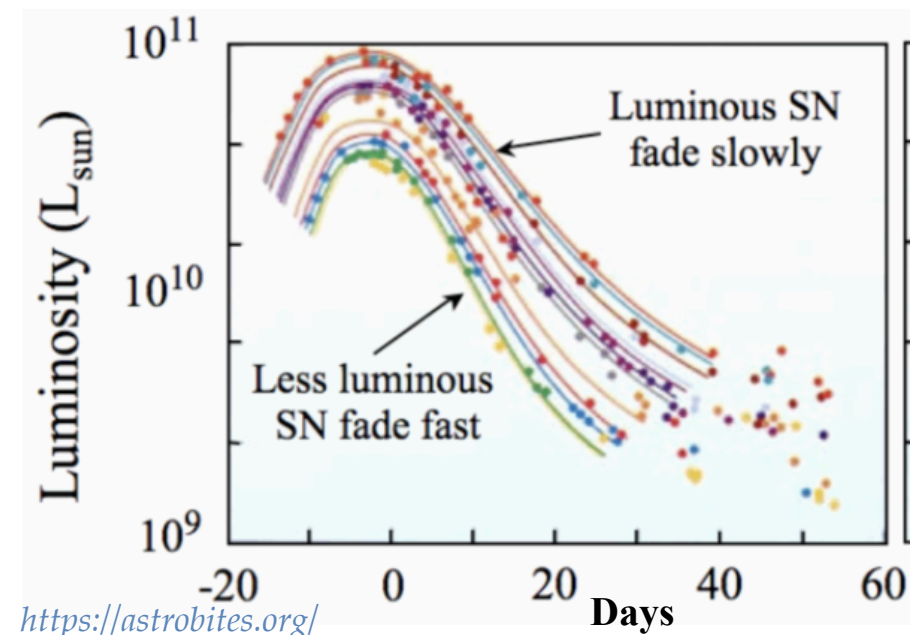


( $D \sim 10^3 - 10^6 \text{ l.y.}$ )



- Pulsating stars  
Period-luminosity relation

## Supernovae Ia

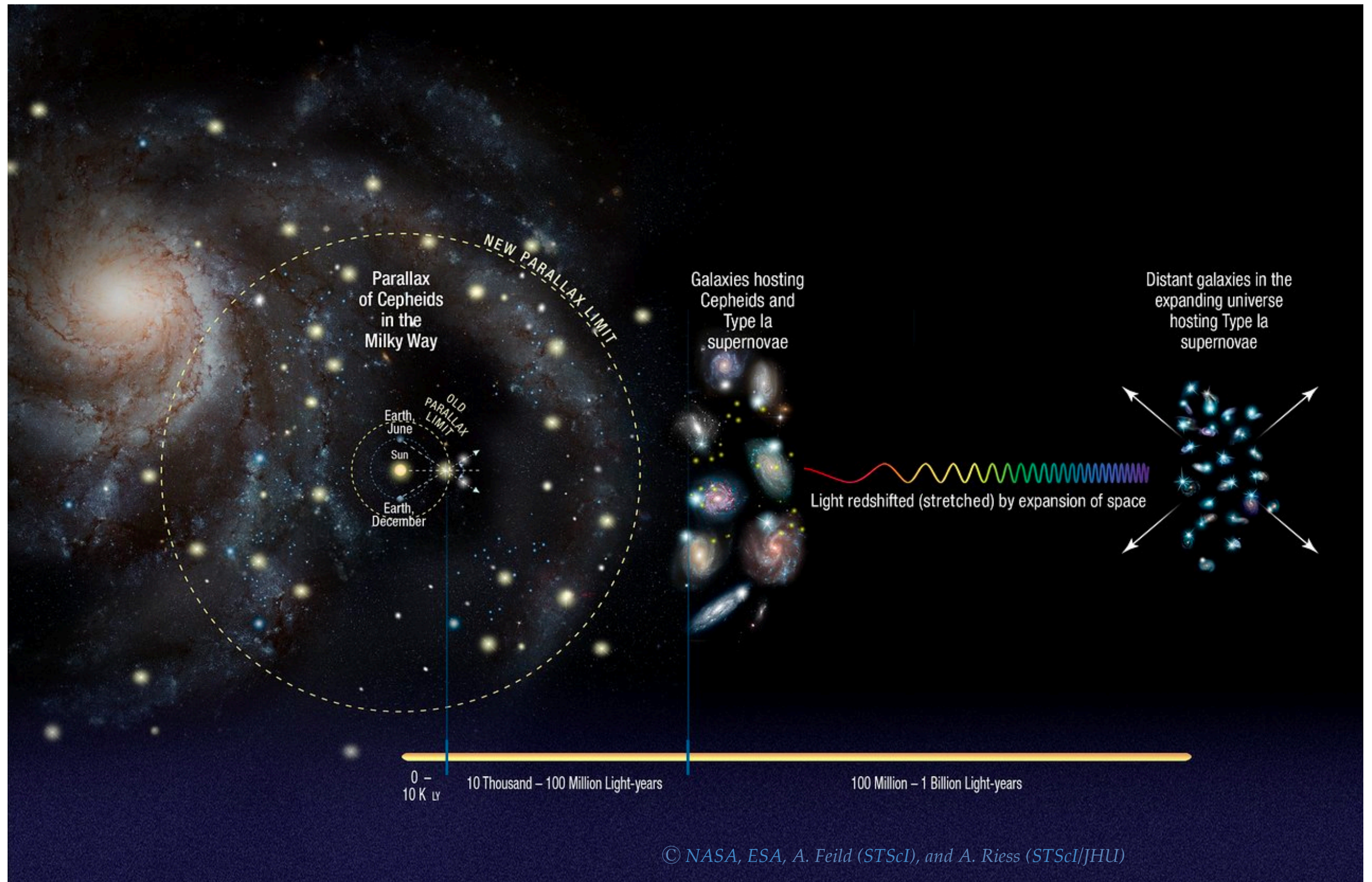


( $D \sim 10^9 \text{ l.y.}$ )

- Bright “standardizable” objects  
relation between peak & slope of the light curve



# Three steps to the Hubble constant

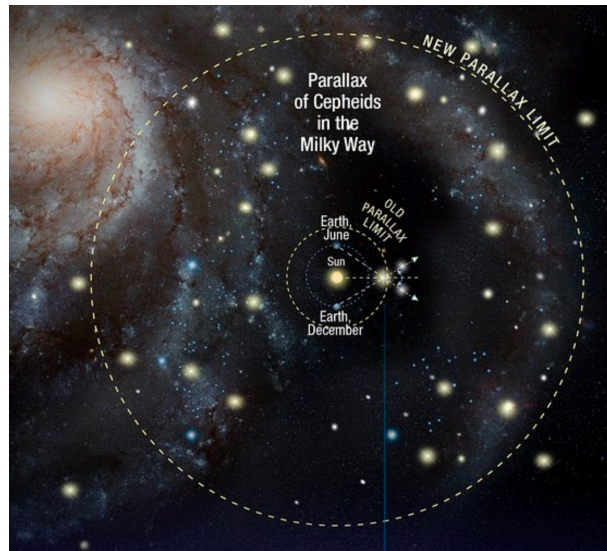




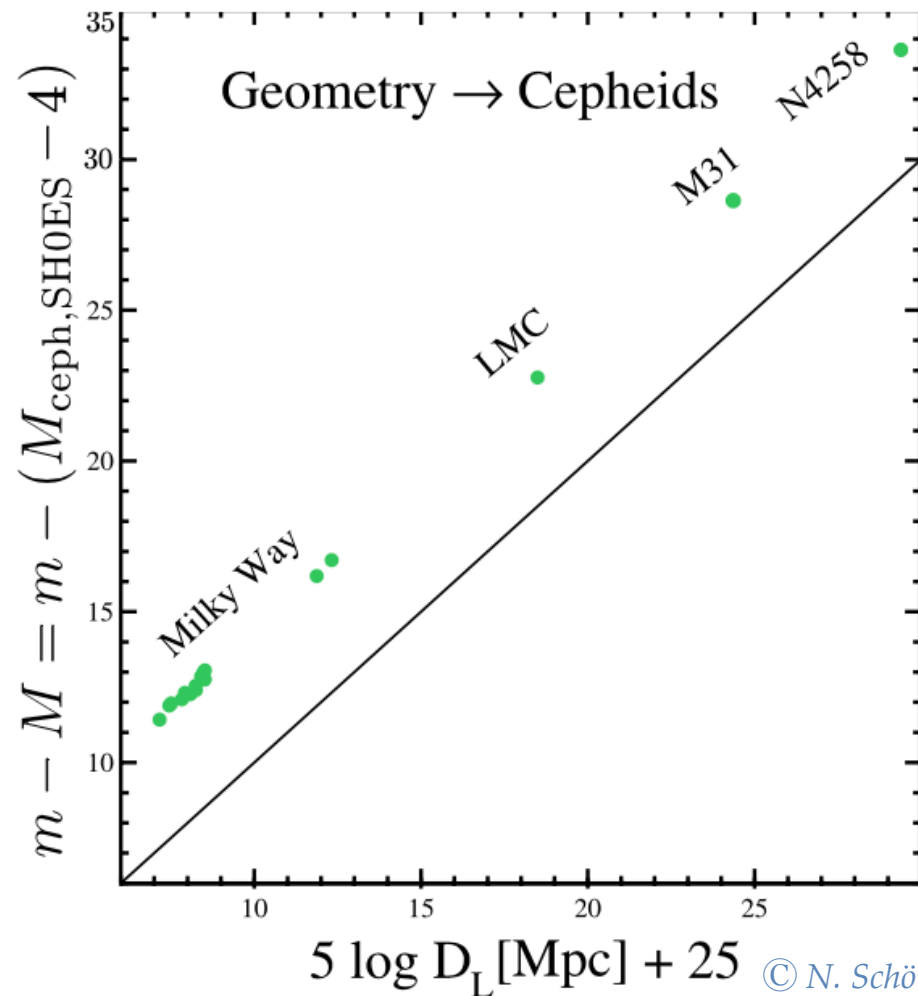
# The cosmic distance ladder

Different geometric calibrators: GAIA parallaxes, masers NGC 4258, DEB in the LMC

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Estimated  
distance



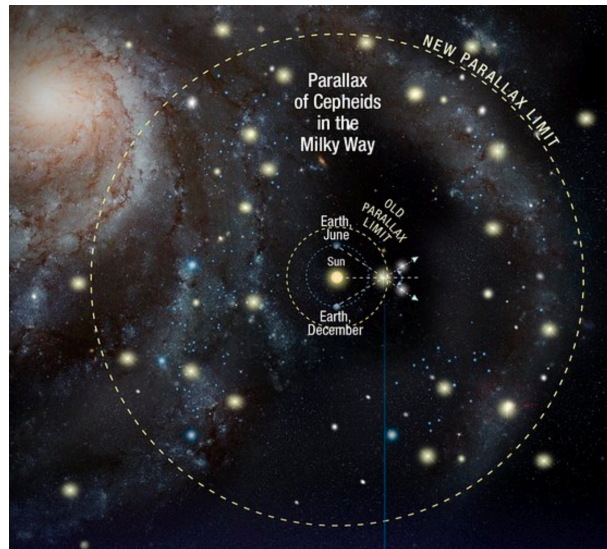
[Riess+1604.01424  
(edited)]

Measured  
distance

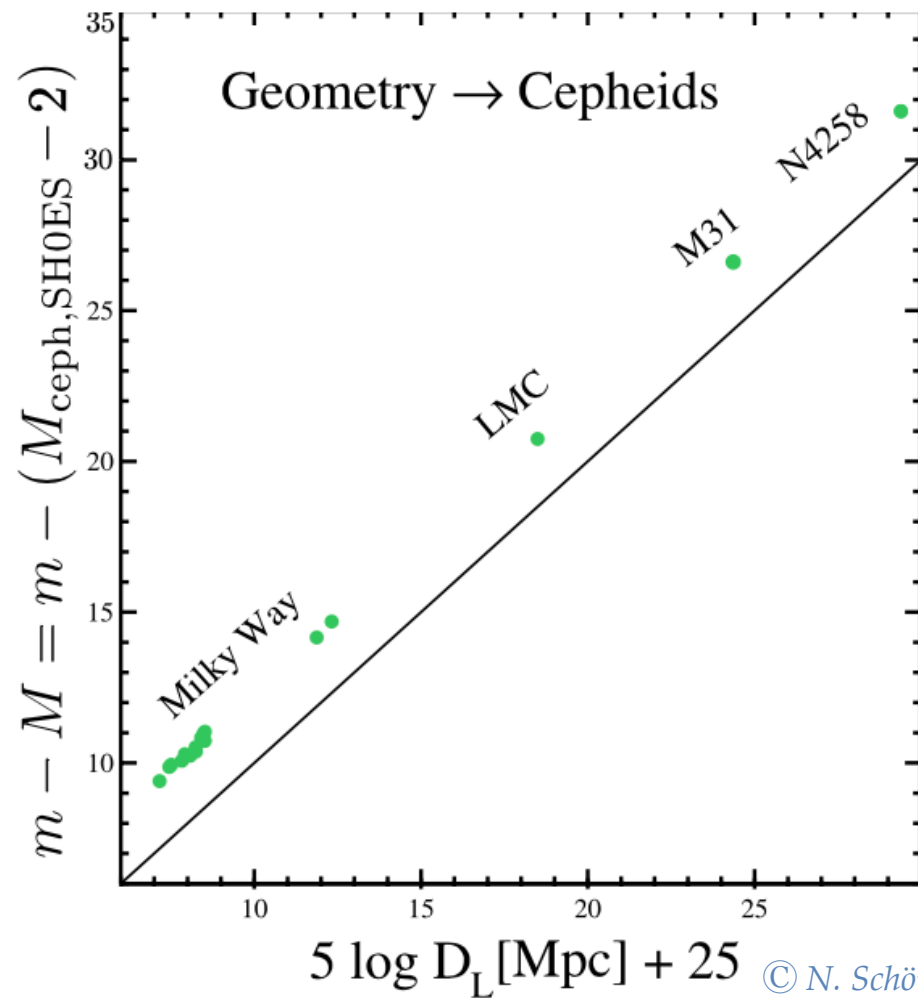
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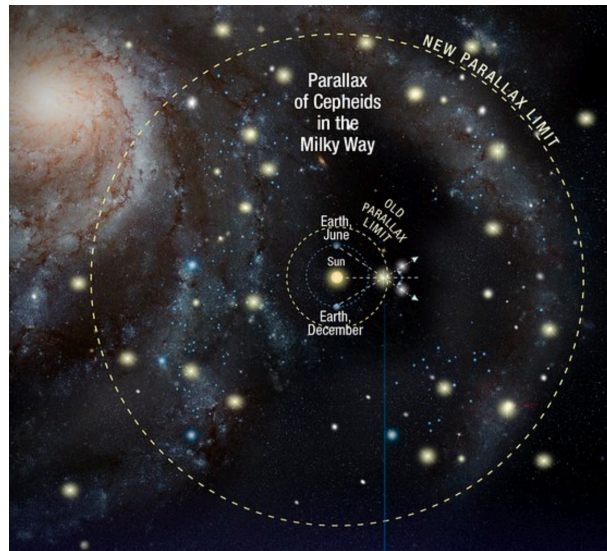
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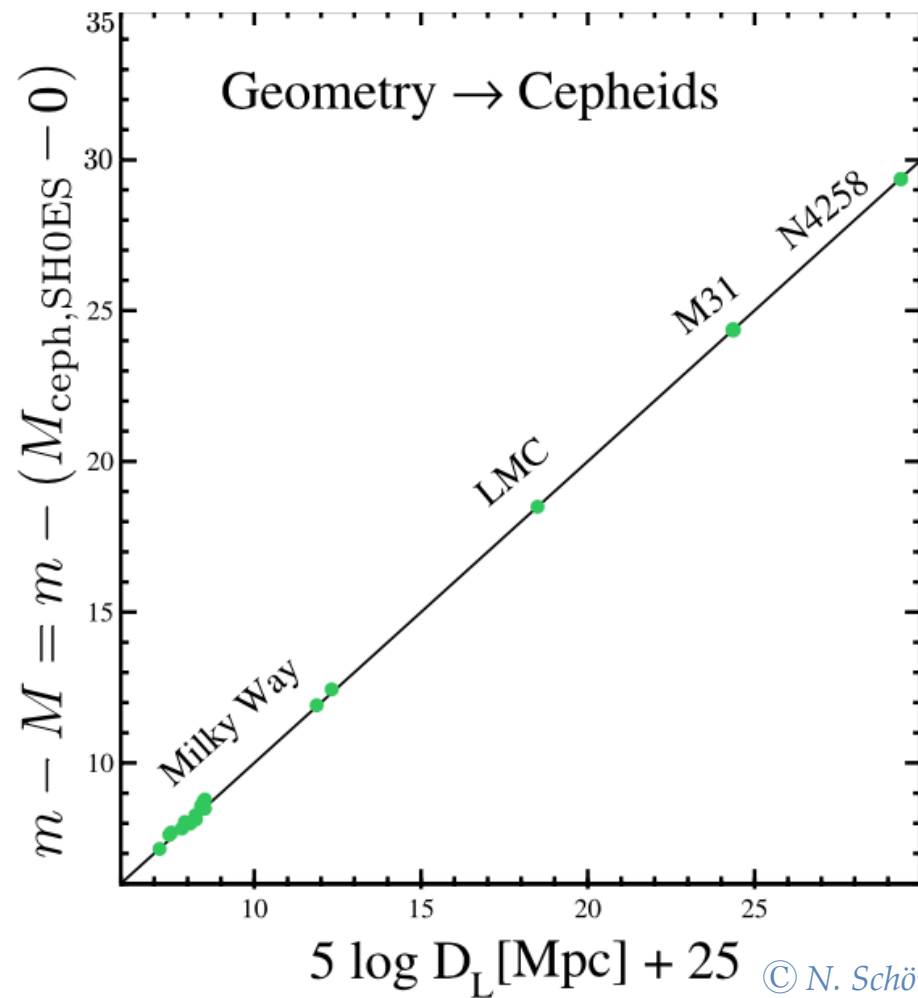
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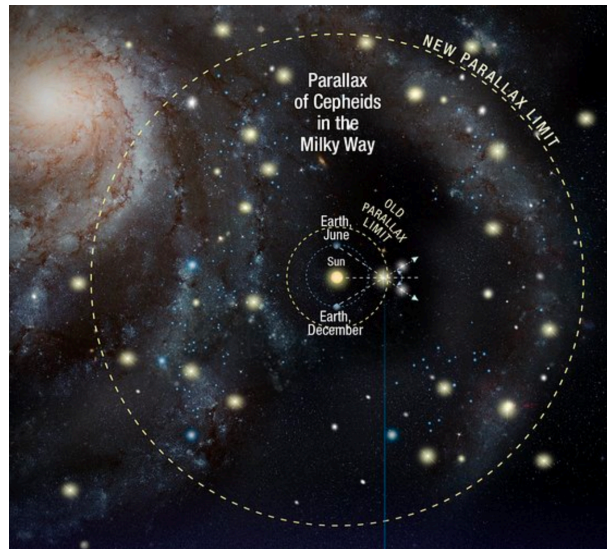
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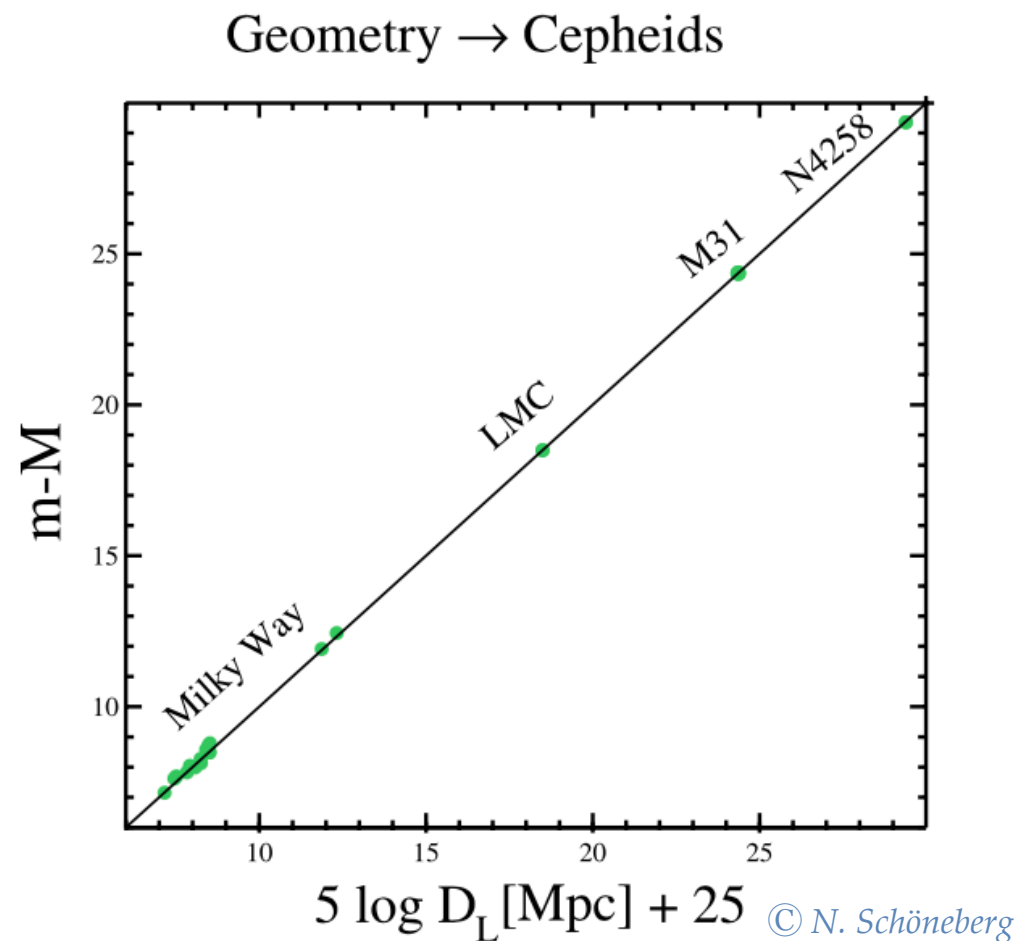
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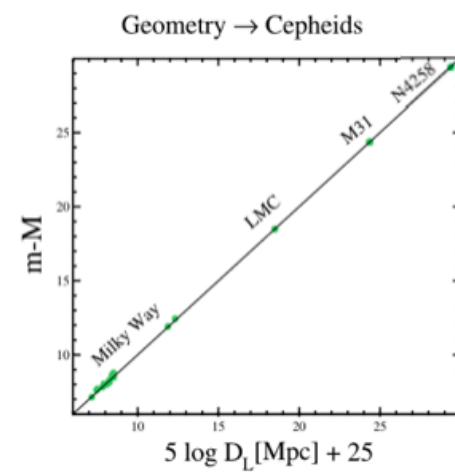
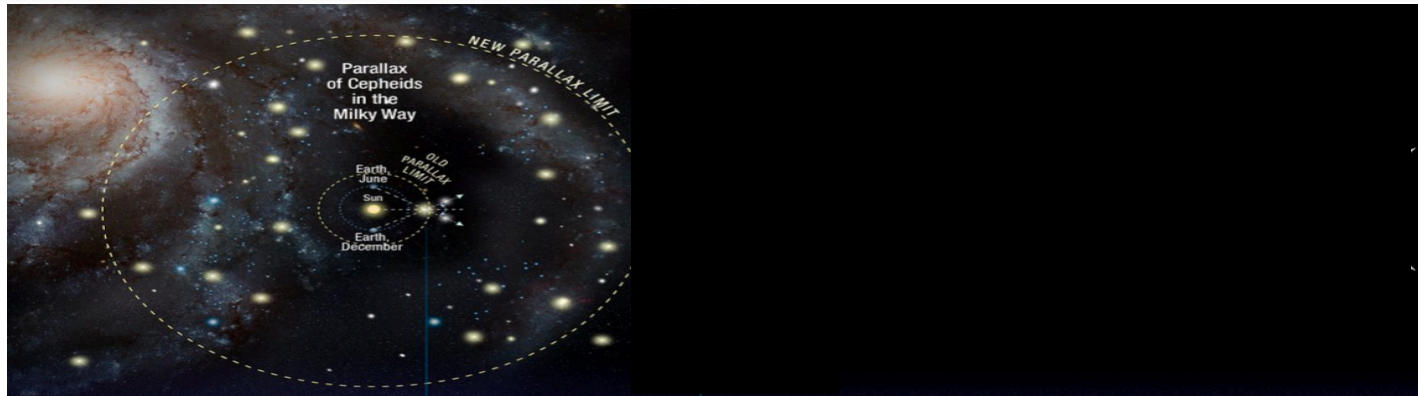
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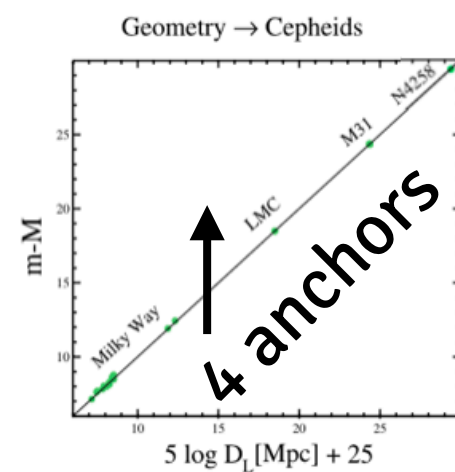
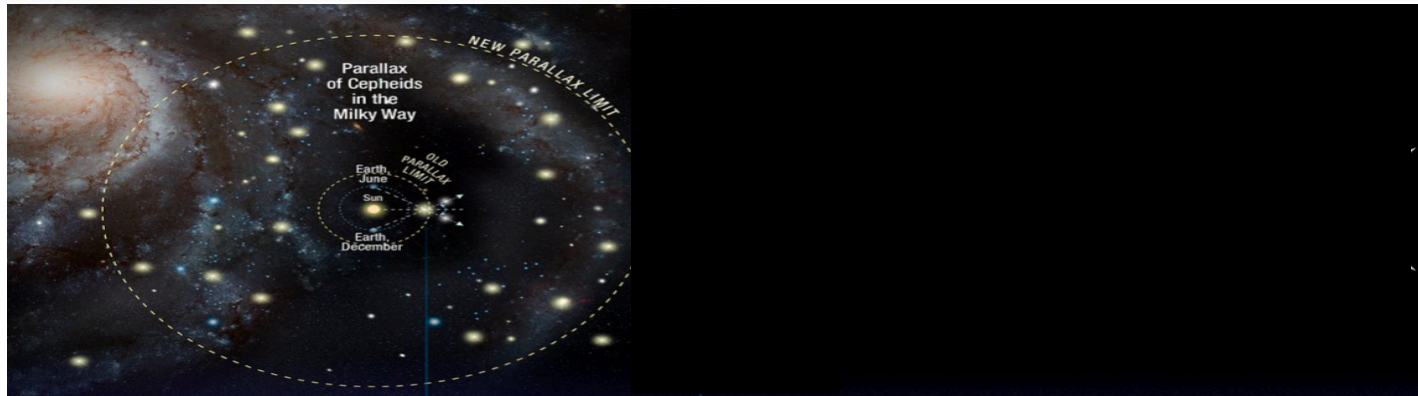
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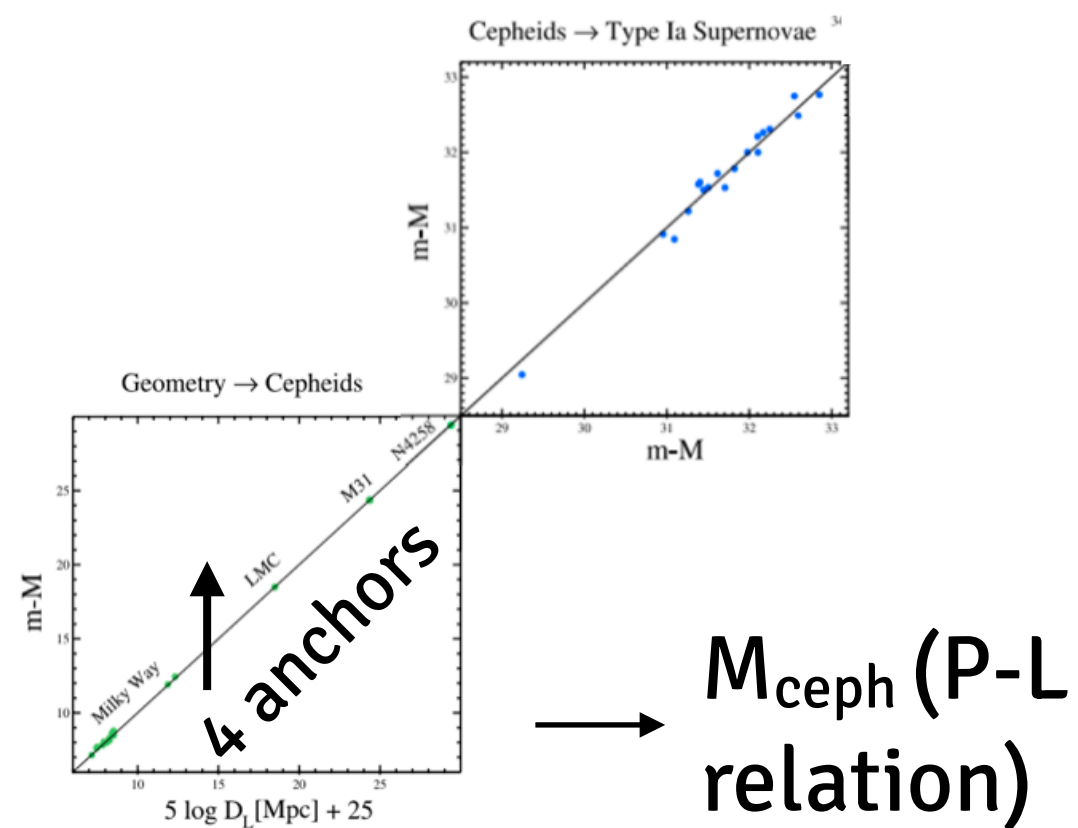
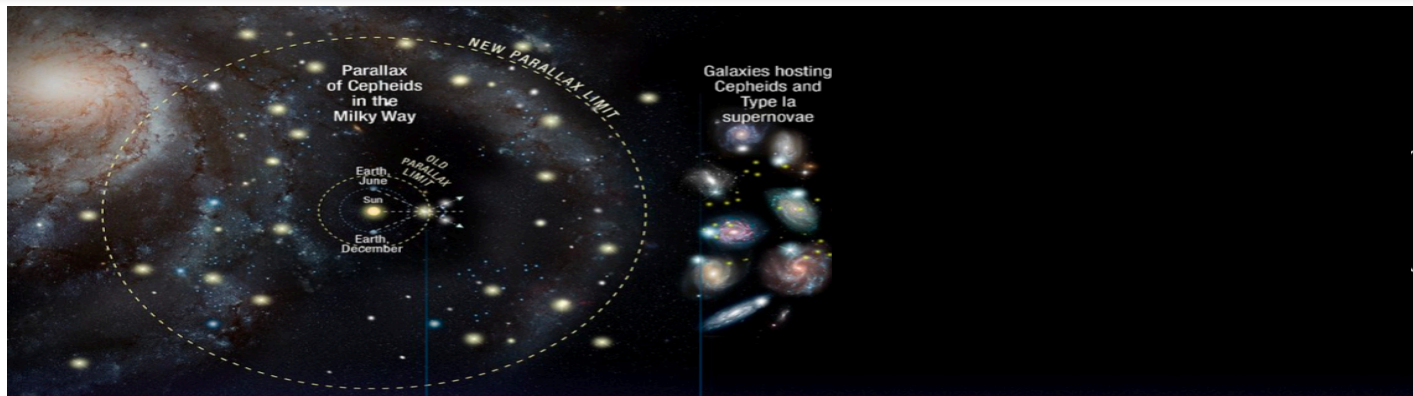
→  $M_{\text{ceph}}$  (P-L relation)

[Riess+1604.01424  
(edited)]

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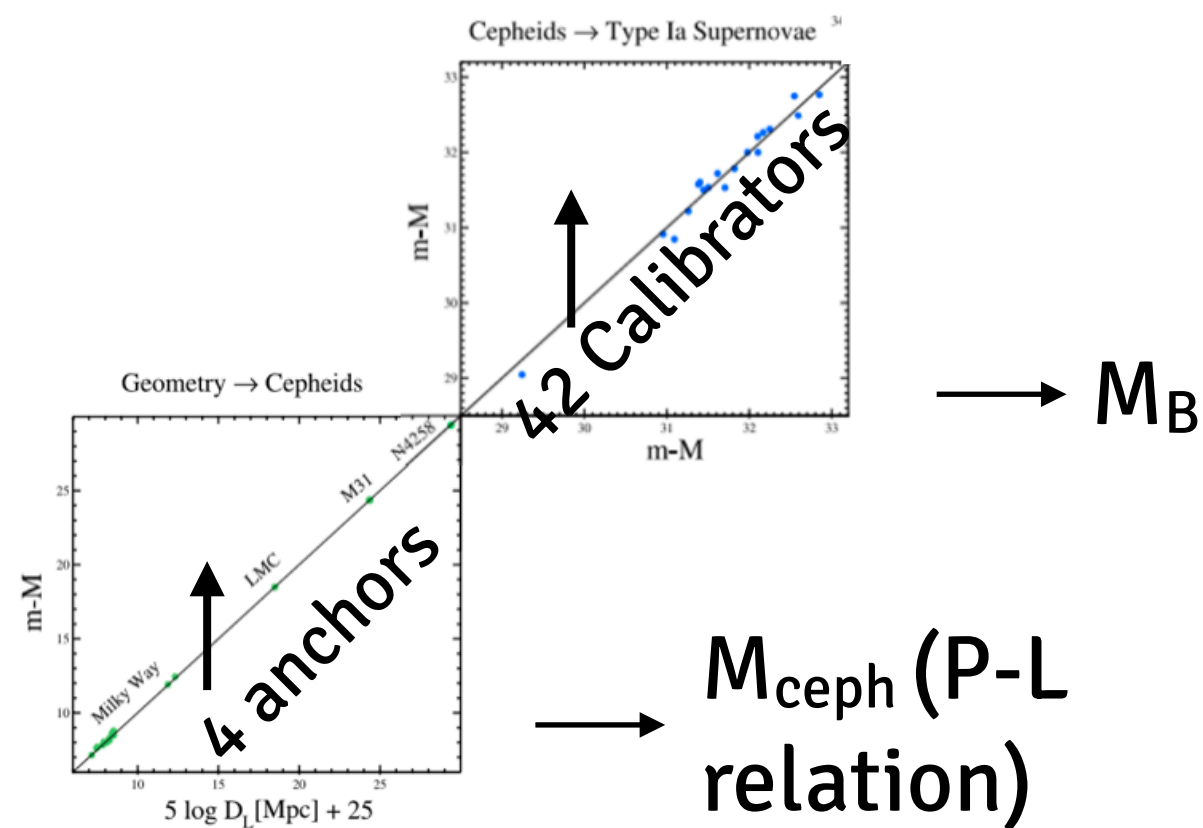
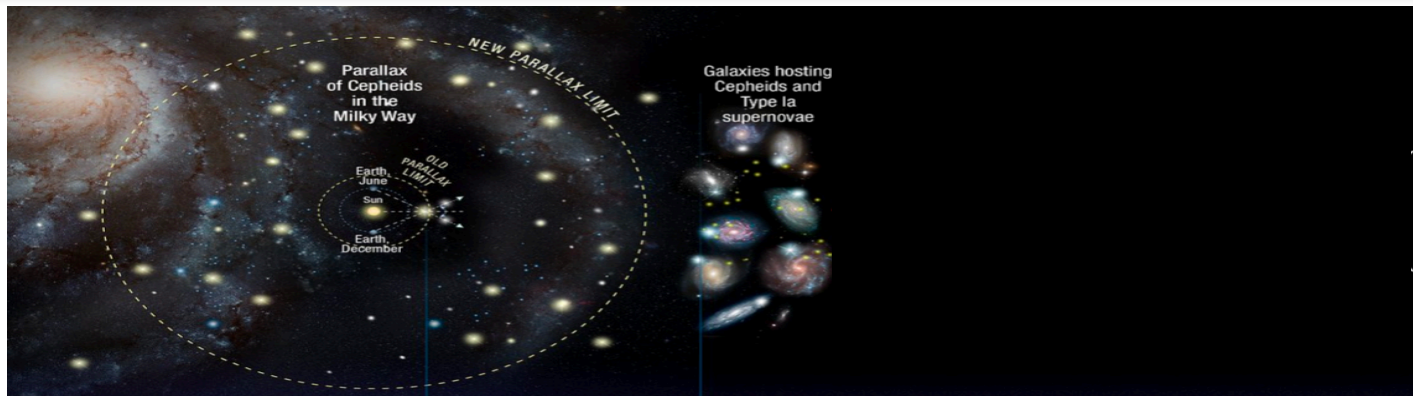
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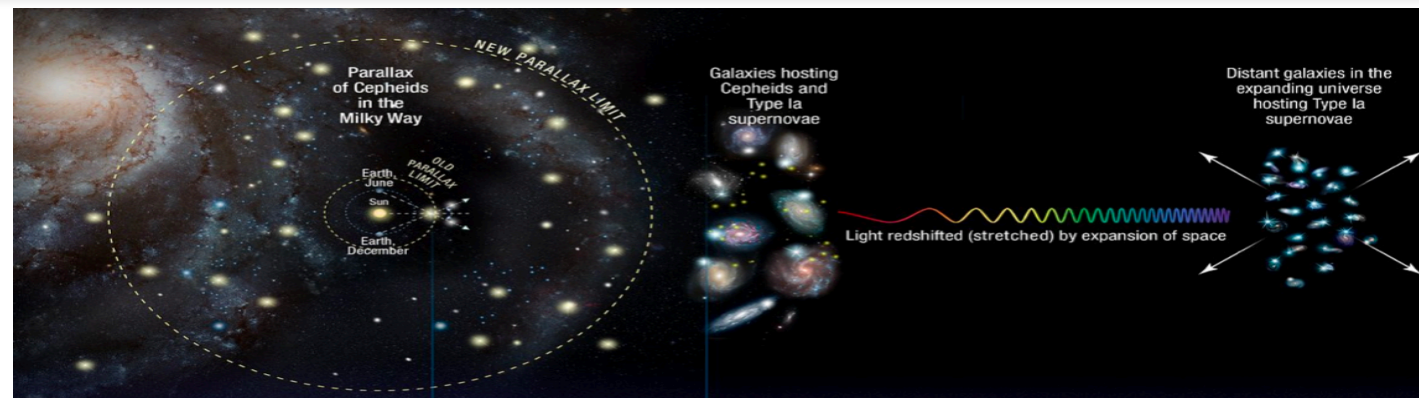
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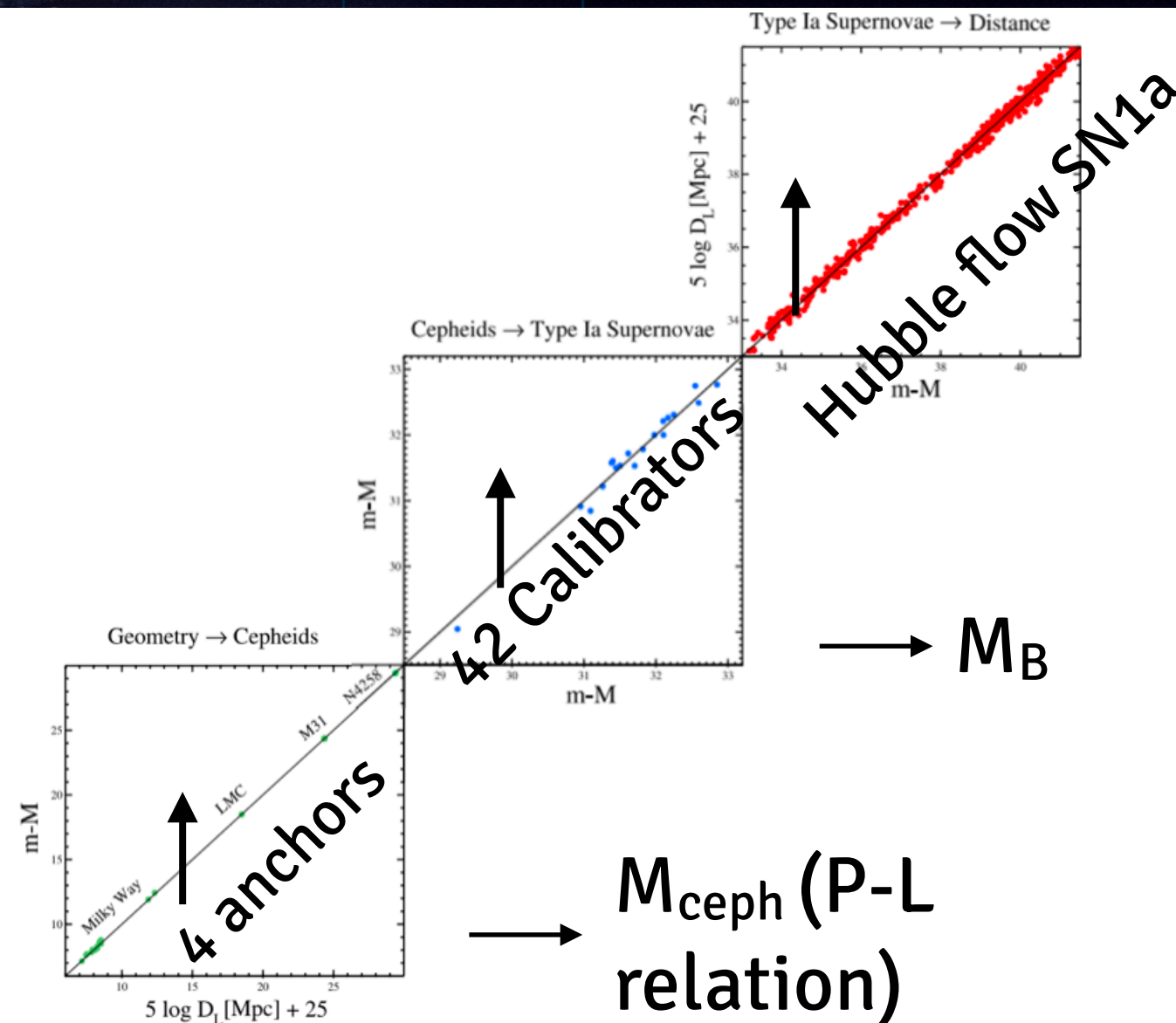
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$D_L + (\text{measured}) z$

$$v \simeq cz \simeq H_0 D_L$$

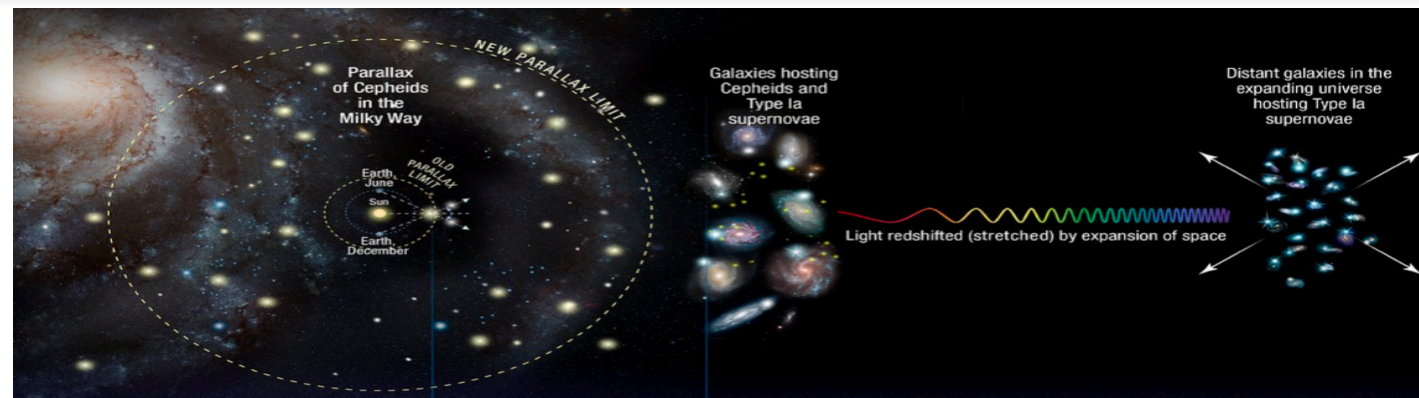


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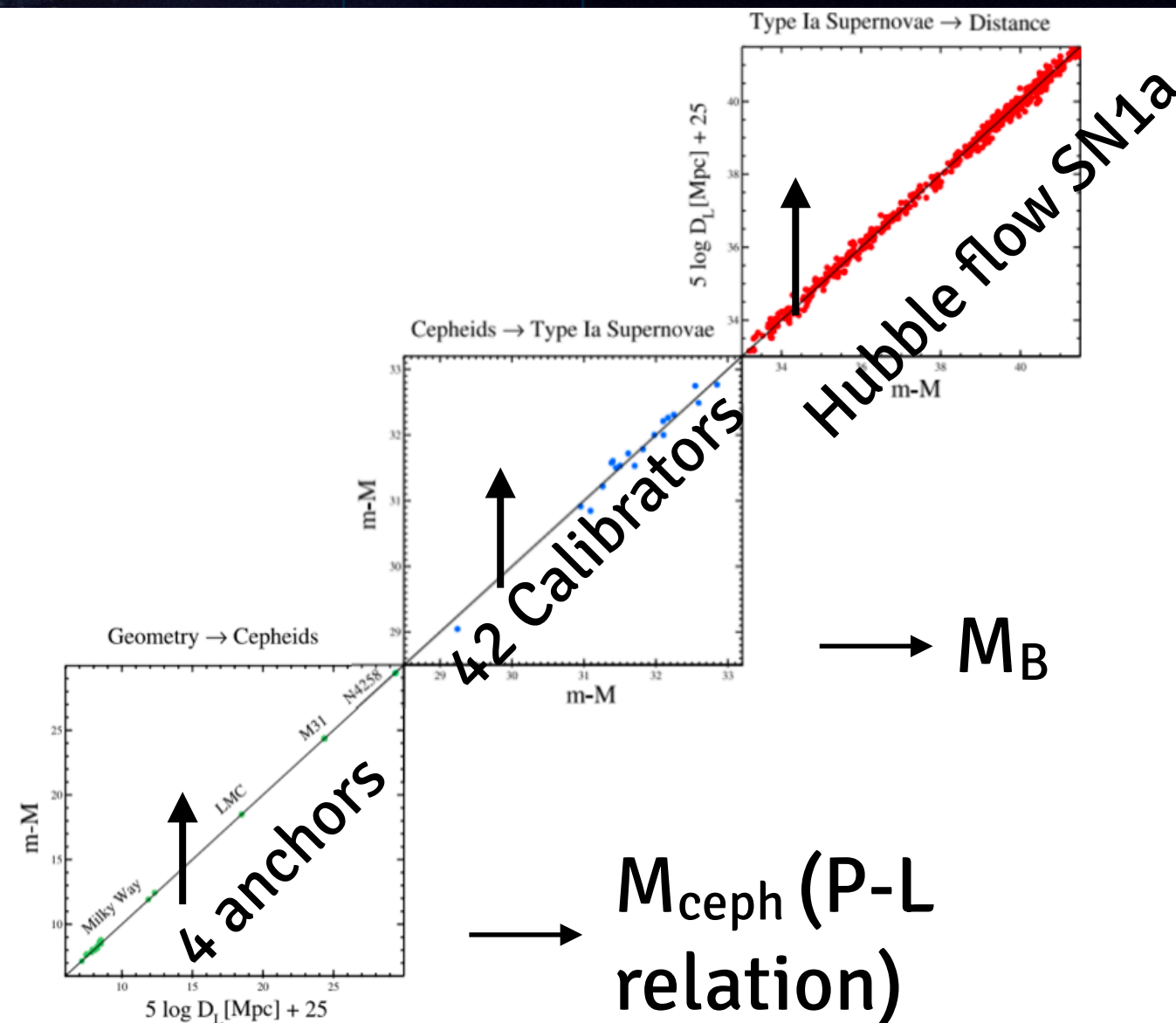
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$D_L + (\text{measured}) z$

$$v \simeq cz \simeq H_0 D_L$$

$$H_0 = 73 \pm 1 \text{ km/s/Mpc}$$



$M_B$

$M_{\text{ceph}}$  (P-L relation)

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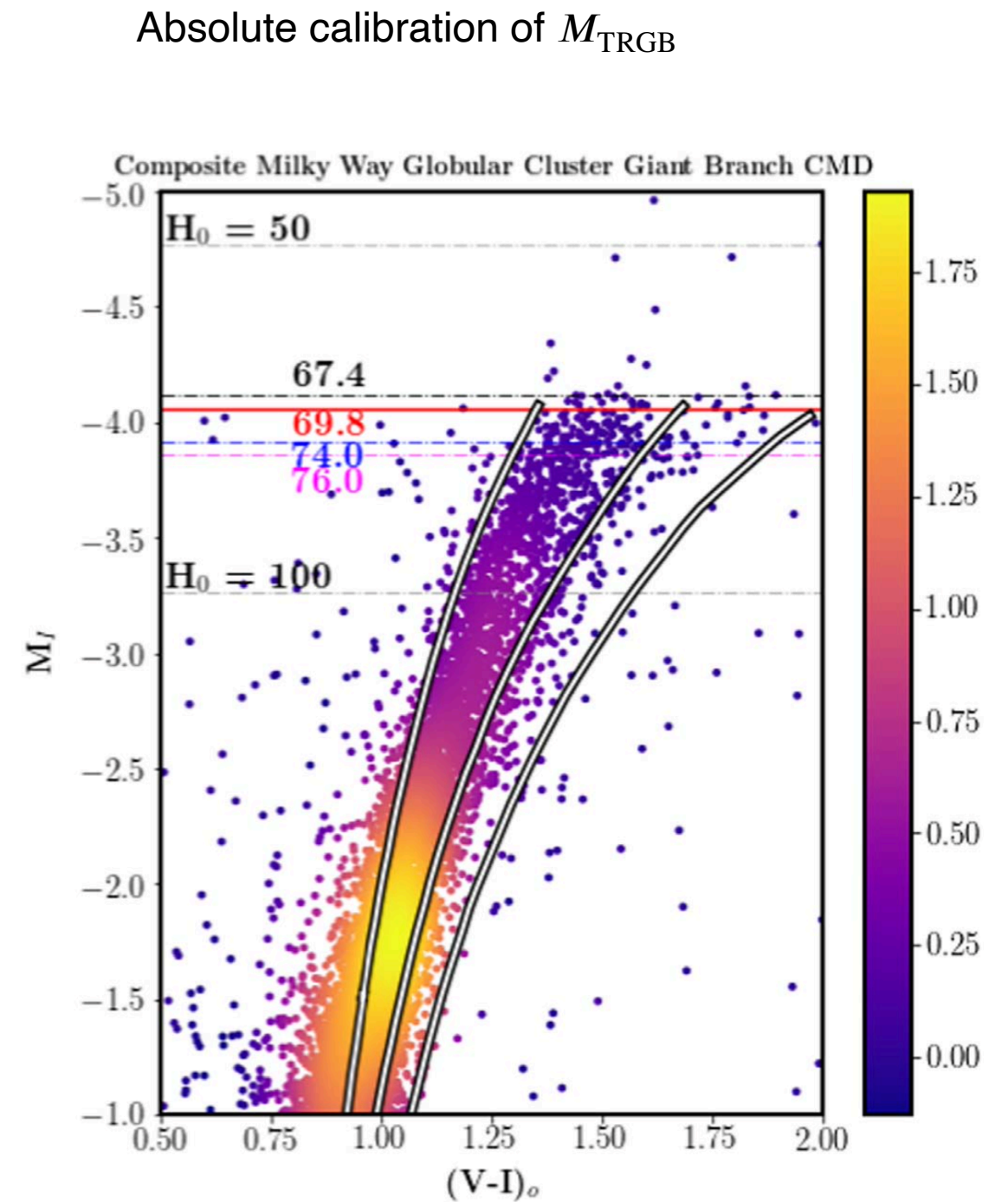
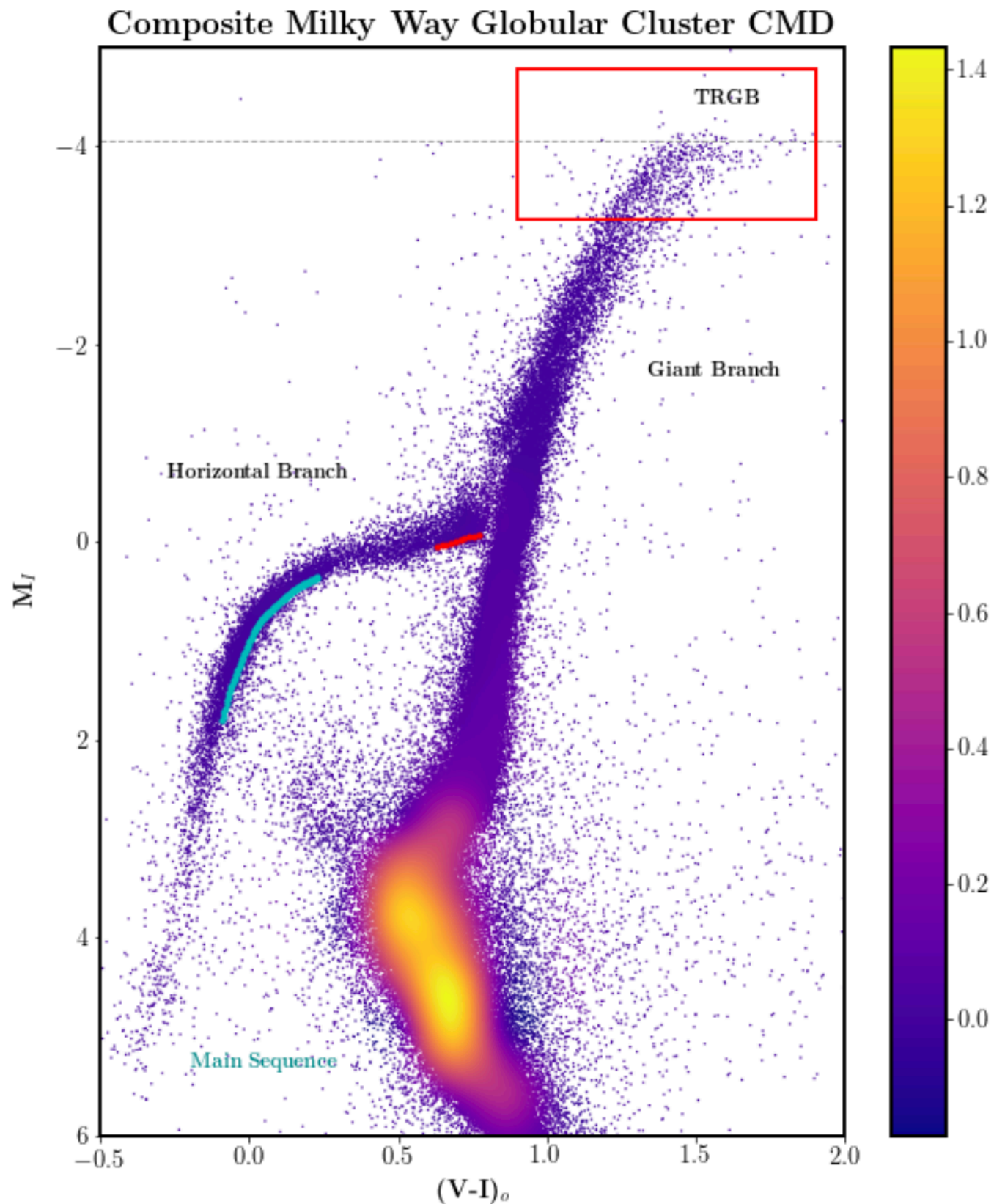
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# Systematics? A non-exhaustive list

*See review Di Valentino++ 2103.01183 for all relevant references*

- SH0ES builds a 3 steps distance ladder: anchors => cepheids => SN1a
- Are there **issues with distance anchor**? (GAIA, LMC, NGC4258)  
*Efstathiou++ 2007.10716, Soltis++2012.09196*
- Are there **issues with cepheids**?
  - Cepheids vs TRGB: disagreement?  
*Freedman++ 2106.15656, Anand++ 2108.00007*
  - Effect of Dust?  
*Mortsell++ 2105.11461*
  - Cepheid crowding?  
*Riess++ 2401.04773*
  - Is the metallicity correction correct?  
*Efstathiou++ 2007.10716*
- Are there **issues with SN1a**? different populations of SN1a between “cepheid-SN1a calibrator” and Hubble flow SN1a?  
*Rigault++ 1412.6501, Jones++1805.05911, Brout&Scolnic 2004.10206*
- Are there **issues with the CMB**? *Di Valentino++ 1911.02087, Calderón++ 2302.14300*

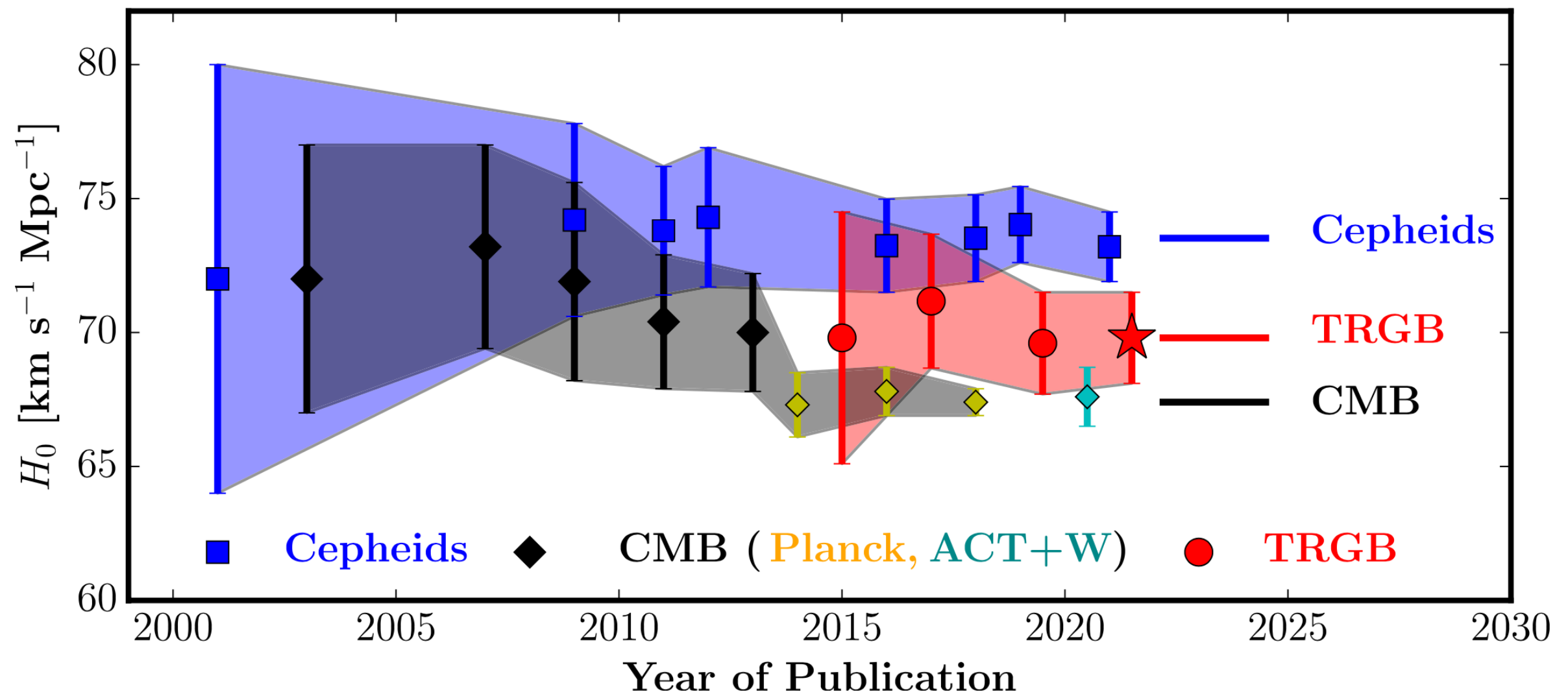
# Tip of the Red Giant branch



*Freedman++ 2106.15656*



# The Chicago Carnegie Hubble Program



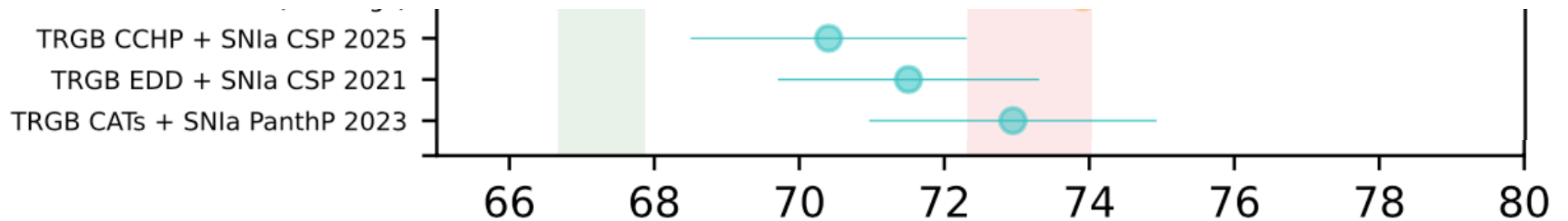
Freedman (2021)

*Freedman++ 2106.15656*

# Tip of the Red Giant branch revisited

**Table 5.** Sources of Differences in  $H_0$  Between TRGB analysis by CATs (Here), CCHP, EDD (in  $H_0$ )

Term	$\Delta\text{CCHP}$	$\Delta\text{EDD}$
	(km/s/Mpc)	(km/s/Mpc)
SN Related		
1. Include SN 2021pit,2021rhu,2007on	0.6	1.3
2. No TRGB detected in N5584,N3021,N1309,N3370	0.0	0.0
3. Peculiar Flows (Pantheon+)	0.4	0.0
4. Hubble Flow Surveys (Pantheon+)	1.1	0.0
<b>SN subtotal</b>	<b>2.0</b>	<b>1.3</b>
TRGB Related		
5. Fiducial TRGB Calibration/Tip-Contrast Relation	1.4	-0.3
<b>Total</b>	<b>3.4</b>	<b>1.0</b>

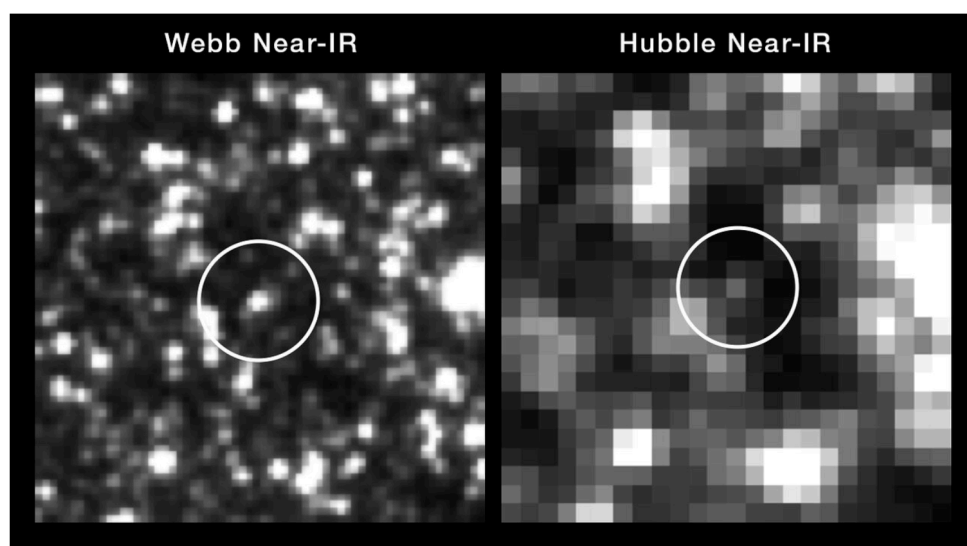
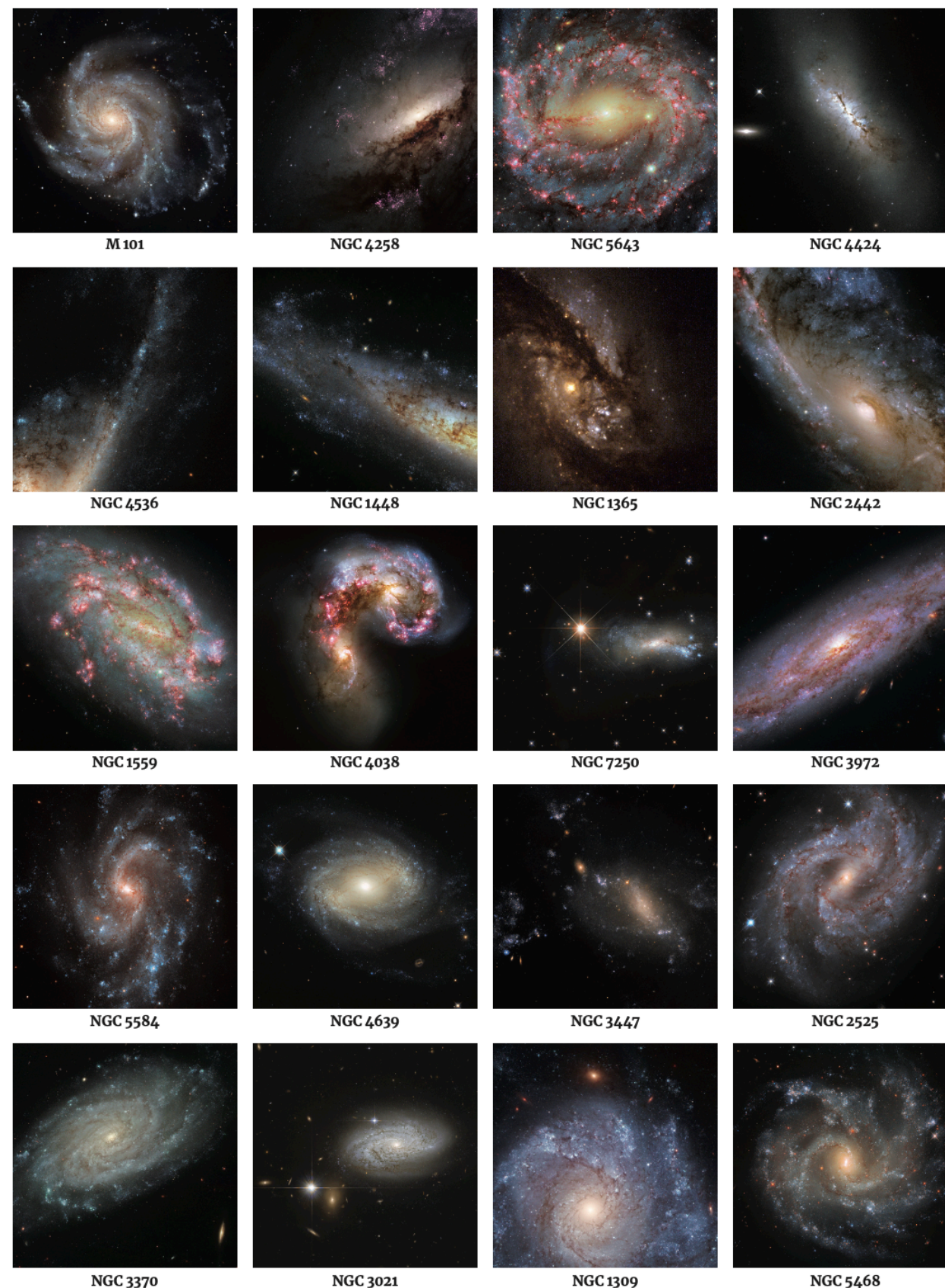
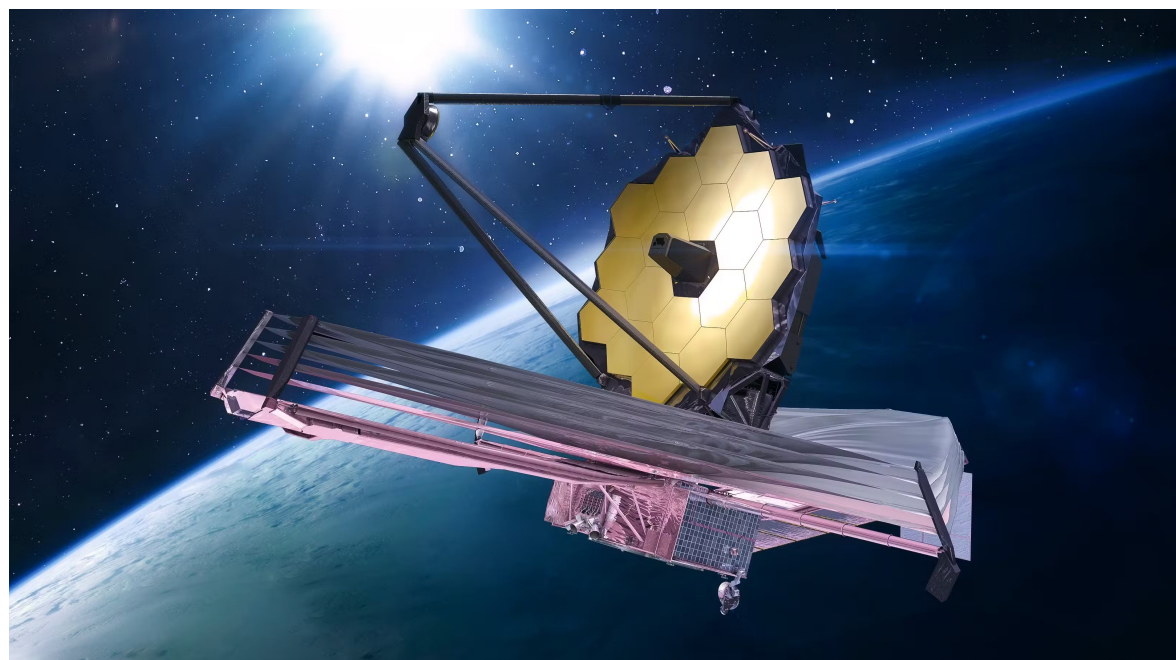


*Scolnic++ 2304.06693*



# JWST and the Hubble tension

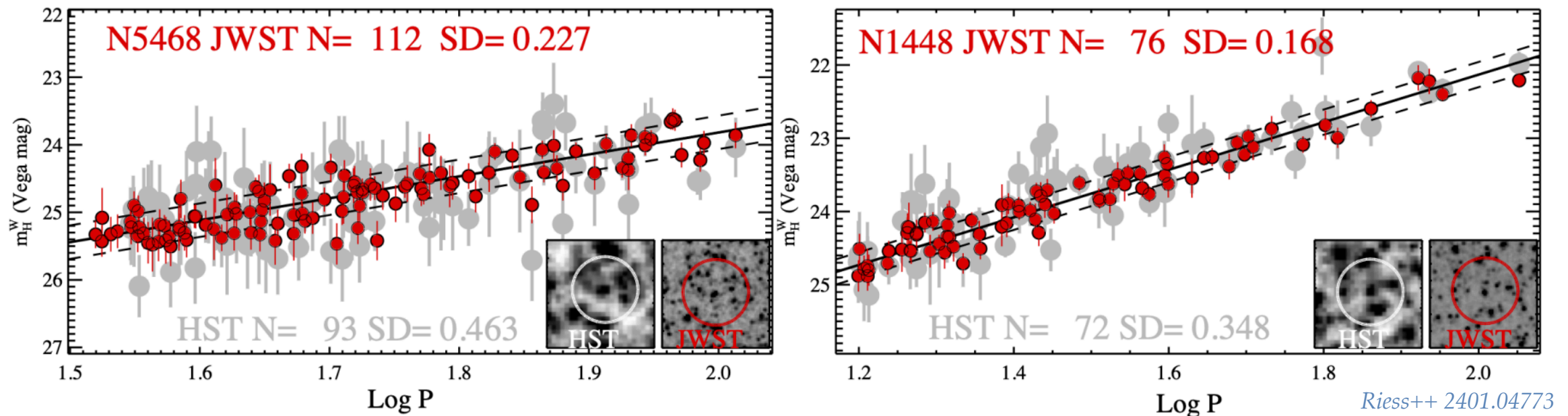
- First analyses with JWST from CCHP and SH0ES.
- Re-observations of 20 key galaxies to check HST results + develop new calibration method.



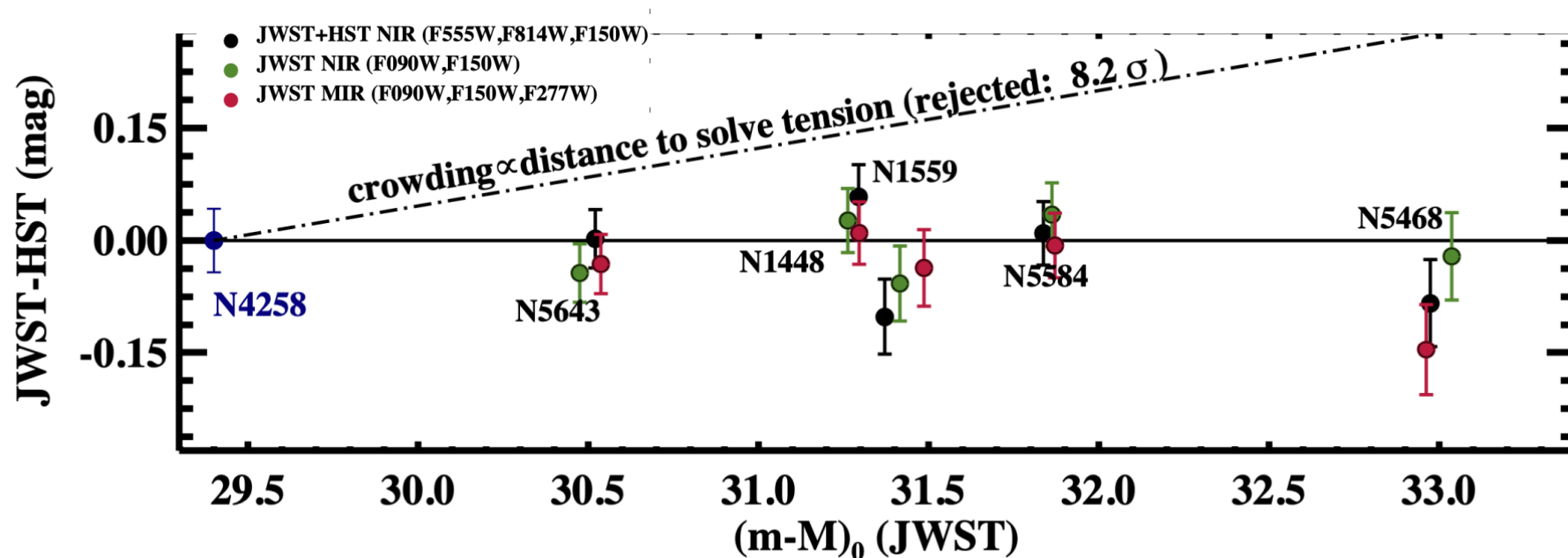


# SHOES finds excellent agreement with HST

- From SH0ES: reanalysis of the PL relations in 8 SN1a hosts galaxies, excellent agreement with HST

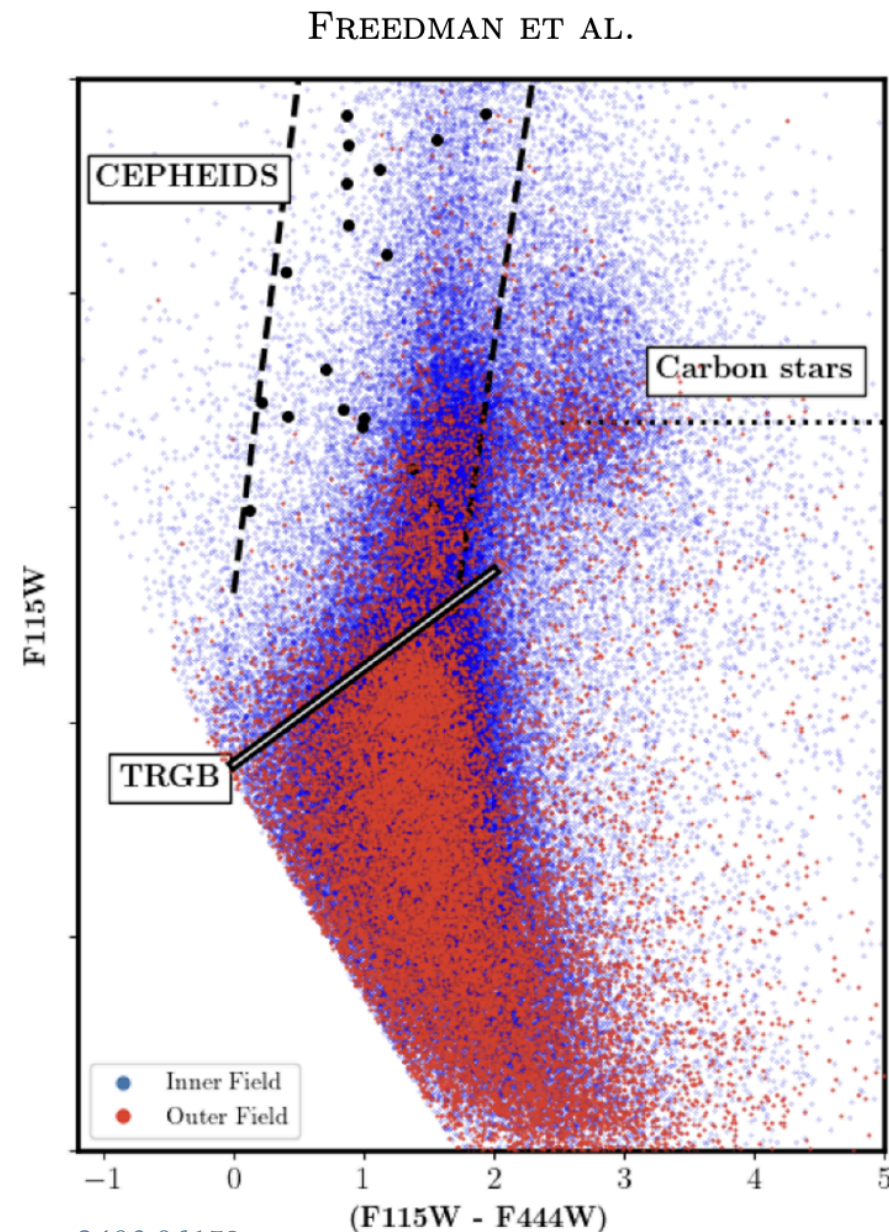


- Rejects “crowding” of cepheids as an explanation for the tension

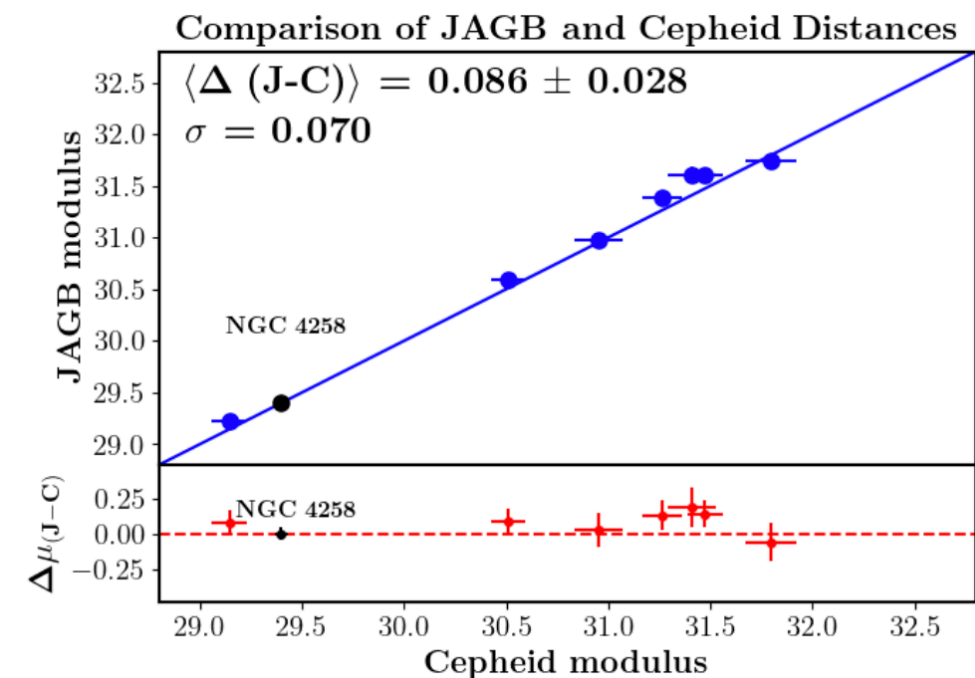
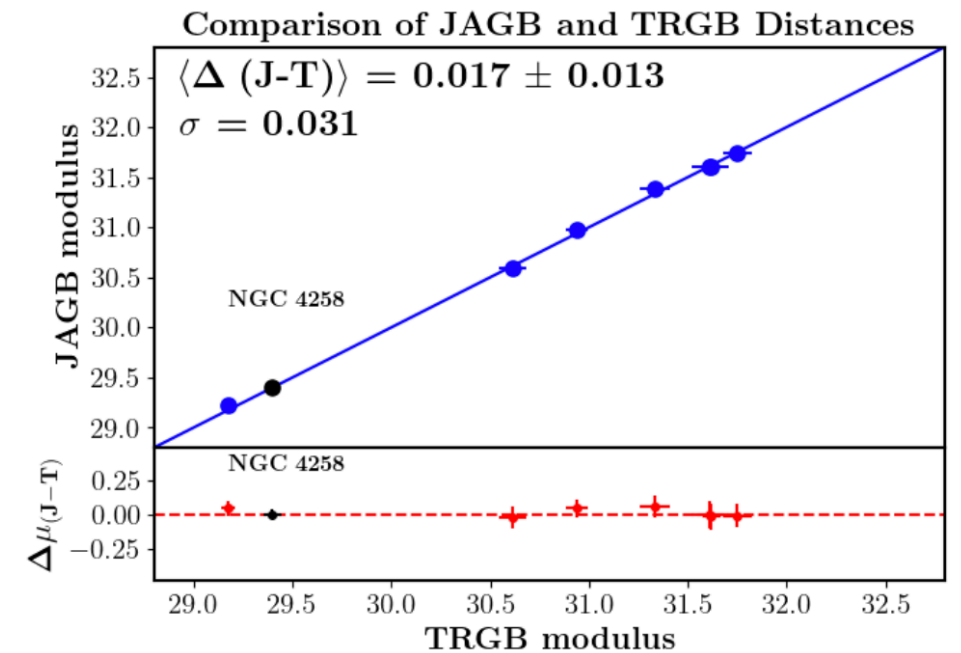


# CCHP: 3 JWST-only measurements of $H_0$

- Observations of 10 SN1a hosts + 1 anchor to re-calibrate cepheids, TRGB and a new 'JAGB' method.



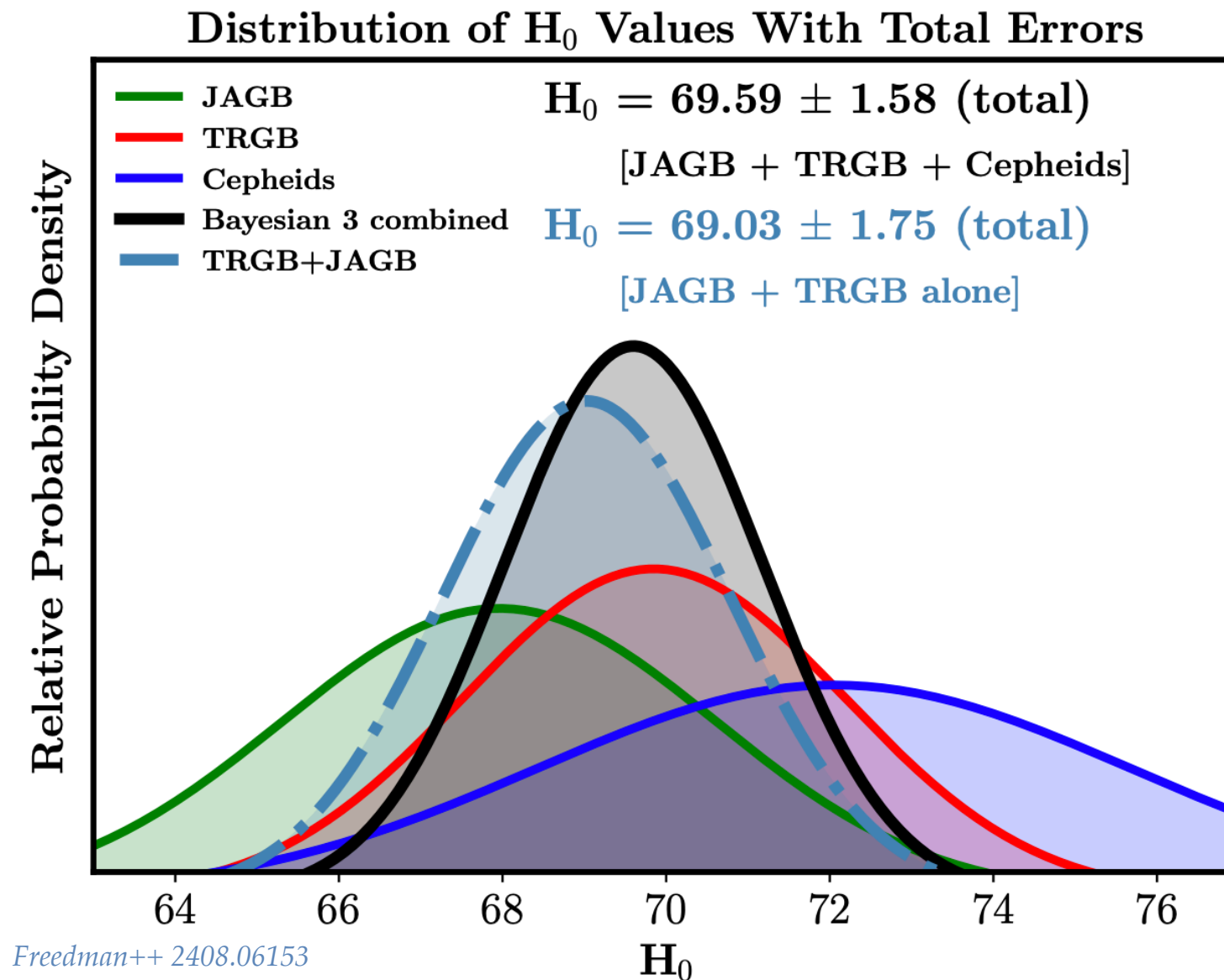
*Freedman++ 2408.06153*



- Finds a bias in the cepheids distance while TRGB and JAGB distance are in good agreement

# CCHP finds no Hubble tension

- JAGB and TRGB value of  $H_0$  in good agreement with  $\Lambda$ CDM, Cepheids are ‘biased high’.
- Error bars are large: JWST alone is not (yet) as good as HST, only 10 hosts galaxies and one anchor.

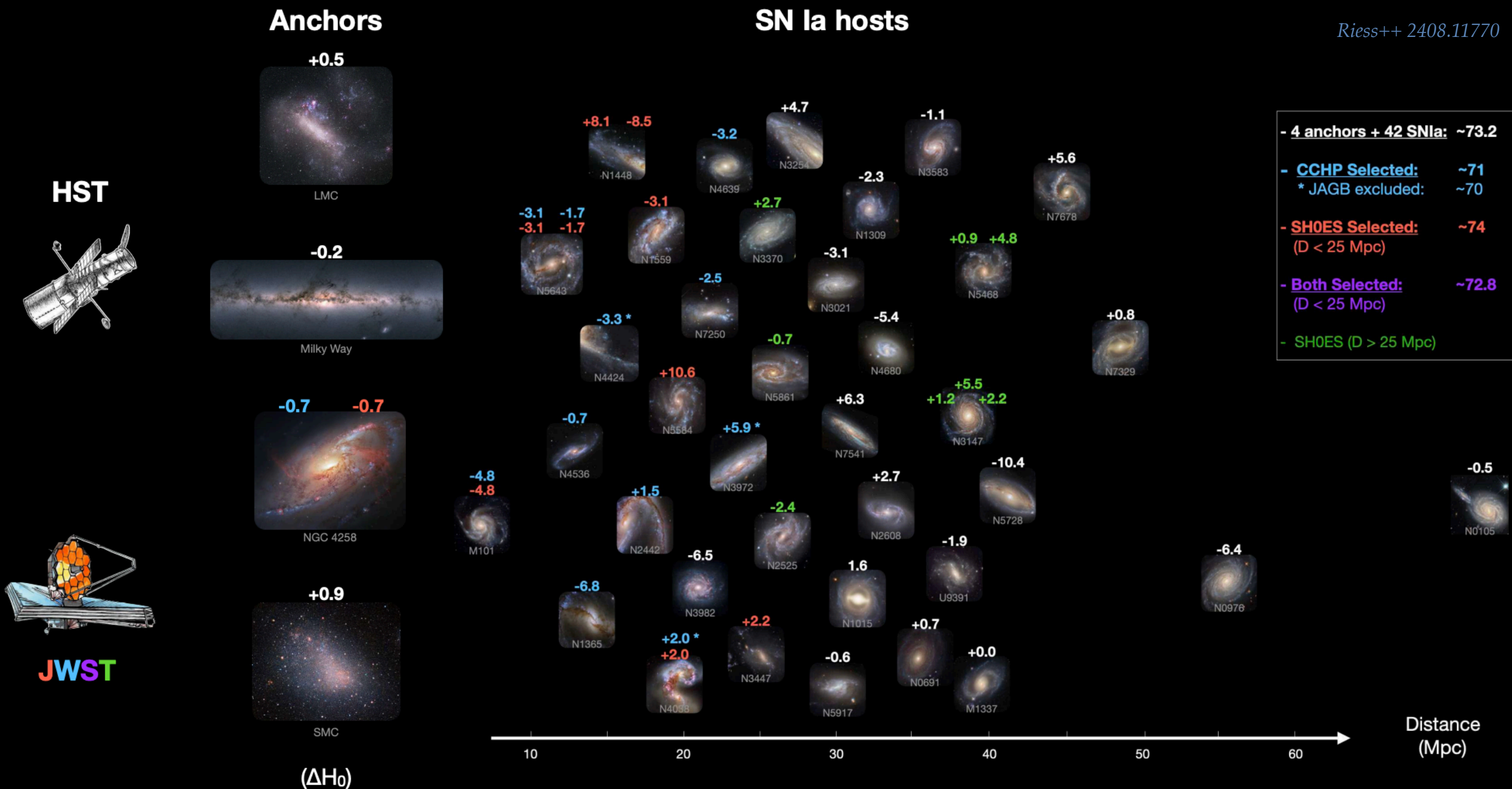


Is this the end of the Hubble tension?



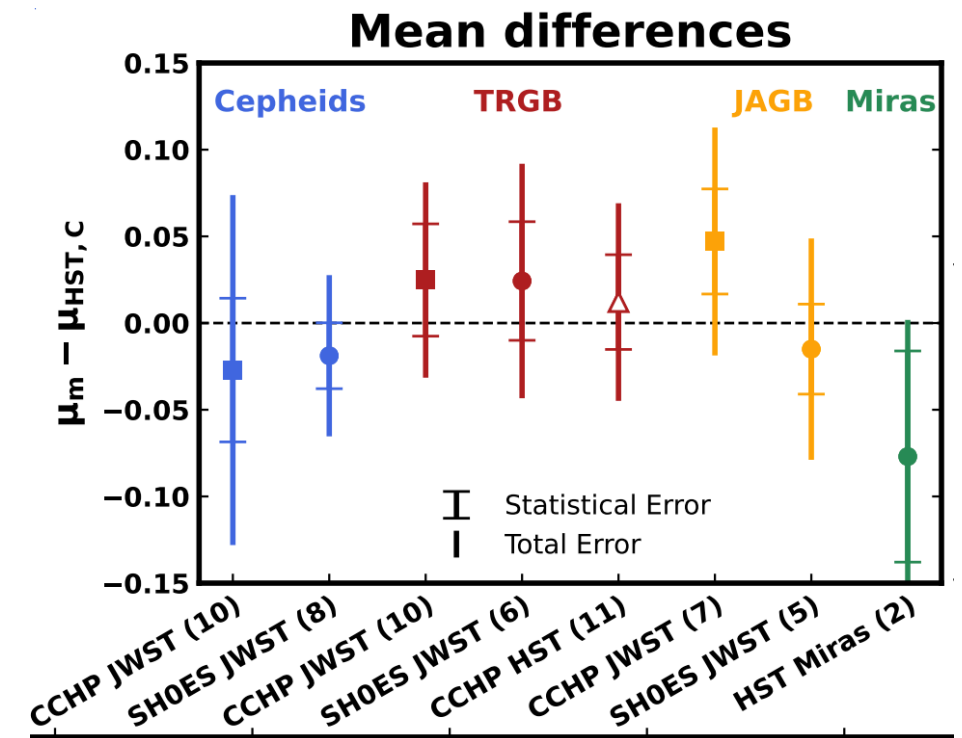
# HST provides a 'complete' picture

- JWST measures (very well) a sub-sample of the full HST sample

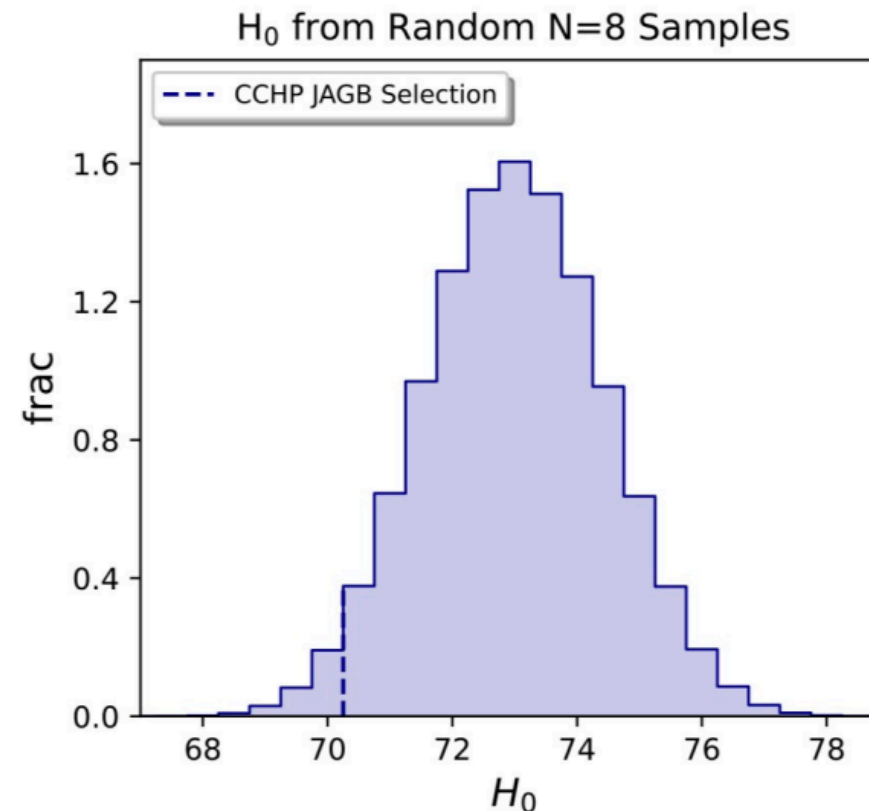
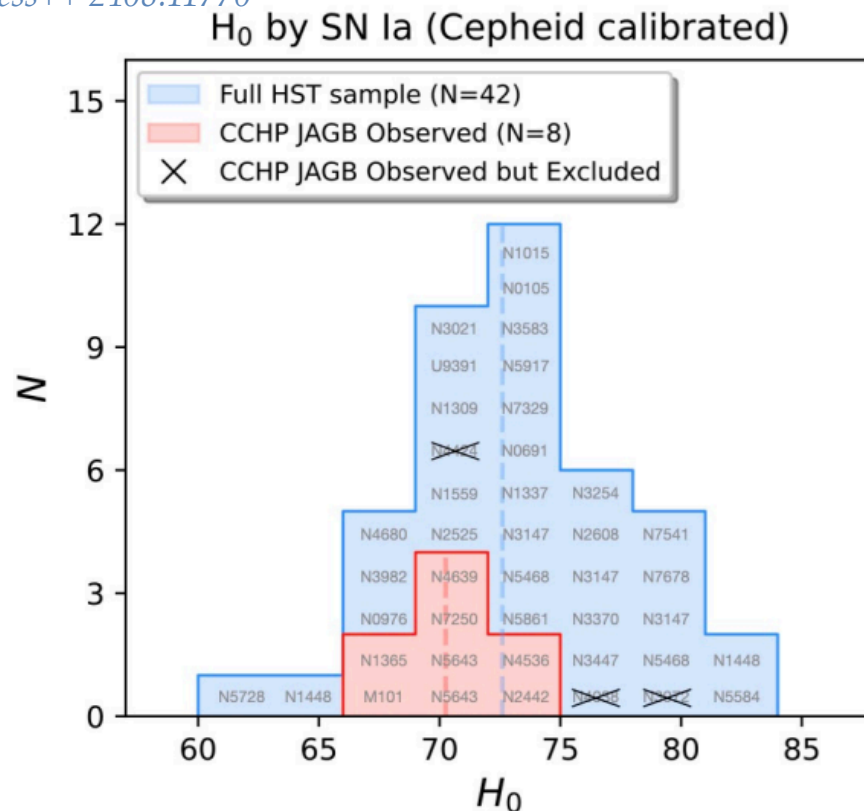


# SHOES suggests a 'bias low' in CCHP samples

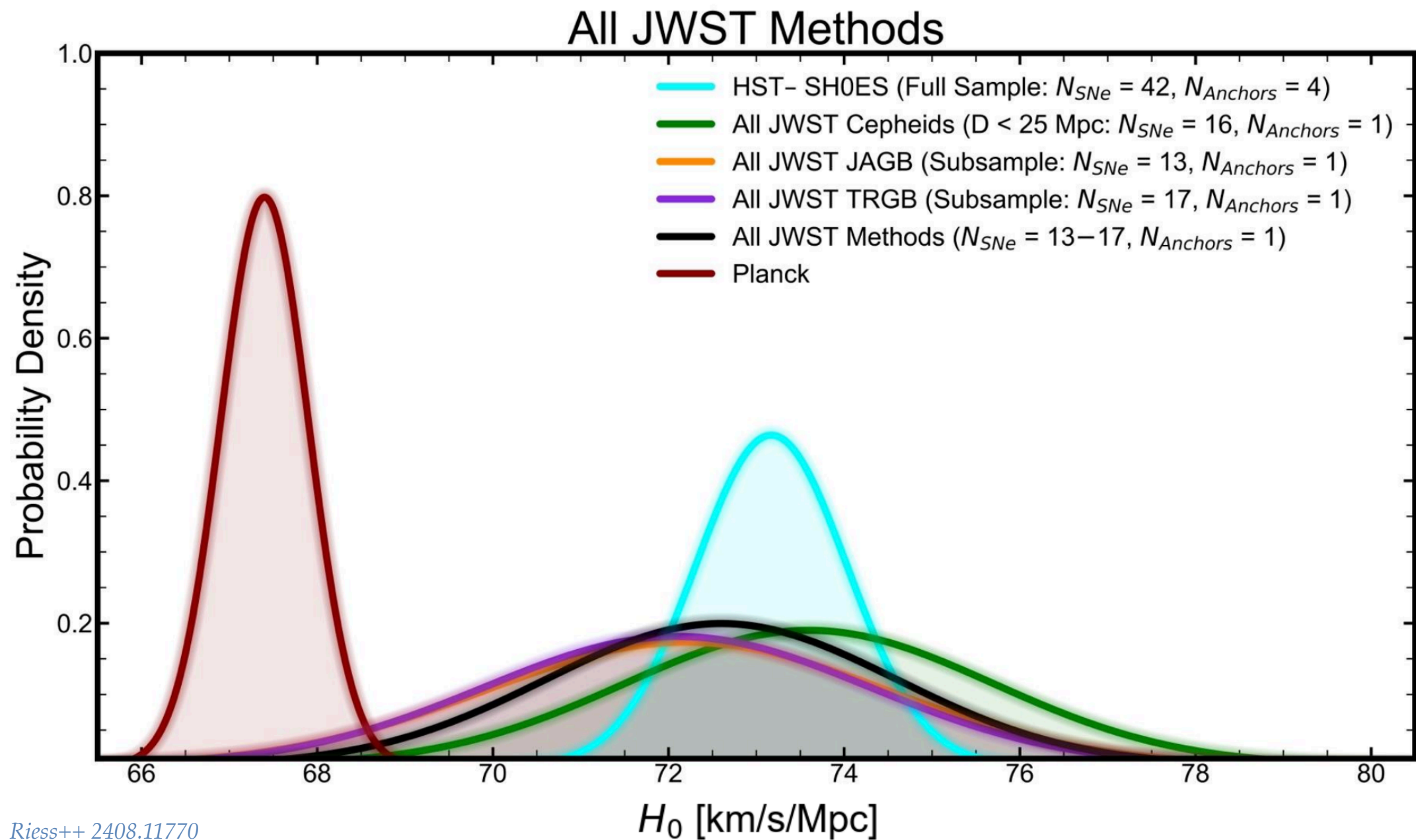
- JWST in very good agreement ( $< 1\sigma$ ) between cepheid distances and all other methods from HST
- Identified a missing source of error in the CCHP cepheid
- JAGB sample of host galaxies is 'biased low' and this is expected!



Riess++ 2408.11770



# SHOES confirms the Hubble tension with JWST



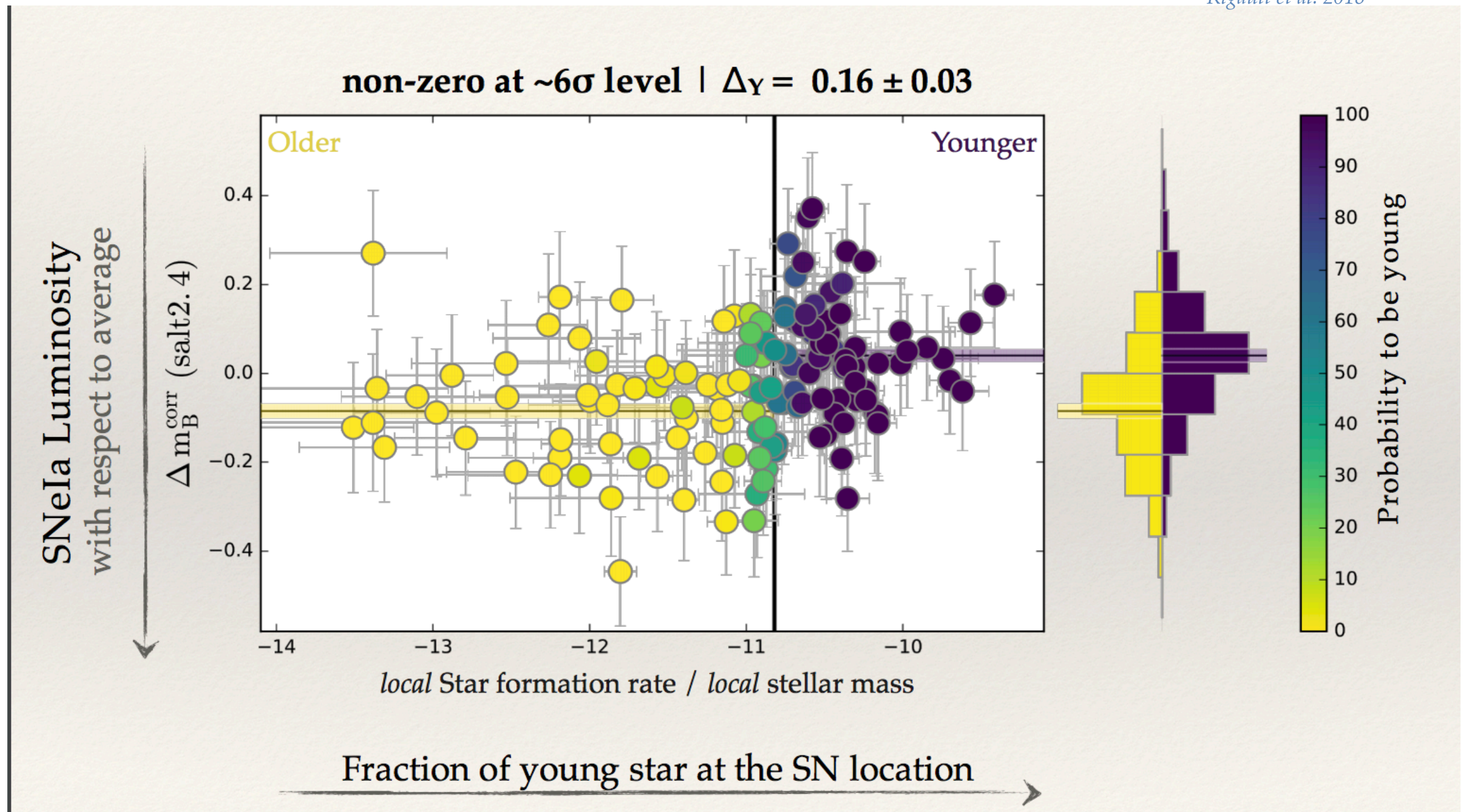
- The situation will be settled by (re-)measuring the remaining SN1a host galaxies and anchors.

**The Hubble tension is alive and well!**



# The progenitor bias

Rigault et al. 2018

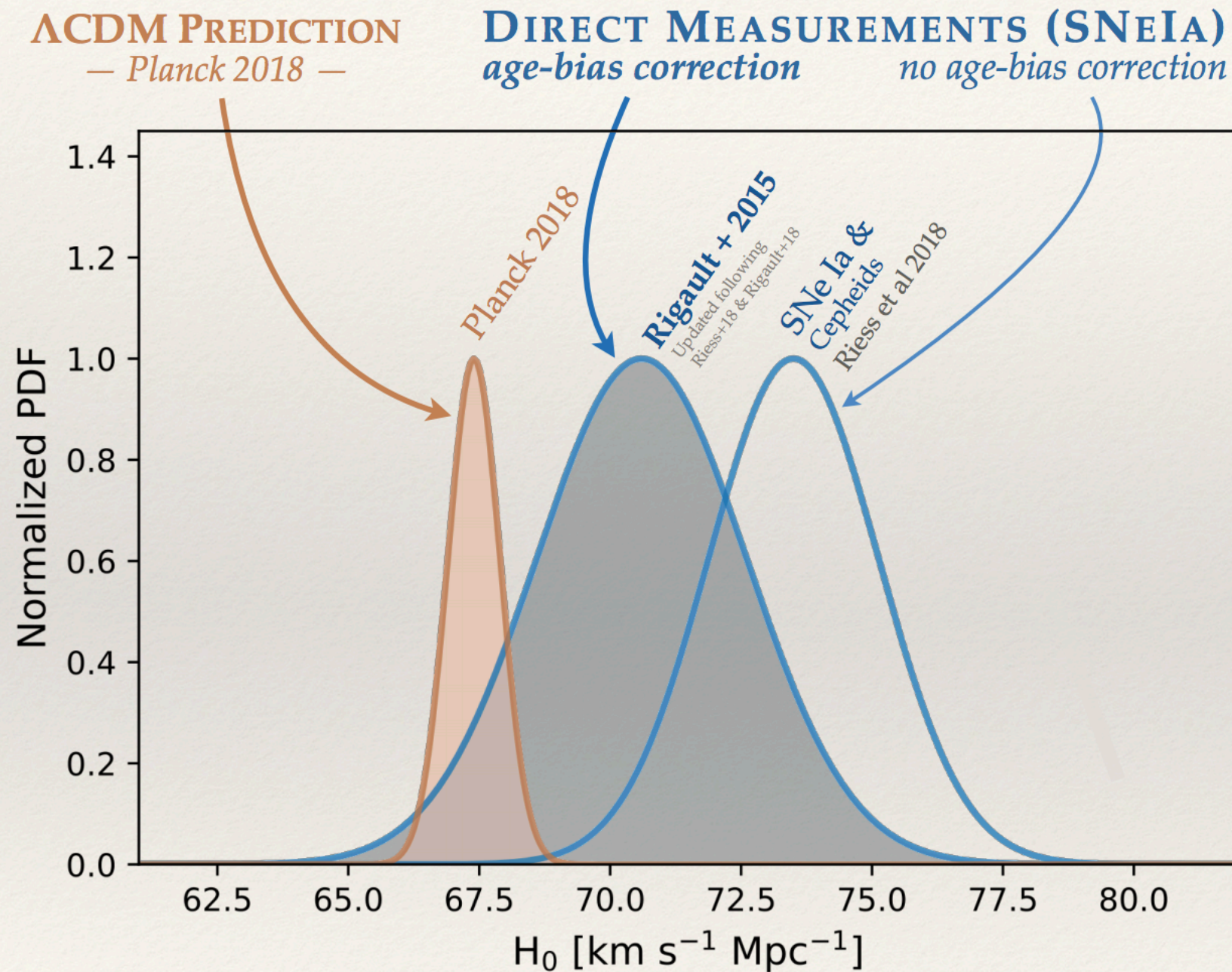


Slide by M. Rigault, IAP 2018



# Impact for $H_0$

Rigault et al. 2015, 2018



Astrophysical bias on  $H_0$   
**Up to 3% if :**

1. Different fraction of prompt  
~90% in Cepheid-SN  
vs. ~50% in Hubble flow-SN
2. Magnitude difference between  
prompts and delayed SNeIa  
age step ~0.15 mag

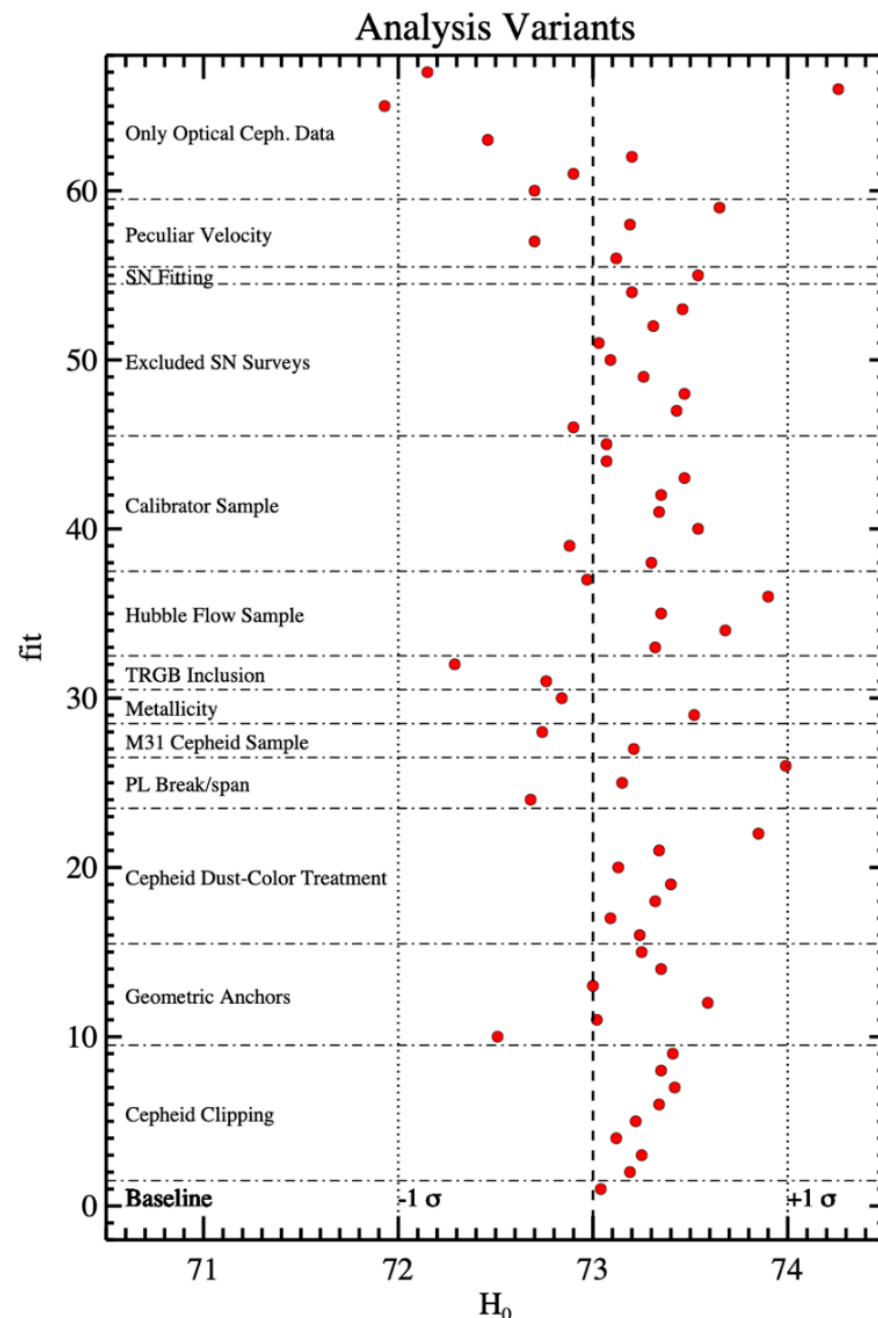
*To be confirmed using Riess's SNeIa*

Slide by M. Rigault, IAP 2018



# SHOES estimates of systematic uncertainties

Analysis Variants: 12 categories, 67 variants, bifurcations, extensions, etc



- Optical Cepheid data only (72.7)
- Different pec. vel map or none (73.1,72.7)
- SN scatter ind. wave+mass step (73.5)
- No pre-2000 SNe (73.2)
- closest half hosts (73.1)
- most crowded half (73.4)
- least crowded half (73.3)
- Skip “local hole”  $z > 0.06$  (73.4)
- All host types (73.3)
- include TRGB (consistent) jointly (72.5)
- No metallicity term (73.5)
- Break in PL at  $P=10$  days (72.7)
- No dust correction (74.8)
- Individual host dust law (73.9)
- Free param dust law (73.3)
- Low  $R_V=2.5$  dust law (73.2)
- Two of three anchors (73.0,73.4,73.2)
- No outlier rejection (73.4)

Bottom line: hard to get below 72.5, above 73.5, propagate dispersion as extra systematic

# A local void?

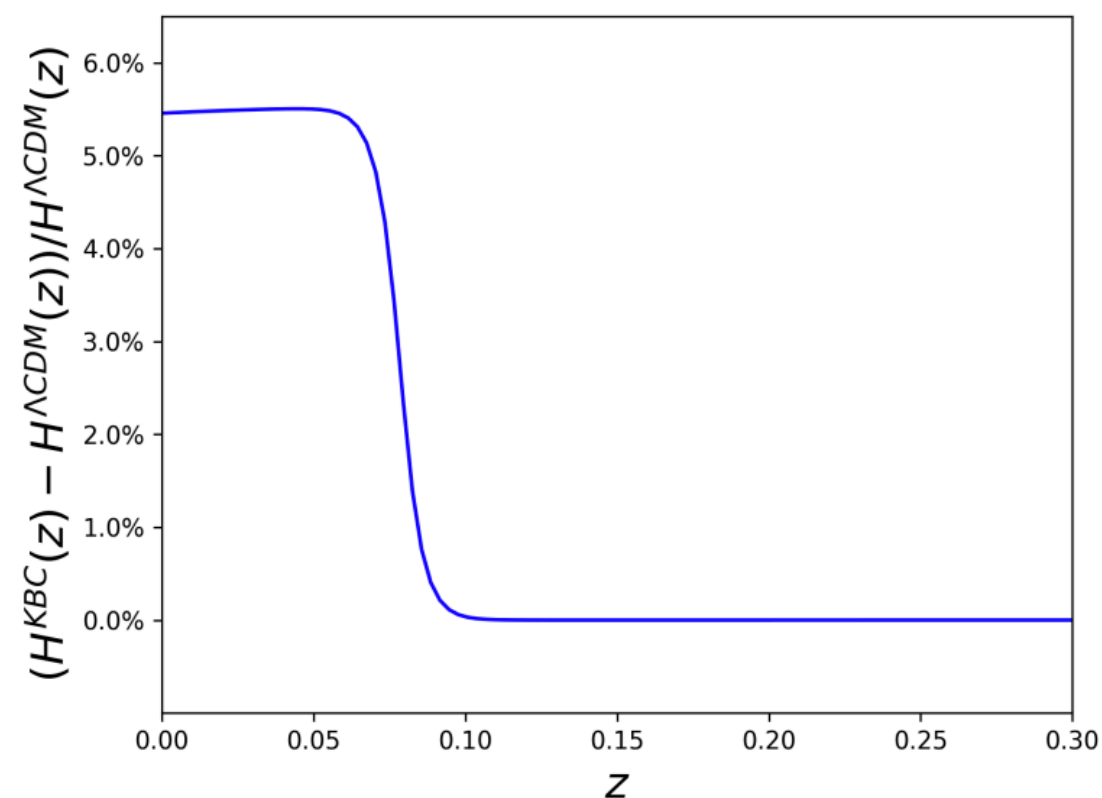
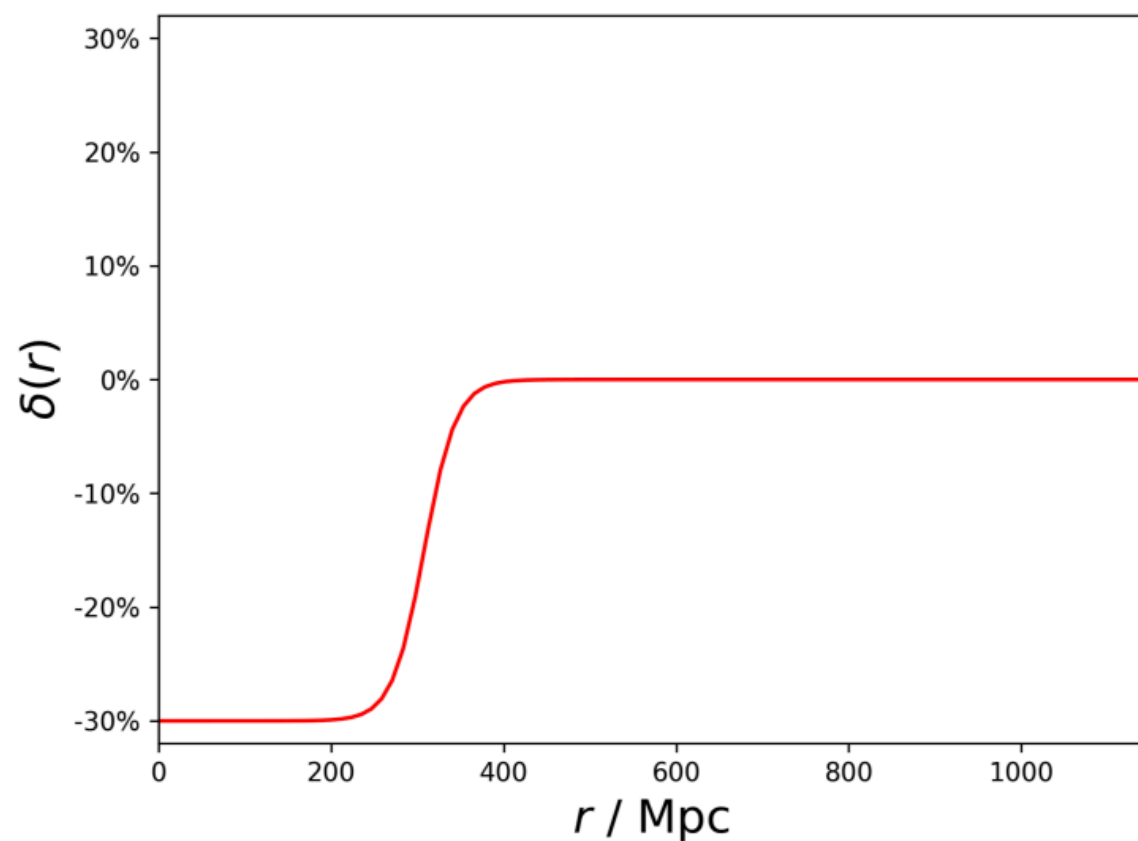
*Kenworthy++ 1901.08681*

$$\frac{\Delta H}{H} = -\frac{1}{3}\delta \cdot f$$

$$ds^2 = -dt^2 + \frac{R'^2(r, t)}{1 + 2r^2 k(r) \tilde{M}^2} dr^2 + R^2(r, t) d\Omega$$

$$\delta(r) = \delta_V \frac{1 - \tanh((r - r_V)/2\Delta_r)}{1 + \tanh(r_V/2\Delta_r)}$$

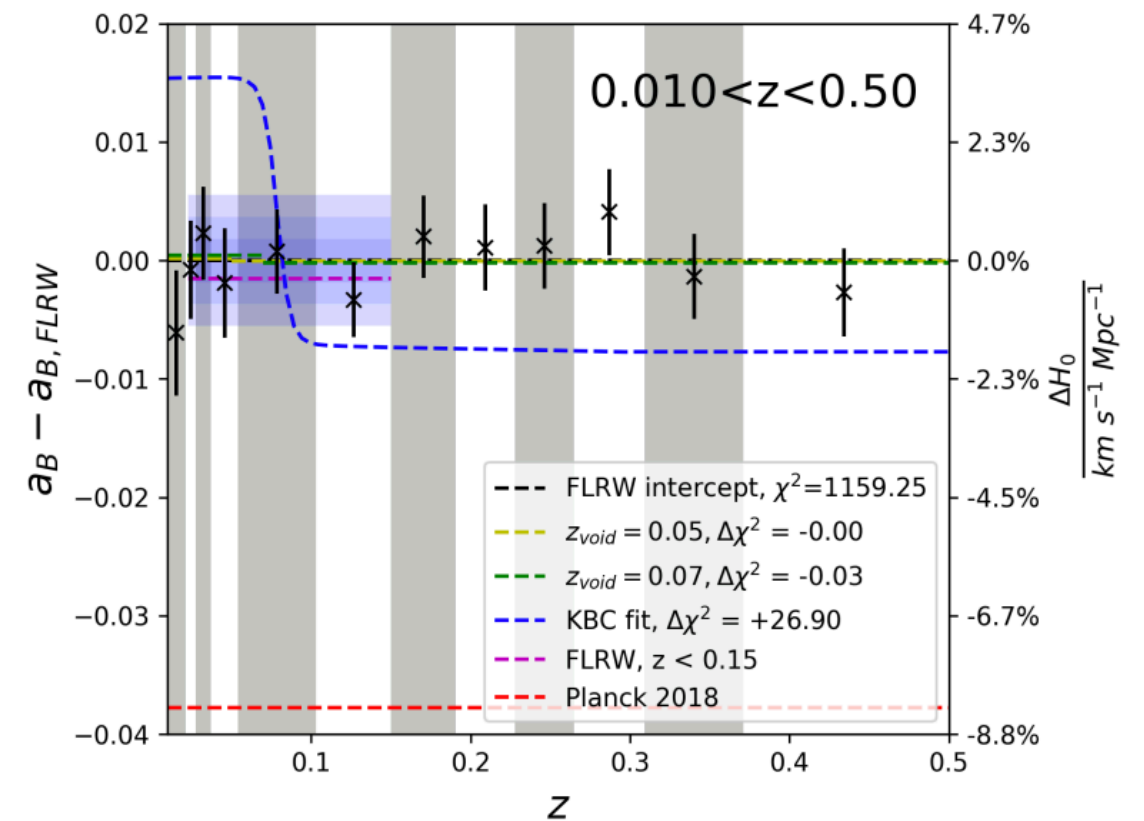
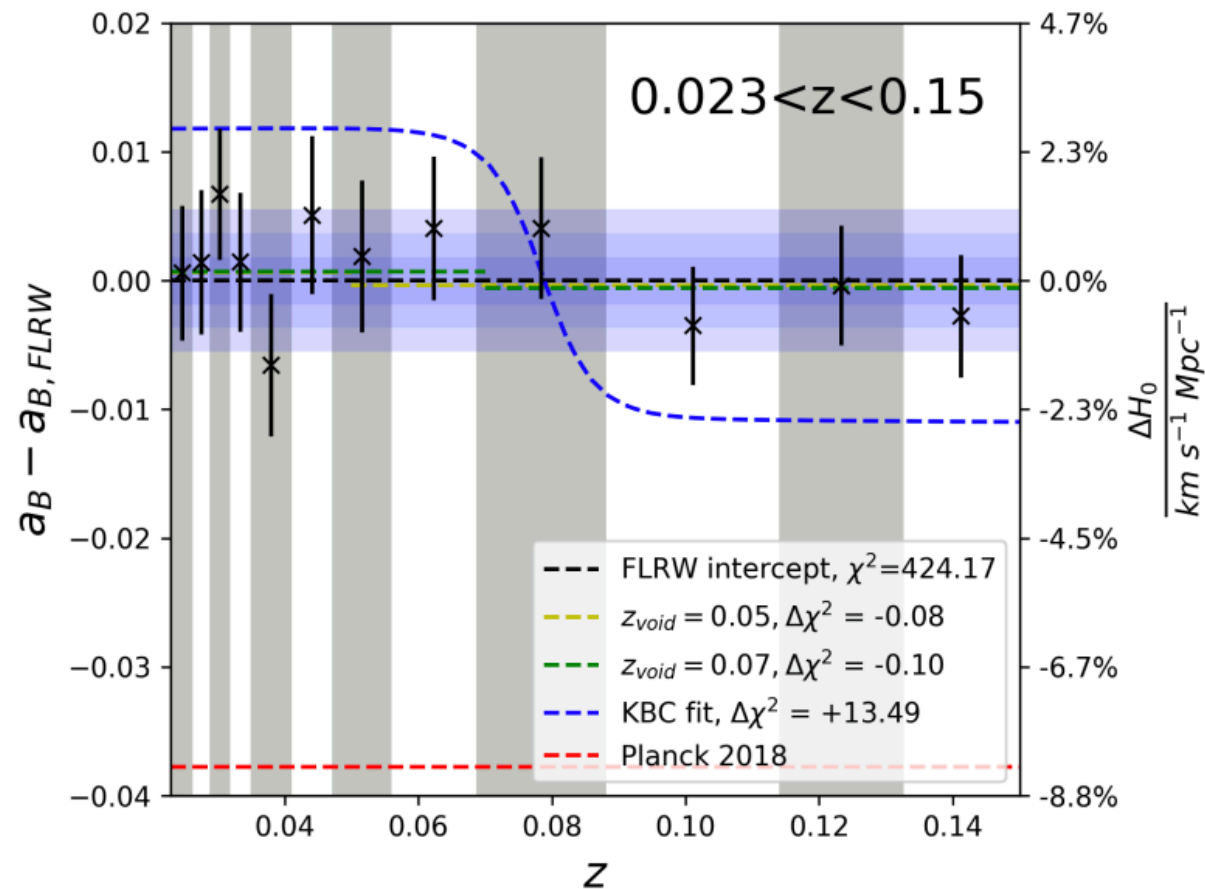
$$\frac{\dot{R}(r, t)^2}{R(r, t)^2} = H_0(r)^2 \cdot (\Omega_M(r) \frac{R_0(r)^3}{R(r, t)^3} + \Omega_k(r) \frac{R_0(r)^2}{R(r, t)^2} + \Omega_\Lambda(r))$$





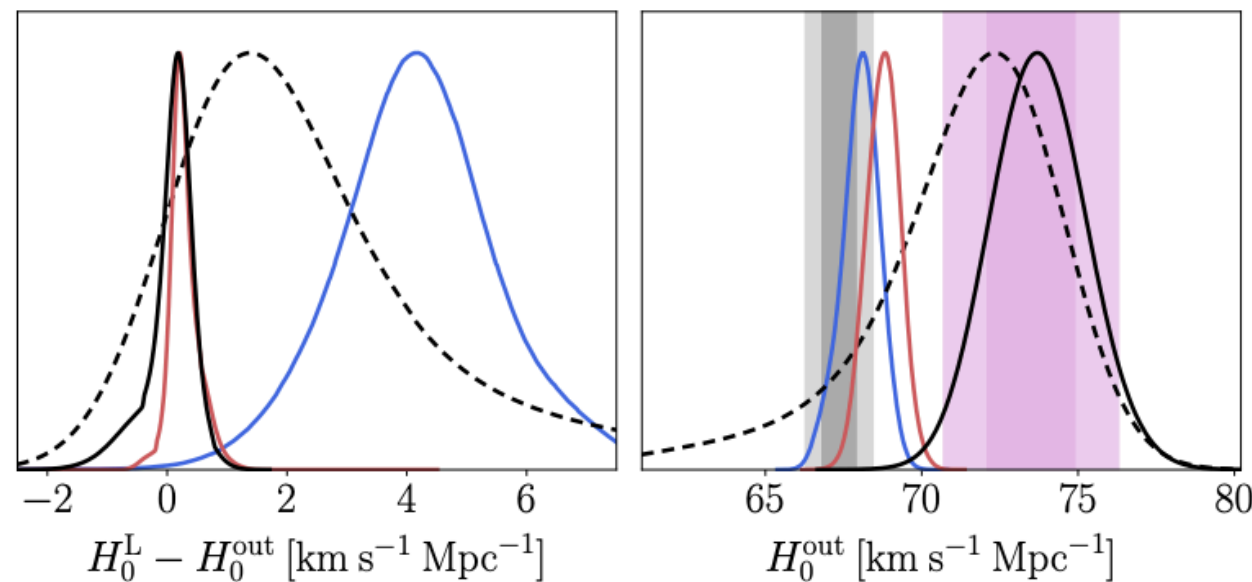
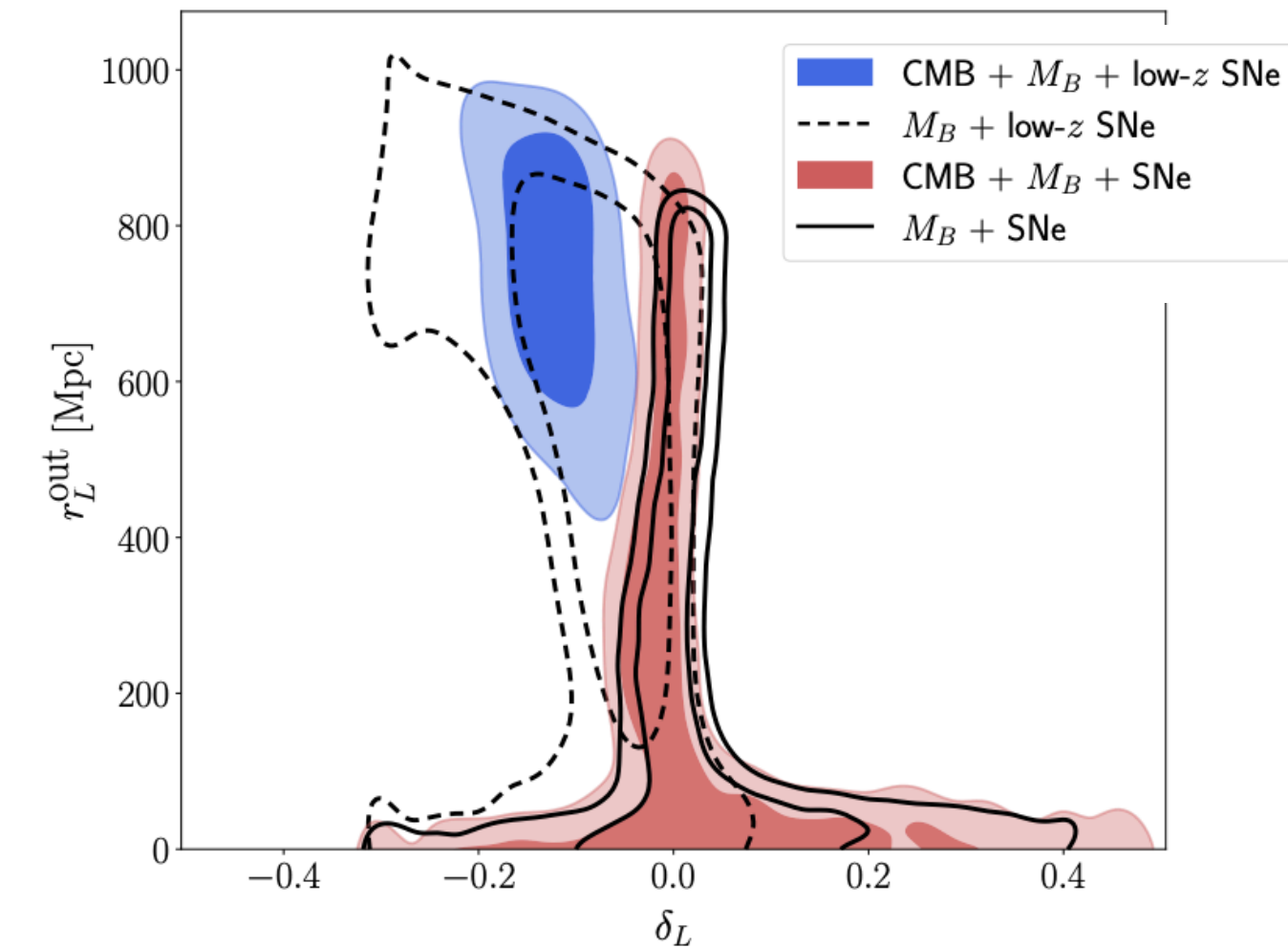
# Incompatible with the SNIa data

Kenworthy++ 1901.08681

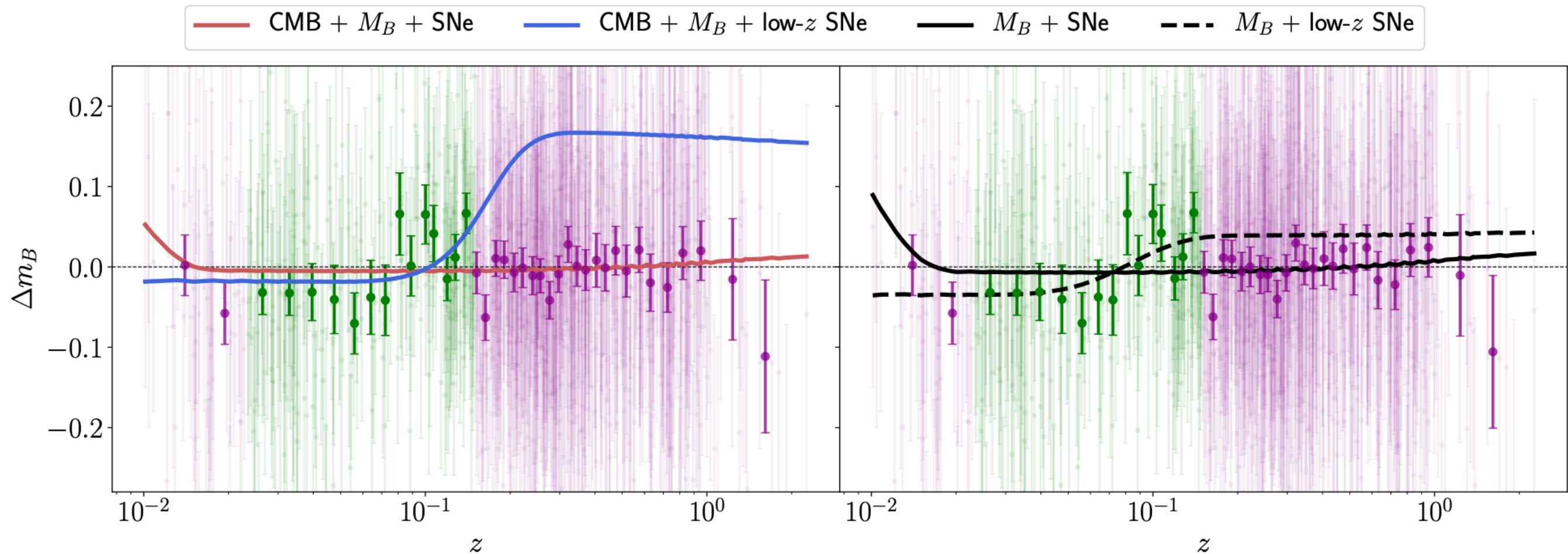


# Impact of local void beyond KBC

Camarena++ 2205.05422



# It cannot explain the Hubble tension

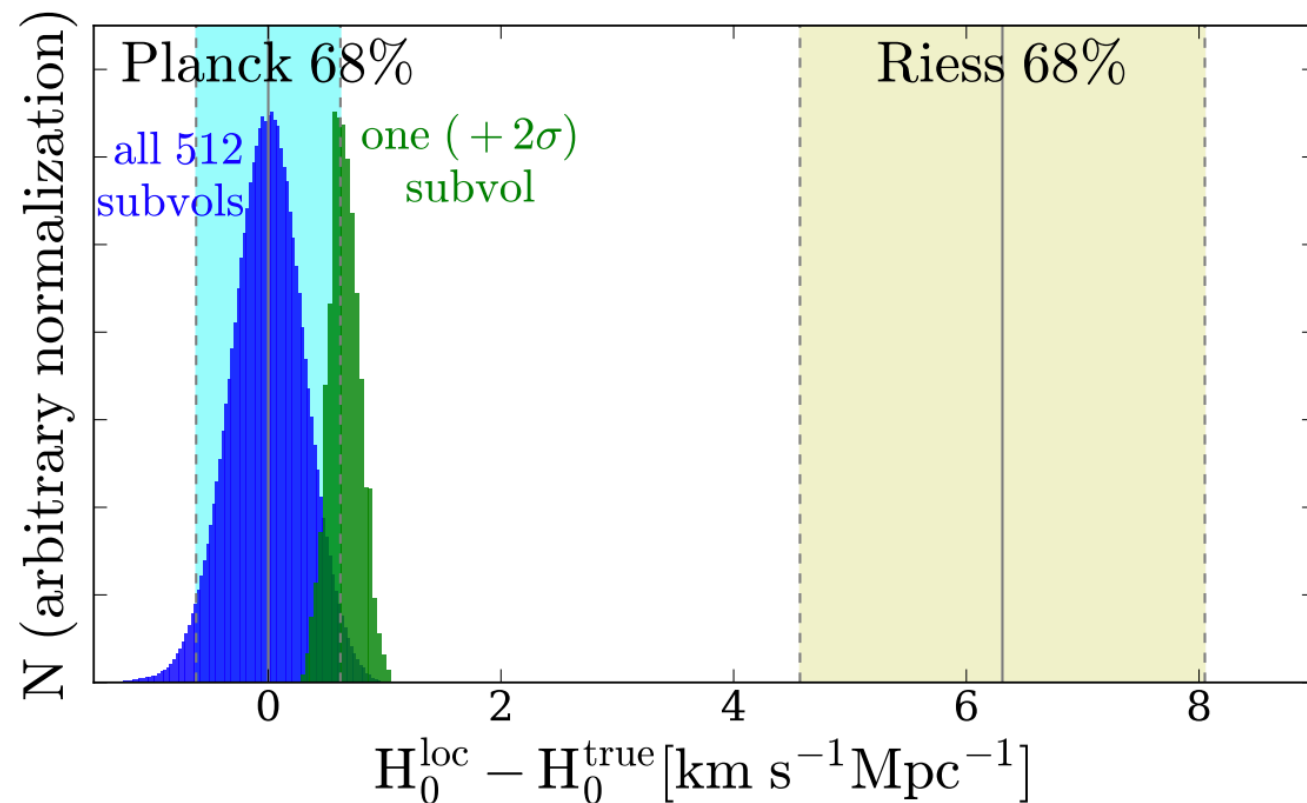


*Camarena++ 2205.05422*



# Sample variance cannot explain the Hubble tension

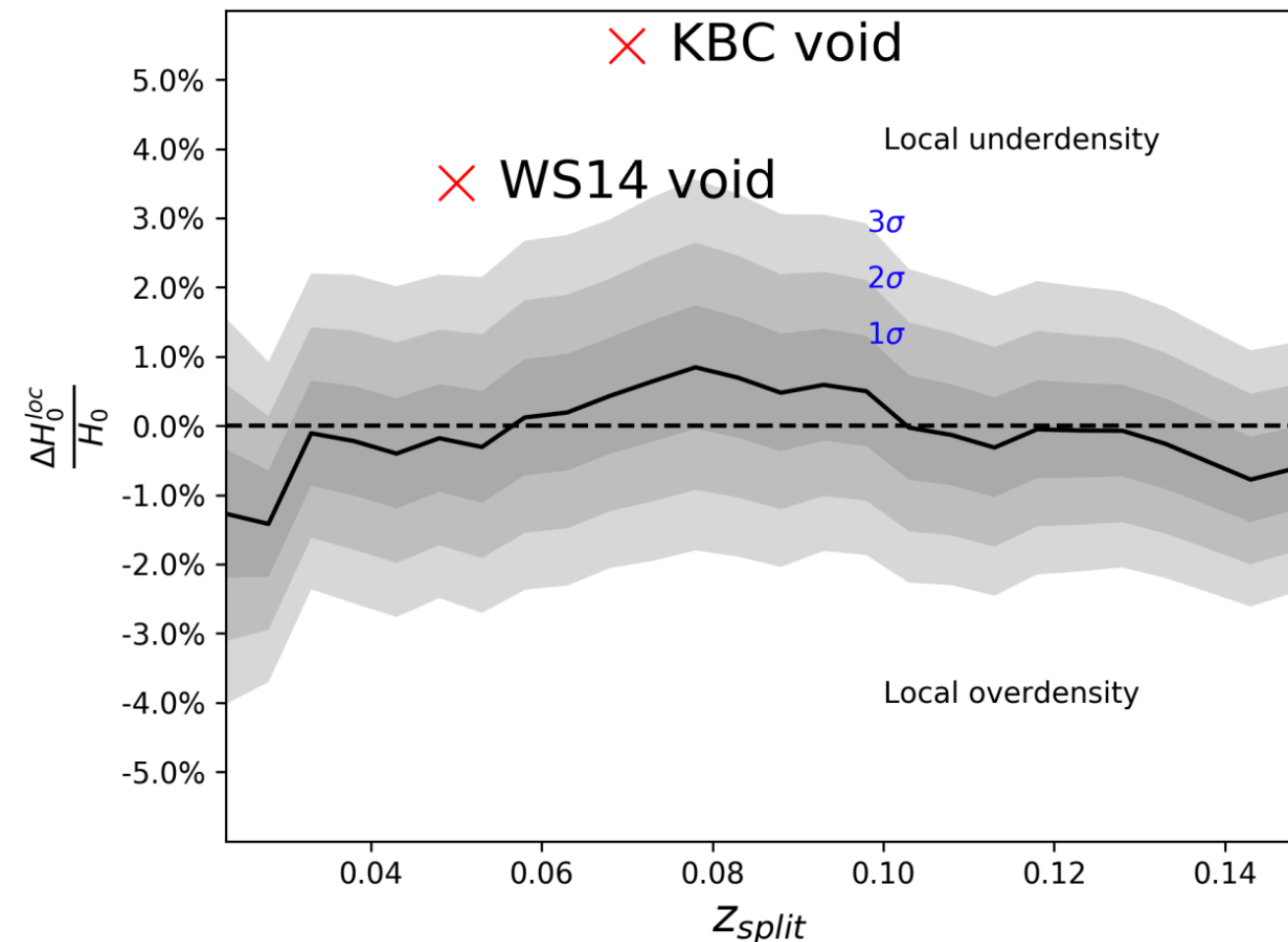
$$\Delta H_0^{\text{loc}} = \frac{1}{N} \sum_{i=1}^N \frac{v_{r,i}}{r_i}$$



*Wu&Huterer 2309.05749*

$$\sigma_{\text{sample variance}} = 0.31 \text{ km s}^{-1} \text{Mpc}^{-1}$$

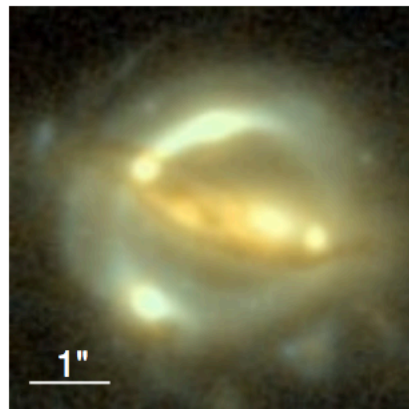
$$|H_0^{\text{Planck}} - H_0^{\text{loc}}| / \sigma_{\text{sample variance}} \simeq 20.$$



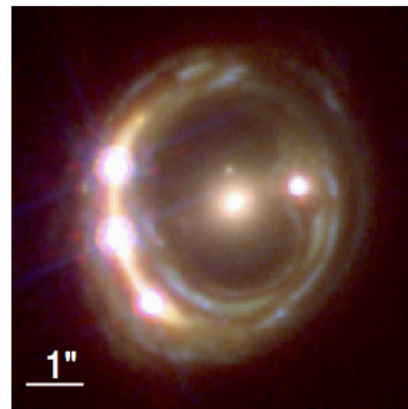
*Kenworthy++ 1901.08681*

# Strongly lensed Quasars measurement of H0

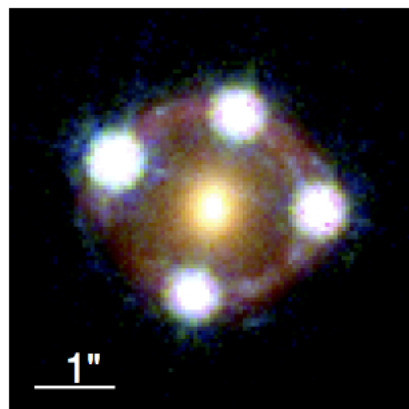
$$D_{\Delta t} \equiv (1 + z_d) \frac{D_d D_s}{D_{ds}}$$



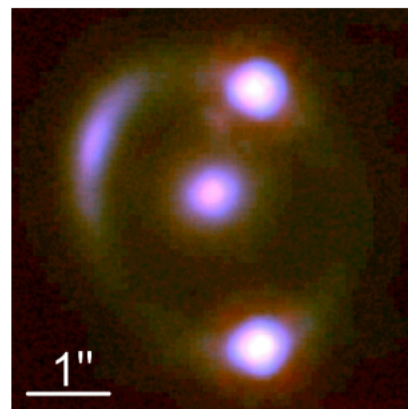
(a) B1608+656



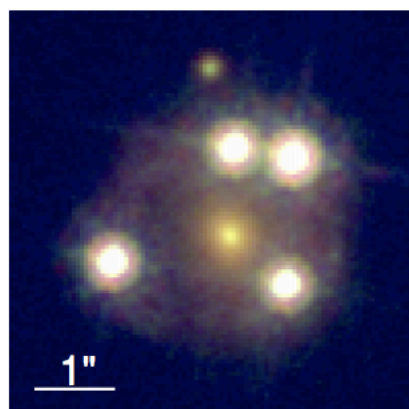
(b) RXJ1131-1231



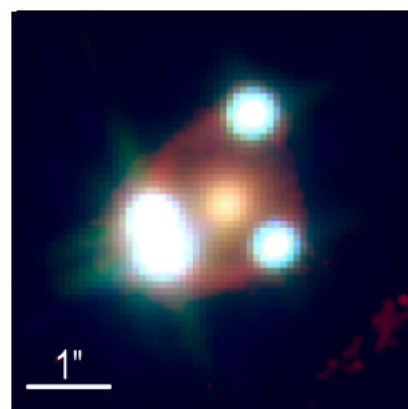
(c) HE 0435-1223



(d) SDSS 1206+4332

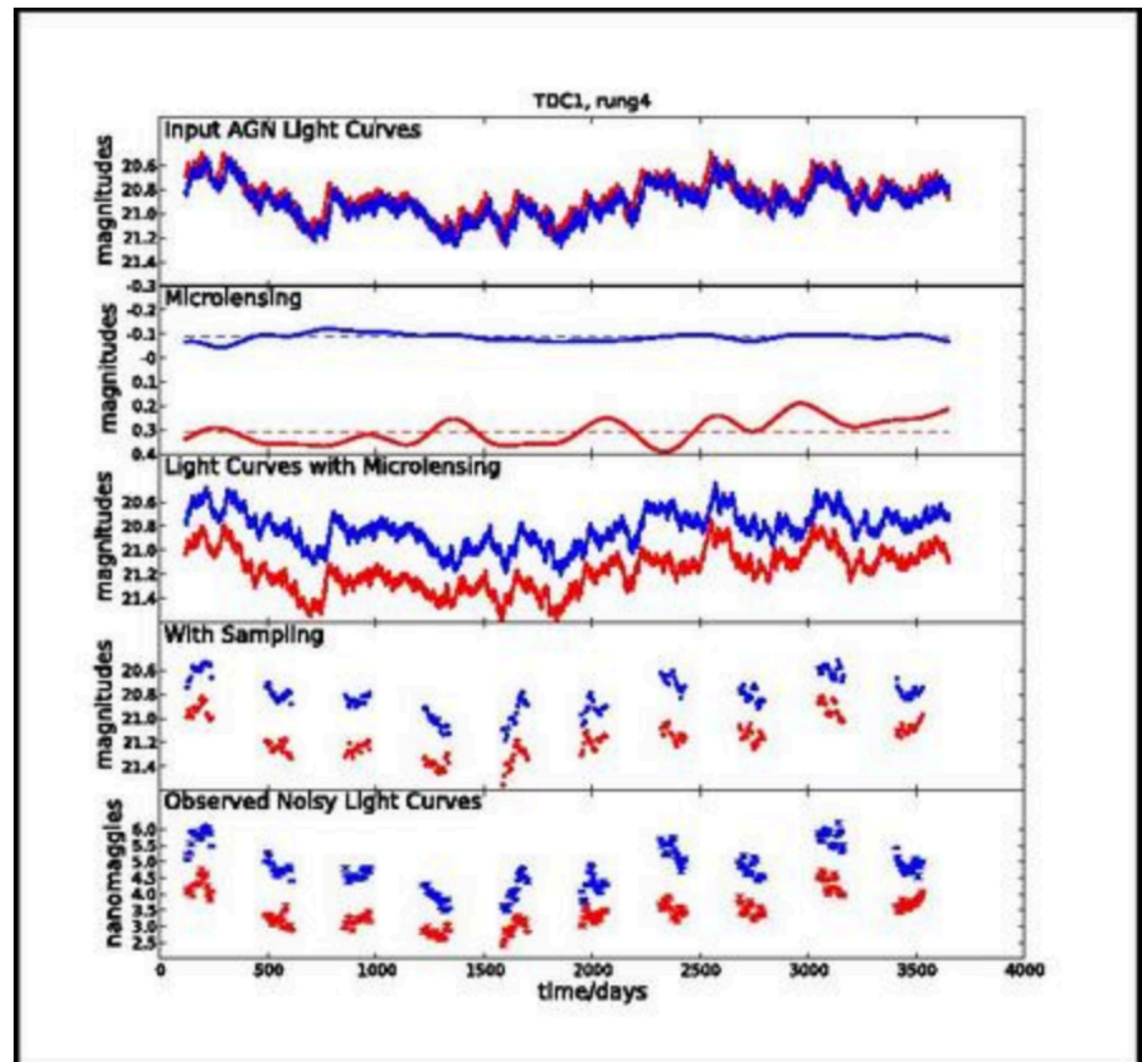


(e) WFI2033-4723

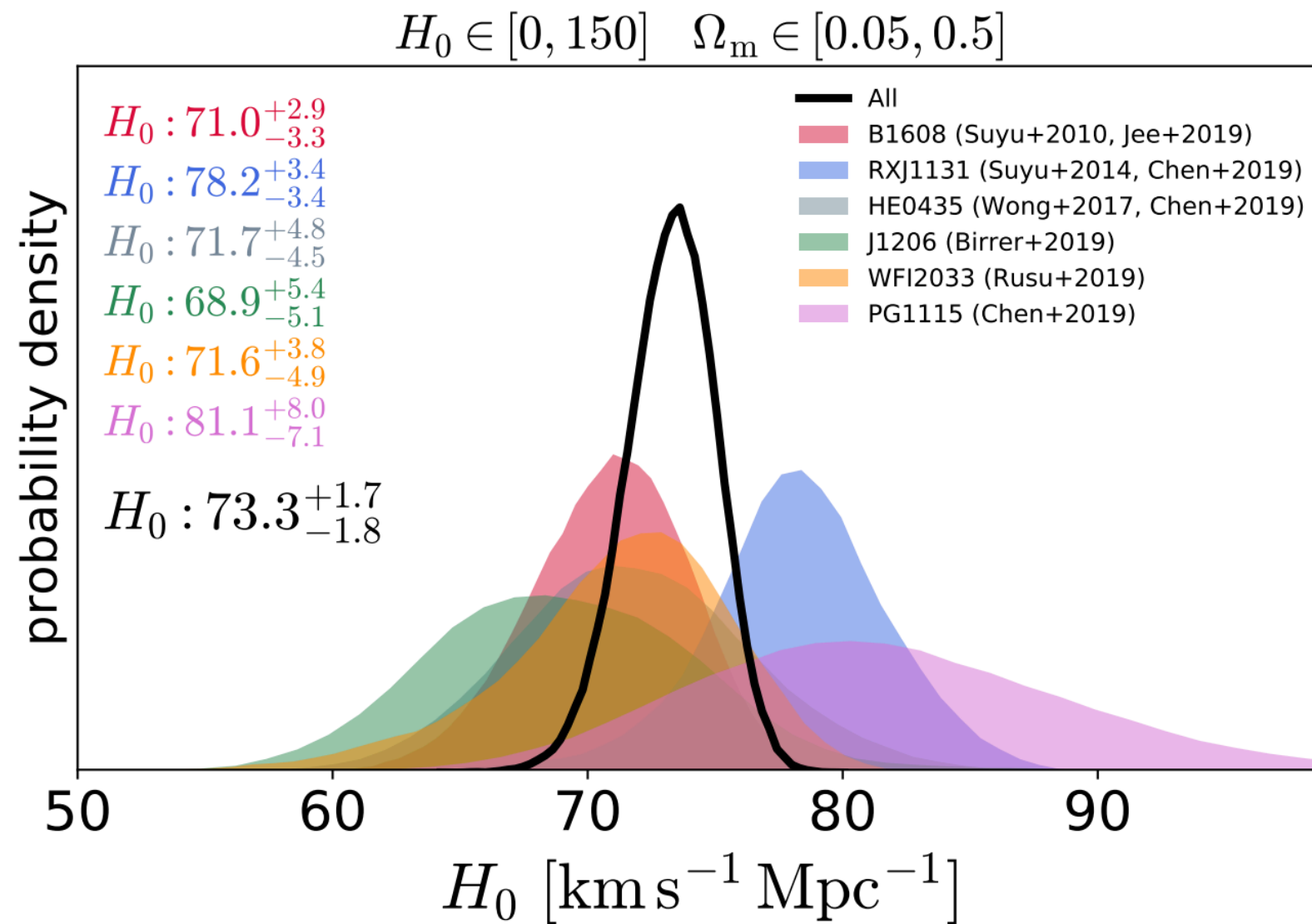


(f) PG 1115+080

*Wong et al. 1907.04869*



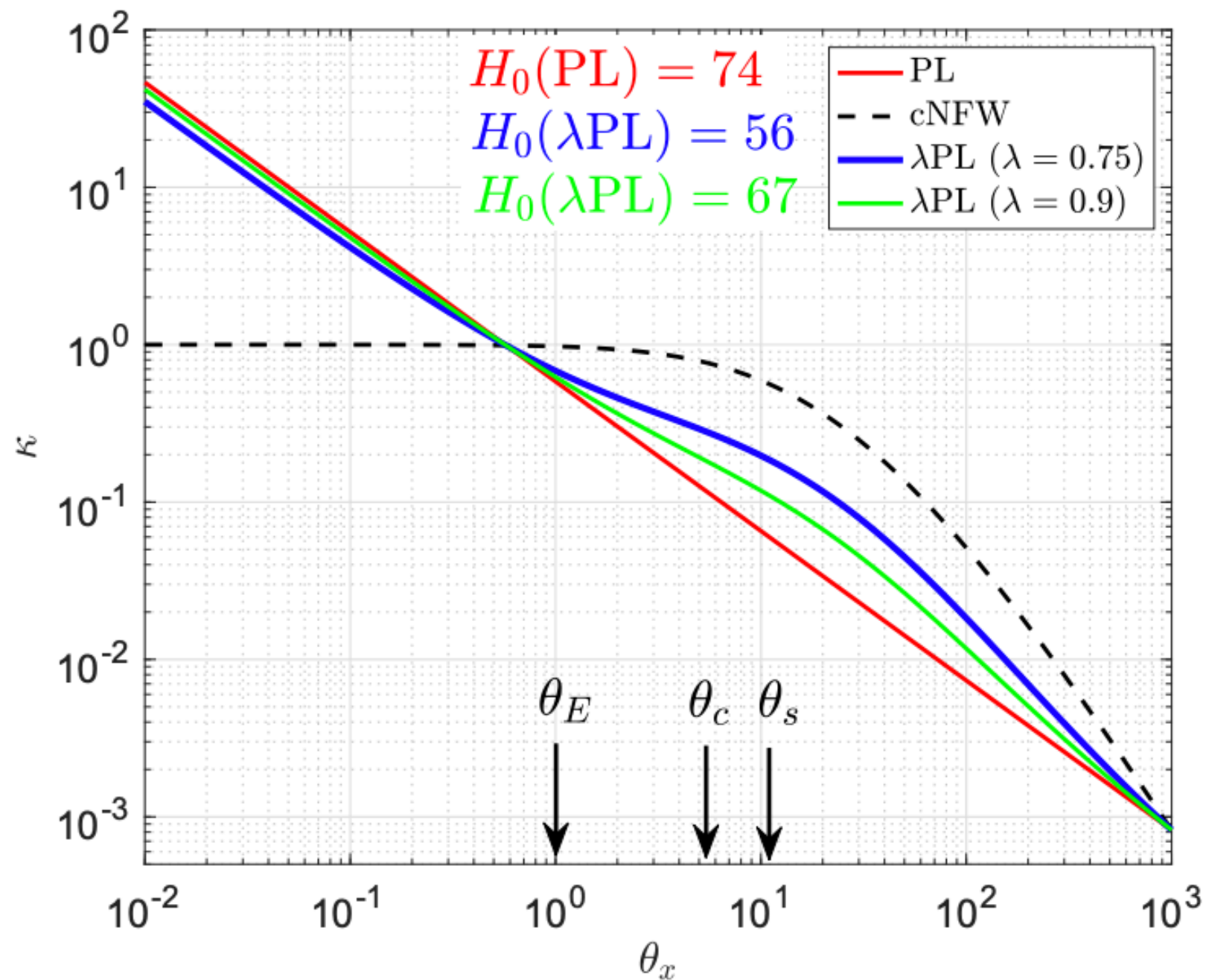
# H0LiCOW: $H_0$ measurement to few %



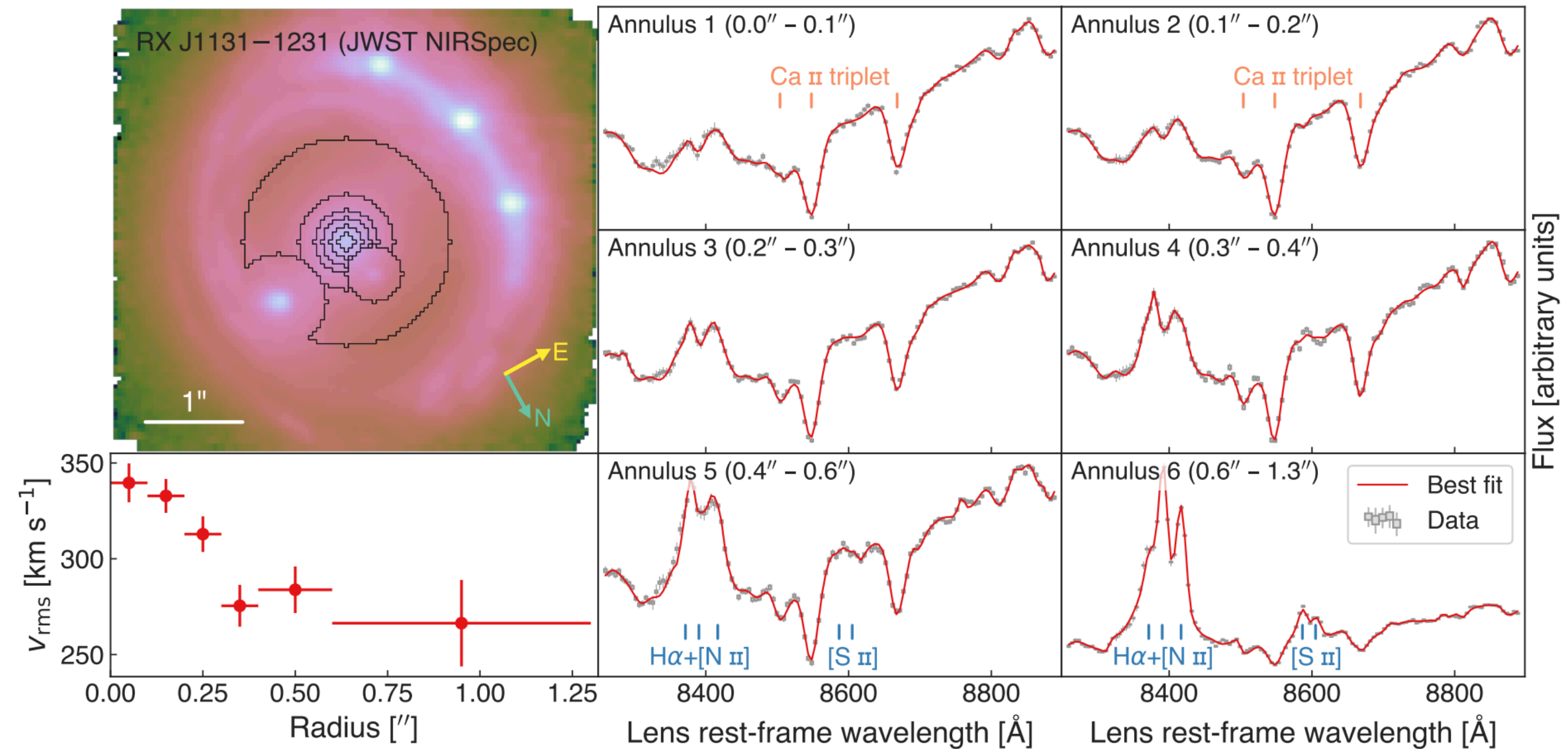
*Wong et al. 1907.04869*



# The “mass-sheet” degeneracy

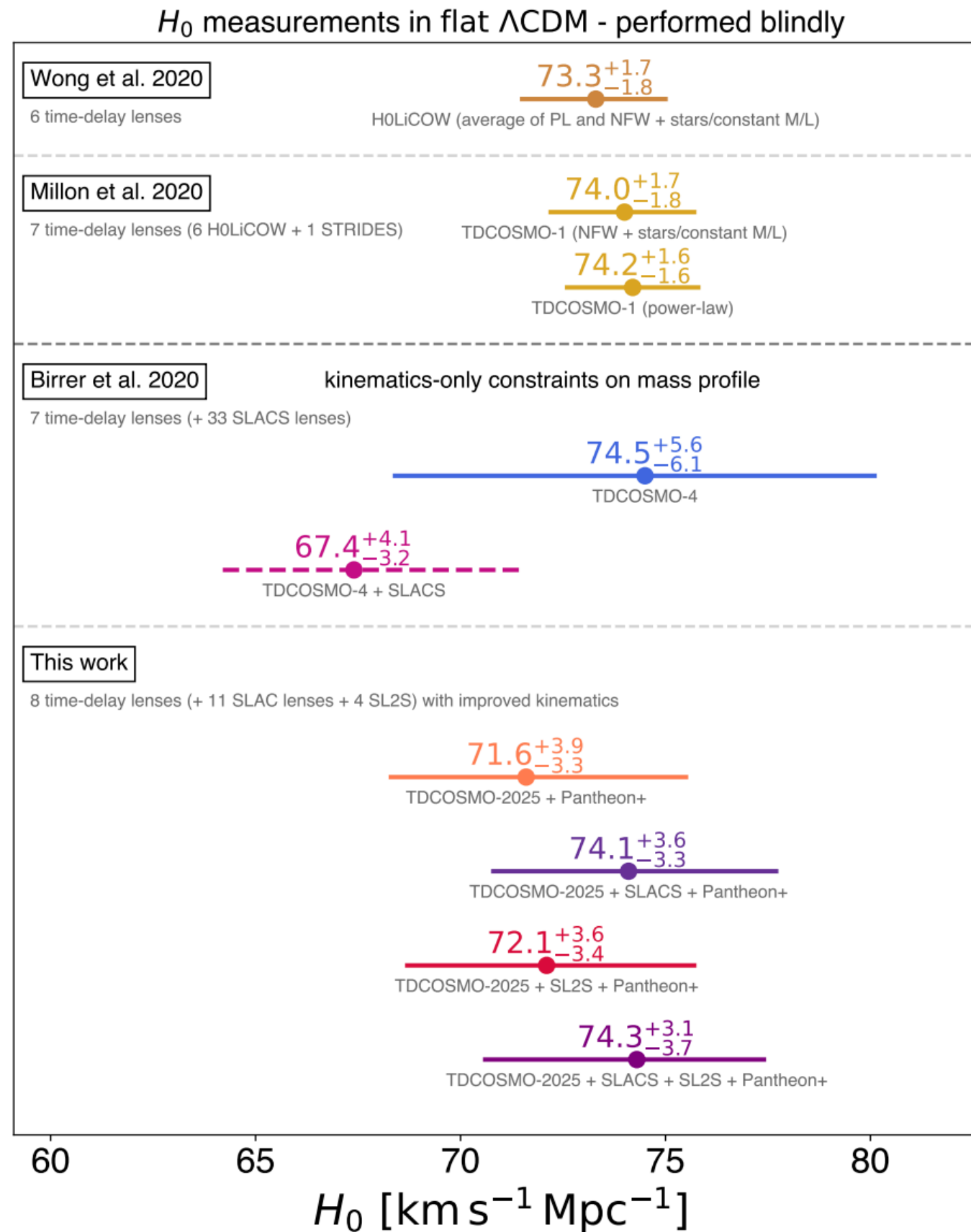


# TD Cosmo: Conservative H0 measurement



*Birrer et al 2506.03023*

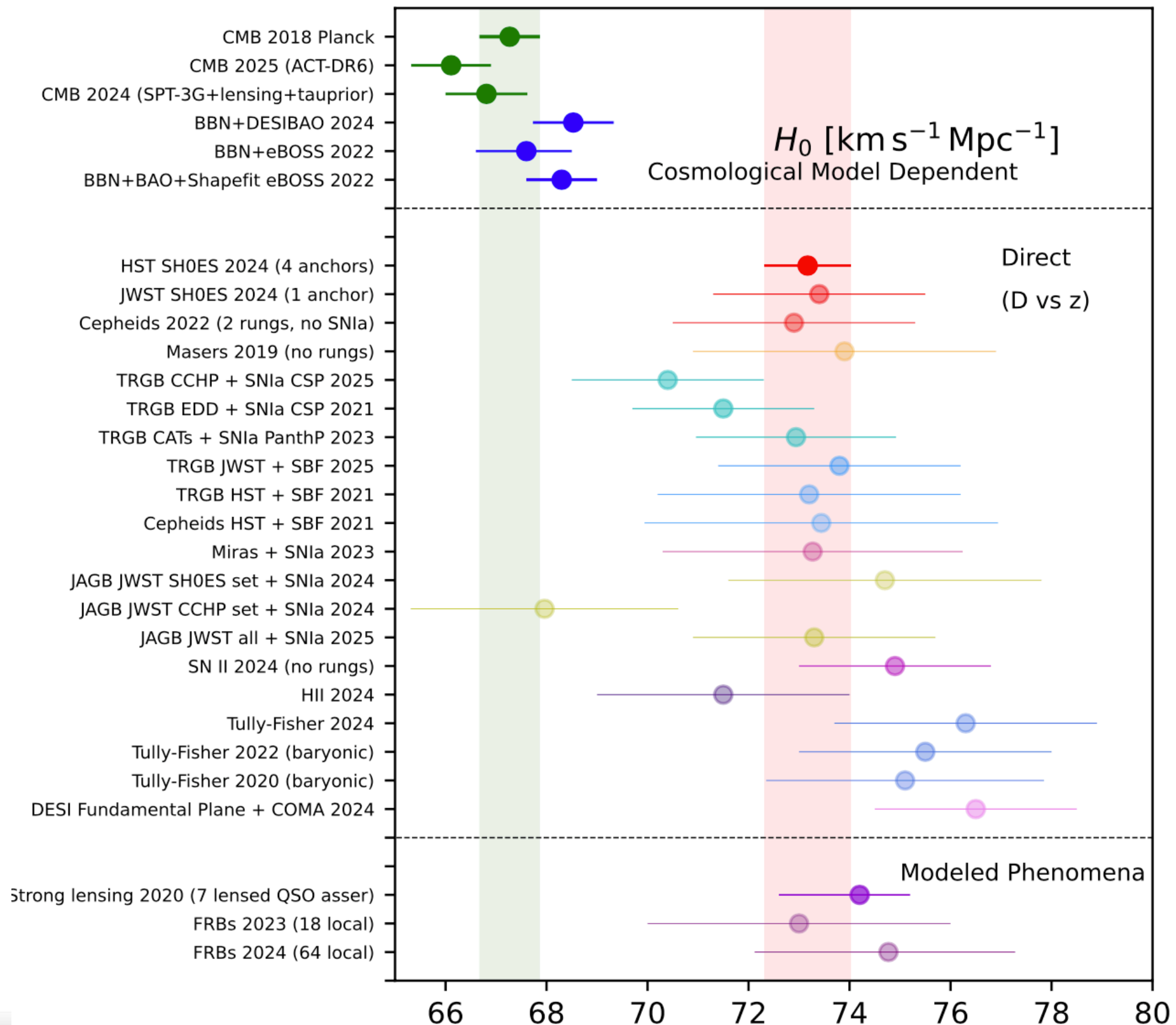
# High $H_0$ but large error bars



*Birrer et al 2506.03023*

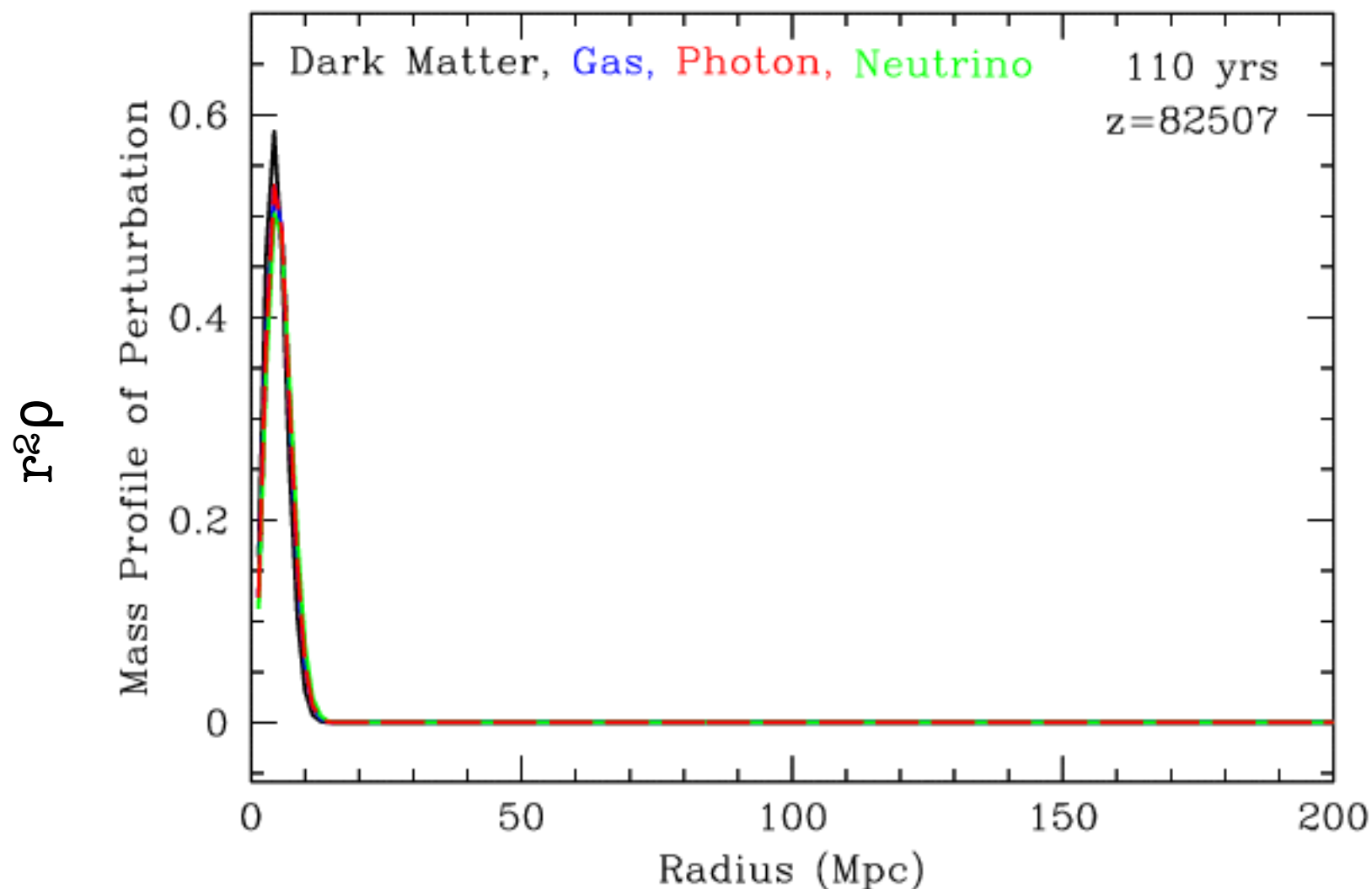


# The Hubble tension



# The BAO: a standard ruler in the sky

- Before recombination (380 000 yr): a tightly coupled photon-baryon plasma with acoustic waves.
- The ‘sound horizon’ is the **distance travelled by sound wave until recombination**.



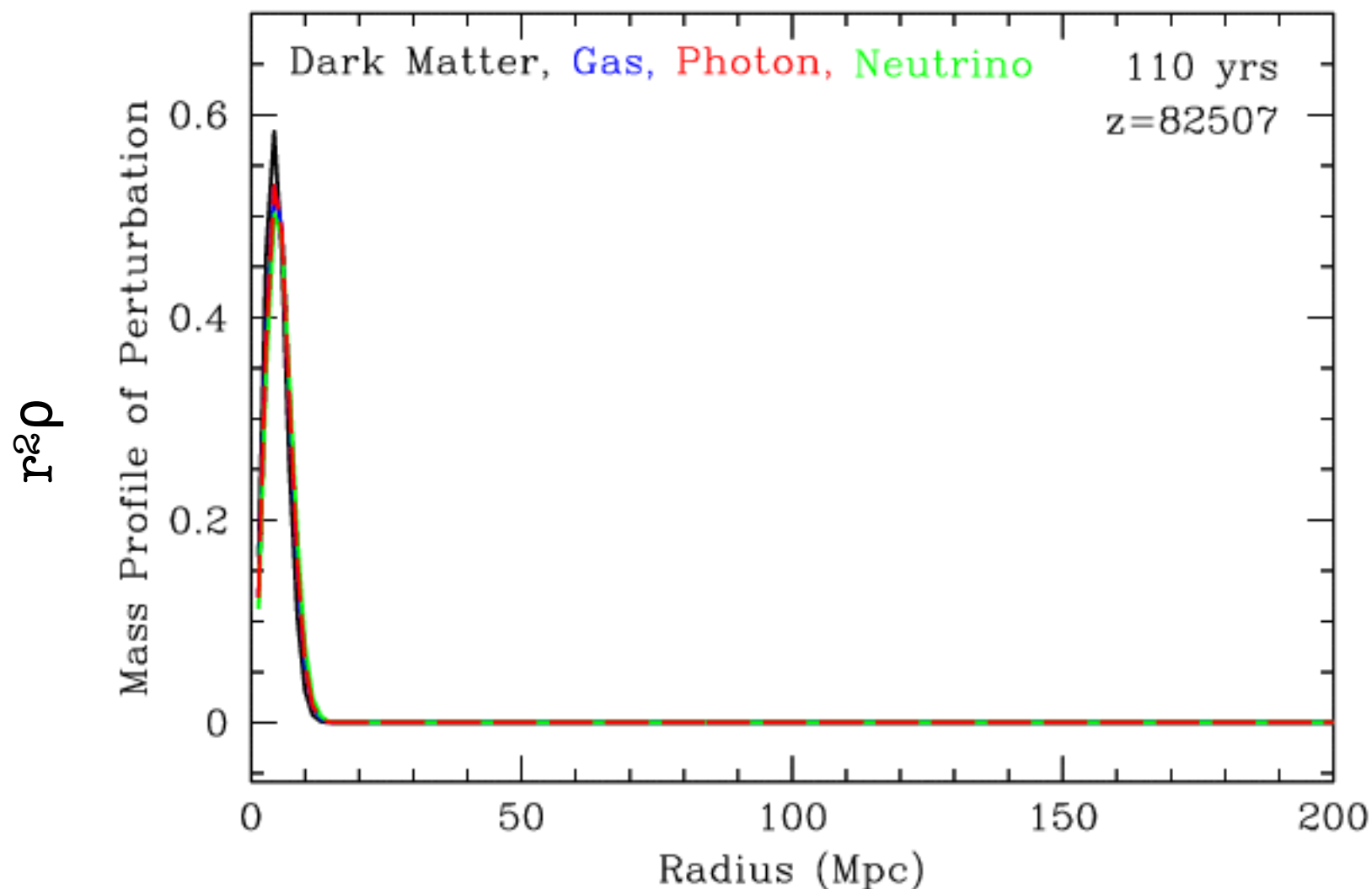
$$r_s = \int_{t_{rh}}^{t_{rec}} c_s(t) dt$$

*credit: Bassett & Hlozek*

© D. Eisenstein

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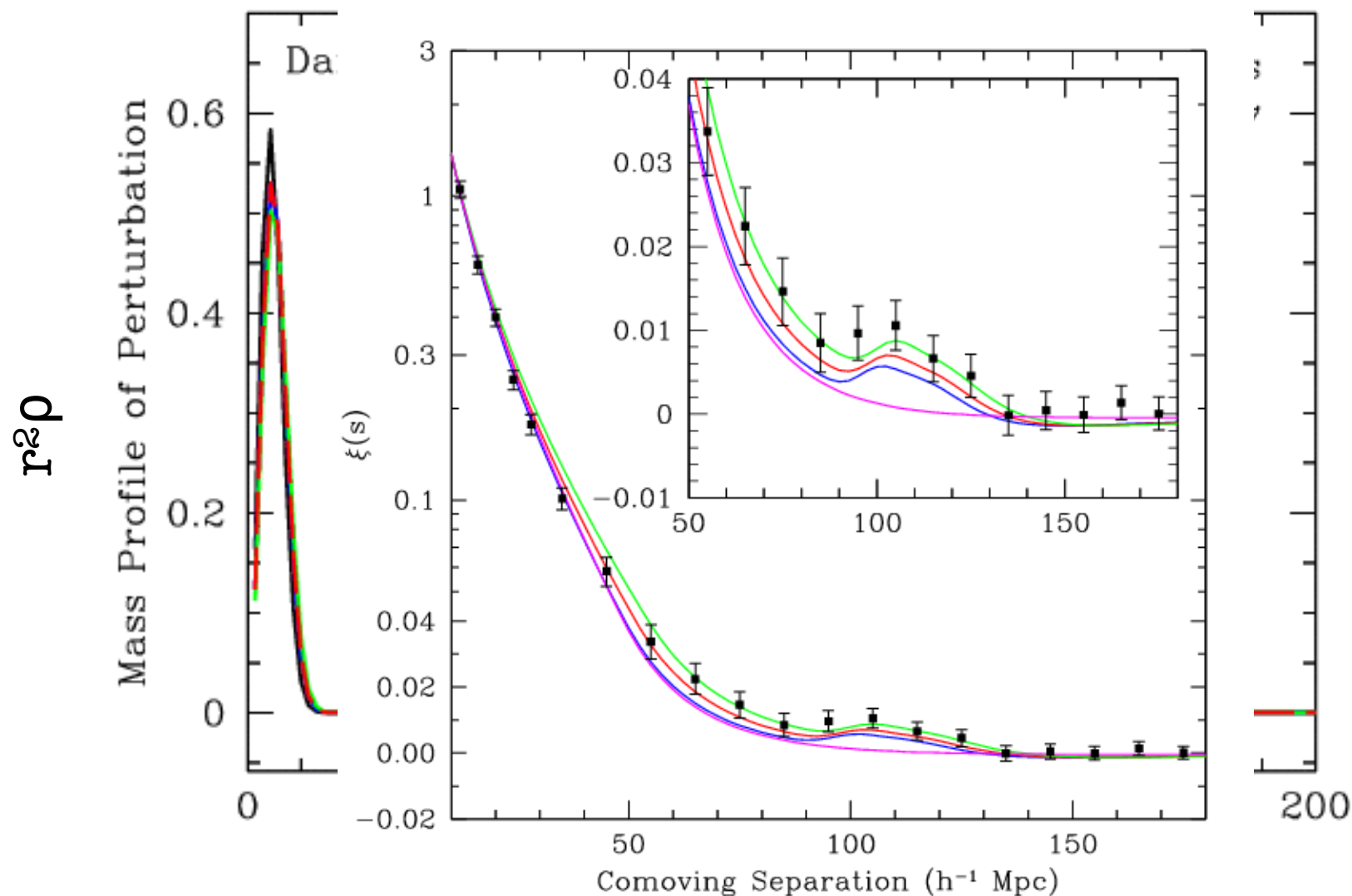
*credit: Bassett & Hlozek*

© D. Eisenstein



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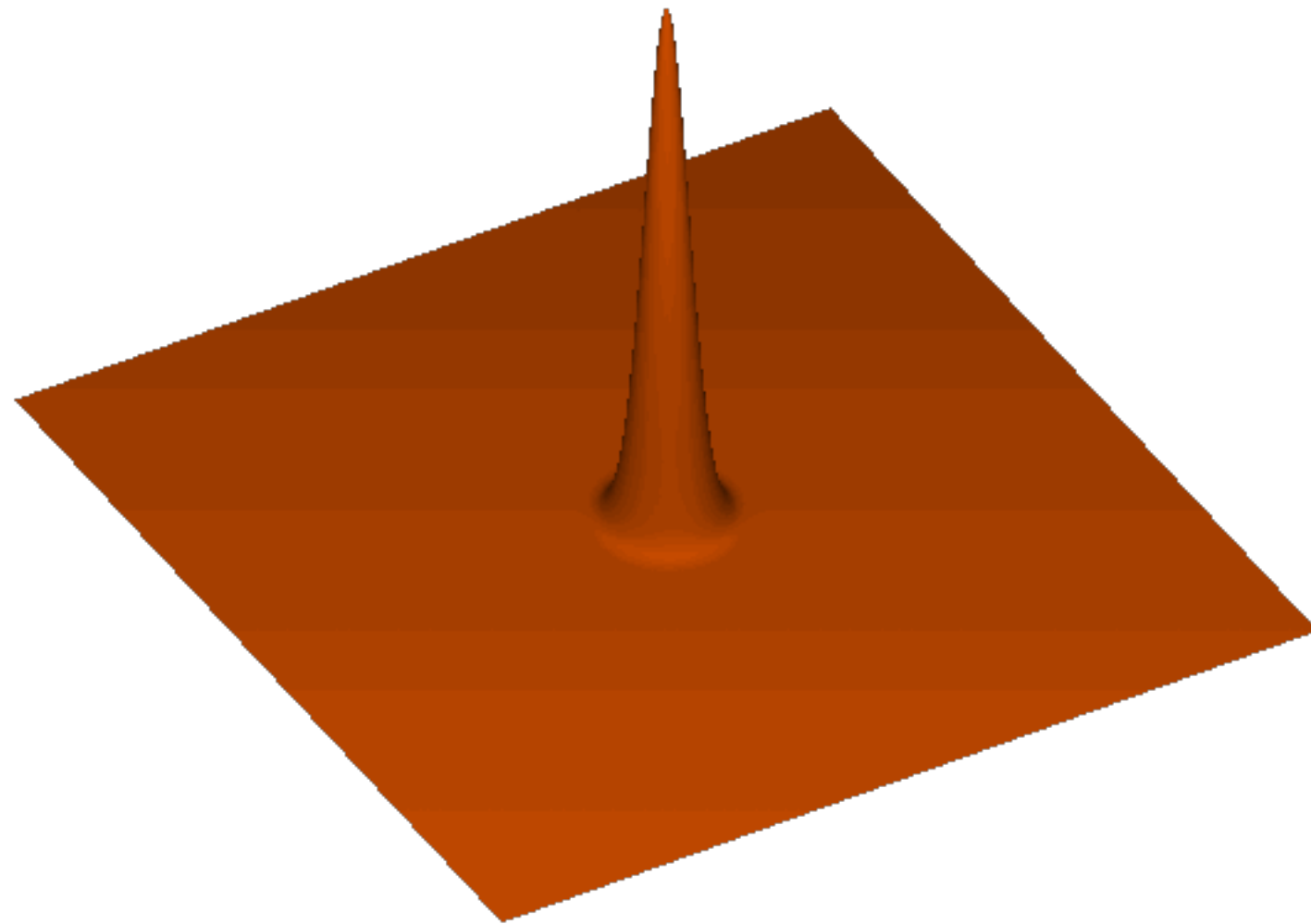
*credit: Bassett & Hlozek*

*Eisenstein et al. 2005*

© D. Eisenstein

# The BAO: a standard ruler in the sky

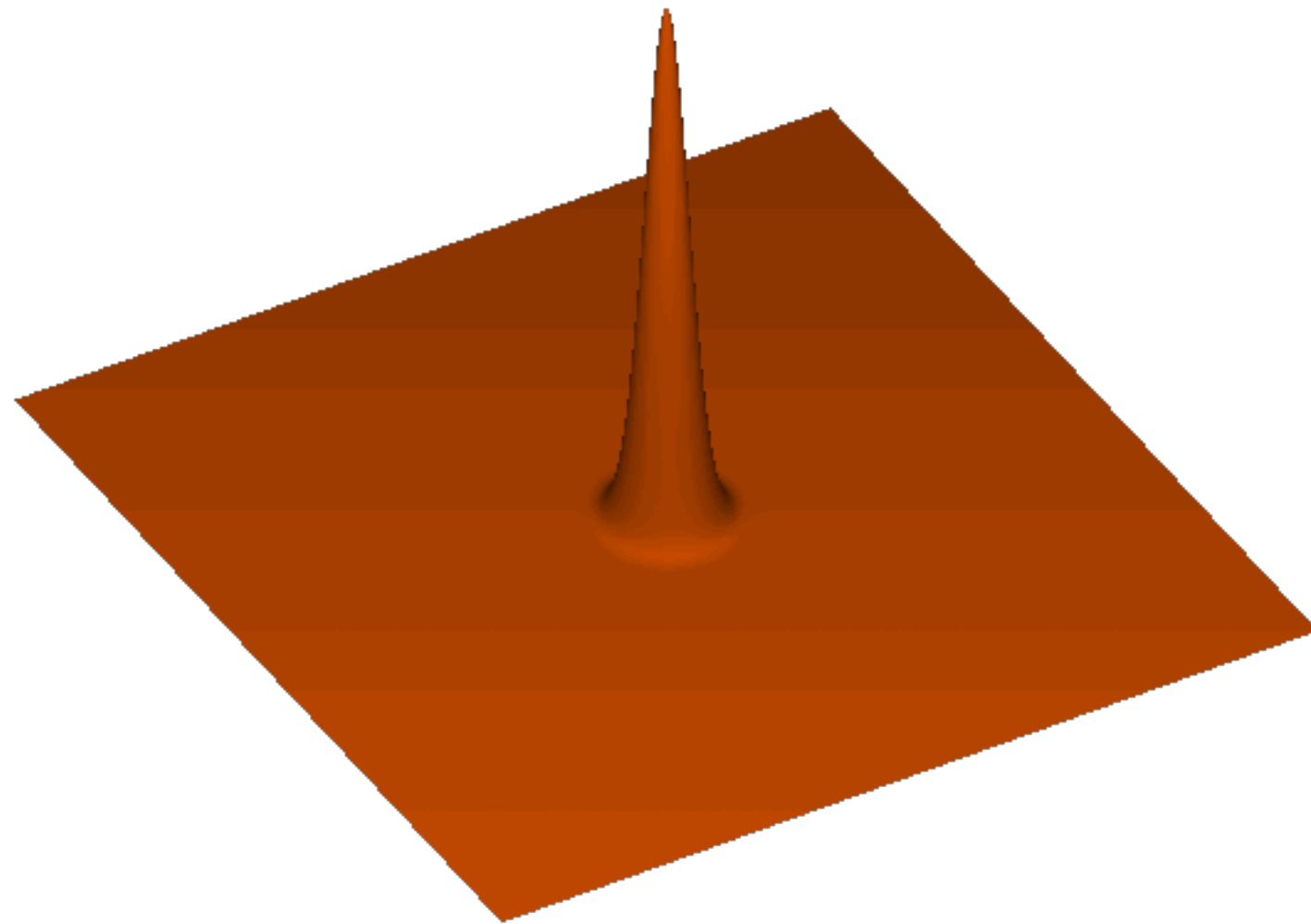
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*credit: Bassett & Hlozek*

# The BAO: a standard ruler in the sky

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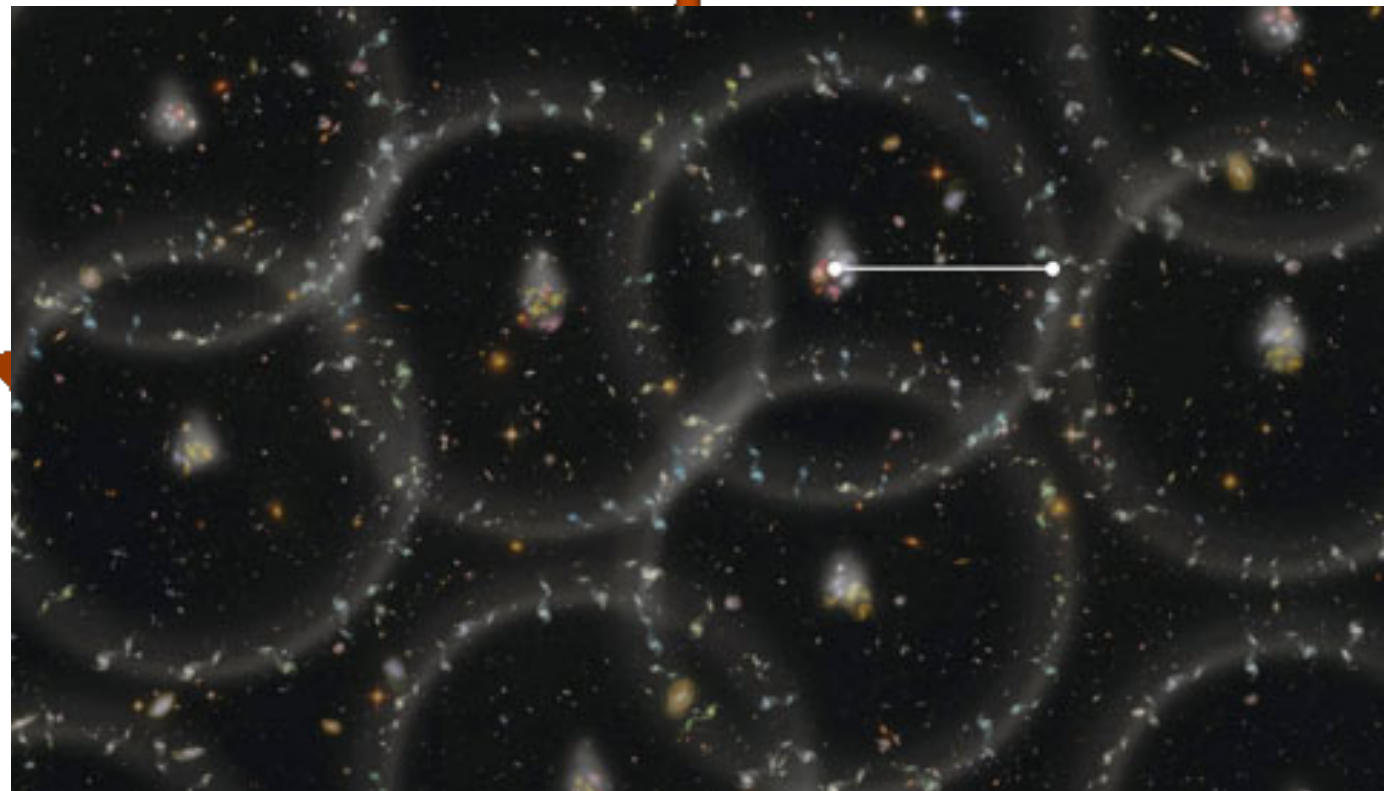


*credit: Bassett & Hlozek*



# The BAO: a standard ruler in the sky

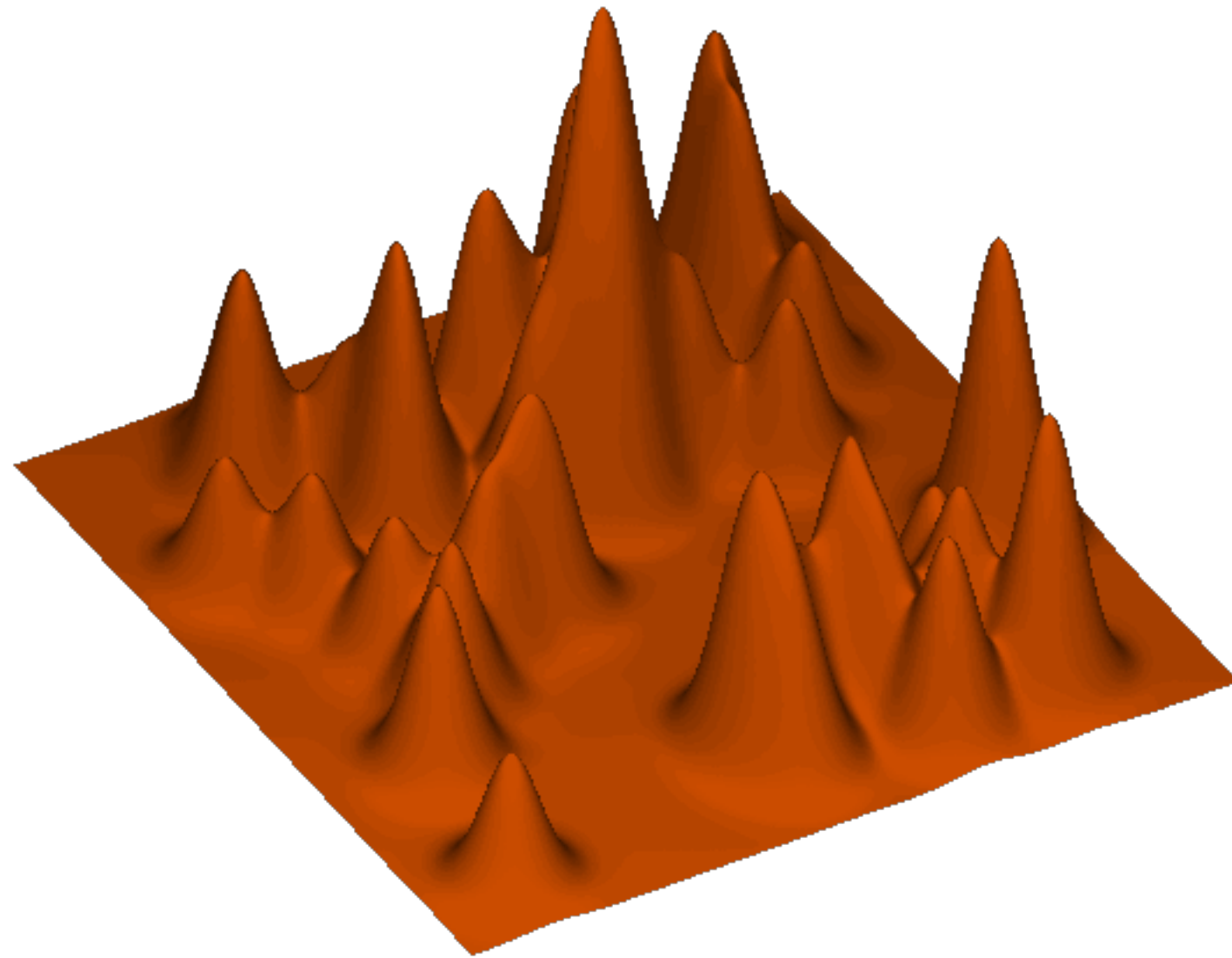
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*credit: Bassett & Hlozek*

# The BAO: a standard ruler in the sky

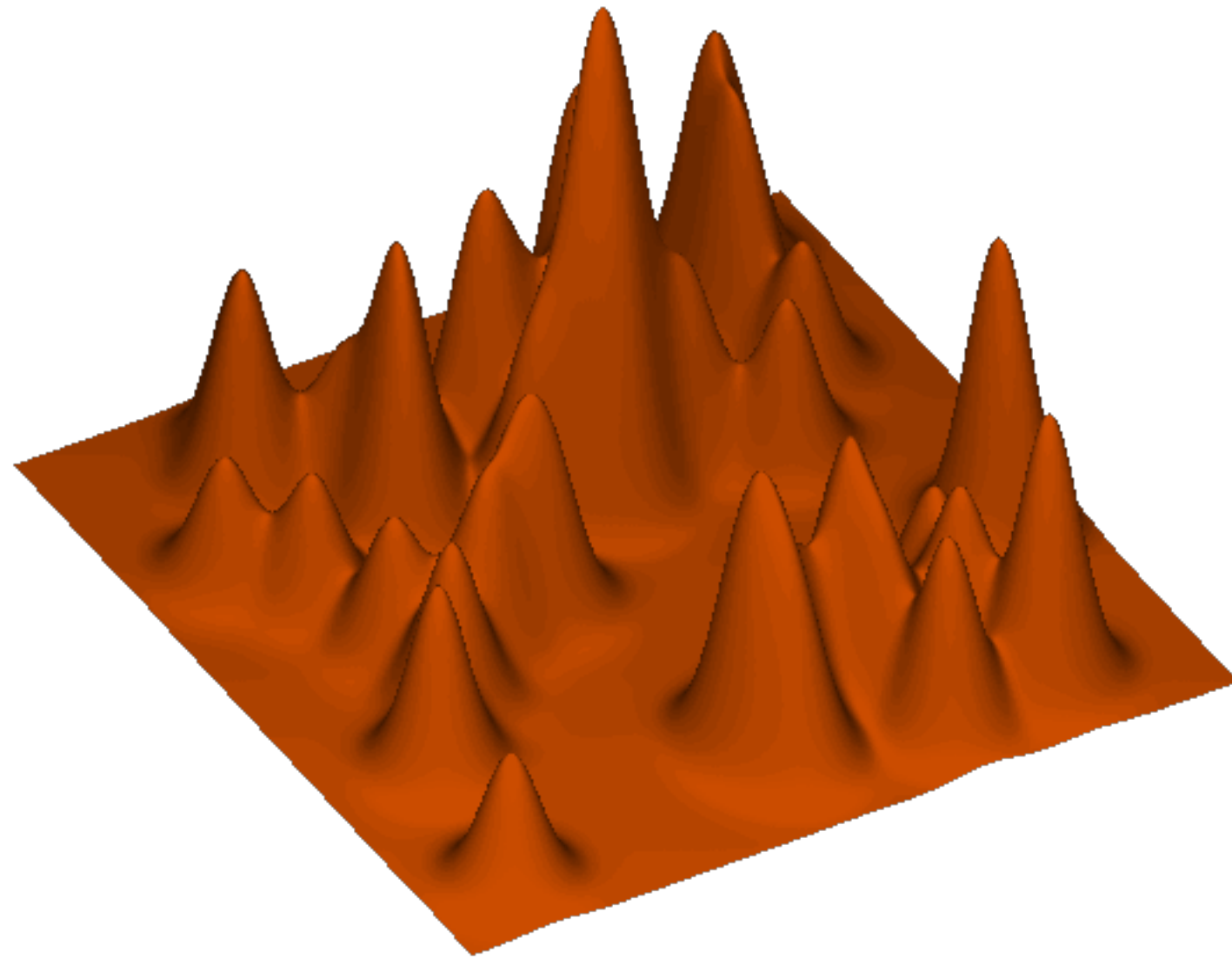
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*credit: Bassett & Hlozek*

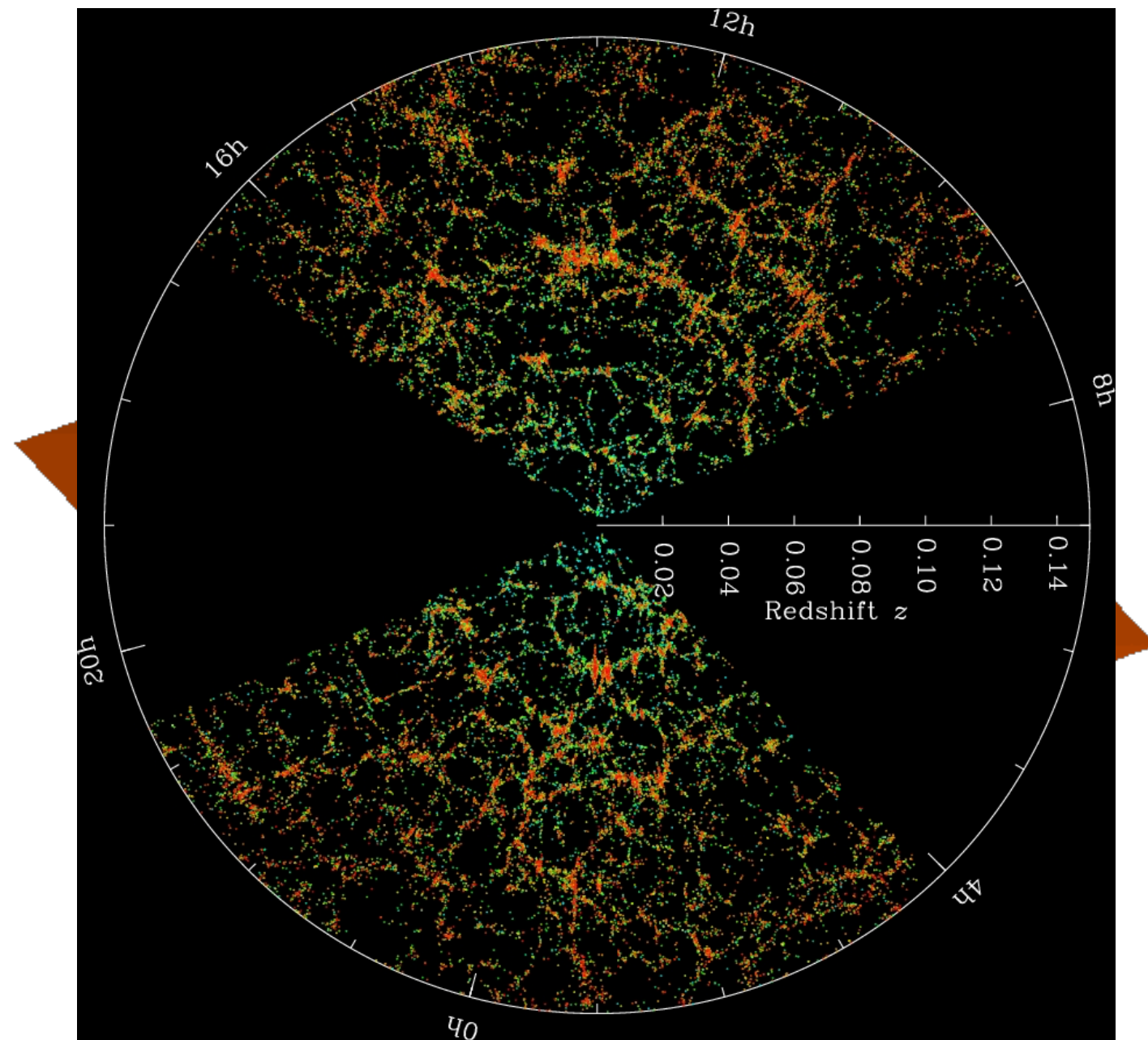
# The BAO: a standard ruler in the sky

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*credit: Bassett & Hlozek*

# The BAO: a standard ruler in the sky



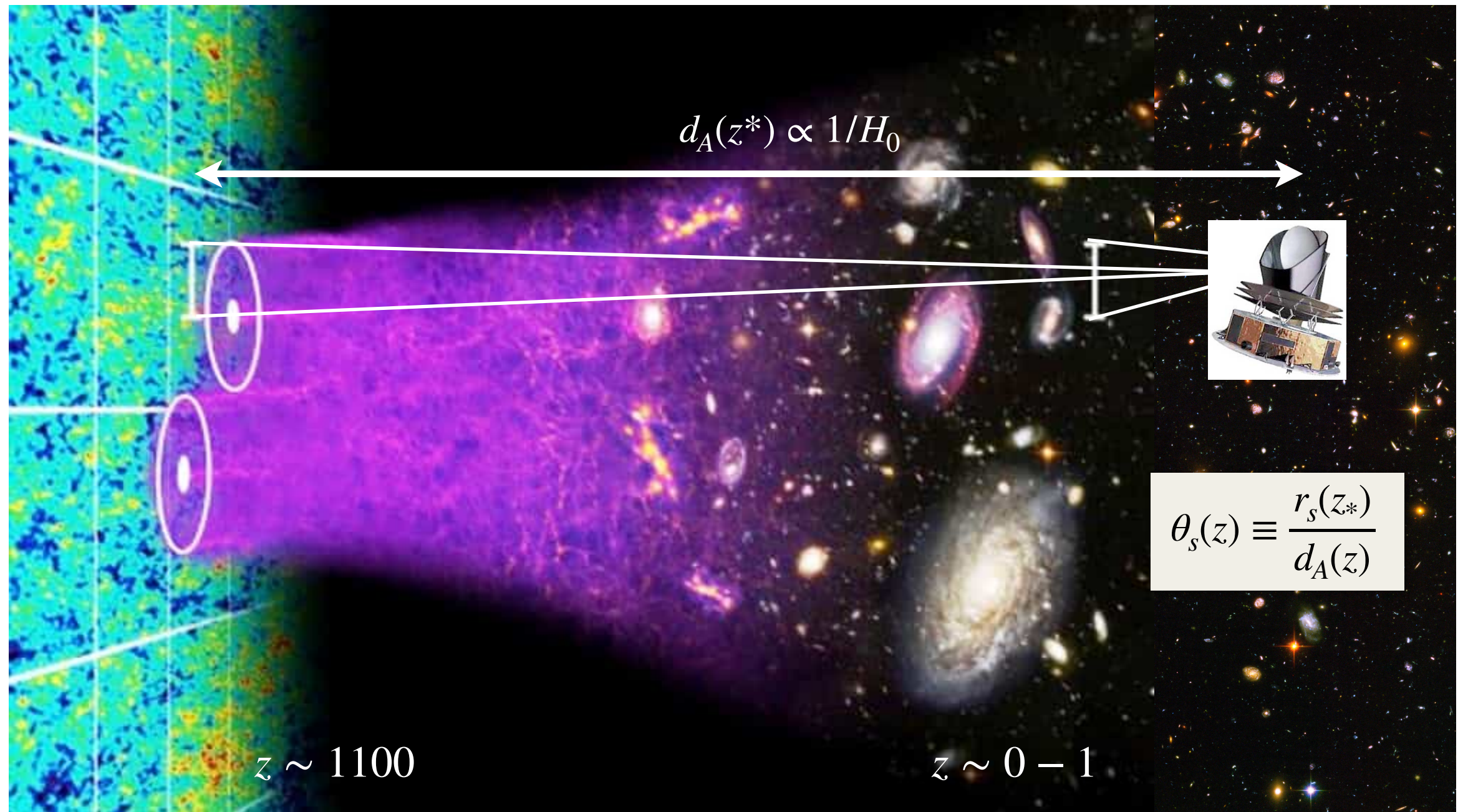
*credit: SDSS collaboration*

*credit: Bassett & Hlozek*



# The BAO: a standard ruler in the sky

- The Baryonic Acoustic Oscillation: a **standard ruler** in the sky

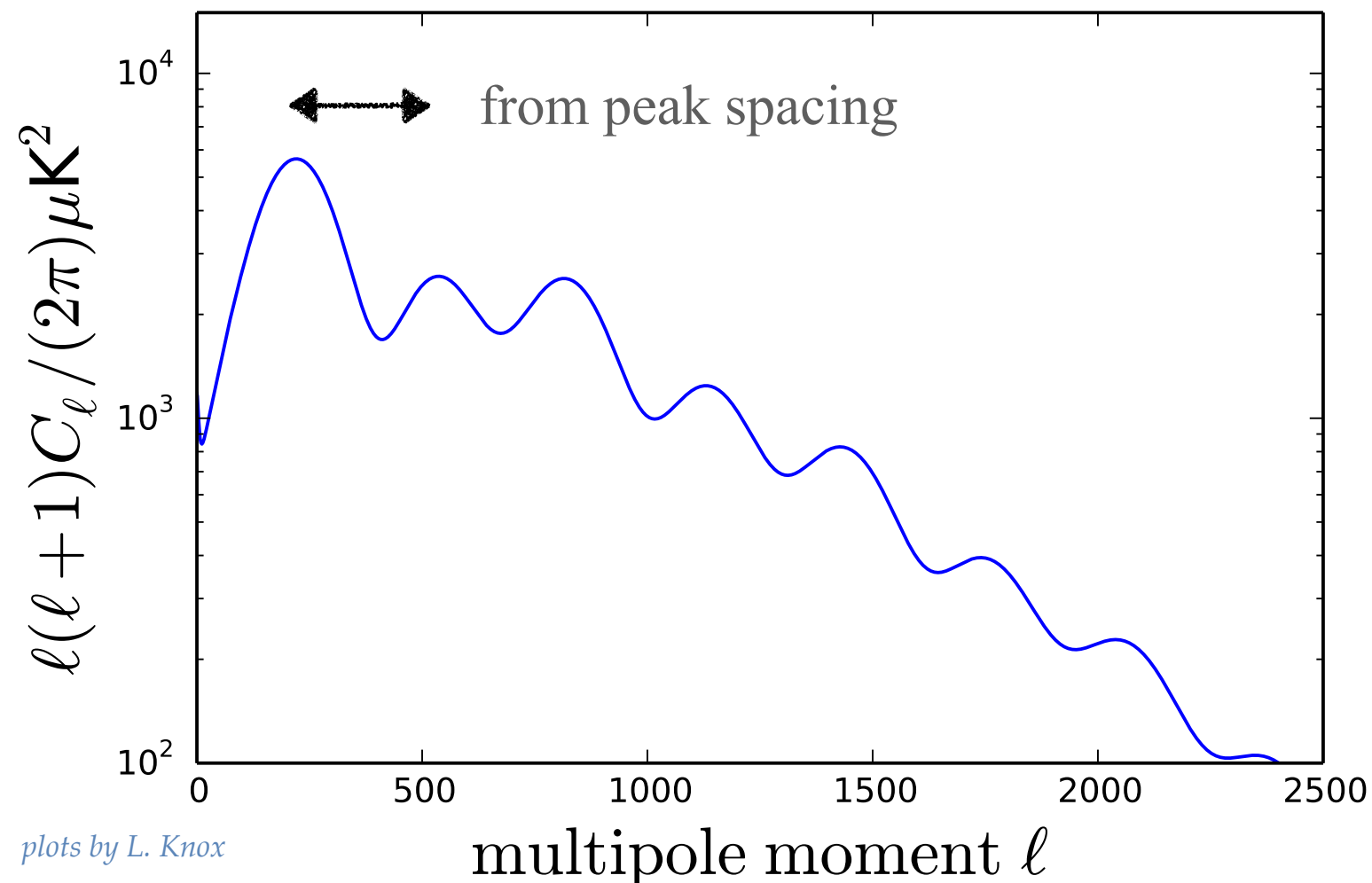


- *Planck* measures  $\theta_s$  at **0.04% precision** but  $r_s$  &  $d_A$  are model dependent.
- $H_0$  appears **only in the angular diameter distance**  $d_A$ . *Summary of other measurements: Verde++ 2311.13305*

# How does CMB data measure $H_0$ ?

- Inference of  $H_0$  comes from the measurement of **three angular scales**  $\theta_s, \theta_d, \theta_{eq}$ .

$\theta_s$  sound horizon at last scattering  $\sim 1.0404$

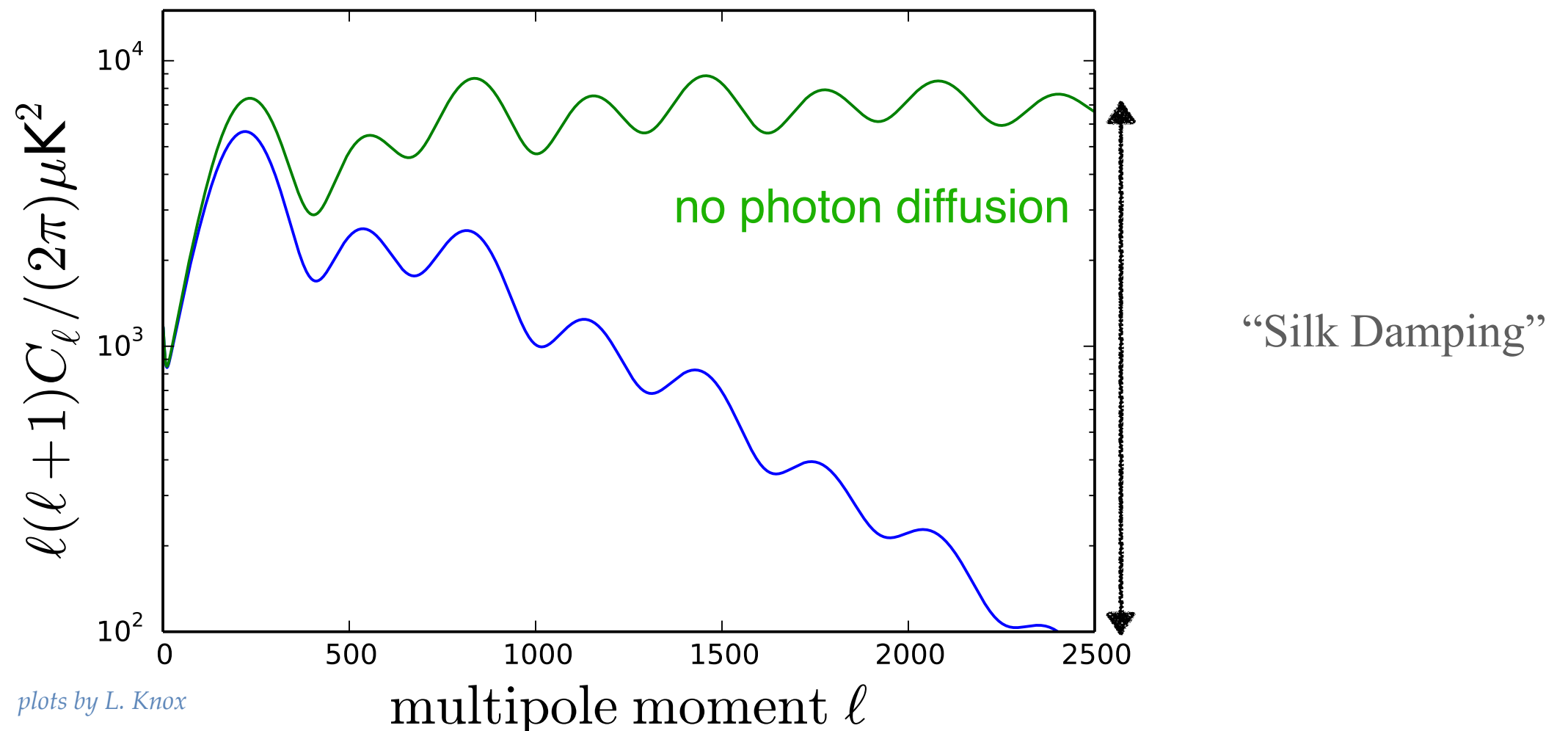


*e.g. Hu&White astro-ph/9609079, Hu++astro-ph/0006436*

# How does CMB data measure $H_0$ ?

- Inference of  $H_0$  comes from the measurement of **three angular scales**  $\theta_s, \theta_d, \theta_{eq}$ .

$\theta_d$  photon diffusion length at last scattering  $\sim 0.1609$



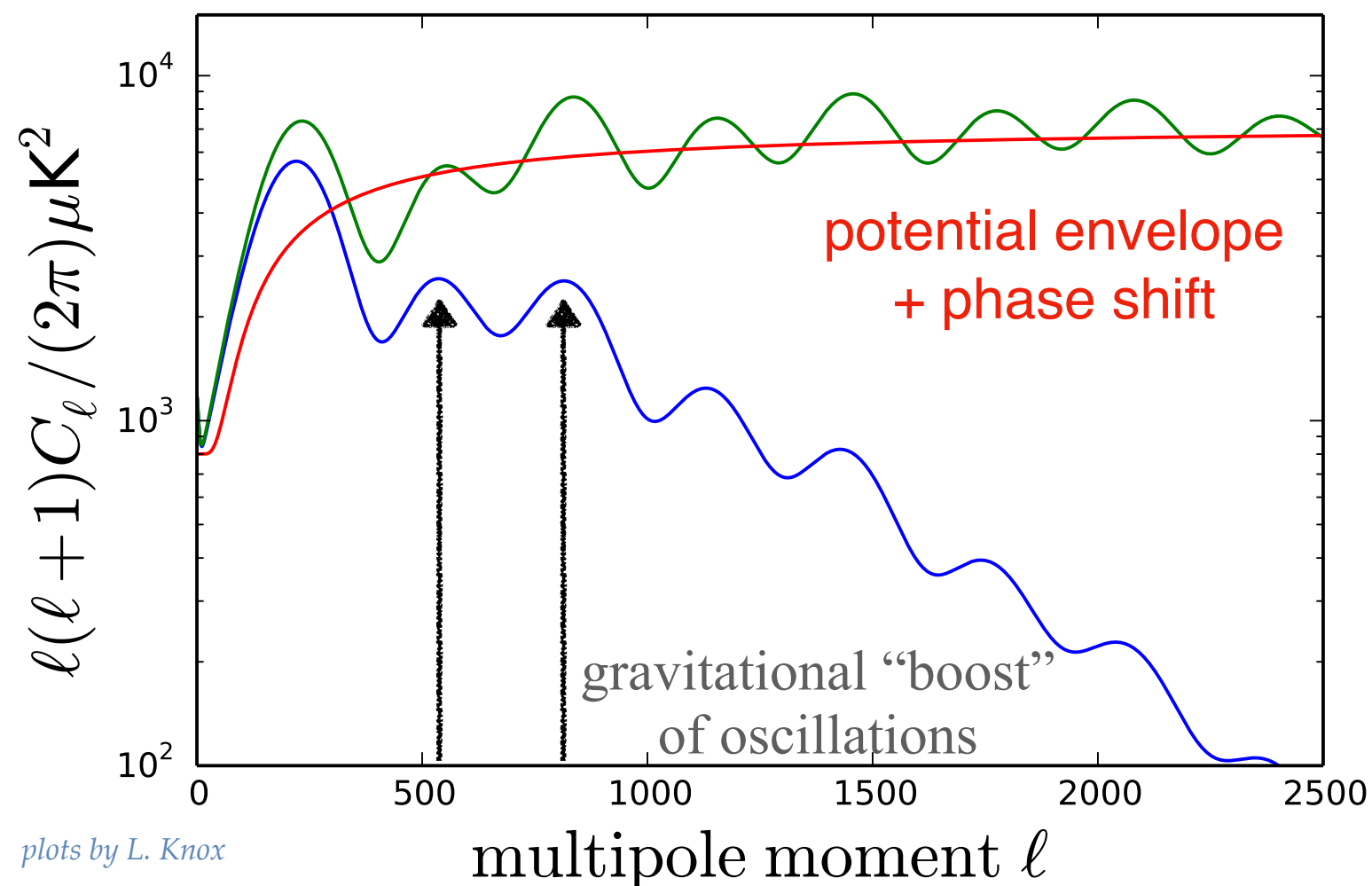
*e.g. Hu&White astro-ph/9609079, Hu++astro-ph/0006436*



# How does CMB data measure $H_0$ ?

- Inference of  $H_0$  comes from the measurement of **three angular scales**  $\theta_s, \theta_d, \theta_{\text{eq}}$ .

$\theta_{\text{eq}}$  horizon size at matter-radiation equality  $\sim 0.81$

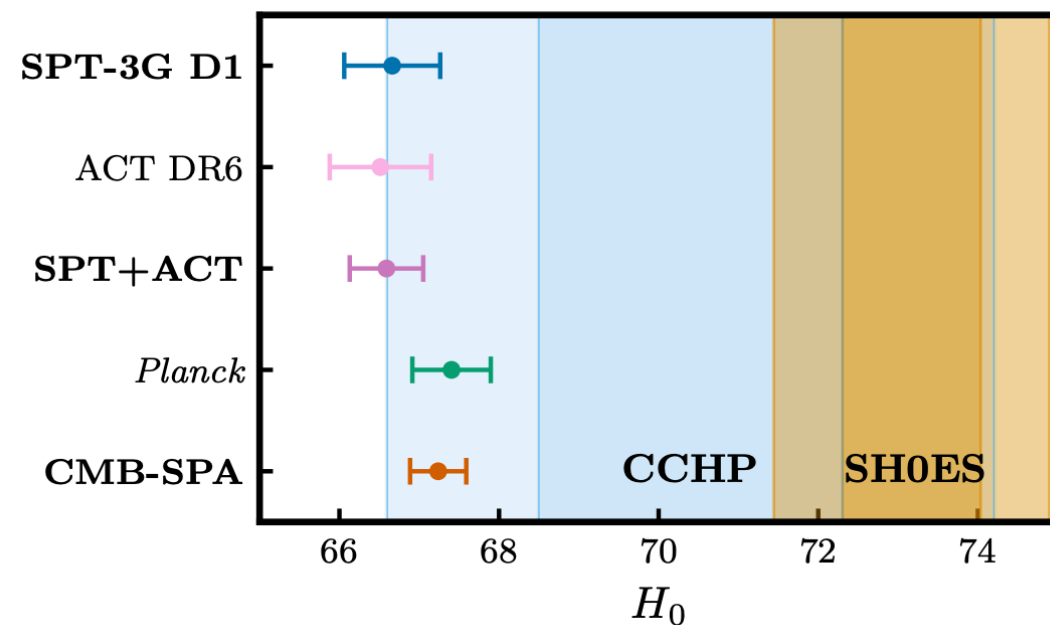


*e.g. Hu&White astro-ph/9609079, Hu++astro-ph/0006436*

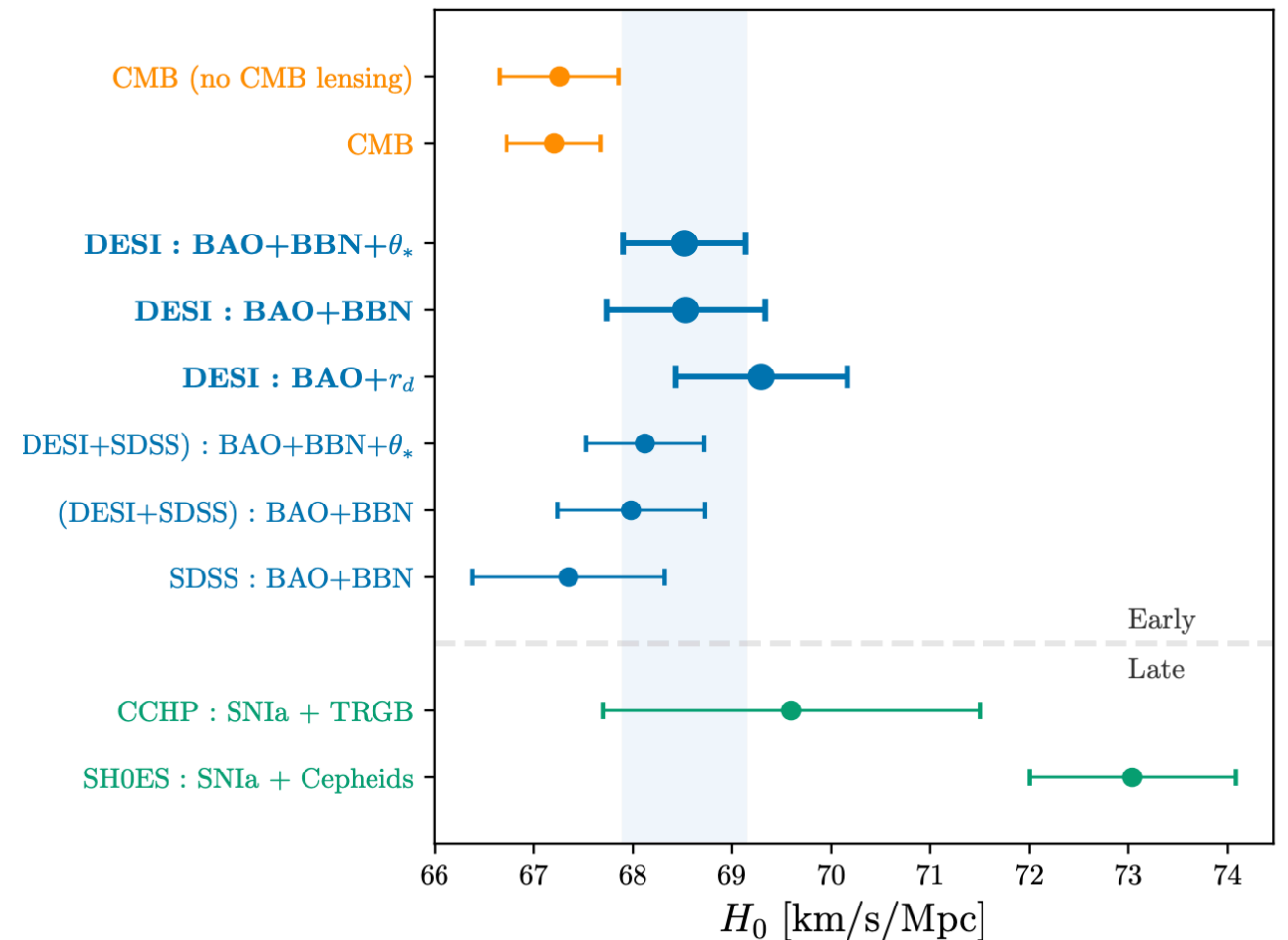


# CMB and BAO measurement of $H_0$

## Comparing CMB measurements



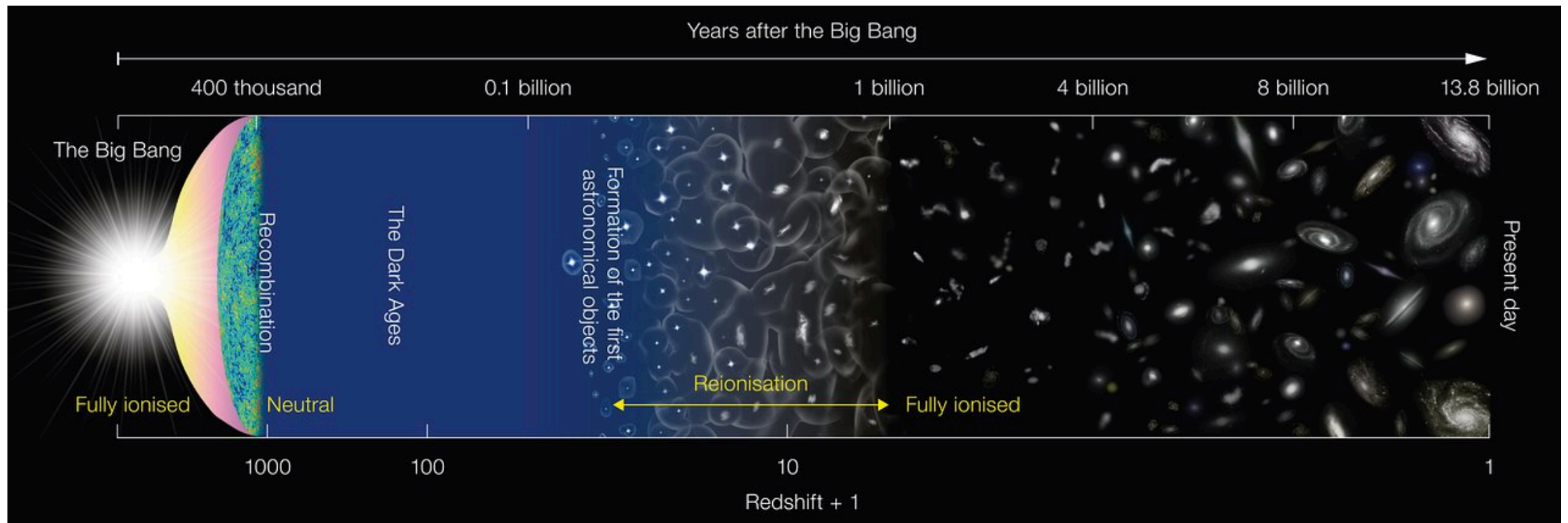
## Comparing BAO+BBN measurements



- The measurement of  $H_0$  in the  $\Lambda$ CDM model using the inverse-distance ladder is robust

# Two ways of solving the Hubble tension

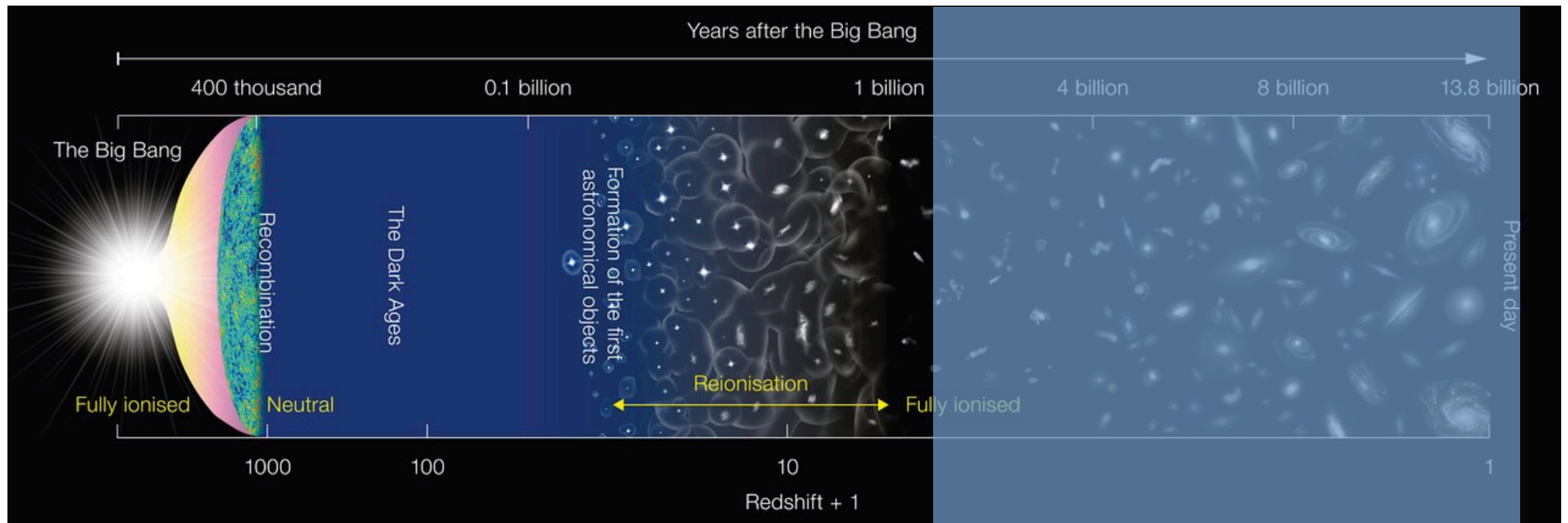
$$\theta_s = \frac{r_s}{r_A} = \frac{H_0 r_s}{\int_0^{z_*} 1/E(x) dx}$$



# Two ways of solving the Hubble tension

$$\theta_s = \frac{r_s}{r_A} = \frac{H_0 r_s}{\int_0^{z_*} 1/E(x) dx}$$

**Late-universe models**



$$\frac{H_0 \nearrow r_s}{\int_0^{z_*} 1/\textcolor{red}{E}(\textcolor{red}{x}) \searrow dx}$$

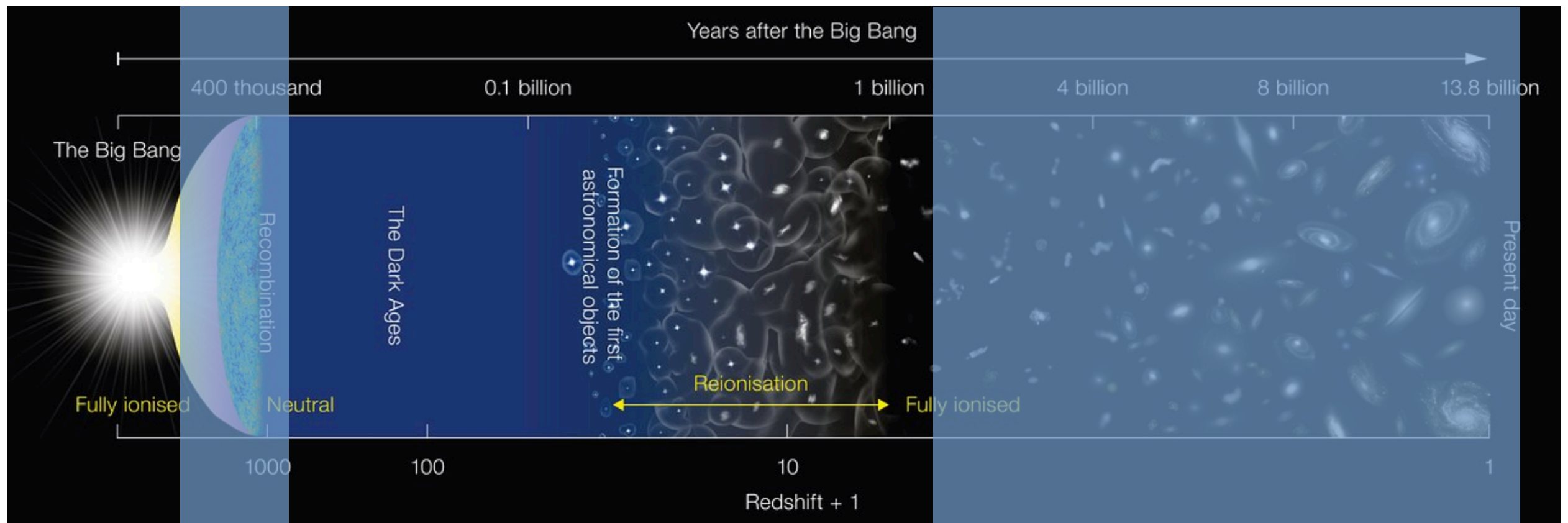
Change  
expansion  
history

# Two ways of solving the Hubble tension

**Early universe models**

$$\theta_s = \frac{r_s}{r_A} = \frac{H_0 r_s}{\int_0^{z_*} 1/E(x) dx}$$

**Late-universe models**



$$\frac{H_0 \nearrow r_s \searrow}{\int_0^z 1/E(x) dx}$$

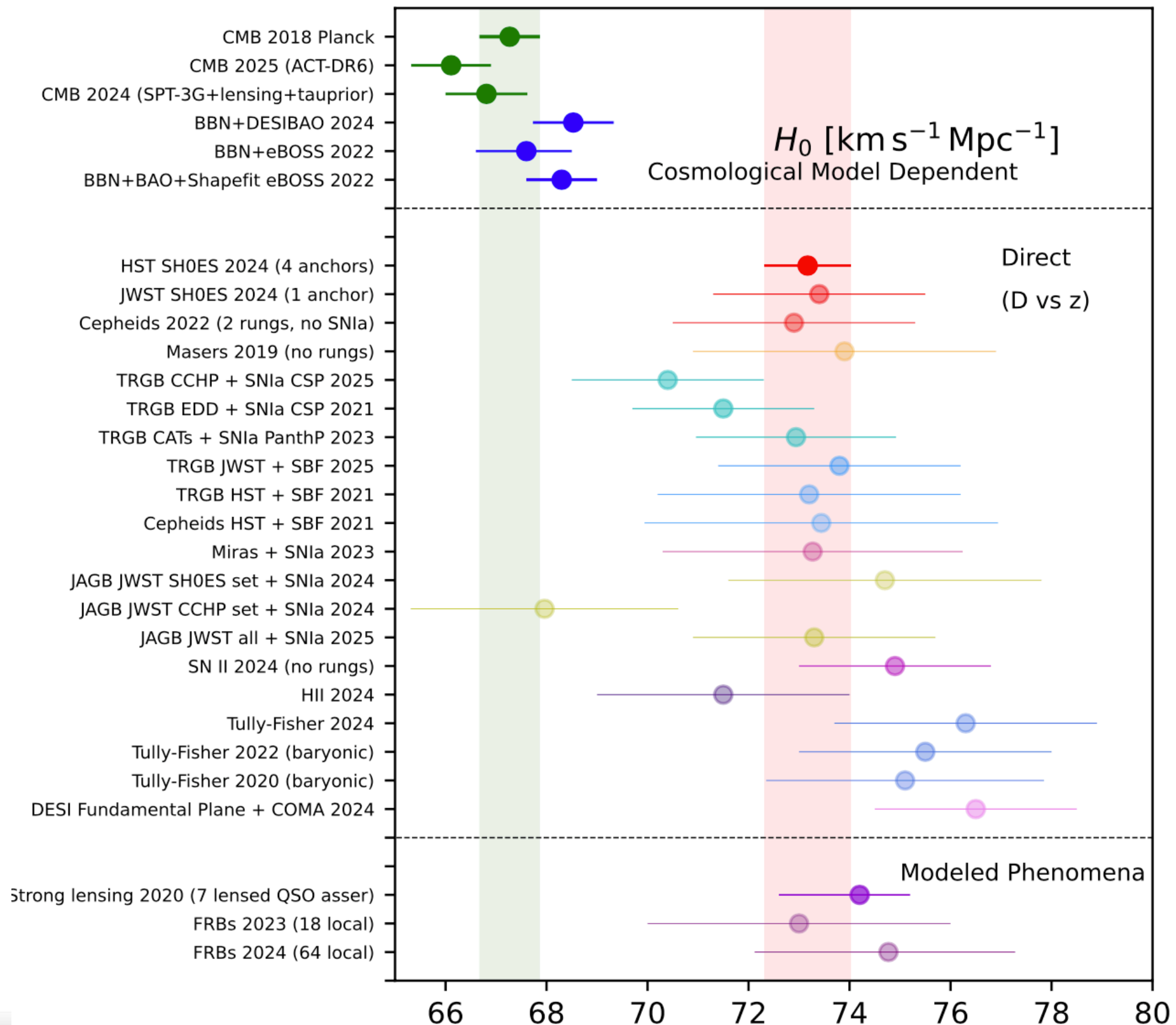
Change calibrator

$$\frac{H_0 \nearrow r_s}{\int_0^{z_*} 1/\textcolor{red}{E}(\textcolor{red}{x}) \searrow dx}$$

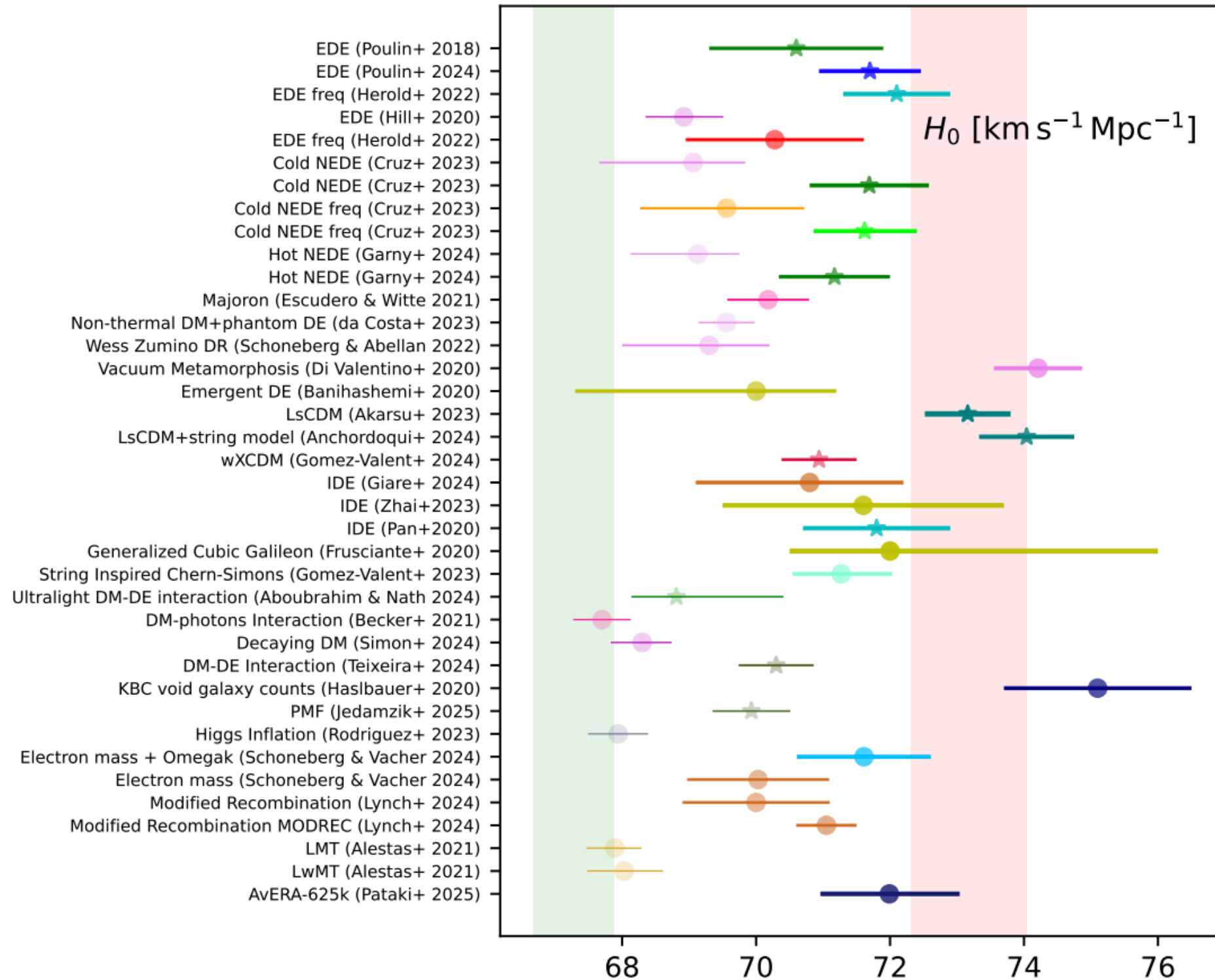
Change  
expansion  
history



# The Hubble tension



- ★ Planck+BAO+SNla+SH0ES
- ★ Planck+BAO+BBN+SNla+SH0ES
- ★ Planck+DESI+SNla PP+SH0ES
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- ★ Planck+BAOtr+DESY5 SN+CC+f $\sigma_{12}$ +SH0ES
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- ★ Planck+DESI+SNla+SH0ES
- ★ Planck+B2K+BAO+SNla
- ★ Planck+DESI+SNla
- ★ Planck+BAO+RSD+SNla
- ★ Planck+BAO+CC+SNla+SH0ES
- ★ SNla



# The $H_0$ Olympics: A fair ranking of proposed models

Nils Schöneberg<sup>a,\*</sup>, Guillermo Franco Abellán<sup>b</sup>, Andrea Pérez Sánchez<sup>a</sup>, Samuel J. Witte<sup>c</sup>, Vivian Poulin<sup>b</sup>, Julien Lesgourgues<sup>a</sup>

<sup>a</sup>*Institute for Theoretical Particle Physics and Cosmology (TTK), RWTH Aachen University, D-52056 Aachen, Germany.*

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## Abstract

Despite the remarkable success of the  $\Lambda$  Cold Dark Matter ( $\Lambda$ CDM) cosmological model, a growing discrepancy has emerged (currently measured at the level of  $\sim 4 - 6\sigma$ ) between the value of the Hubble constant  $H_0$  measured using the local distance ladder and the value inferred using the cosmic microwave background and galaxy surveys. While a vast array of  $\Lambda$ CDM extensions have been proposed to explain these discordant observations, understanding the (relative) success of these models in resolving the tension has proven difficult – this is a direct consequence of the fact that each model has been subjected to differing, and typically incomplete, compilations of cosmological data. In this review, we attempt to make a systematic comparison of seventeen different models which have been proposed to resolve the  $H_0$  tension (spanning both early- and late-Universe solutions), and quantify the relative success of each using a series of metrics and a vast array of data combinations. Owing to the timely appearance of this article, we refer to this contest as the “ $H_0$  Olympics”; the goal being to identify which of the proposed solutions, and more broadly which underlying mechanisms, are most likely to be responsible for explaining the observed discrepancy (should unaccounted for systematics not be the culprit). This work also establishes a foundation of tests which will allow the success of novel proposals to be meaningfully “benchmarked”.

**Keywords:** Hubble Tension, Dark Energy, Dark Matter Phenomenology, Dark Radiation, Early Dark Energy, Varying fundamental constants

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# The $H_0$ olympics: fairly ranking models

- We compare 17 different models suggested to resolve the Hubble tension.

Schöneberg (VP) ++ 2107.10291

$$\frac{H_0 \nearrow r_s}{\int_0^{z_*} 1/E(x) \searrow dx}$$

Late-Universe models

- CPL Dark Energy
- Emergent Dark Energy
- Generalized Emergent Dark Energy
- Decaying Dark matter to massless particles
- Decaying Dark matter to massive particles

$$\frac{H_0 \nearrow r_s \searrow}{\int_0^z 1/E(x) dx}$$

Dark Radiation models

- Free-streaming  $N_{\text{eff}}$
- Self-Interacting  $N_{\text{DR}}$
- Mixture of  $N_{\text{eff}} + N_{\text{DR}}$
- DM-DR interaction +  $N_{\text{DR}}$
- Self interacting  $\nu + N_{\text{eff}}$

Exotic Early Universe models

- Early Dark Energy
- New Early Dark Energy
- Early modified Gravity
- Primordial magnetic fields
- Varying electron mass  $m_e$
- Varying electron mass  $m_e + \Omega_k$



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- I/ Frequentist: Can a model give a good fit to all data including SH0ES and be favored over  $\Lambda$ CDM.
- II/ Bayesian: Can a model be favored over  $\Lambda$ CDM independently of SH0ES and “predict” a high  $H_0$ .

# A late-time solution to the Hubble tension?

Measured  $\theta_s \equiv \frac{r_s(z_*)}{d_A(z_*)}$  Assumed from  $\Lambda$ CDM

$$d_A(z) \equiv \int_0^z \frac{dz'}{H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda(1+z)^{3(1+w)} + \dots}}$$

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$H_0 \uparrow \Rightarrow \Omega_X(z) \downarrow$

- ‘phantom dark energy’  $w < -1$ , DE-DM interactions, decaying DM, and many more...

[\[http://arxiv.insert\\_your\\_favorite\\_model\\_here.com\]](http://arxiv.insert_your_favorite_model_here.com)

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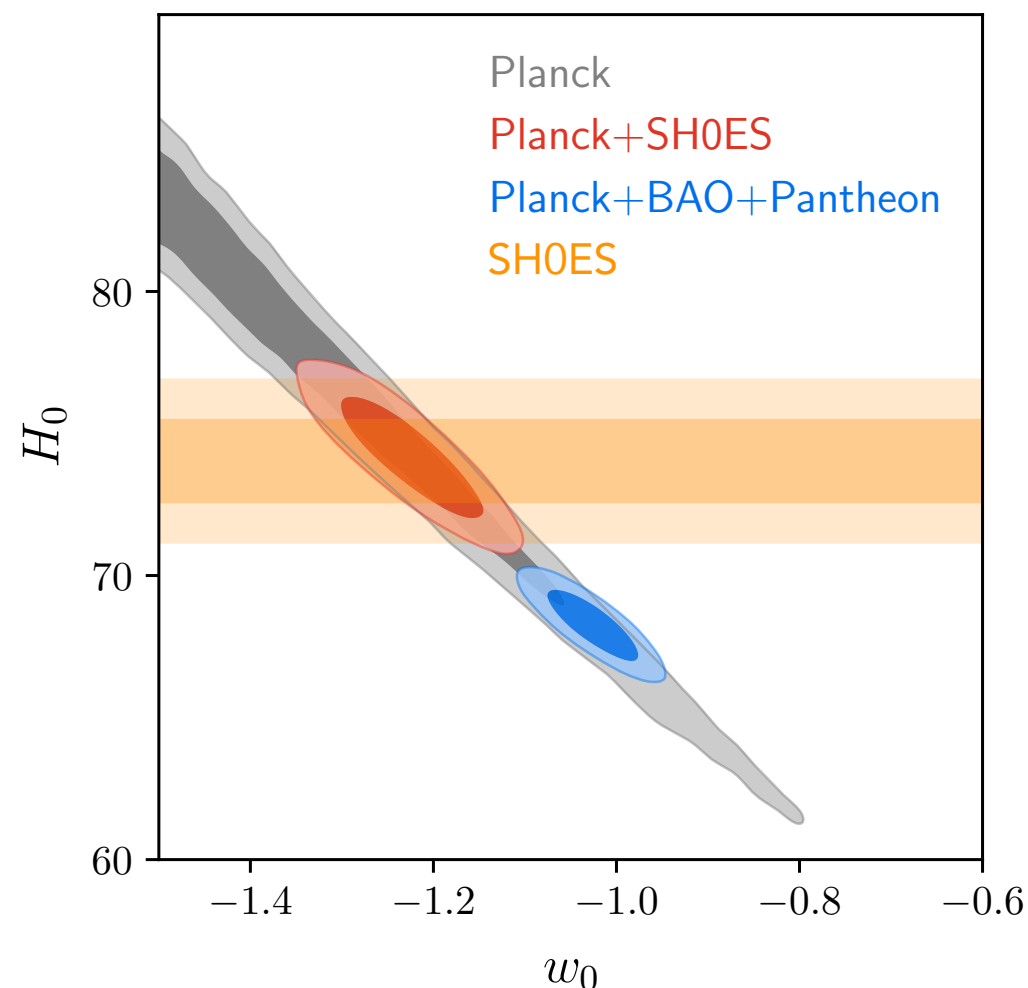
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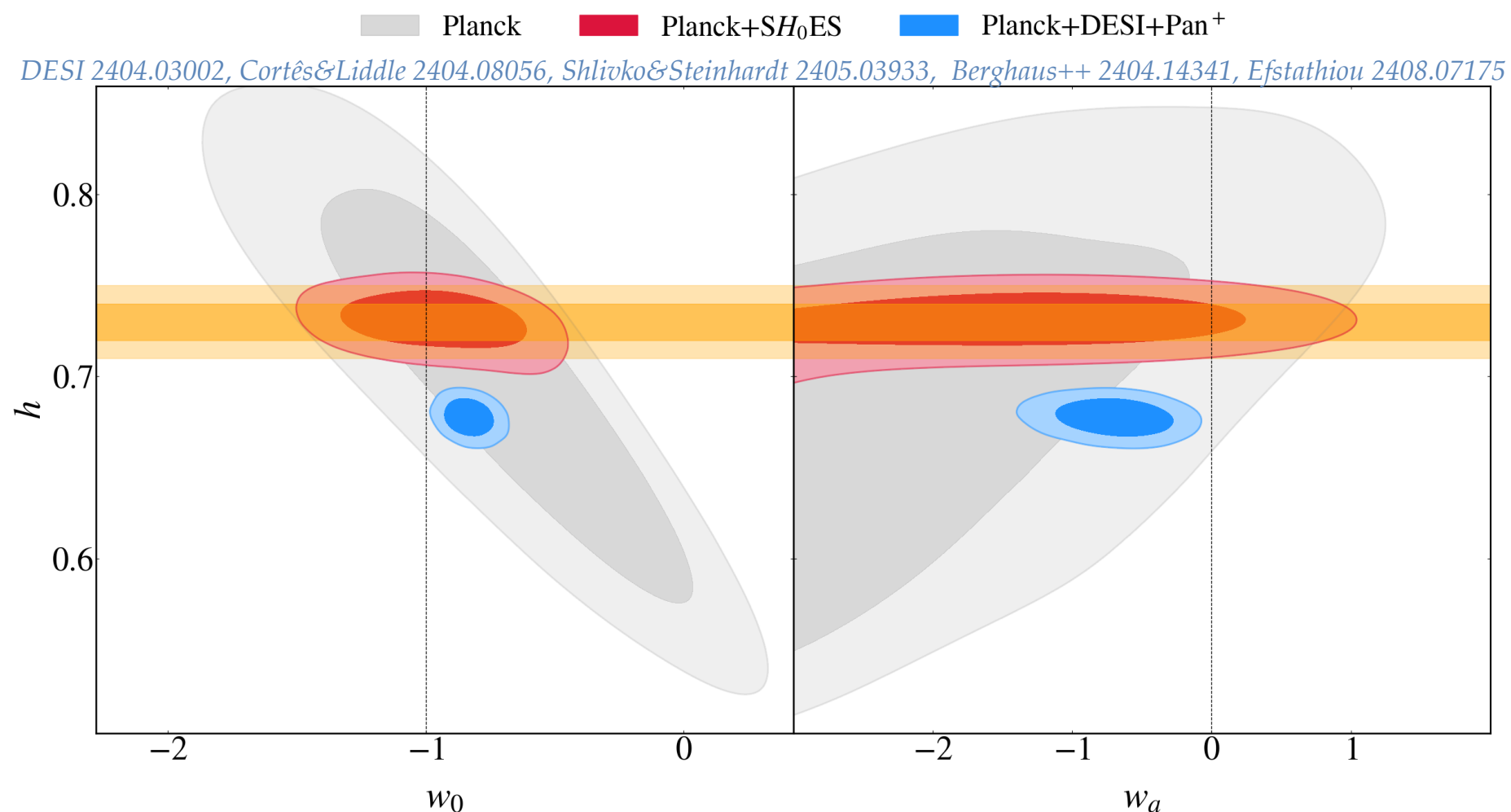
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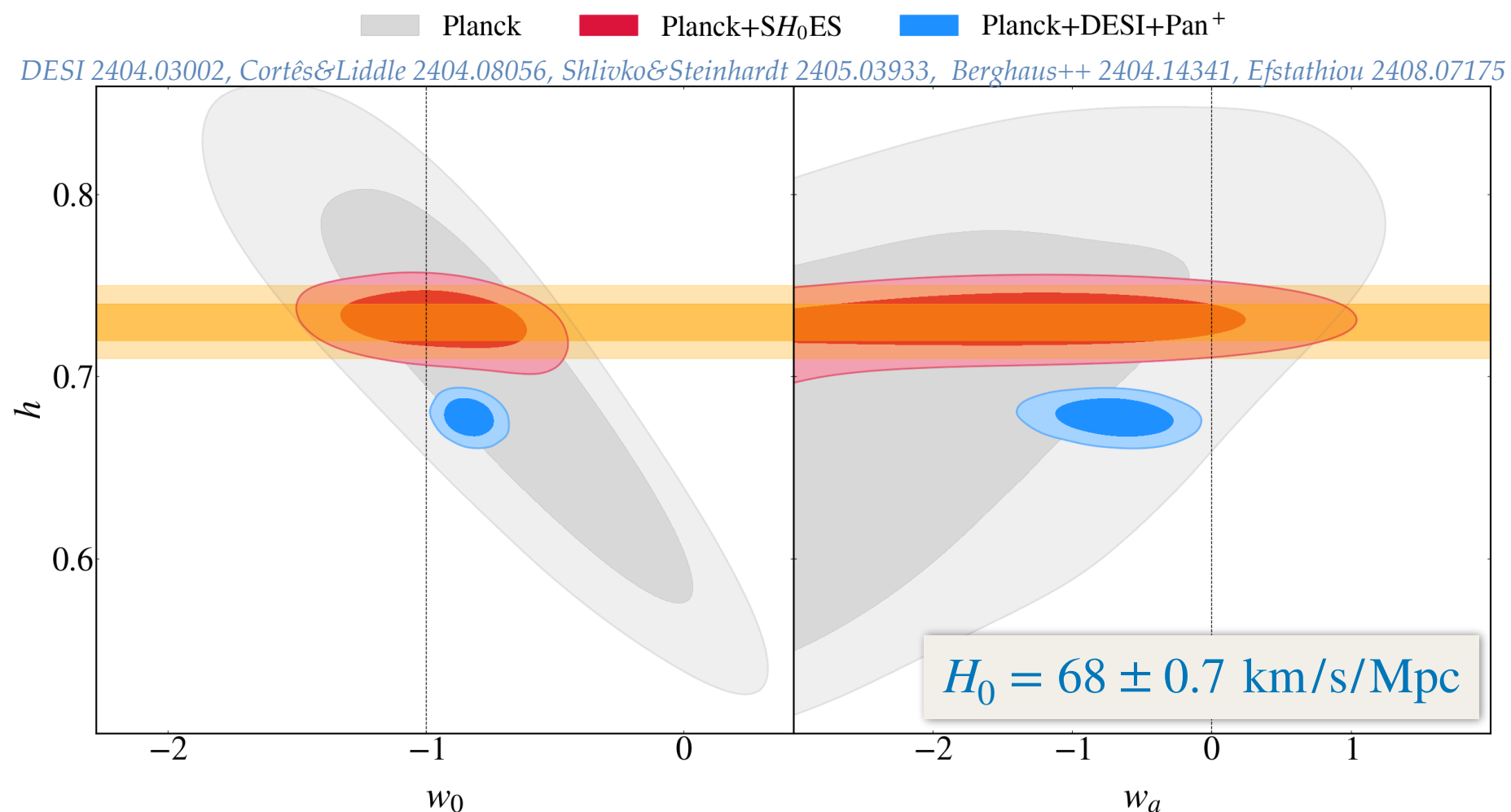
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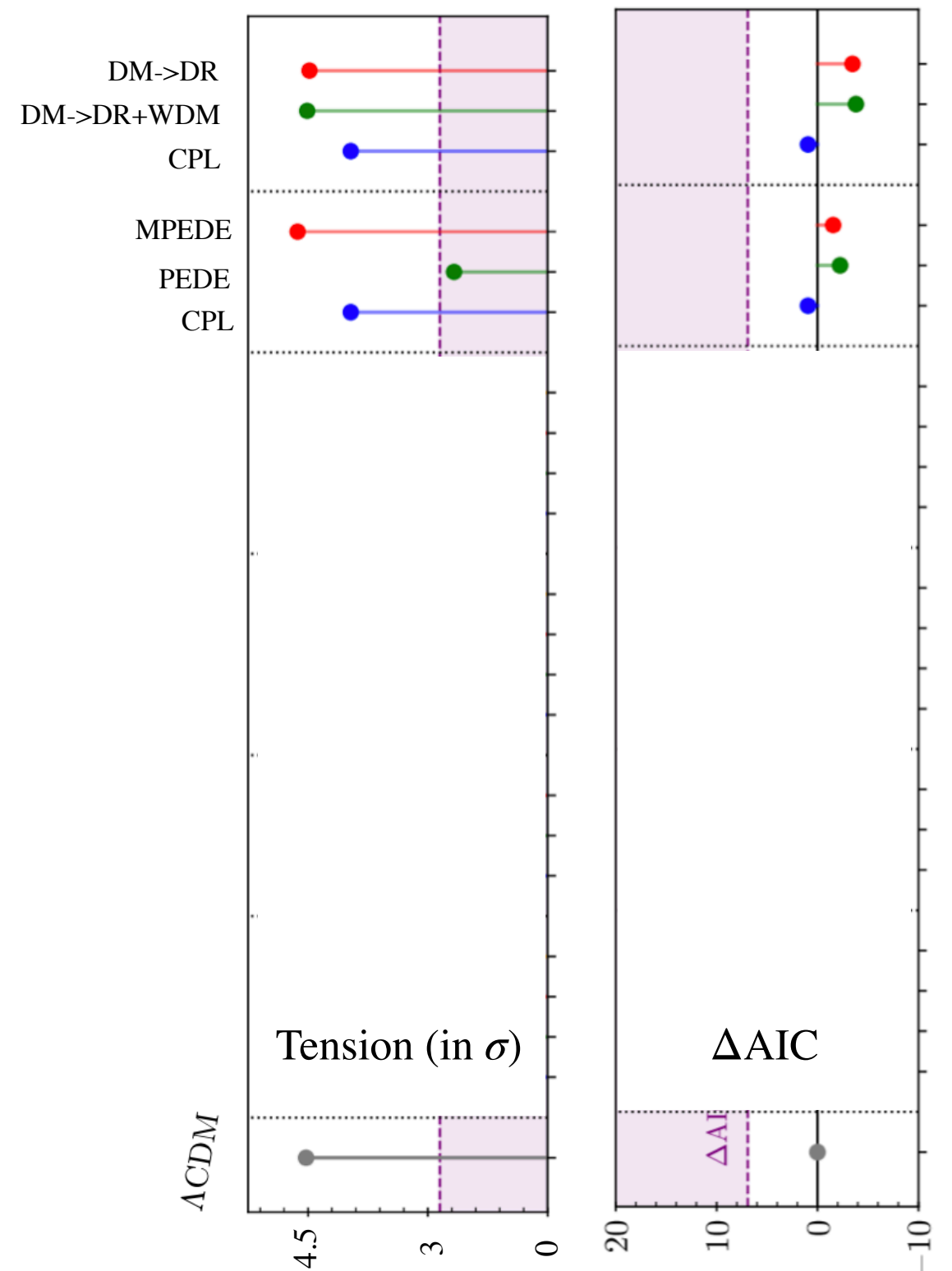
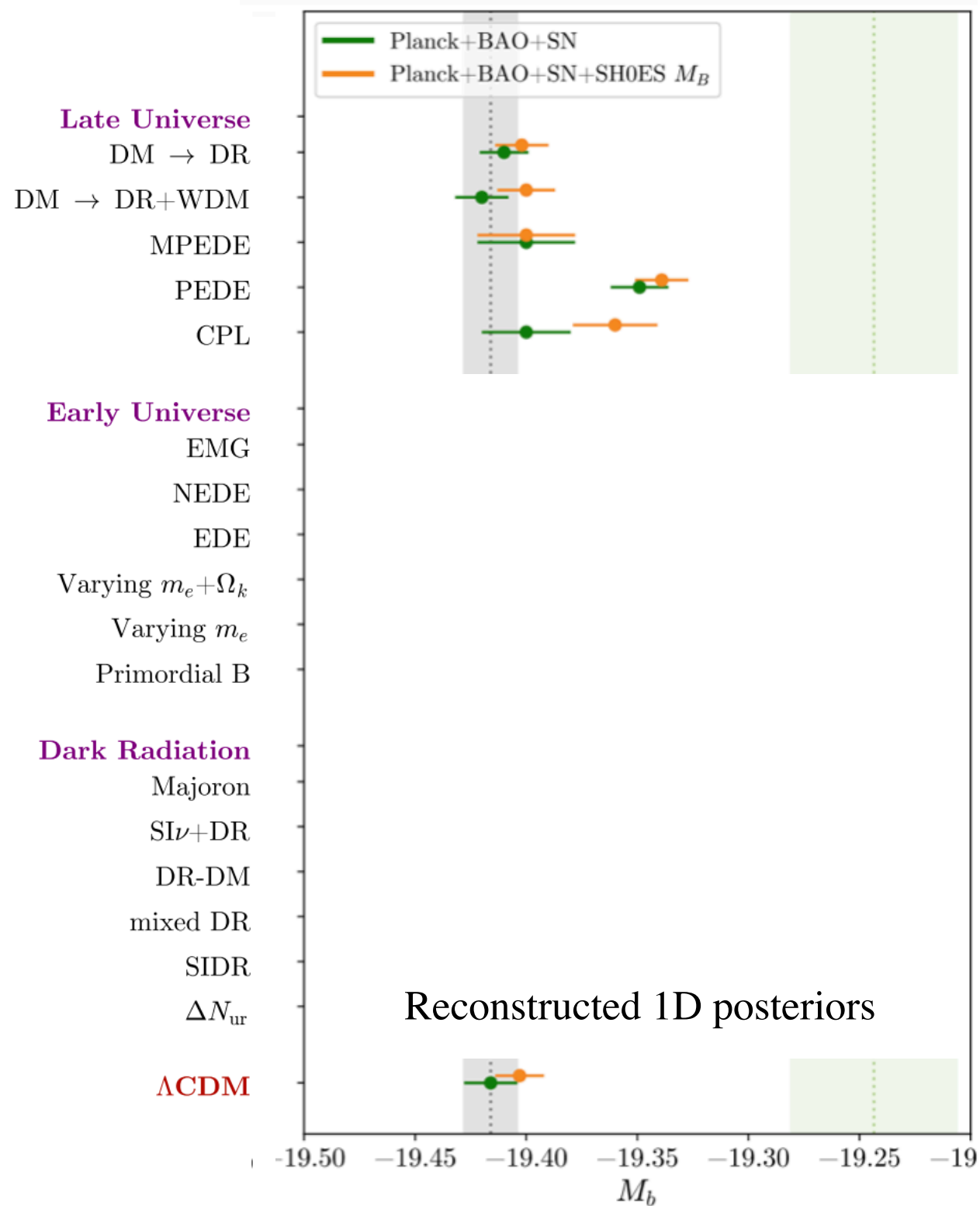
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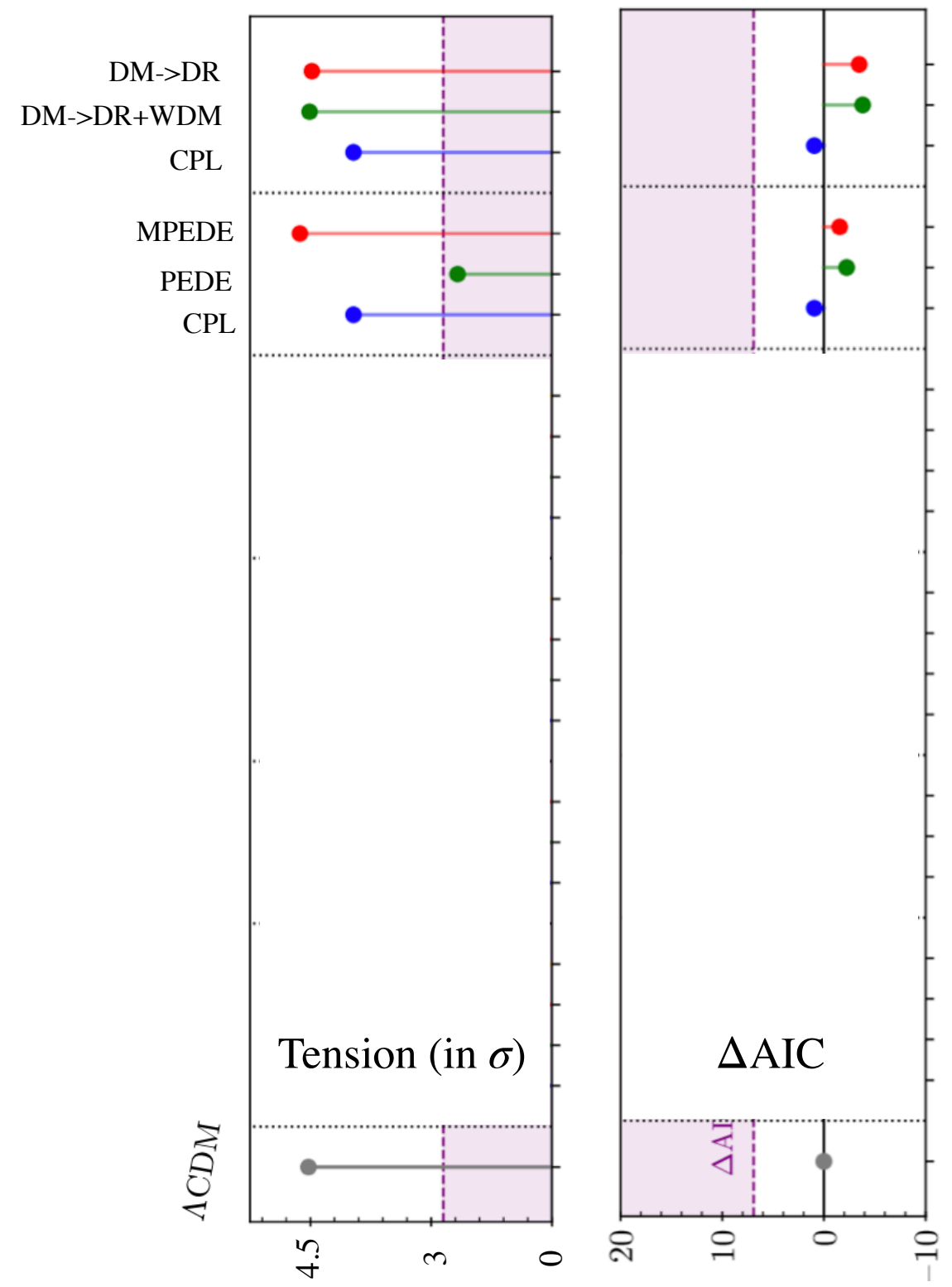
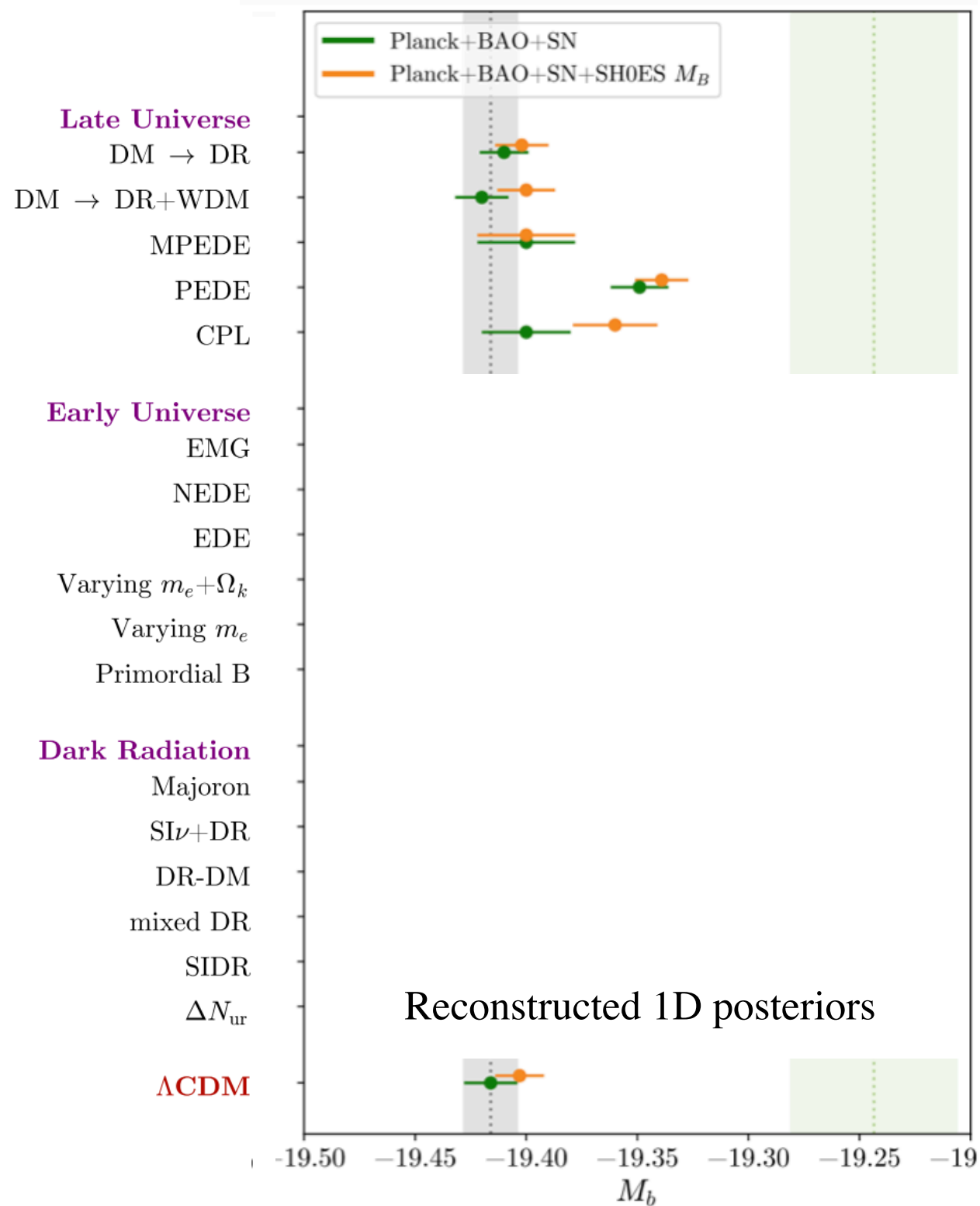
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Late-universe models are excluded as a resolution to the tension (alone)



# A ‘no-go’ theorem for late-time solutions

---

$$\text{BAO: } \theta_d(z) = \frac{r_s(z_{\text{drag}})}{D_A(z)}$$

$$\text{SN1a: } m(z) = 5 \log_{10}(D_L(z)) + M_b$$

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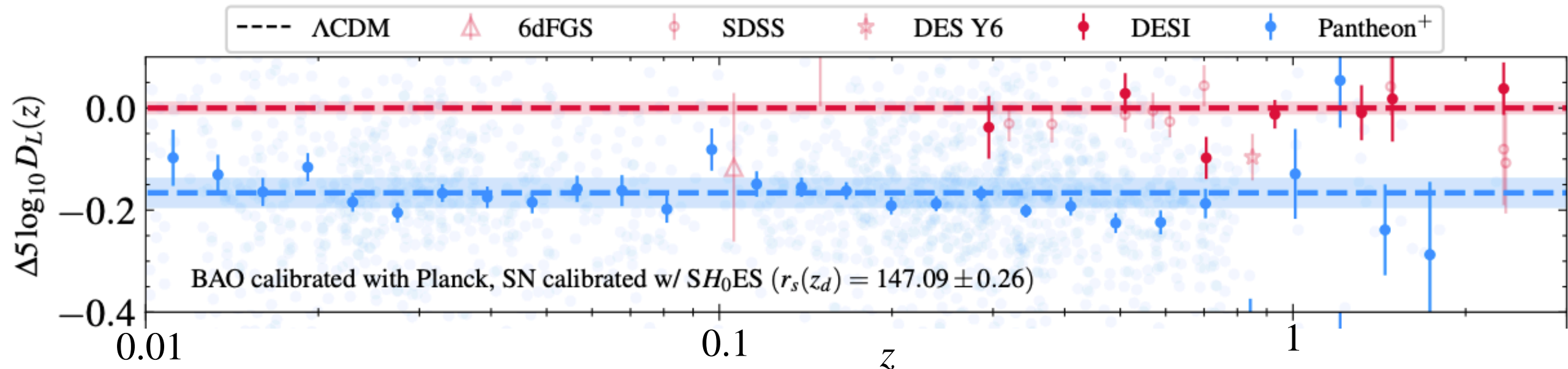
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VP, Smith, Calderon, Simon 2407.18292



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Camarena&Marra 2101.08641, Efstathiou 2103.08723, Raveri 2309.06795

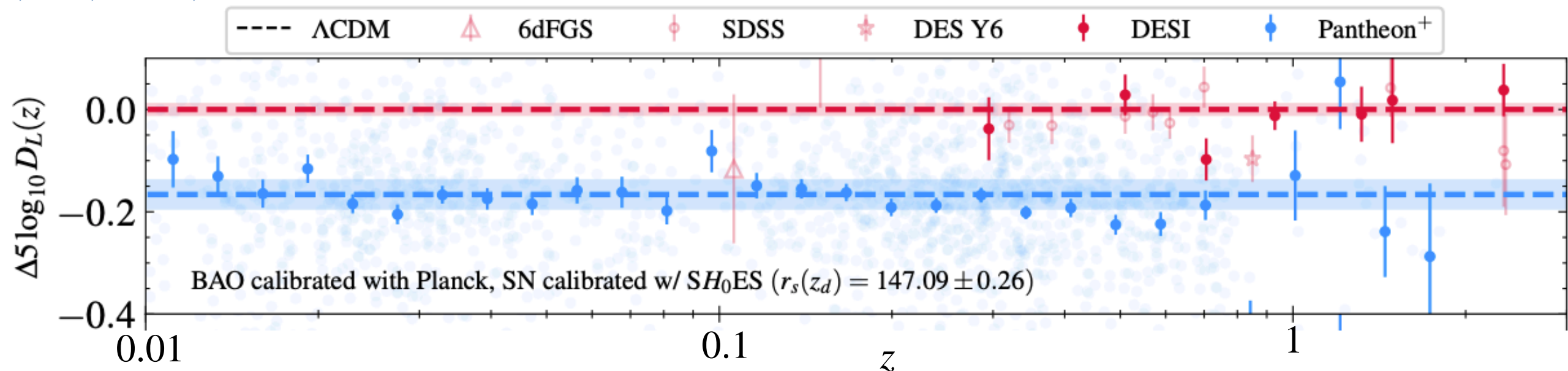
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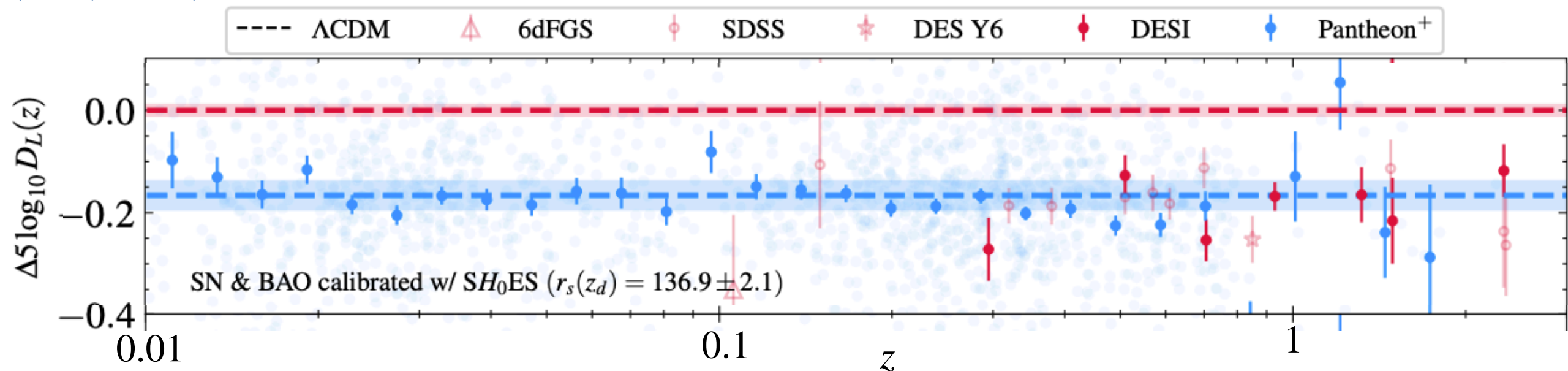
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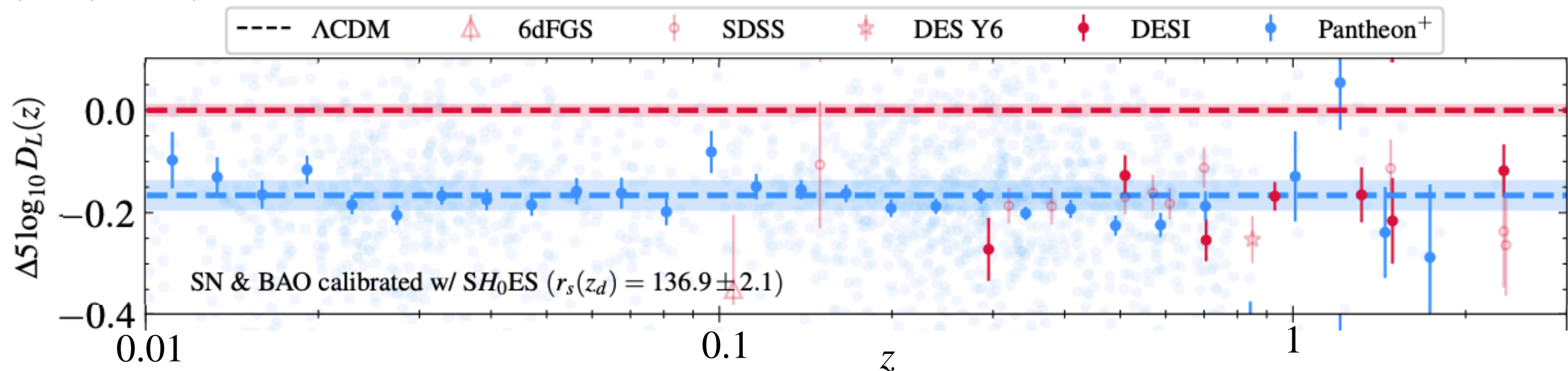
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- A single “constant” shift is currently sufficient  $\Rightarrow$  **changing calibrators favored!** *Teixeira (VP) ++ 2504.10464*

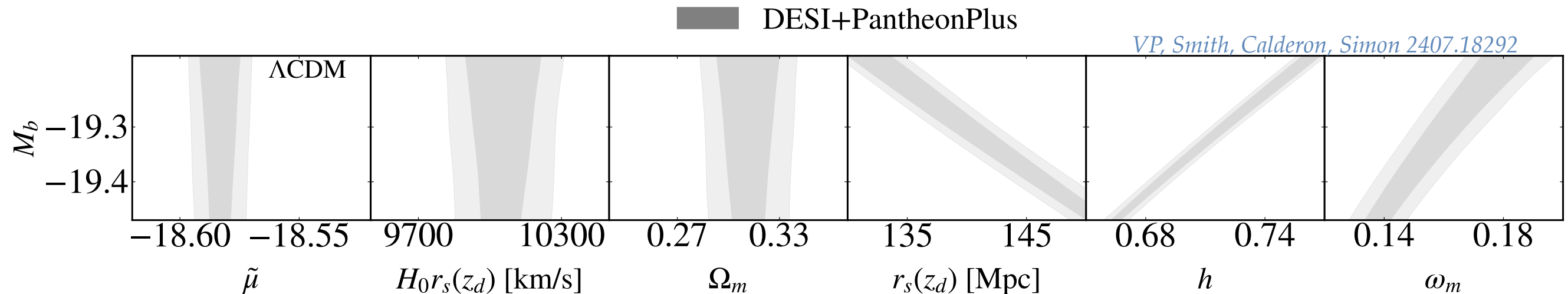
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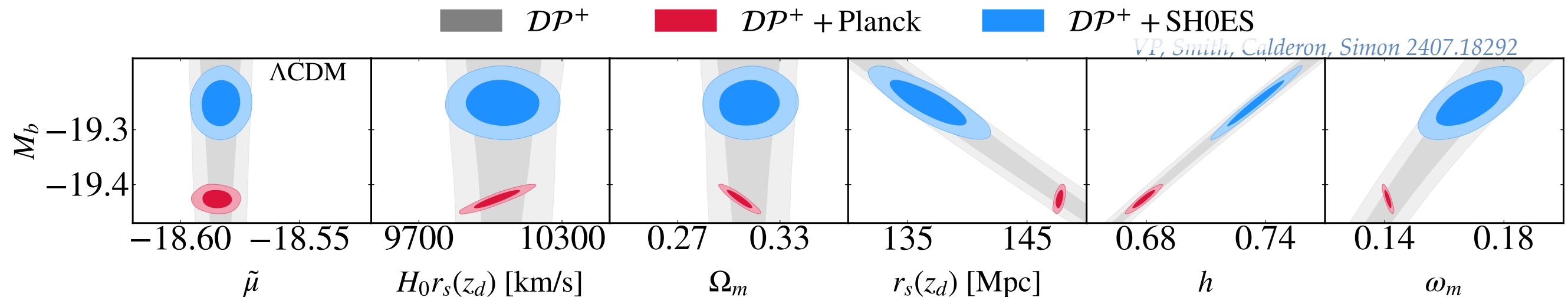


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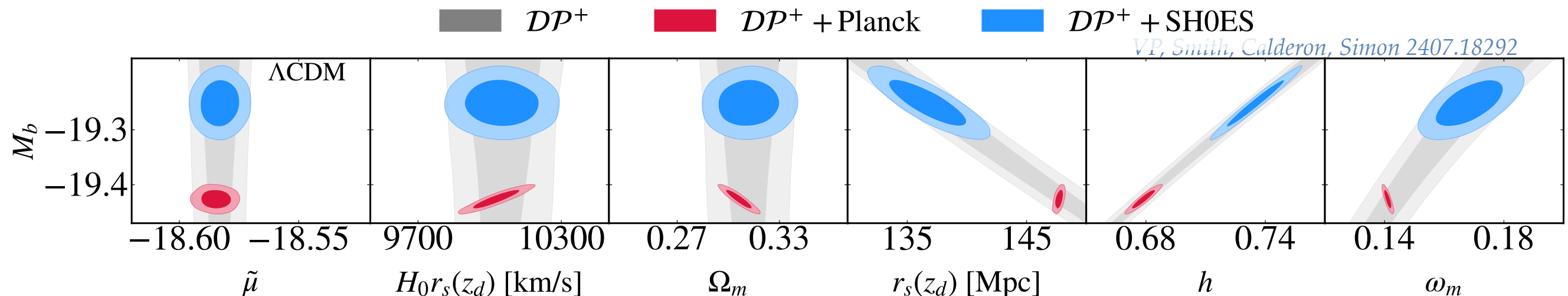
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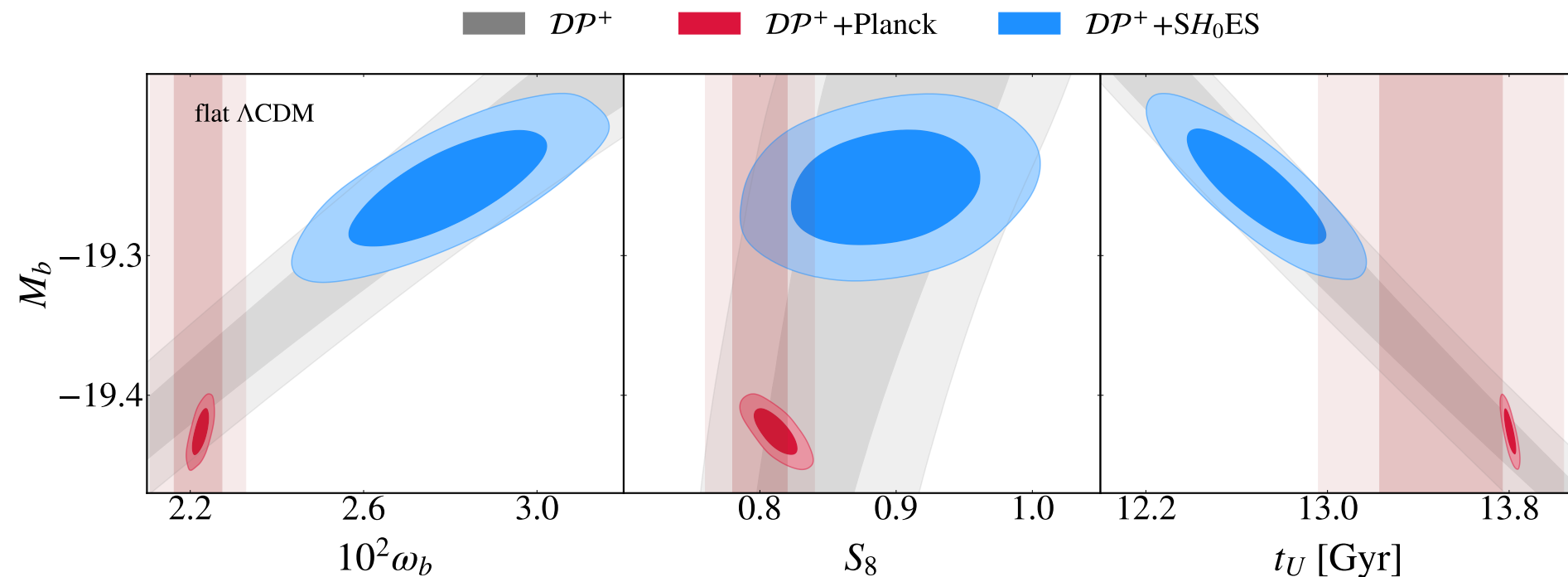


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- Challenge for new physics: **Reduce the sound horizon** and compensate the **larger  $\omega_m$  on the CMB**

See also Jedamzik++ 2010.04158, Blanchard++ 2205.05017, Pedrotti++ 2408.04530

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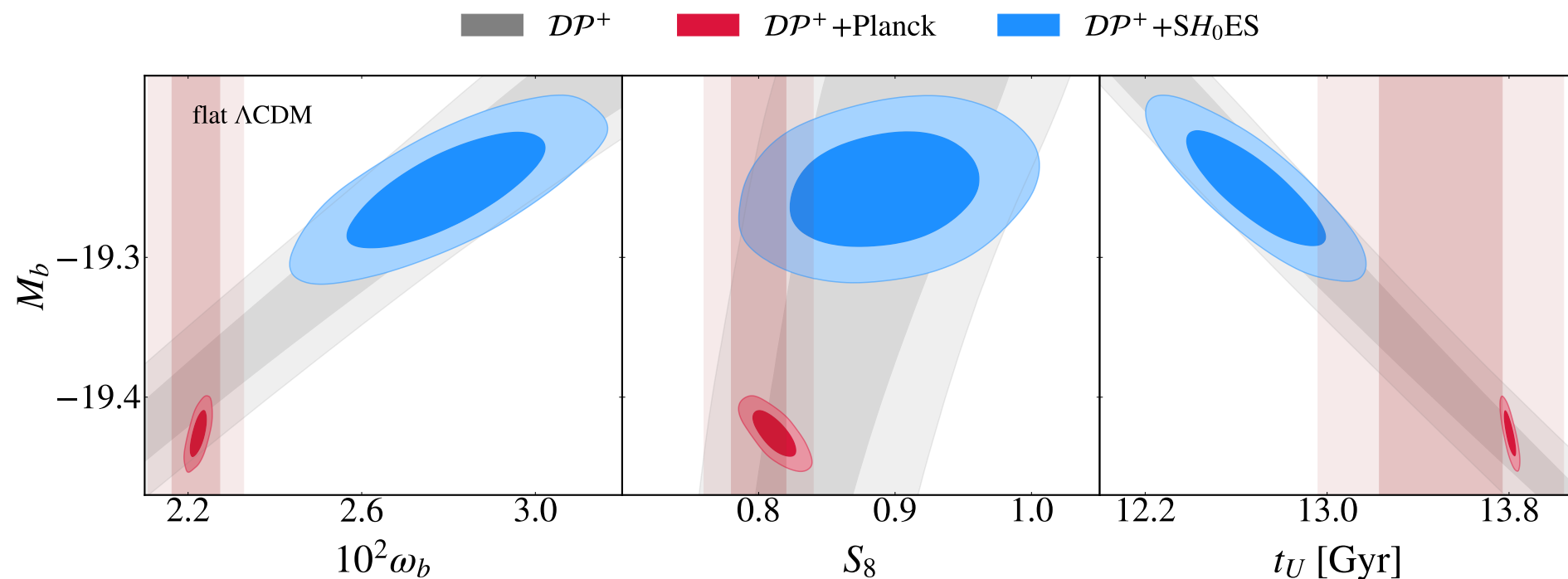
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*VP, Smith, Calderon, Simon 2407.18292*

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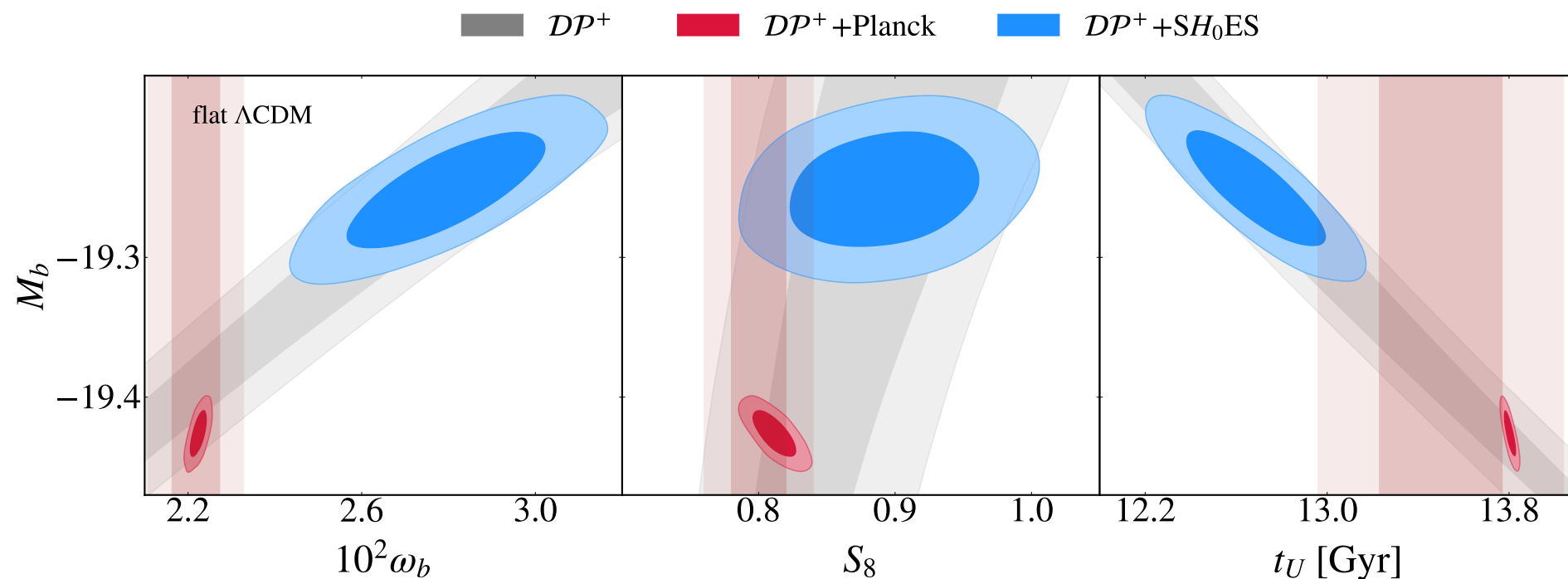
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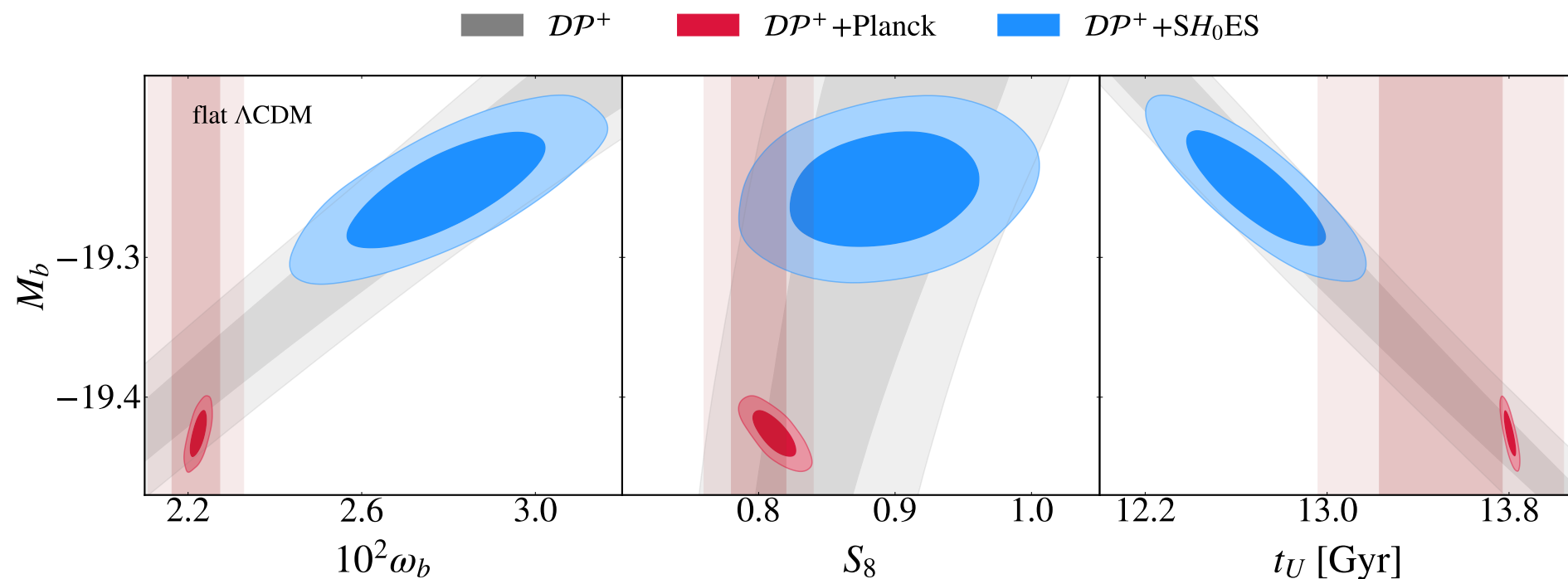
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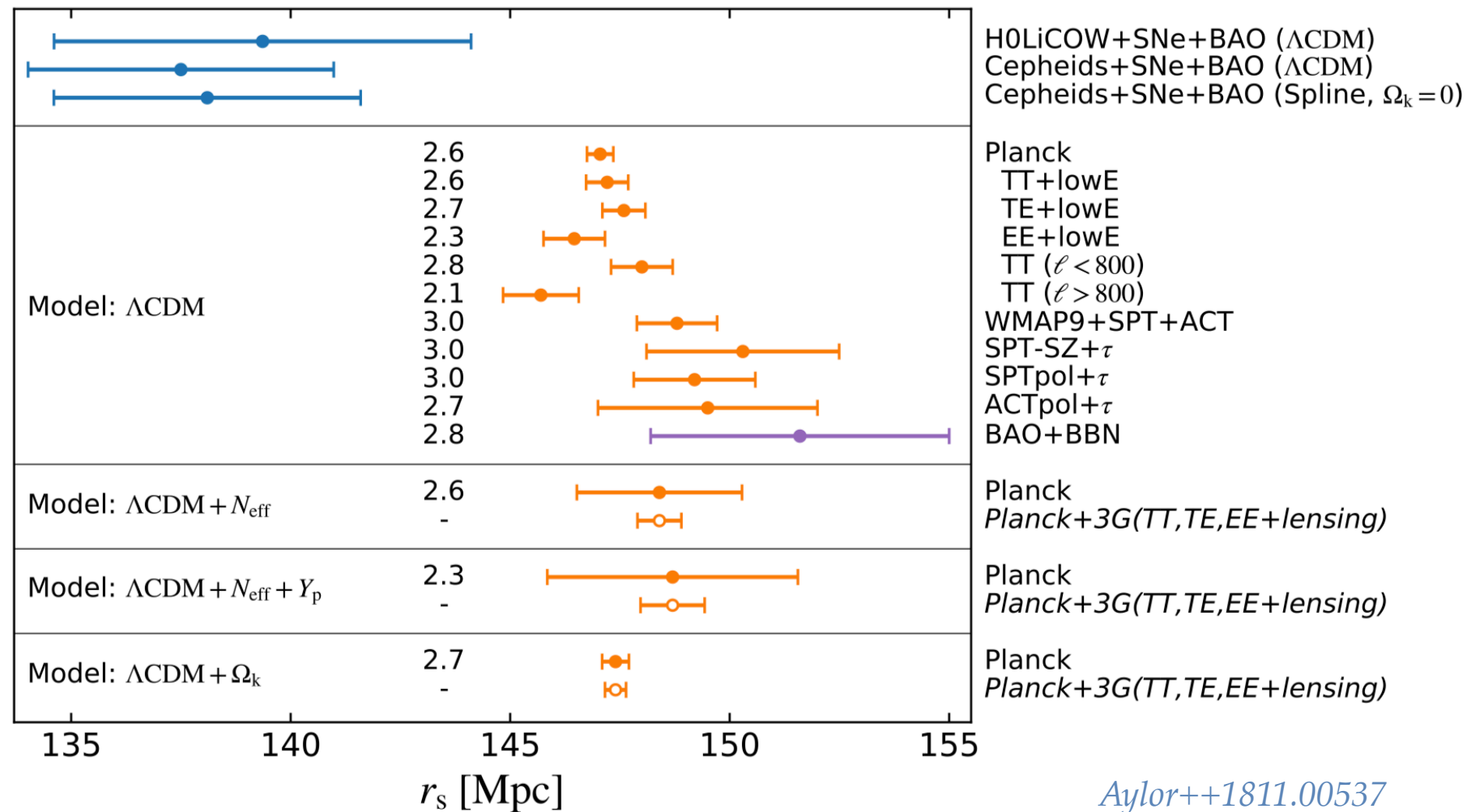
*Jedamzik & Pogosian 2010.04158*

- Age of the universe tension:**  $t_U$  is younger by about 1 Gyr than in Planck/ $\Lambda$ CDM!

*Bernal++ 2102.05066, Boyle-Kolchin 2103.15824, Vagnozzi 2105.10425*

# Solving the Cosmic Calibration Tension

- One can deduce the co-moving sound horizon  $r_s$  from  $H_0$  and BAO: CMB estimate must **decrease by  $\sim 10$  Mpc**

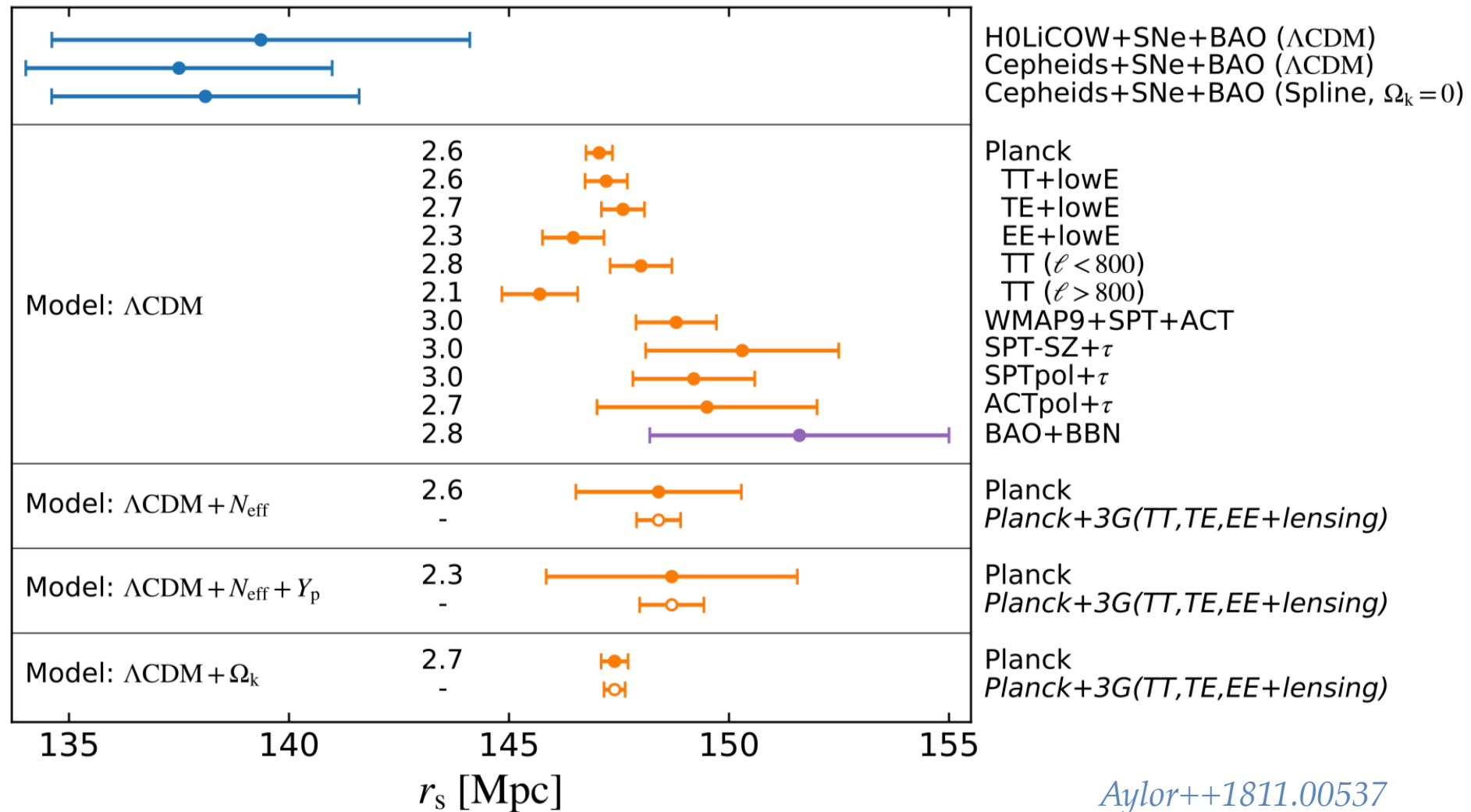


$$r_s = \int_{\infty}^{z_*} dz \frac{c_s(z)}{8\pi G/3\sqrt{\rho_{\text{tot}}(z)}}$$

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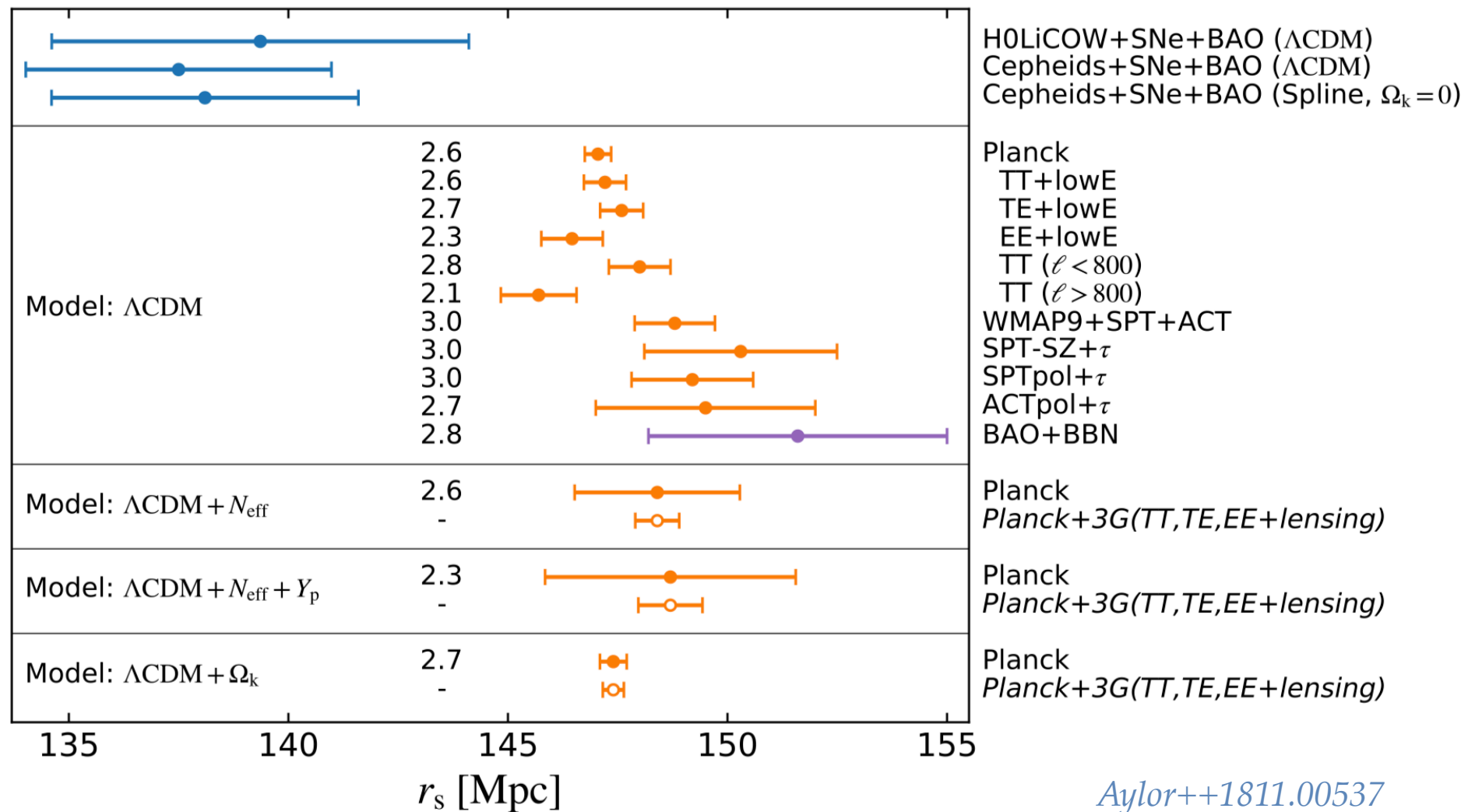
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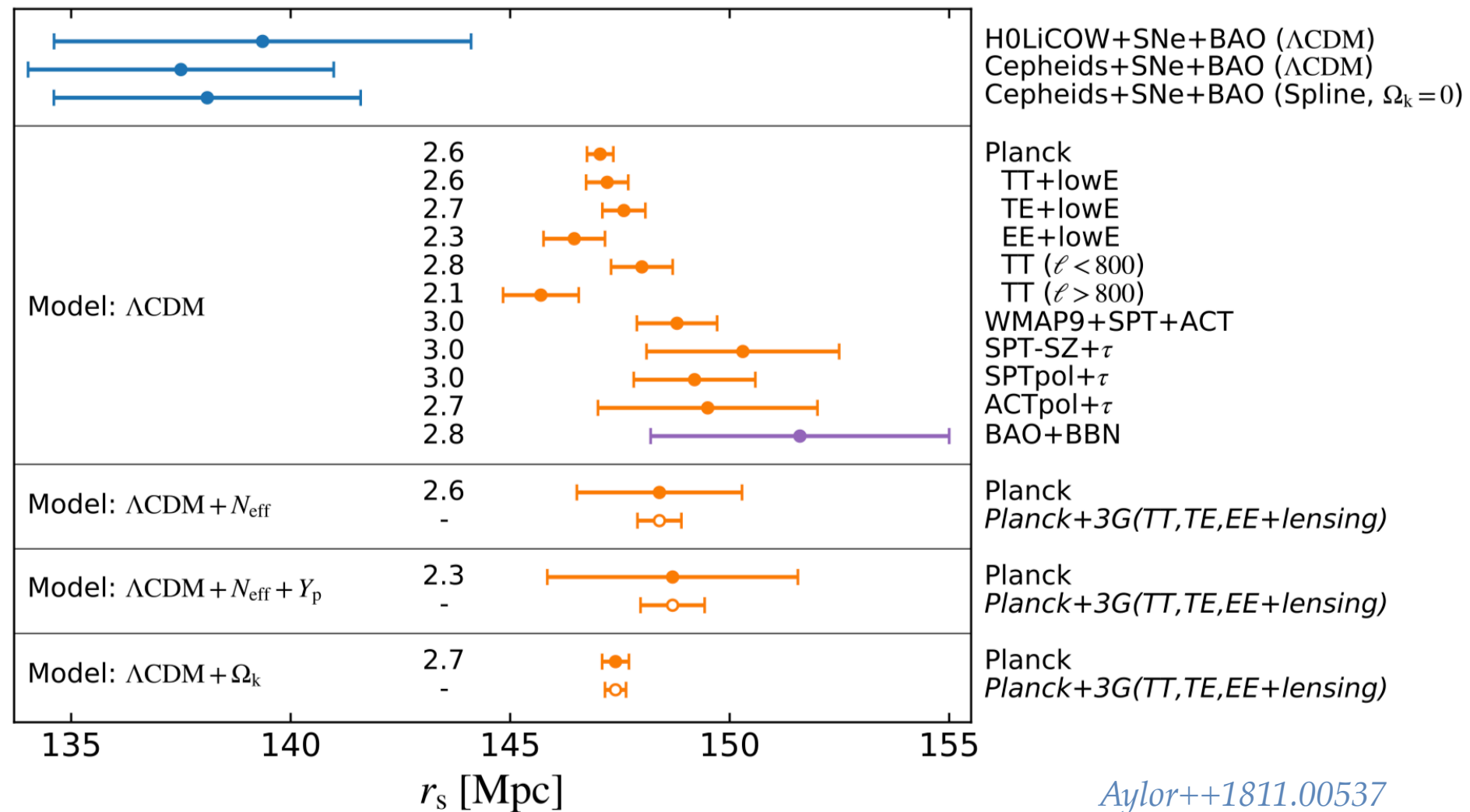
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increase  $\rho(z)$ :  $N_{\text{eff}}$ ? Early Dark Energy?  
Modified Gravity?

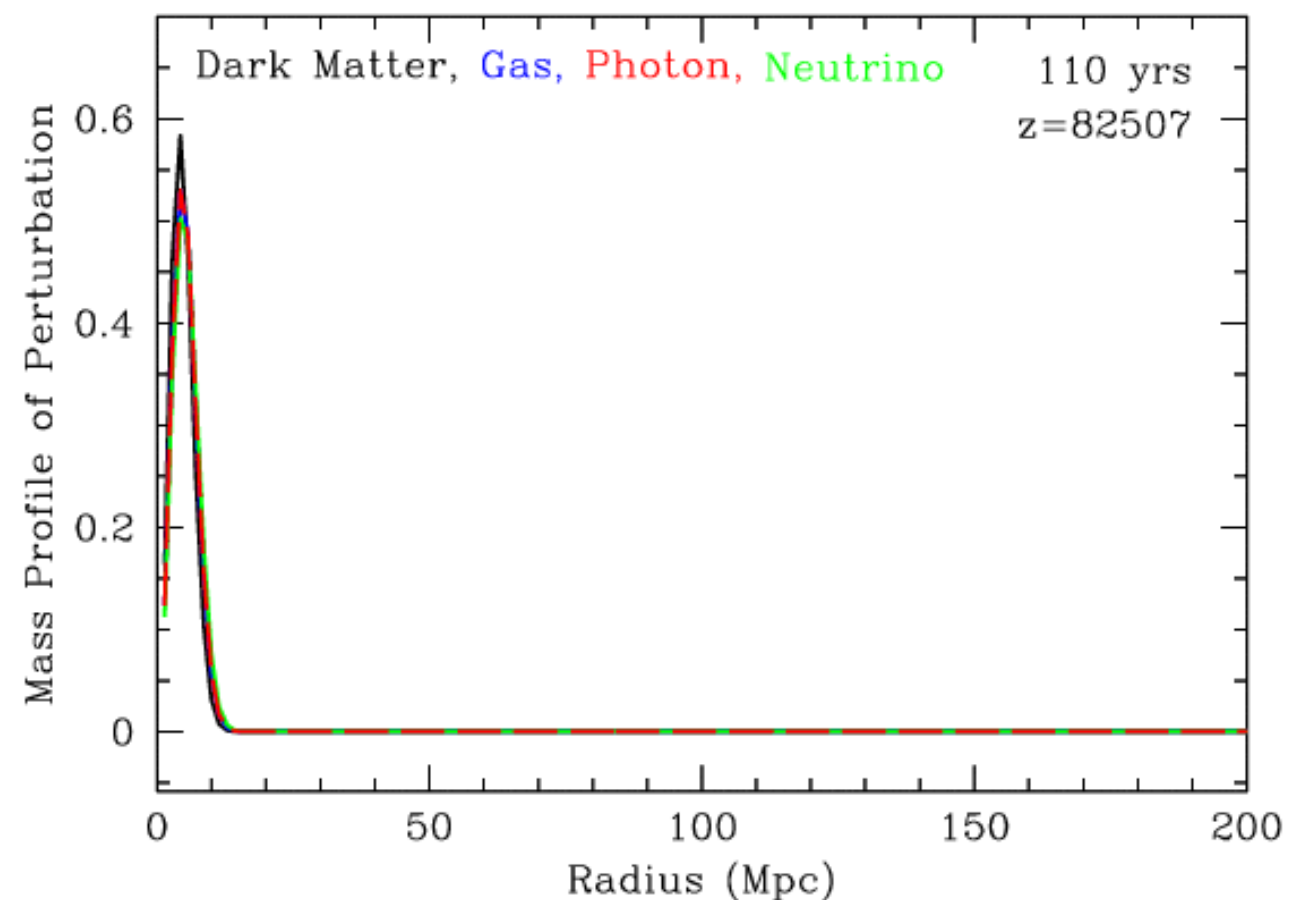
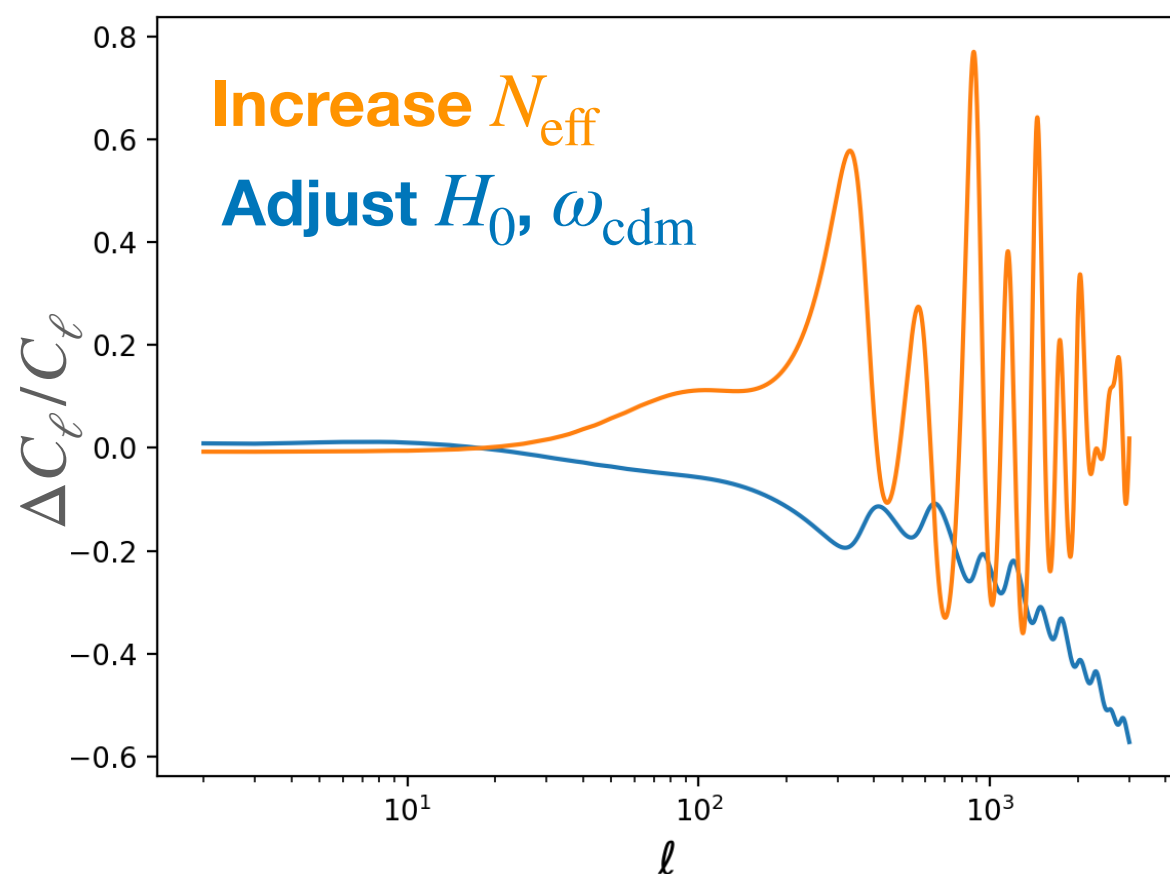
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# Relativistic species $N_{\text{eff}}$

- Additional relativistic degrees of freedom can be parametrized by  $N_{\text{eff}}$

$$\rho_R = \rho_\gamma \left( 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right)$$

- Standard Model neutrinos behave as *free-streaming radiation* since  $T \sim 1 \text{ MeV}$  with  $N_{\text{eff}} = 3.044$



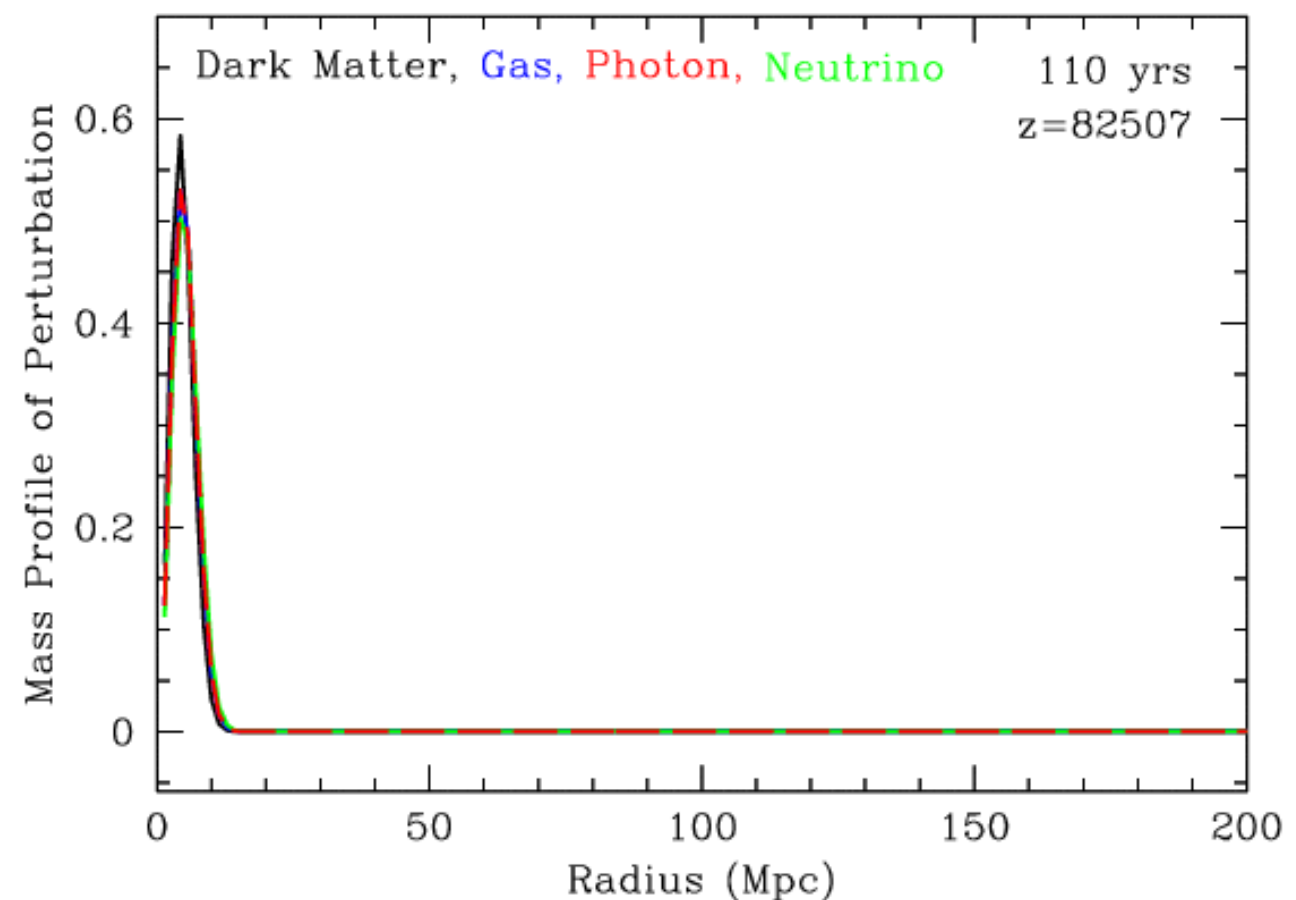
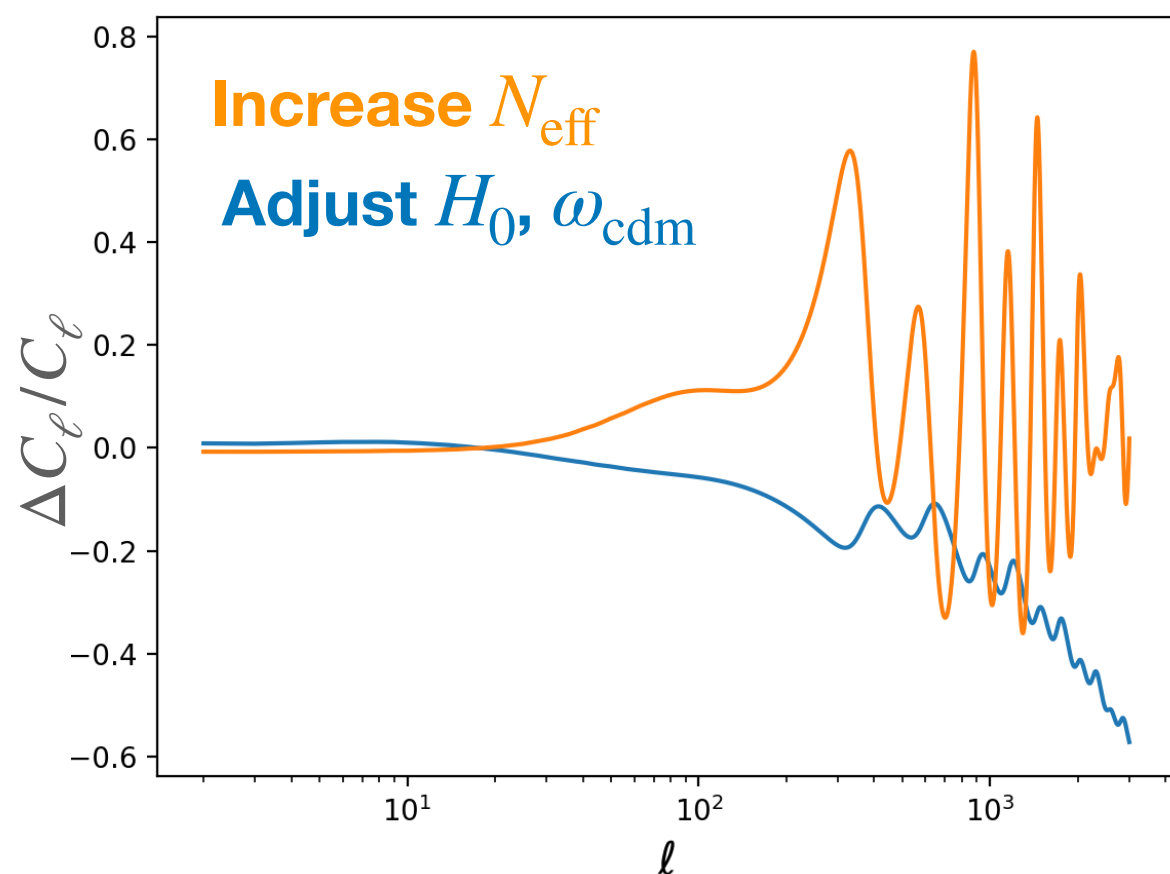
- Most of the “background” effects can be compensated for by changing  $\omega_{\text{cdm}}, H_0$ !
- Standard  $\nu$ -perturbations **phase-out and reduce  $\gamma$ -perturbations** (“ $\nu$ -drag”).

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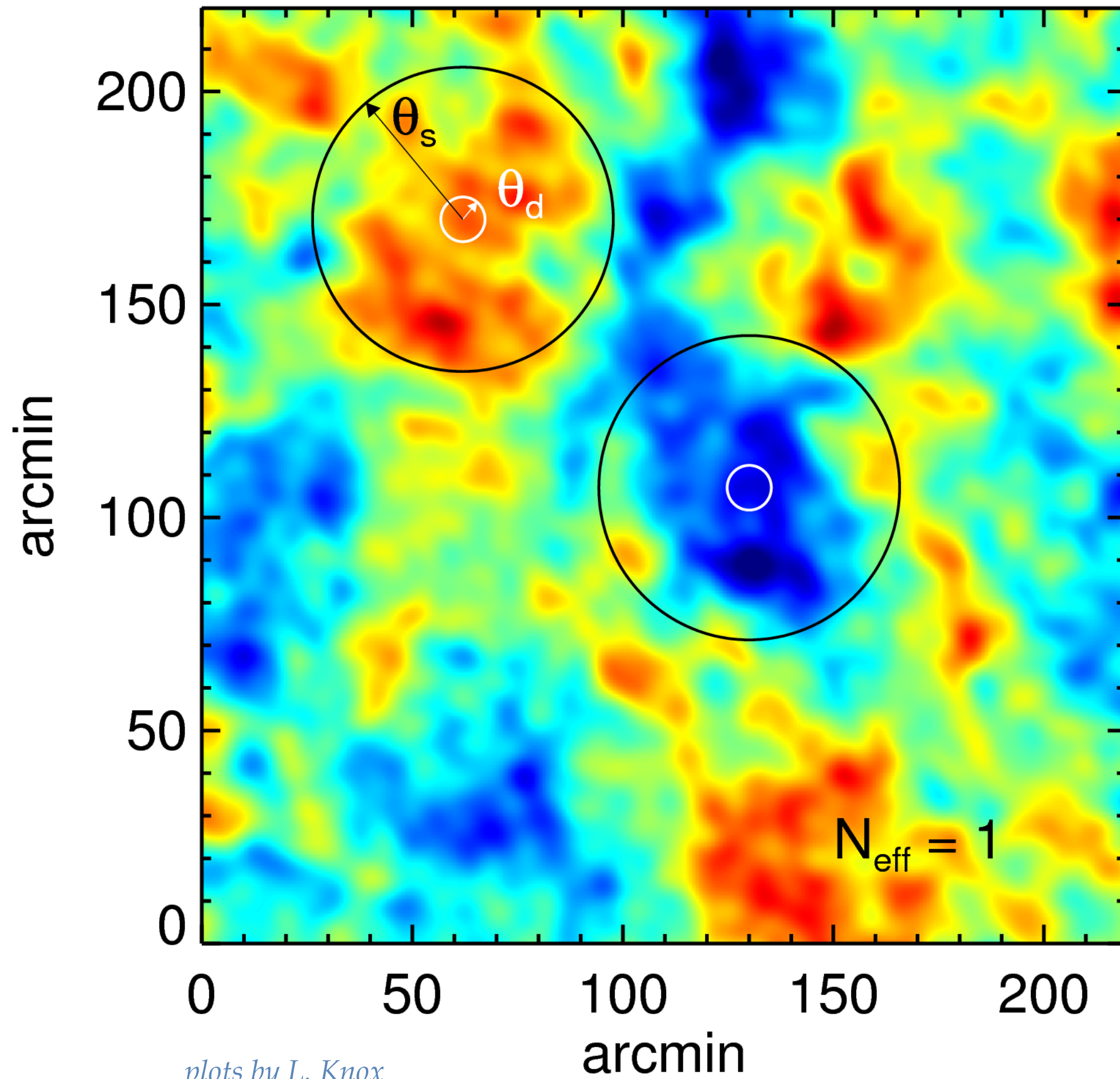
$$\rho_R = \rho_\gamma \left( 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right)$$

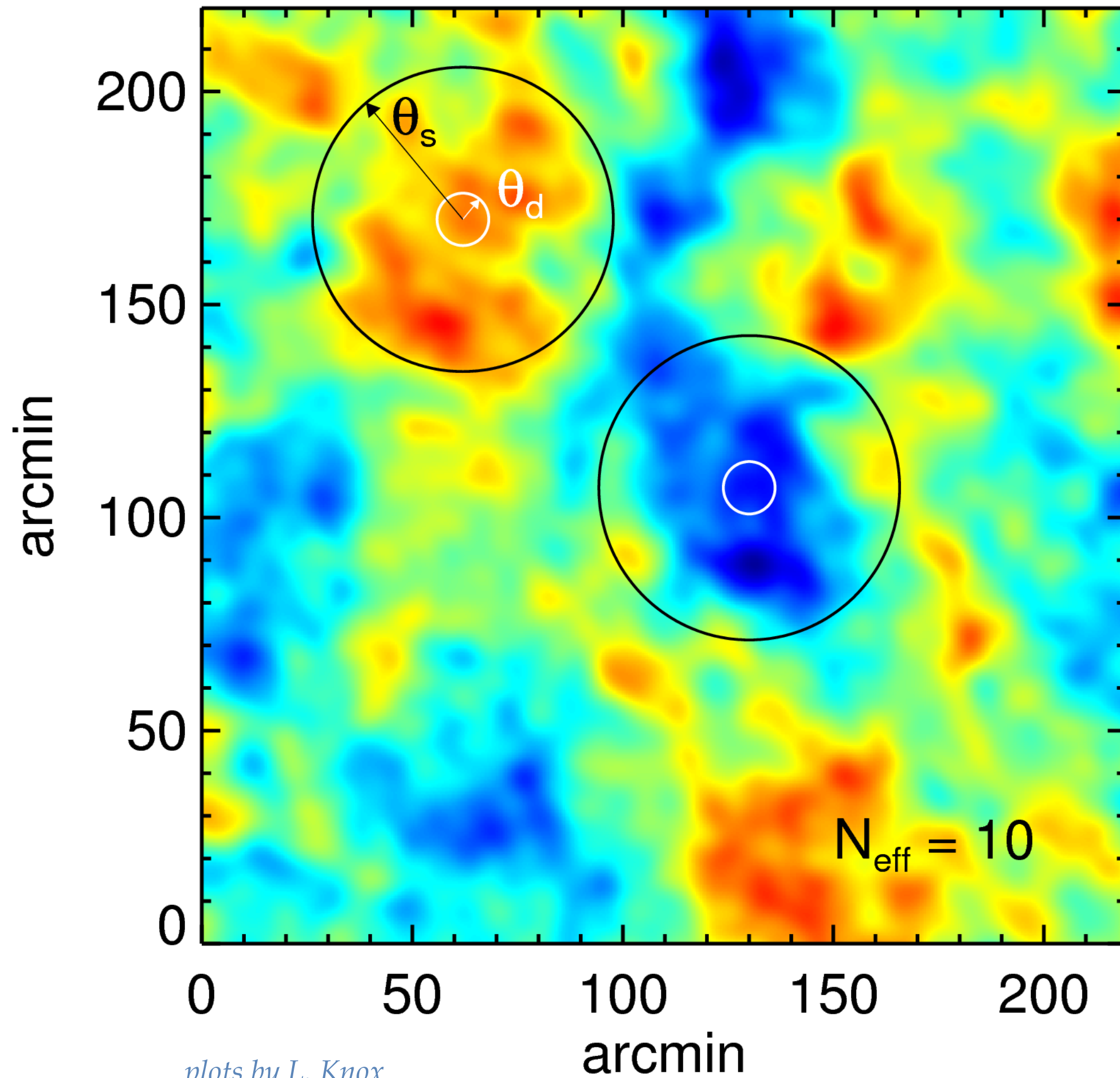
- Standard Model neutrinos behave as *free-streaming radiation* since  $T \sim 1 \text{ MeV}$  with  $N_{\text{eff}} = 3.044$



- Most of the “background” effects can be compensated for by changing  $\omega_{\text{cdm}}, H_0$ !
- Standard  $\nu$ -perturbations **phase-out and reduce  $\gamma$ -perturbations** (“ $\nu$ -drag”).





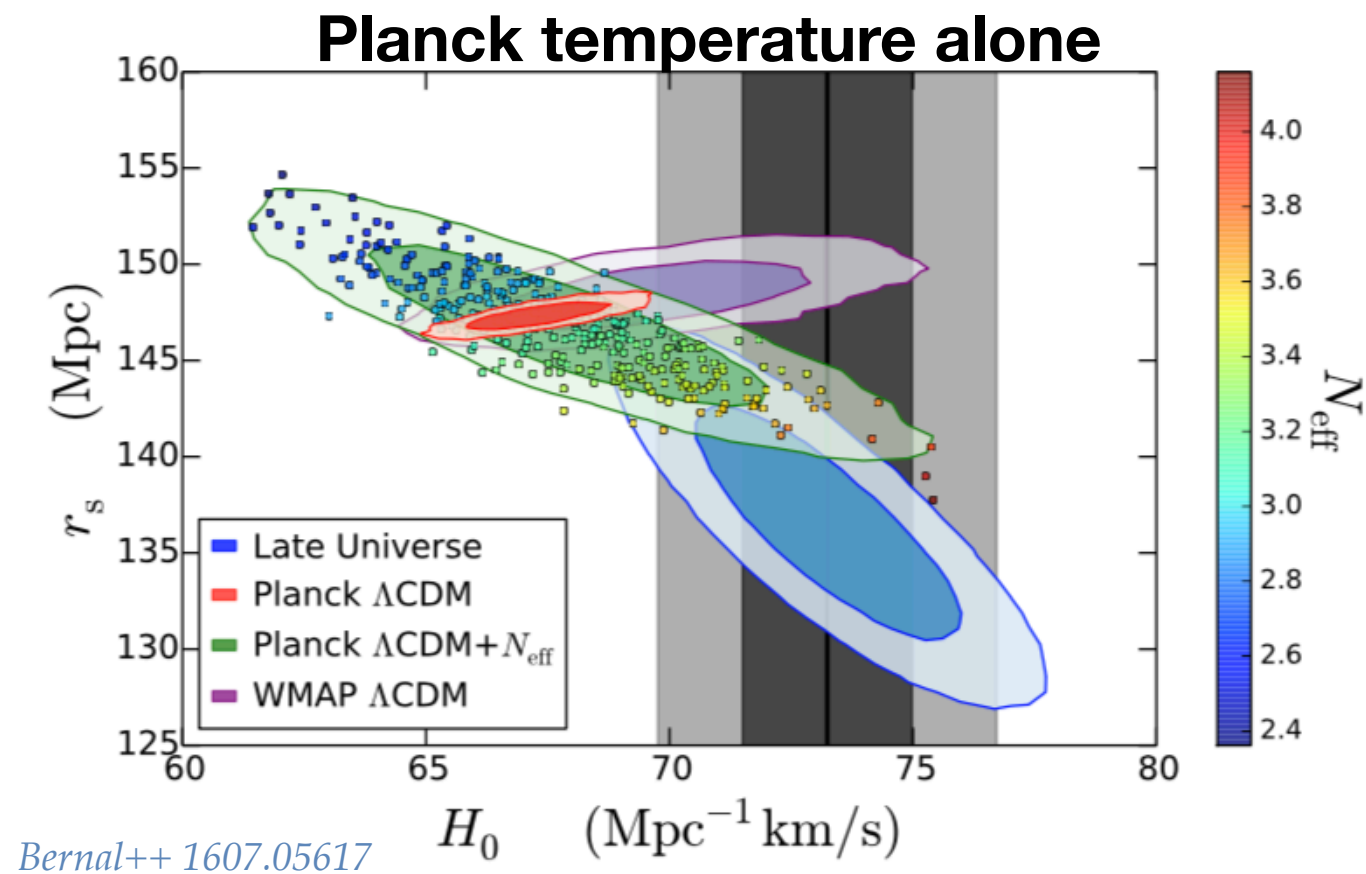


# $N_{\text{eff}}$ cannot resolve the Hubble tension (sadly)

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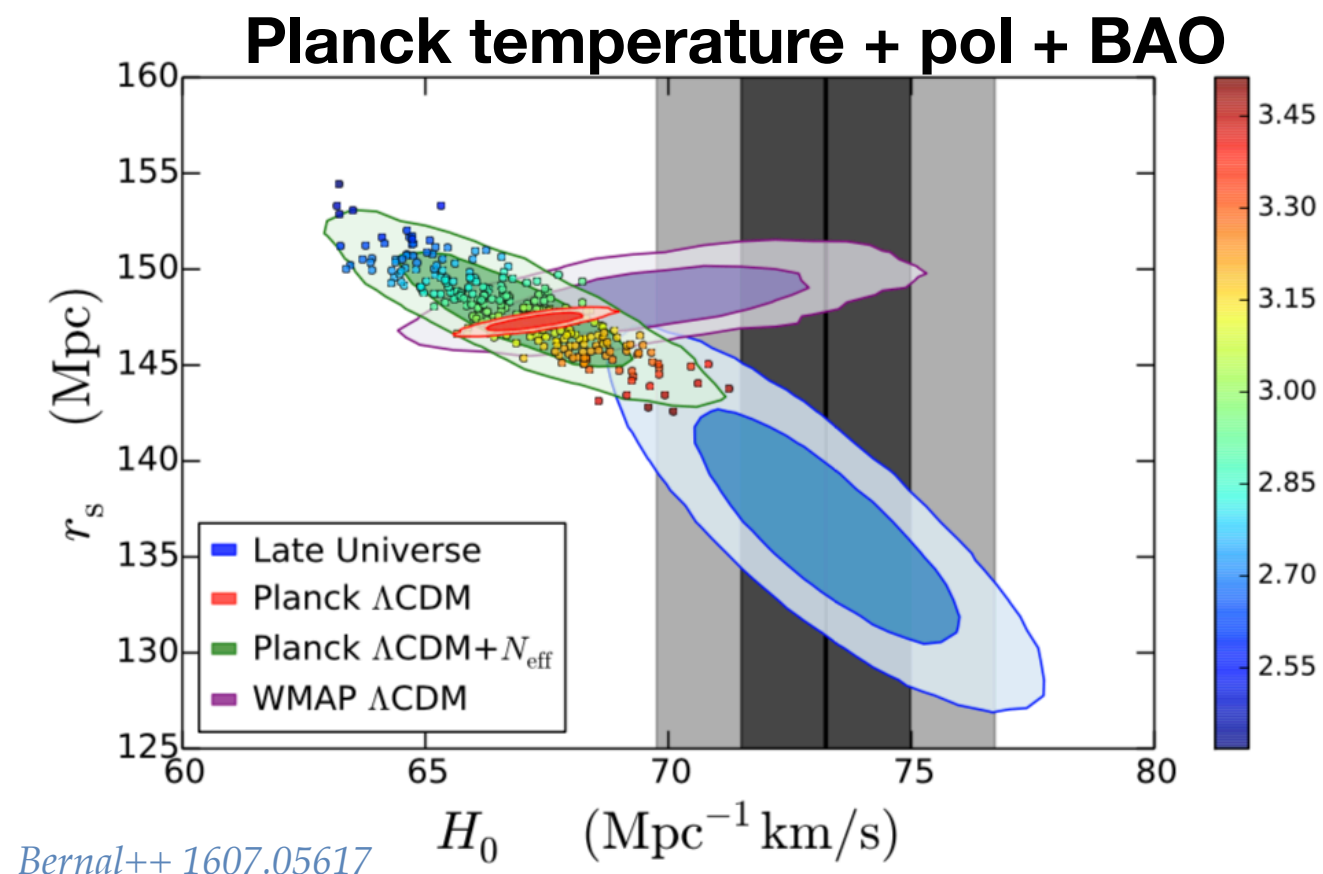
- $\Delta N_{\text{eff}}$  (free-streaming)  $\sim 0.5 - 1$  is needed





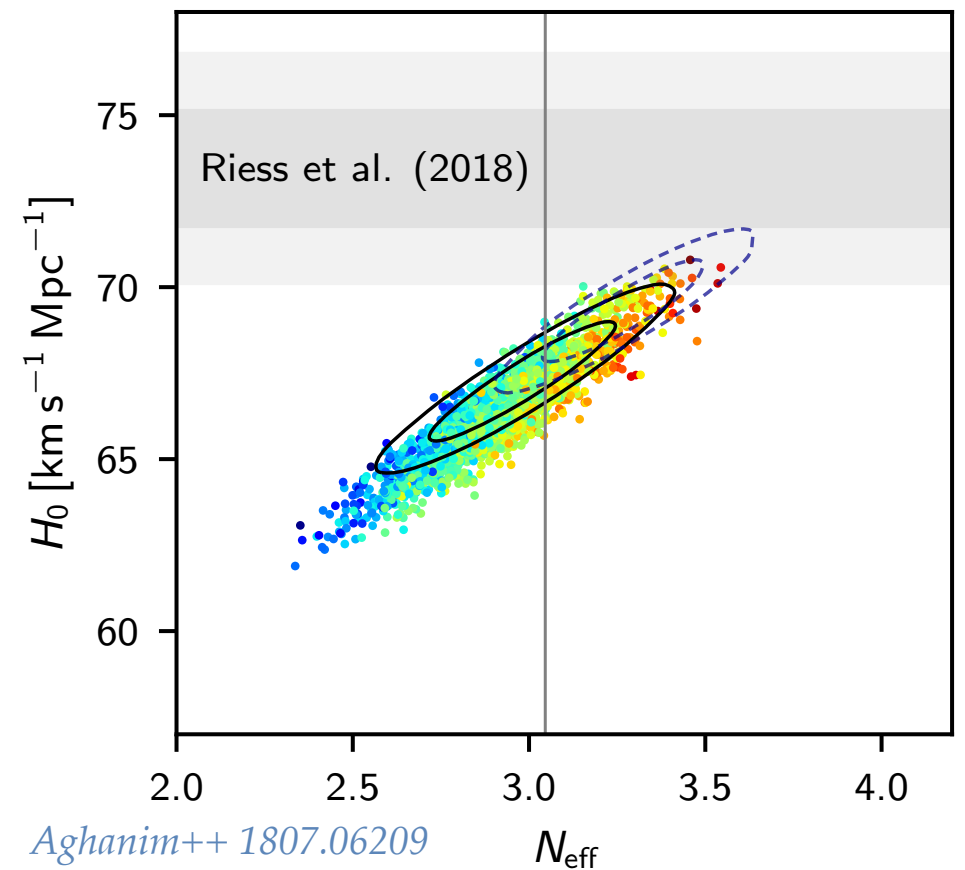
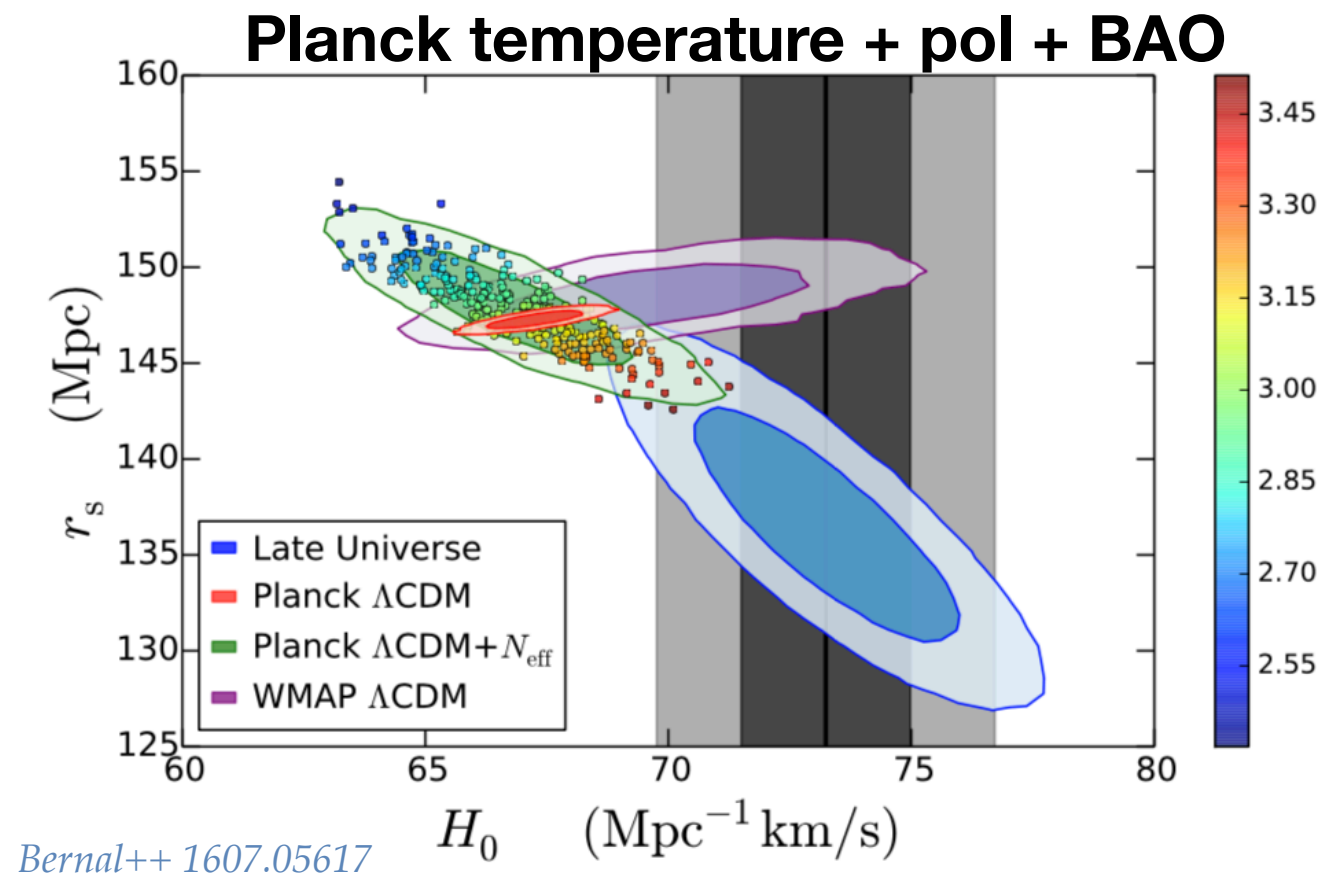
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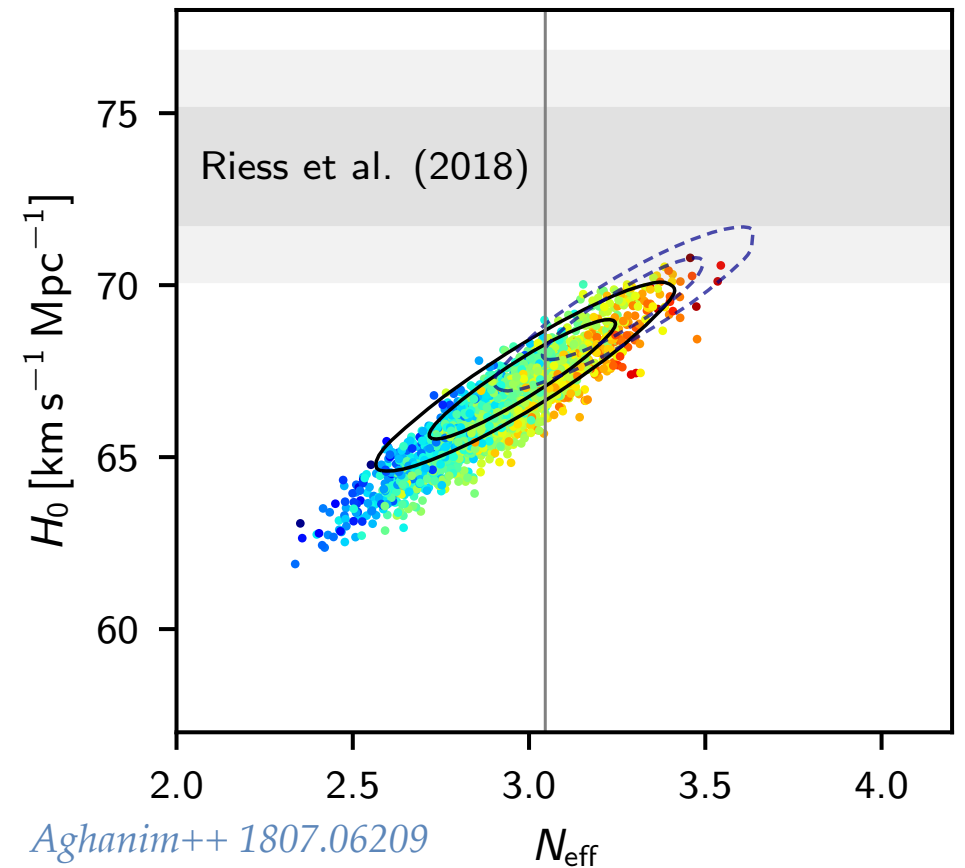
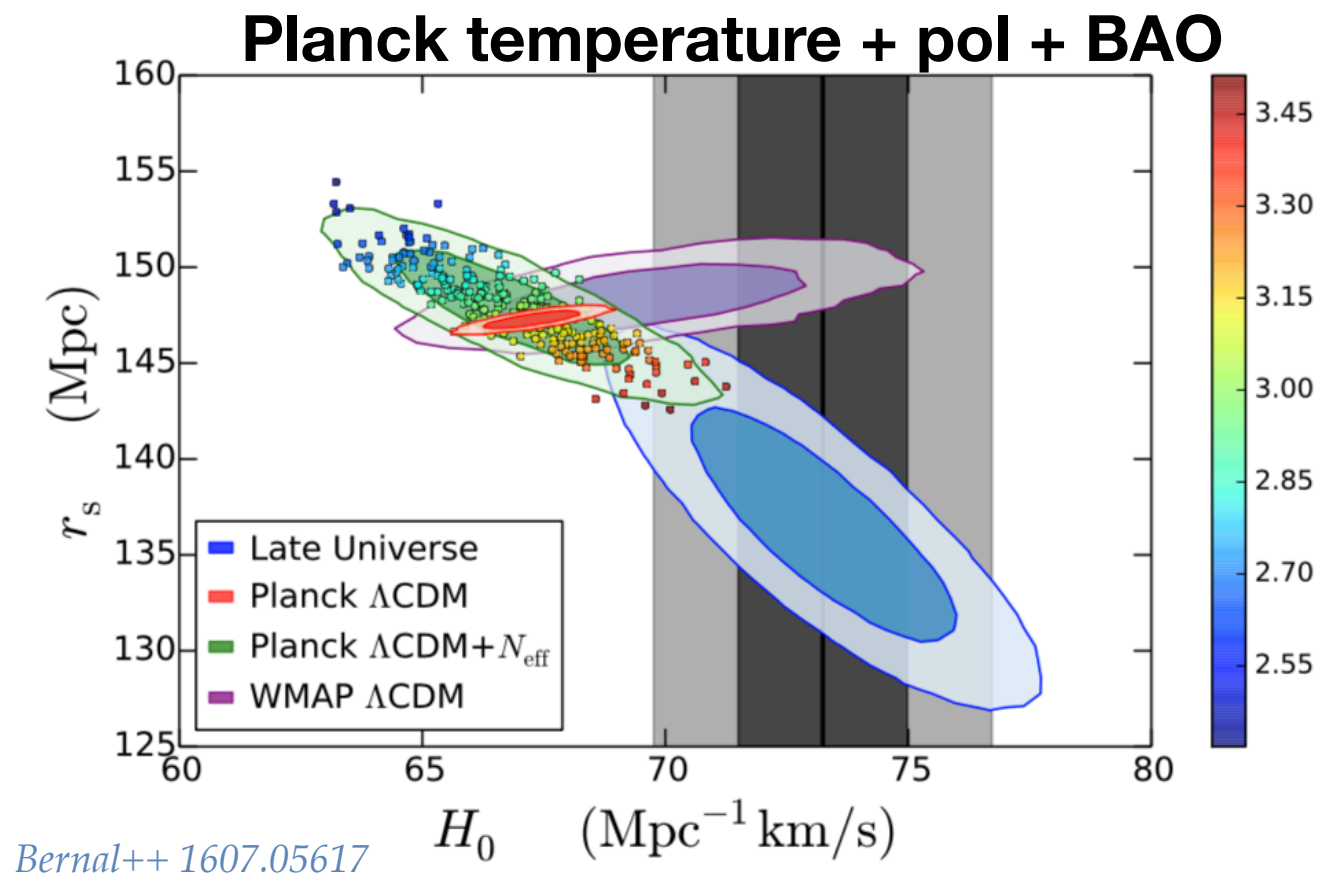
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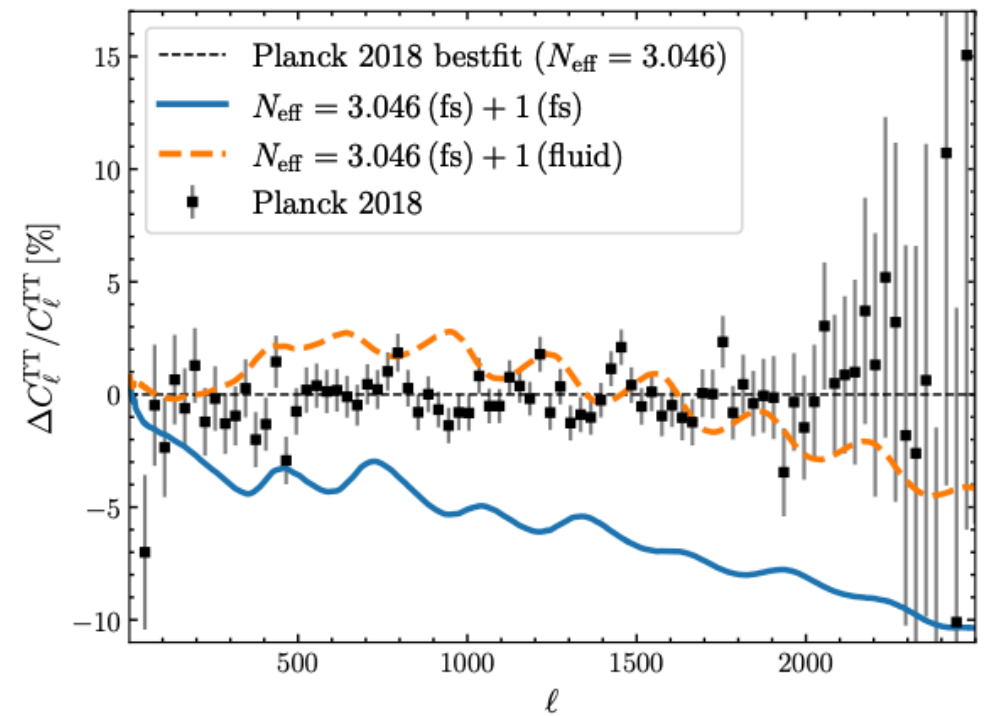
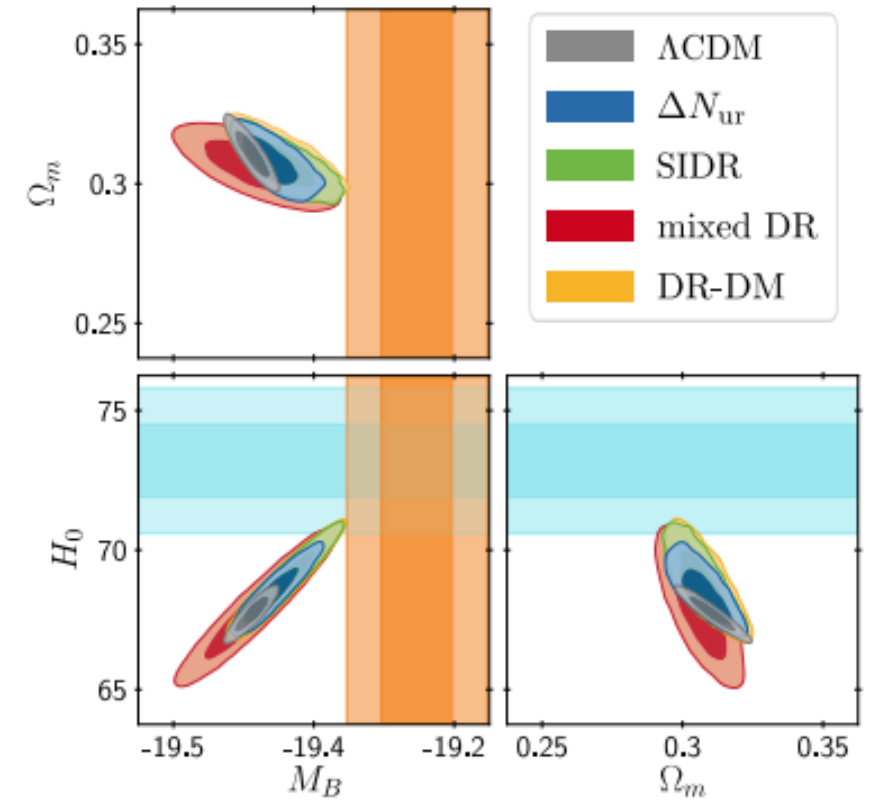
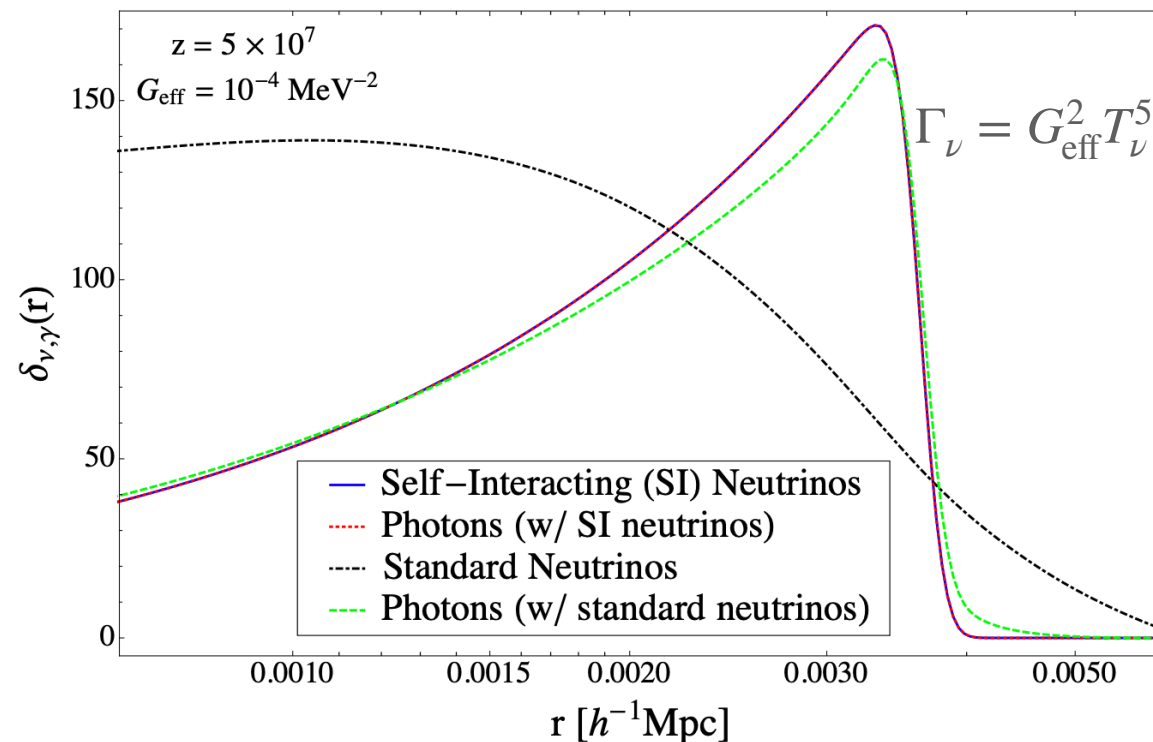
**Planck+BAO constrains  $N_{\text{eff}} = 2.99 \pm 0.17$  and  $H_0 = 67.3 \pm 1.1 \text{ km/s/Mpc}$**

**Is it possible to relax this bound?**

# Introducing exotic $\nu$ -interactions

- Exotic  $\nu$  self-interaction can **erase free-streaming** and make  $\nu$  behaves as **perfect fluid**.
- Once interactions are switched on:  **$\gamma$ -perturbations are enhanced / phase is washed-out.**
- This helps a bit but **not enough to explain  $H_0$**

*Cyr-Racine++ 1306.1536*





# Interacting neutrinos could resolve $H_0$ tension

see also Ghosh ++1908.09843

- Free-streaming neutrinos lead to a phase shift:

*Bashinsky&Seljak, astro-ph/0310198, Baumann++ 1508.06342*

- Self-interacting neutrinos: no phase shift,  $\theta_s$  is larger than in  $\Lambda$ CDM  $\Rightarrow$  larger  $H_0$

$$\theta_{\text{peak}} = \theta_s + \delta\theta \sim 0.6 \left( \frac{\rho_\nu}{\rho_g} \right)$$

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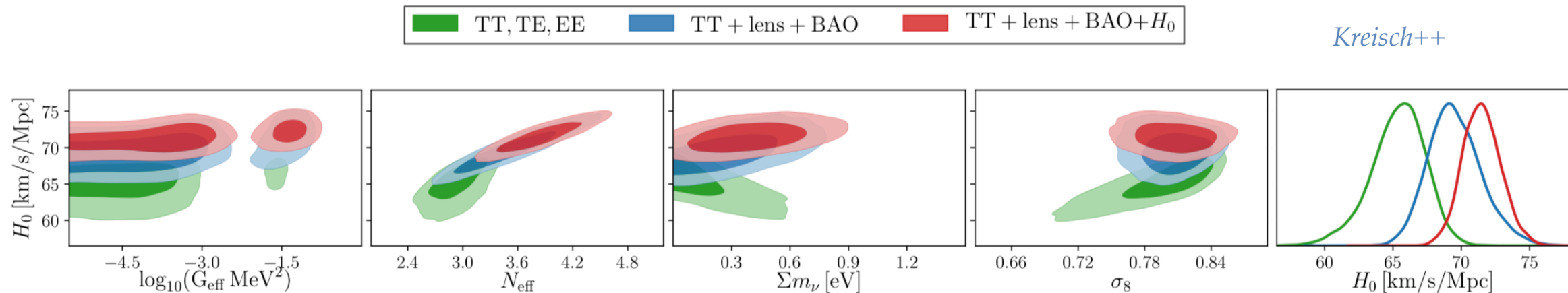
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- 2015 data: solution requires 4 strongly interacting neutrinos with  $M \sim 0.4\text{eV}$

- “For free”: solve  $S_8$  tension and reactor anomalies!

- BBN & Lab. requires majorana neutrinos and a heavy mediator coupled to  $\nu_\tau$

*Blinov++ 1905.02727*

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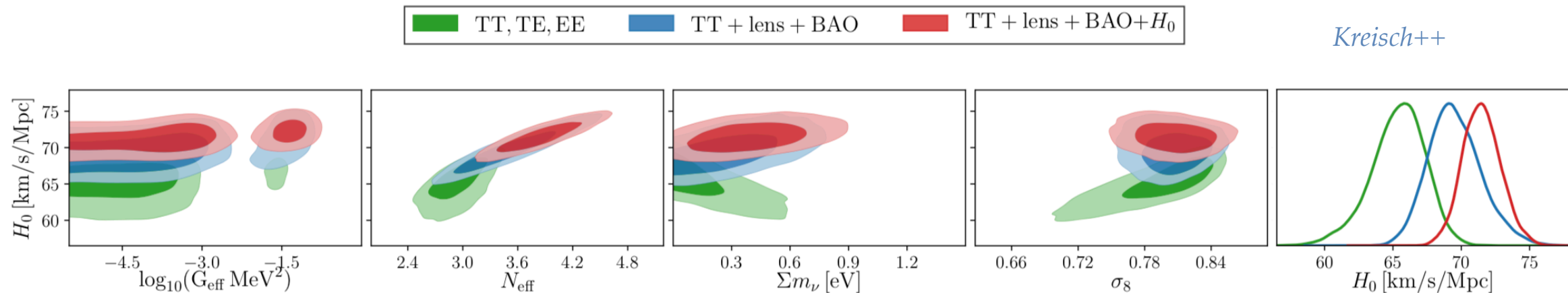
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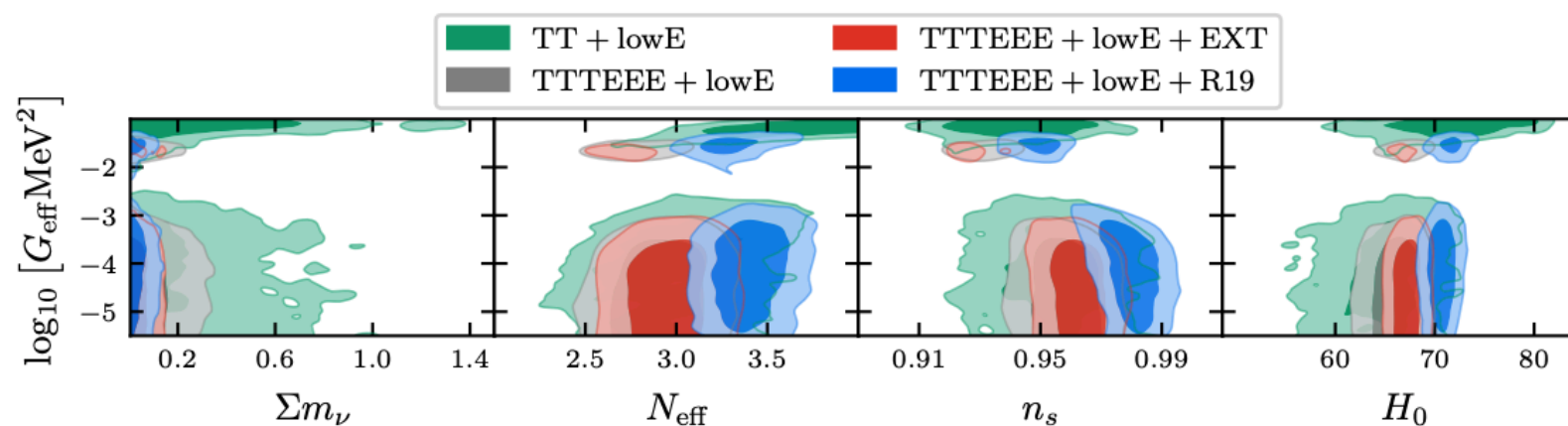
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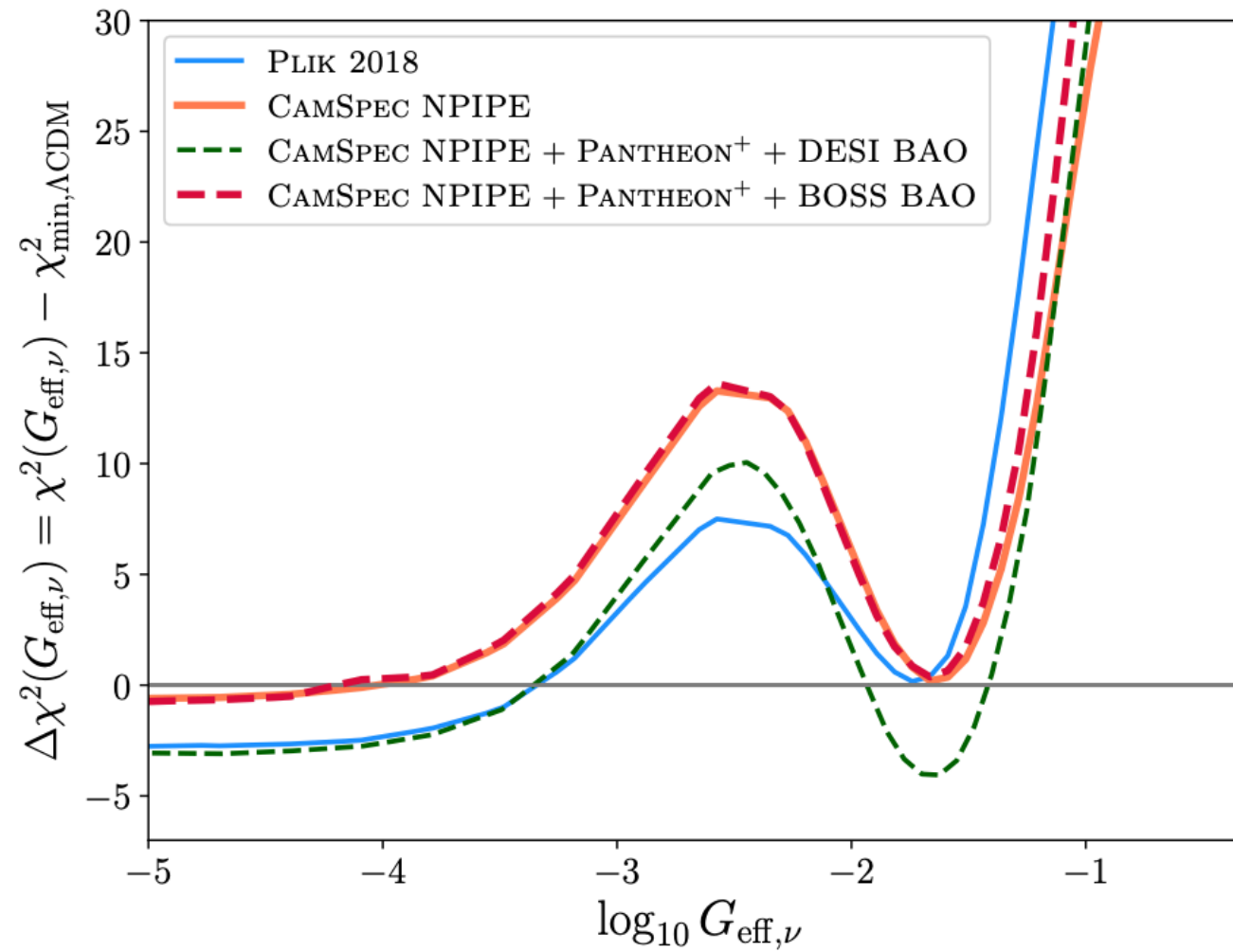
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*Blinov++ 1905.02727*

- 2018 Planck polarization data disfavor the strongly interacting mode.



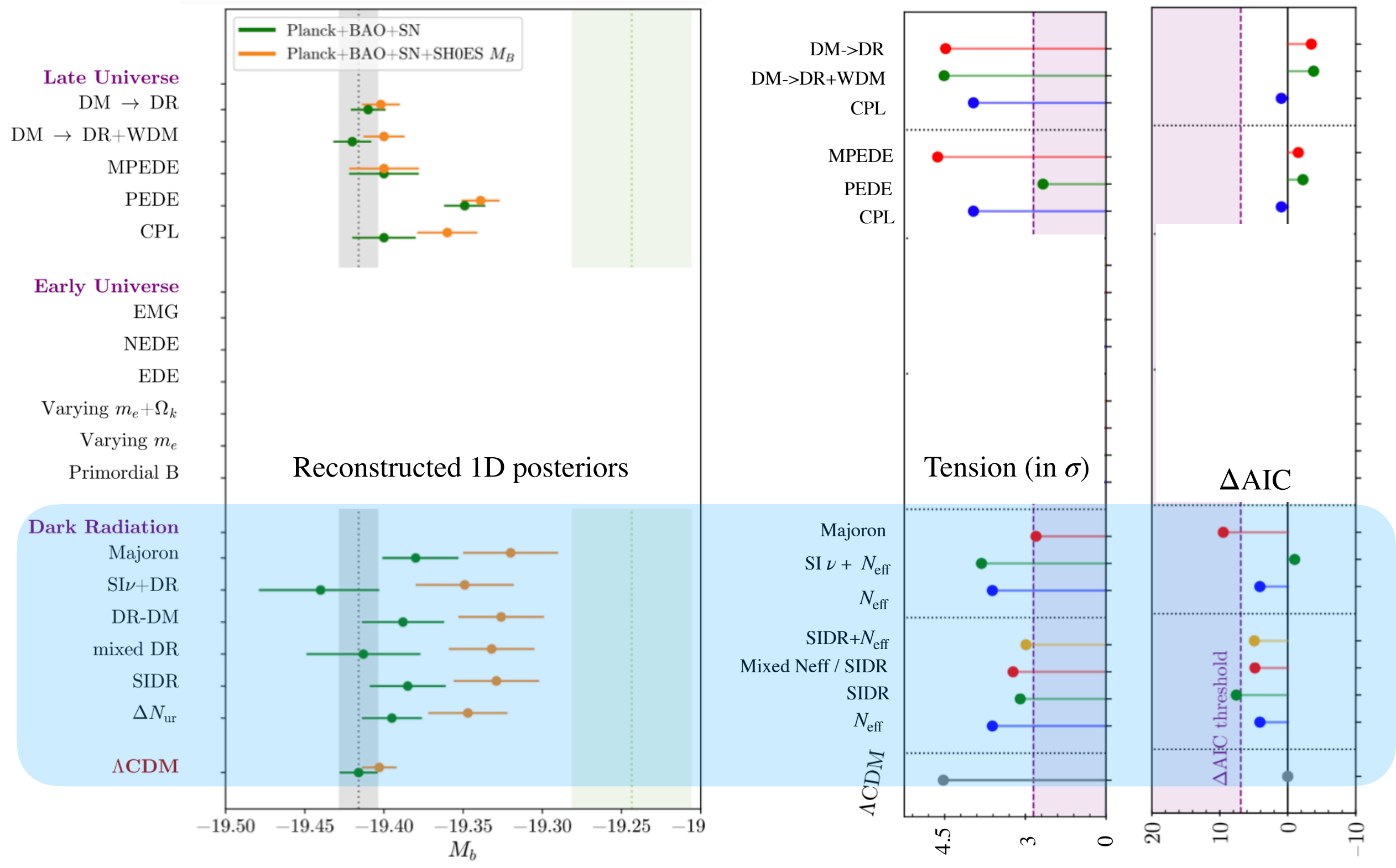
# Update with NPIPE & DESI



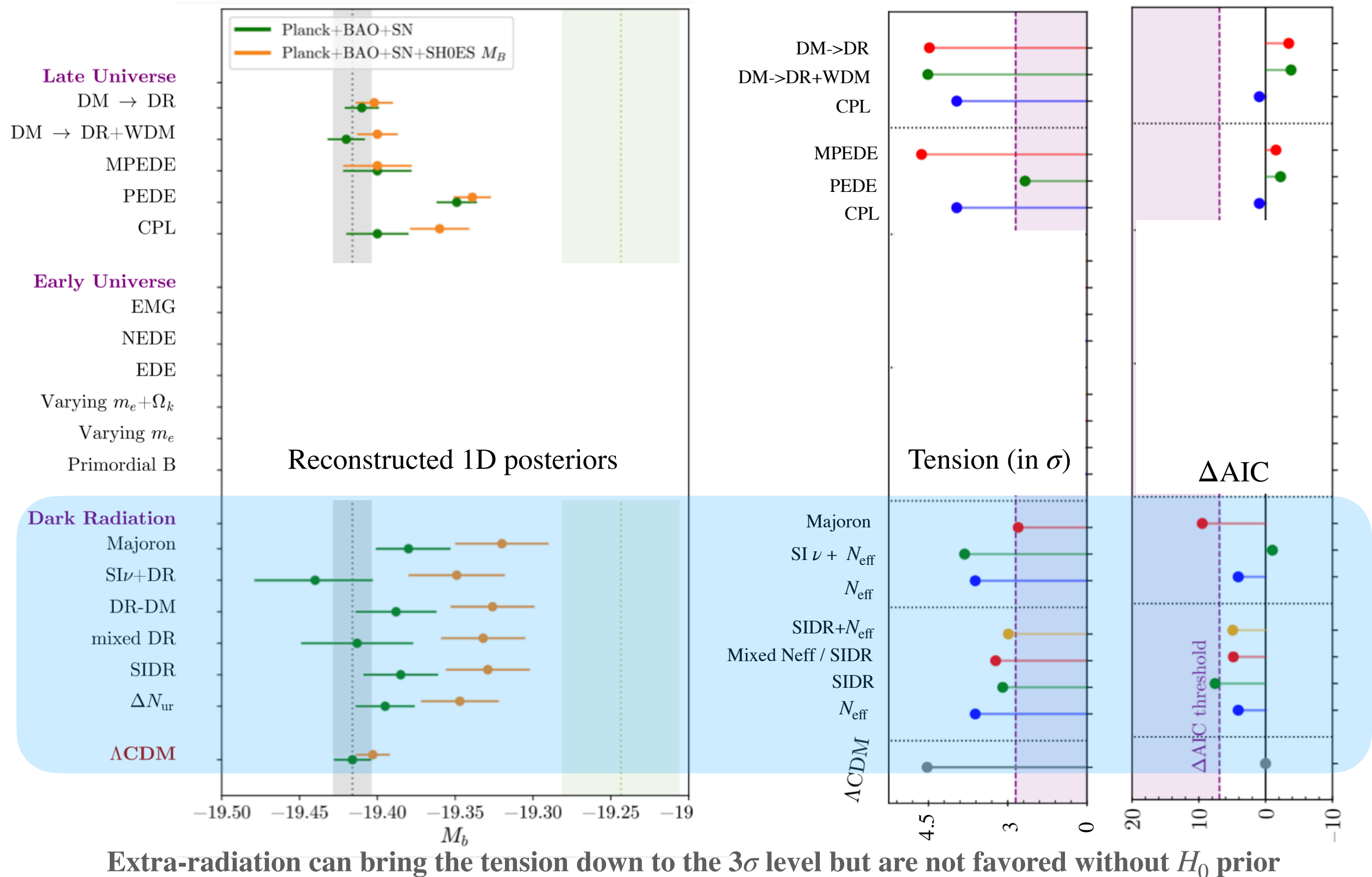
	SIν	
	BOSS BAO	DESI BAO
$\log_{10} G_{\text{eff},\nu}$	$-1.63(-1.66)^{+0.13}_{-0.10}$	$-1.61(-1.66)^{+0.14}_{-0.11}$
$-2 \log \mathcal{L}(\log_{10} G_{\text{eff},\nu})$	$-1.66^{+0.14}_{-0.13}$	$-1.66^{+0.11}_{-0.13}$
$H_0$	$67.58(67.2)^{+0.91}_{-1.4}$	$68.6(68.0)^{+1.2}_{-1.4}$



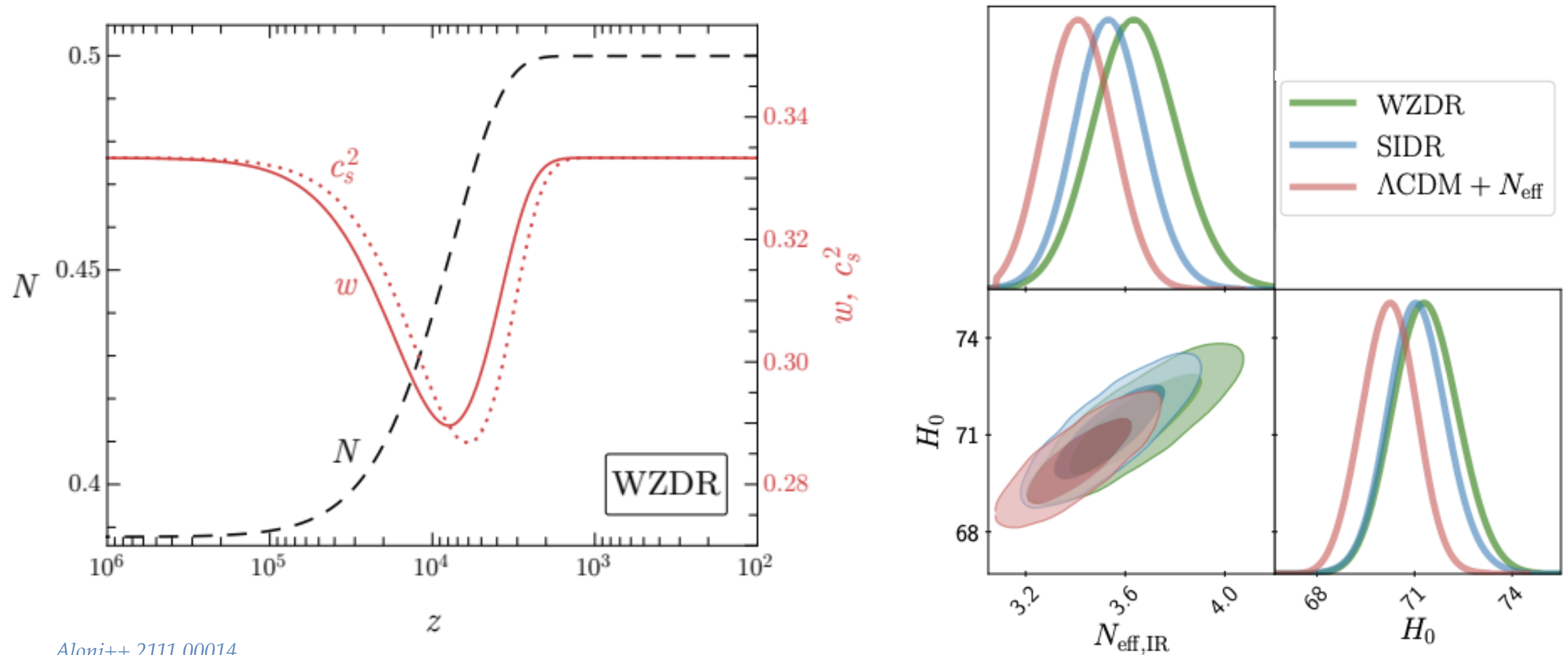
# Status of “ $N_{\text{eff}}$ –like” solutions



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# A step in resolving the H0 tension



Aloni++ 2111.00014

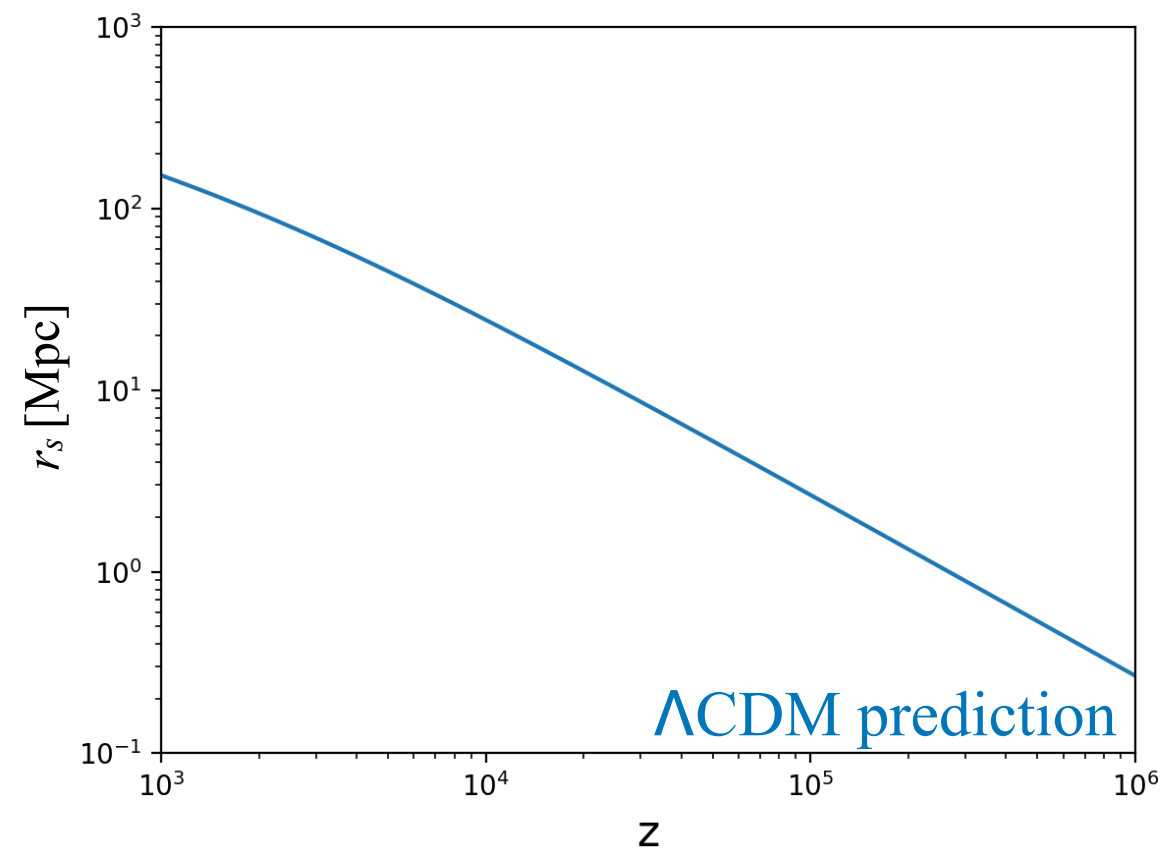
- If  $N_{\text{eff}}$  has a step around  $z \sim 10^4$  e.g. from decoupling of a scalar  $\phi$  with  $m \sim 1\text{eV}$  reheating a bath of fermion  $\psi$ .

$$\frac{N_{\text{IR}}}{N_{\text{UV}}} = \left( \frac{g_*^\phi + g_*^\psi}{g_*^\psi} \right)^{1/3} = \left( \frac{15}{7} \right)^{1/3} \simeq 1.29$$

- WZDR model provides a significantly better fit than standard  $N_{\text{eff}}$  or SIDR

# Exotic energy injection to resolve the $H_0$ tension

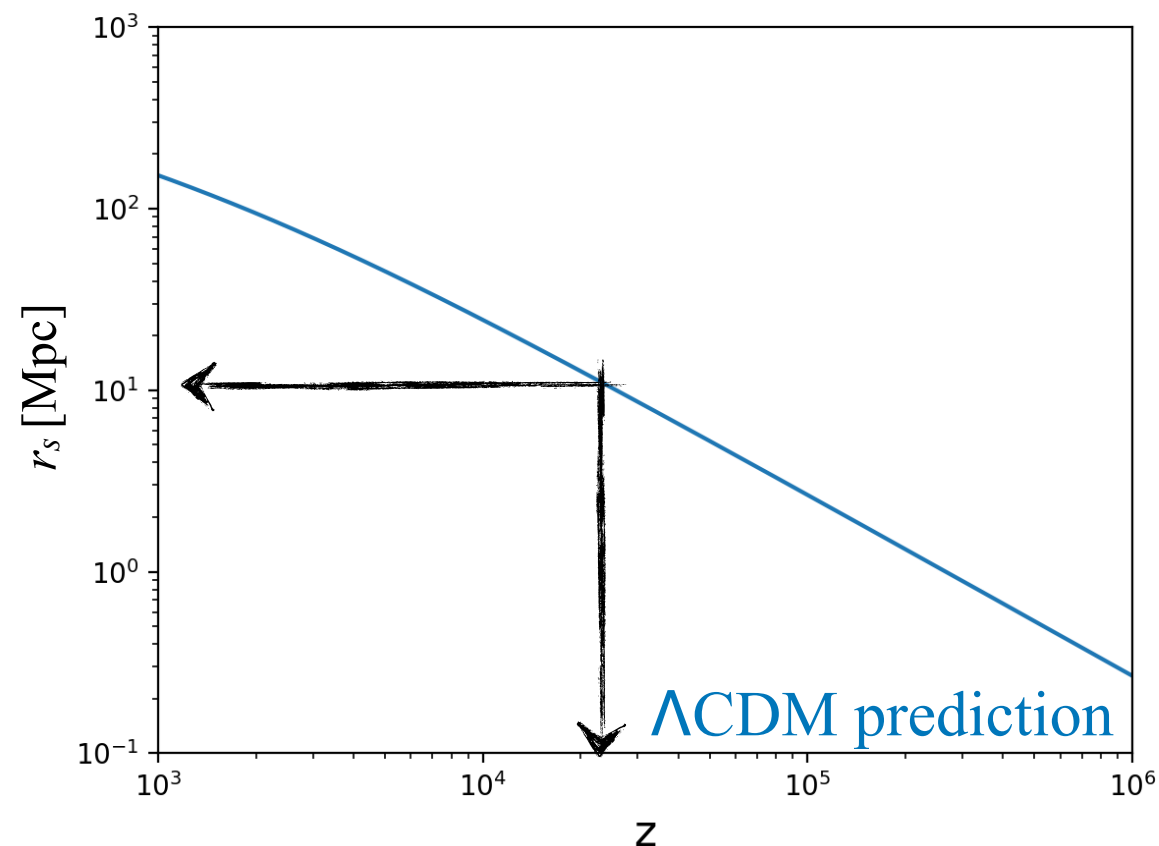
- $r_s$  must decrease by  $\sim 10\text{Mpc}$ .



*See the 'Hubble Hunter's guide' Knox&Millea 1908.03663*

# Exotic energy injection to resolve the $H_0$ tension

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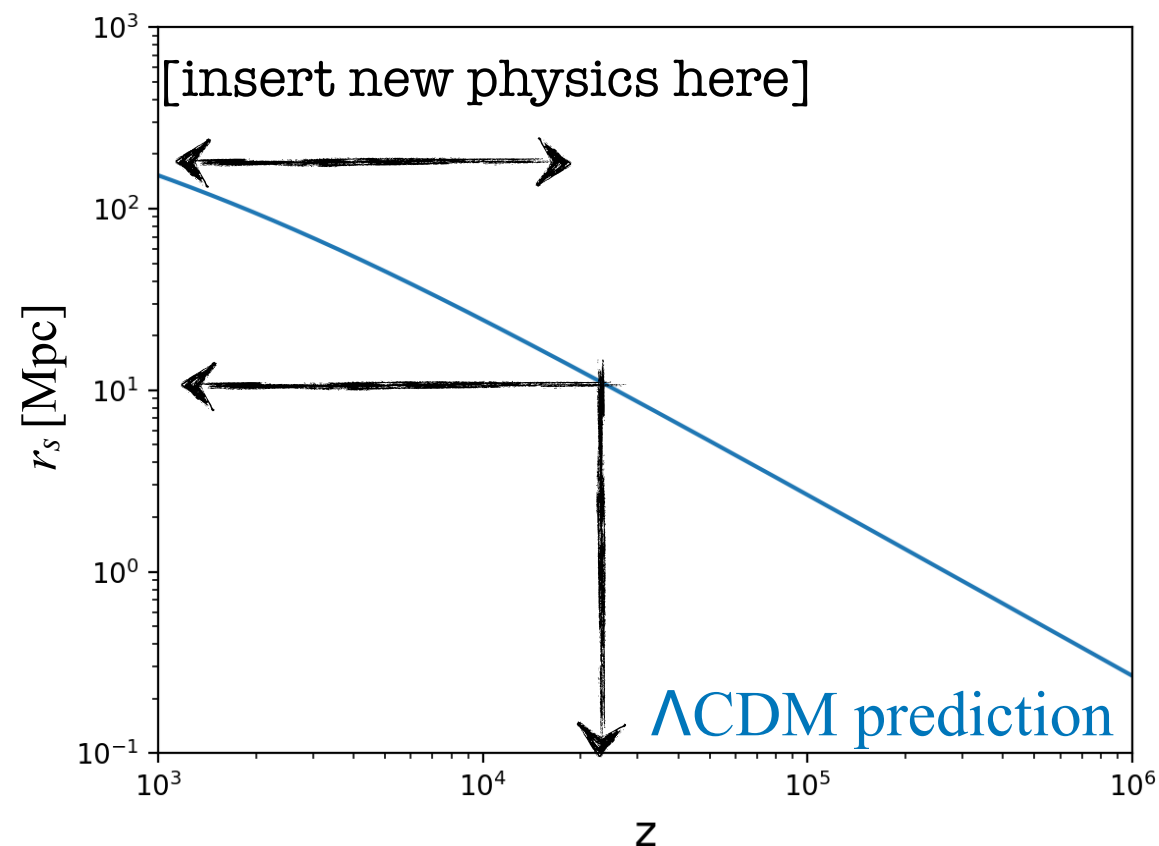


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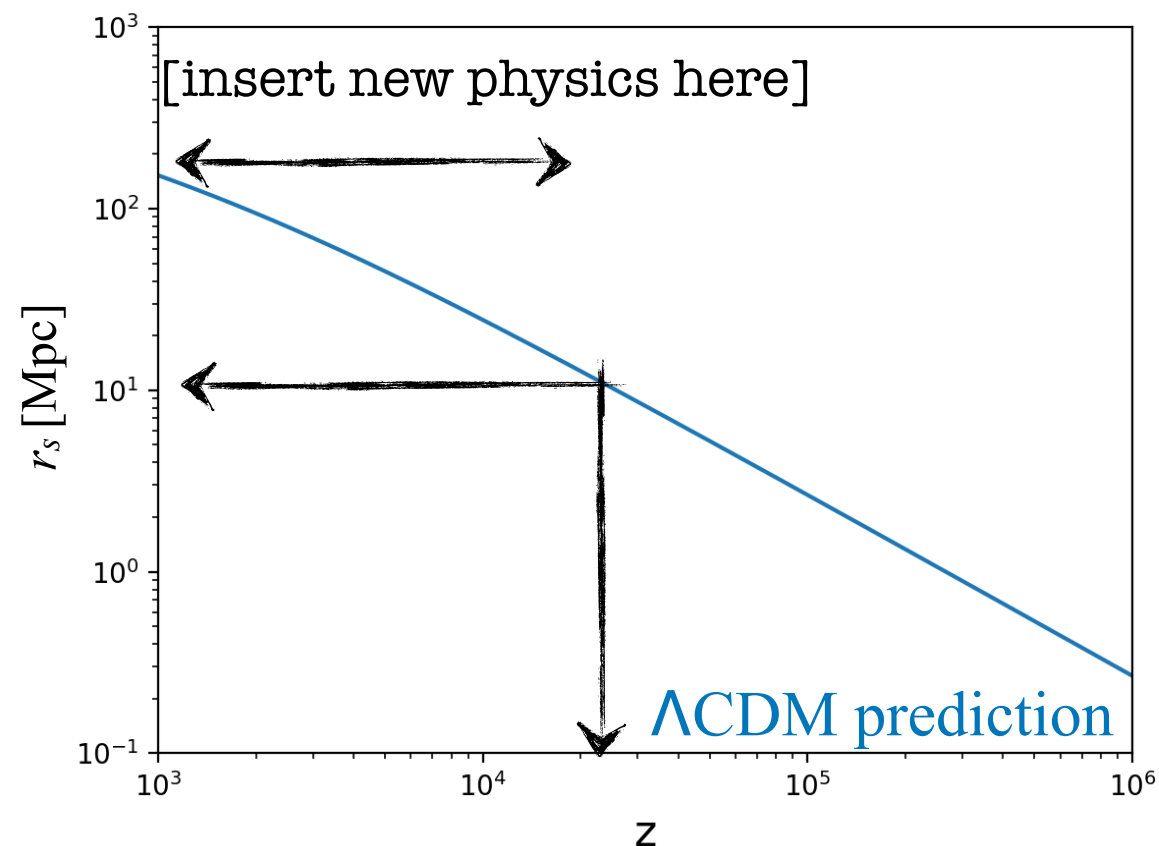
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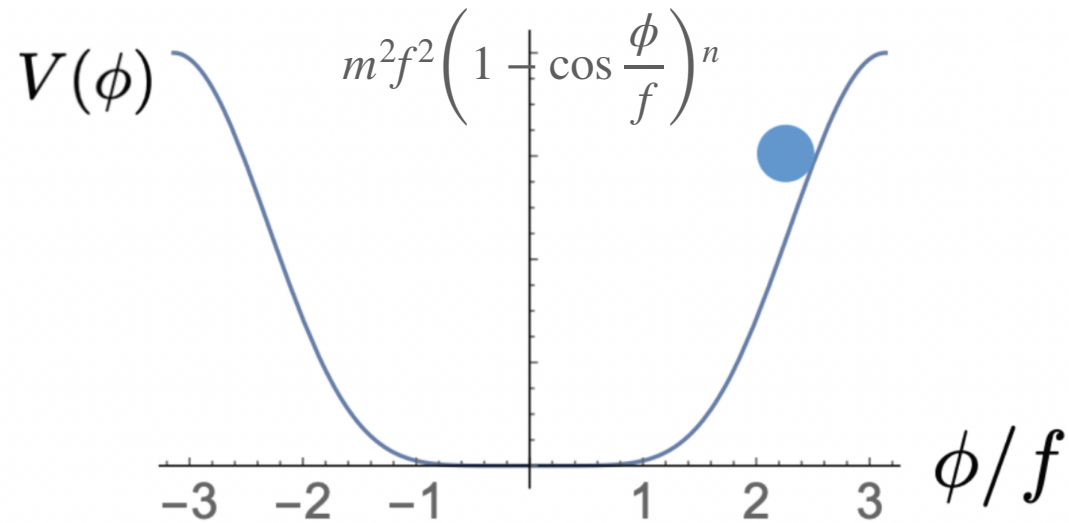
- Inject energy **between recombination and  $z \sim 2 \times 10^4$**  to reduce  $r_s$

*See the 'Hubble Hunter's guide' Knox&Millea 1908.03663*

# What is Early Dark Energy?

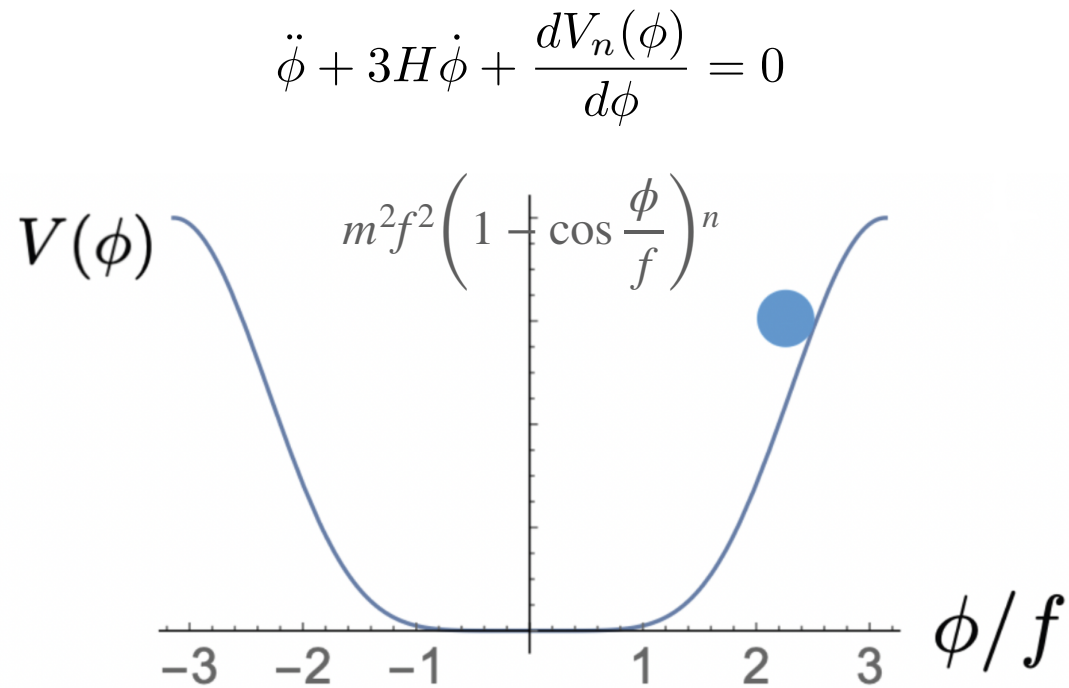
- Initially **slowly-rolling field** (due to Hubble friction) that later **dilutes faster than matter**

$$\ddot{\phi} + 3H\dot{\phi} + \frac{dV_n(\phi)}{d\phi} = 0$$

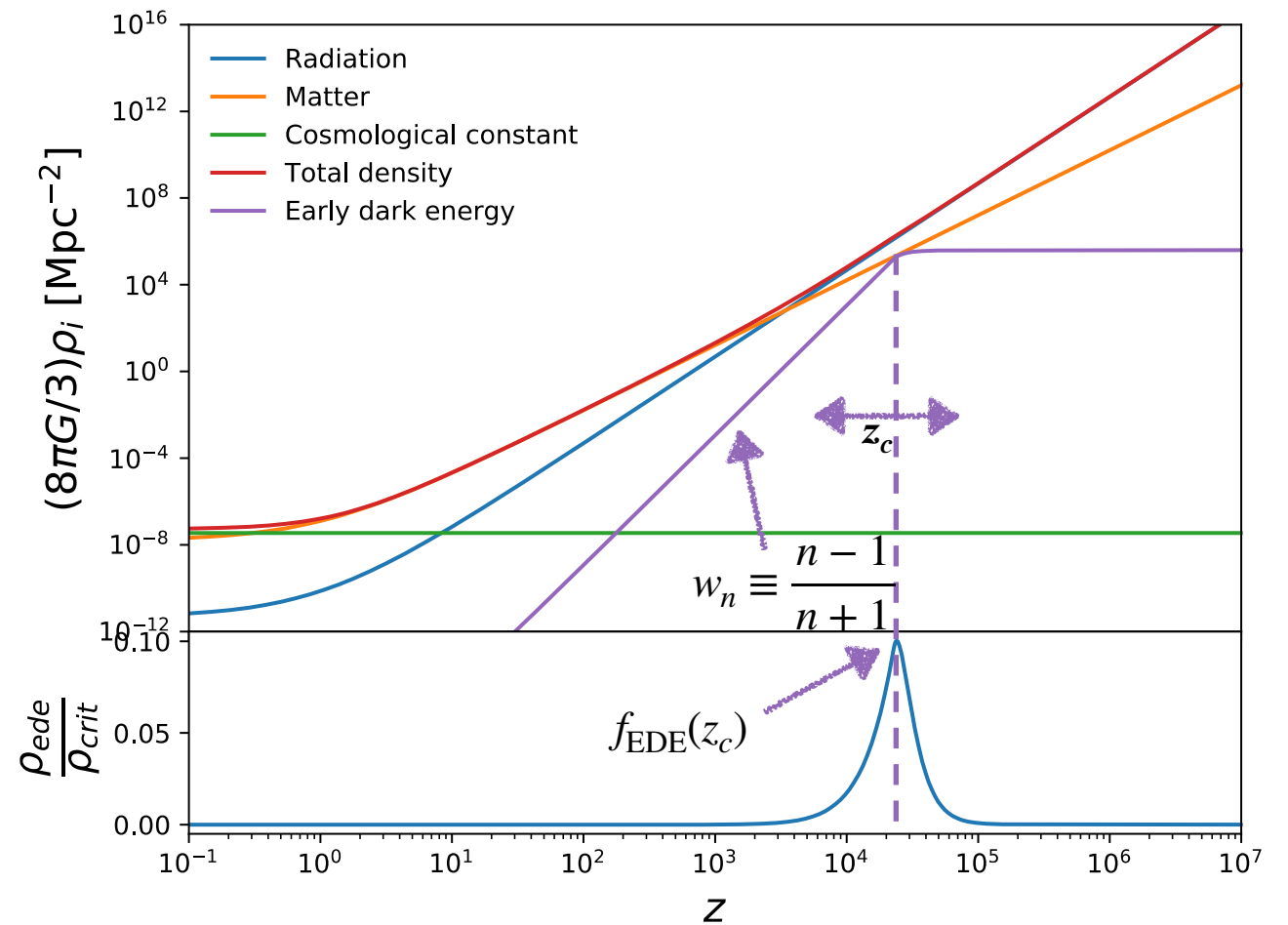


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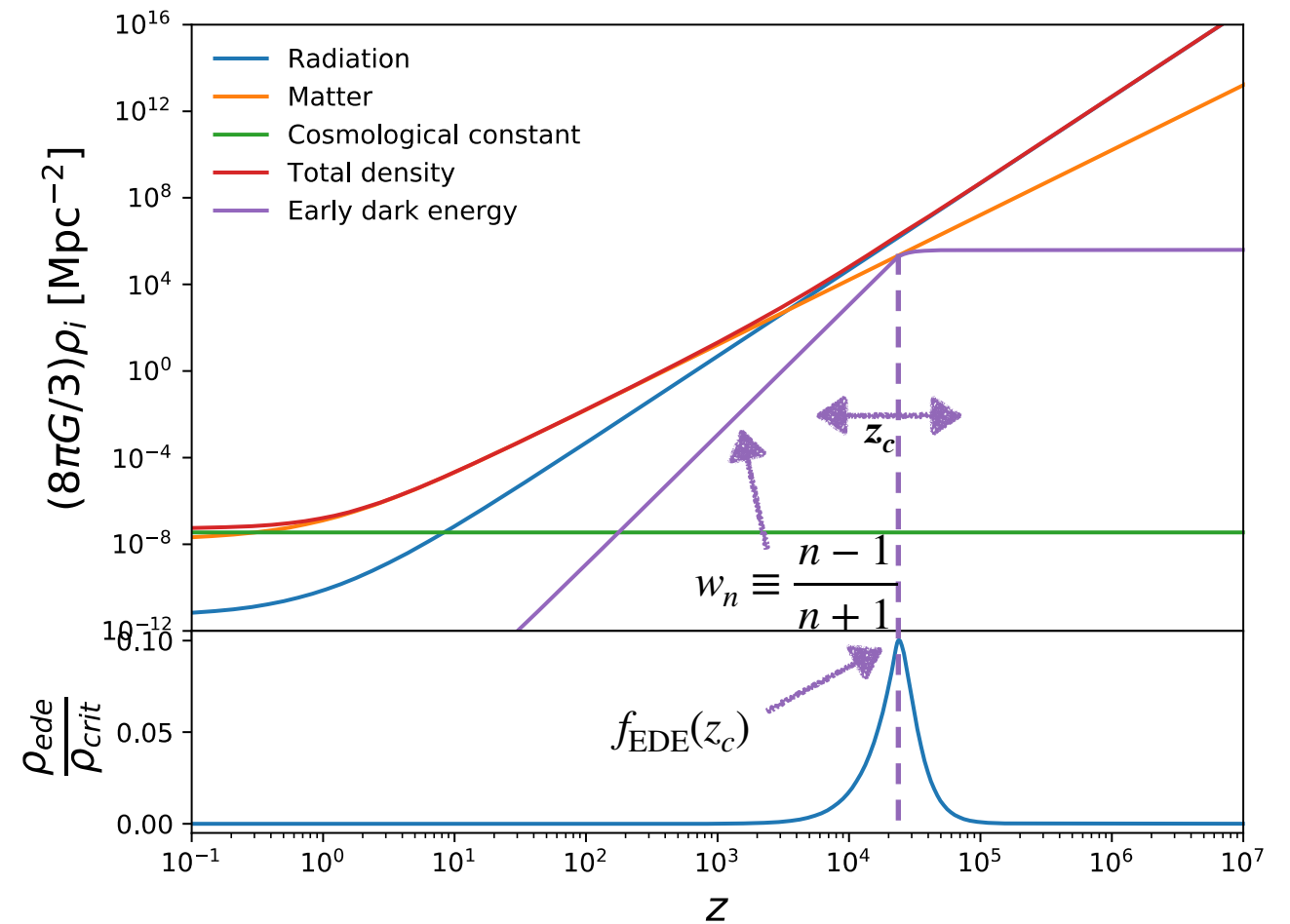
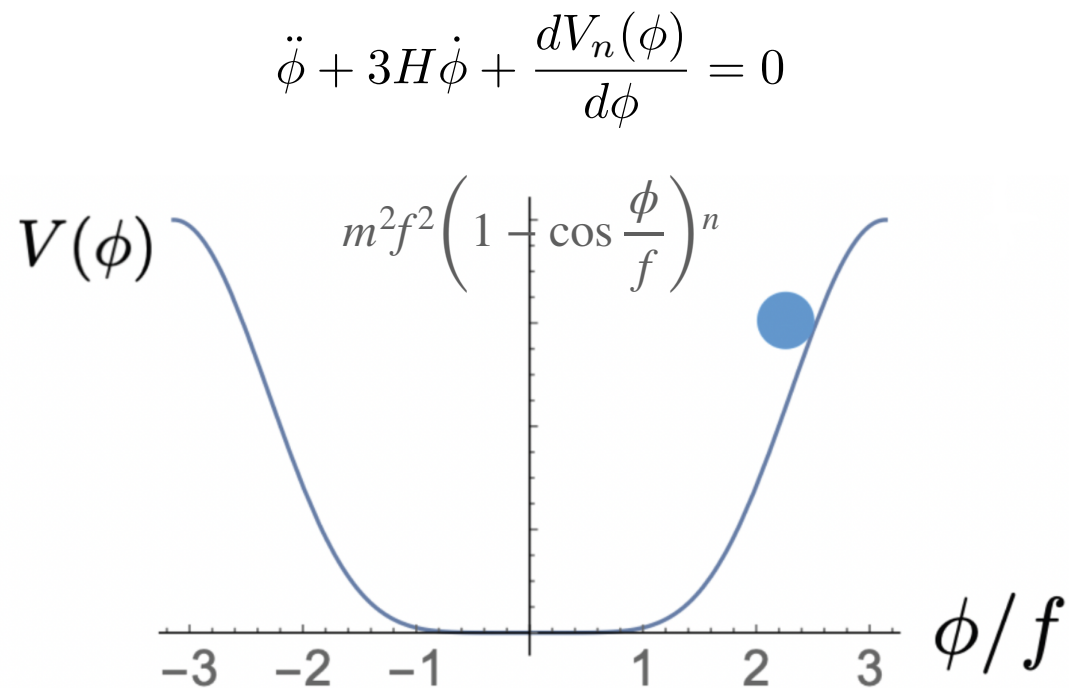


- Specified by  $f_{\text{EDE}}(z_c)$ ,  $z_c$ ,  $w(n)$ ,  $c_s^2(k, \tau)$   
 $n = 1$ : matter,  $n = 2$ : radiation, etc.

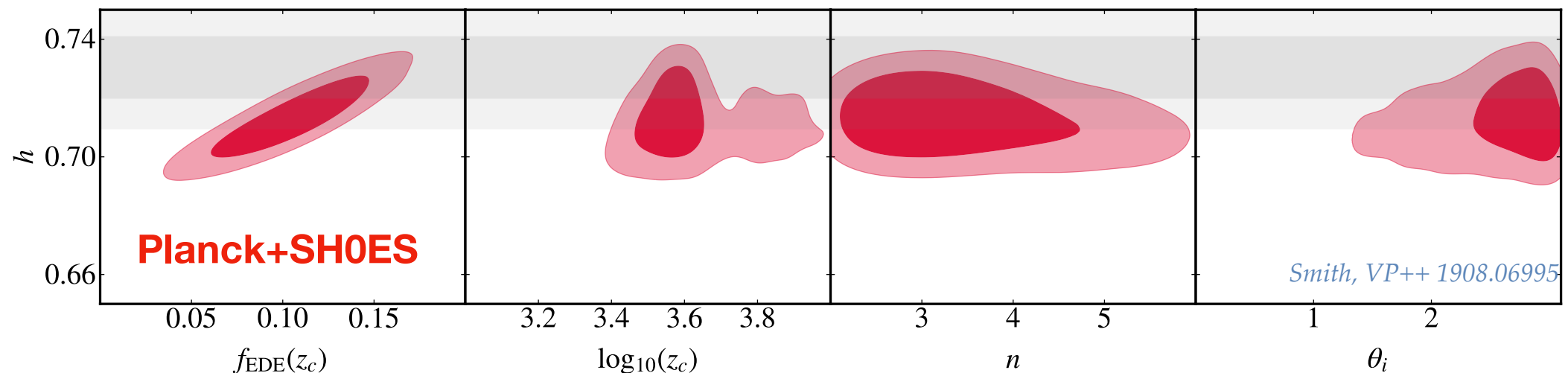


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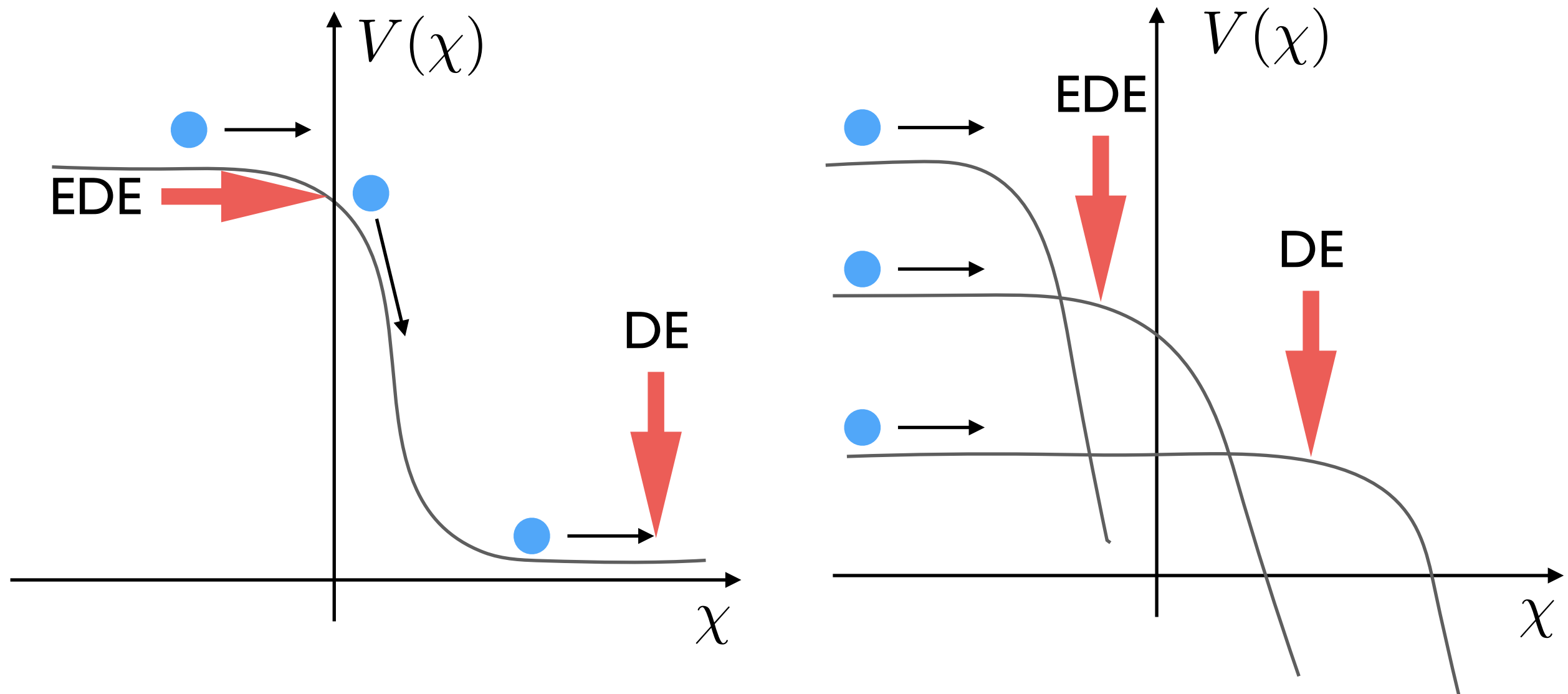


# A New Understanding Of Dark Energy?

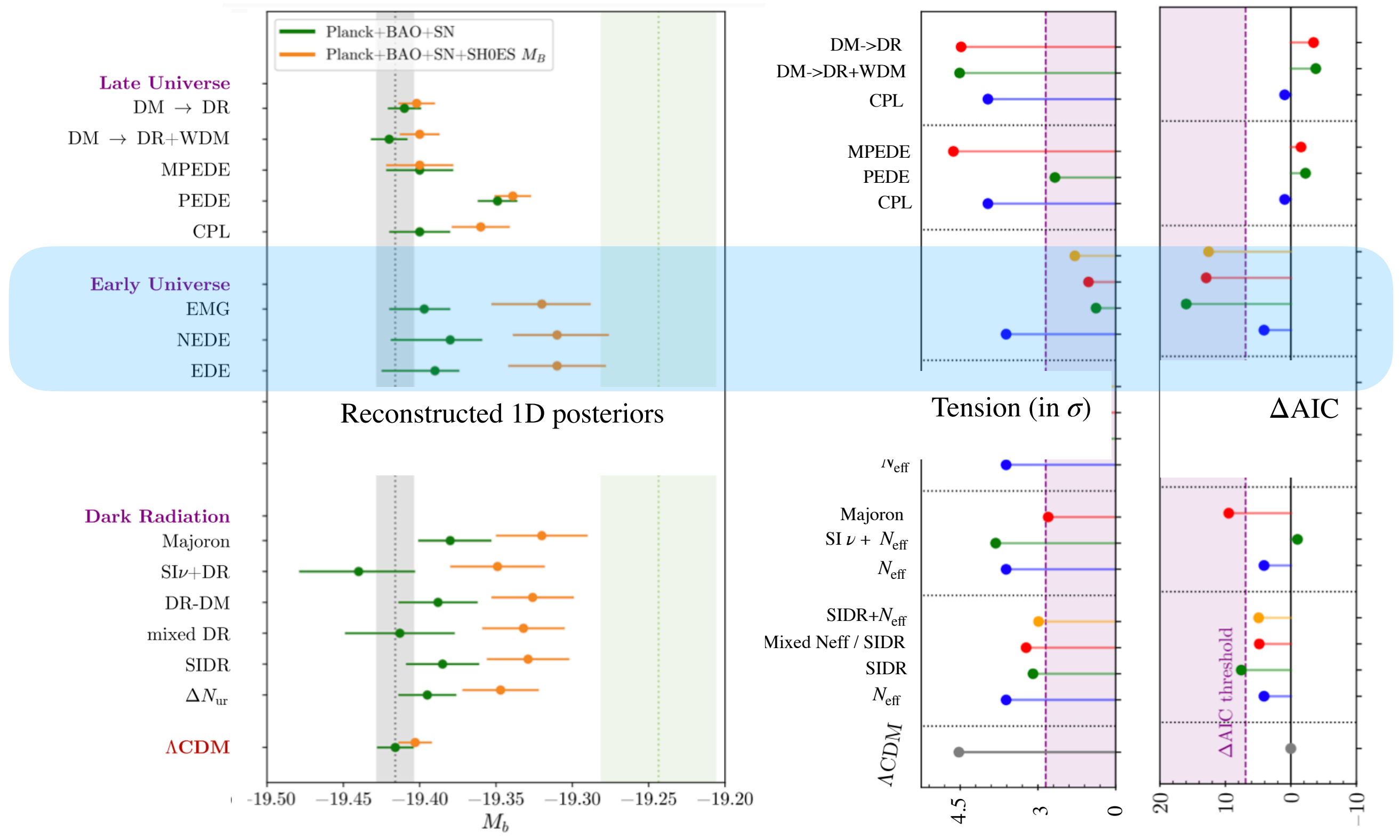
- The idea that **DE altered the early universe is not new**: explains the DE coincidence problem

*e.g. Dodelson++astro-ph/0002360, Griest astro-ph/0202052, Bielefeld (Caldwell)++ 1305.2209, Kamionkowski++1409.0549*

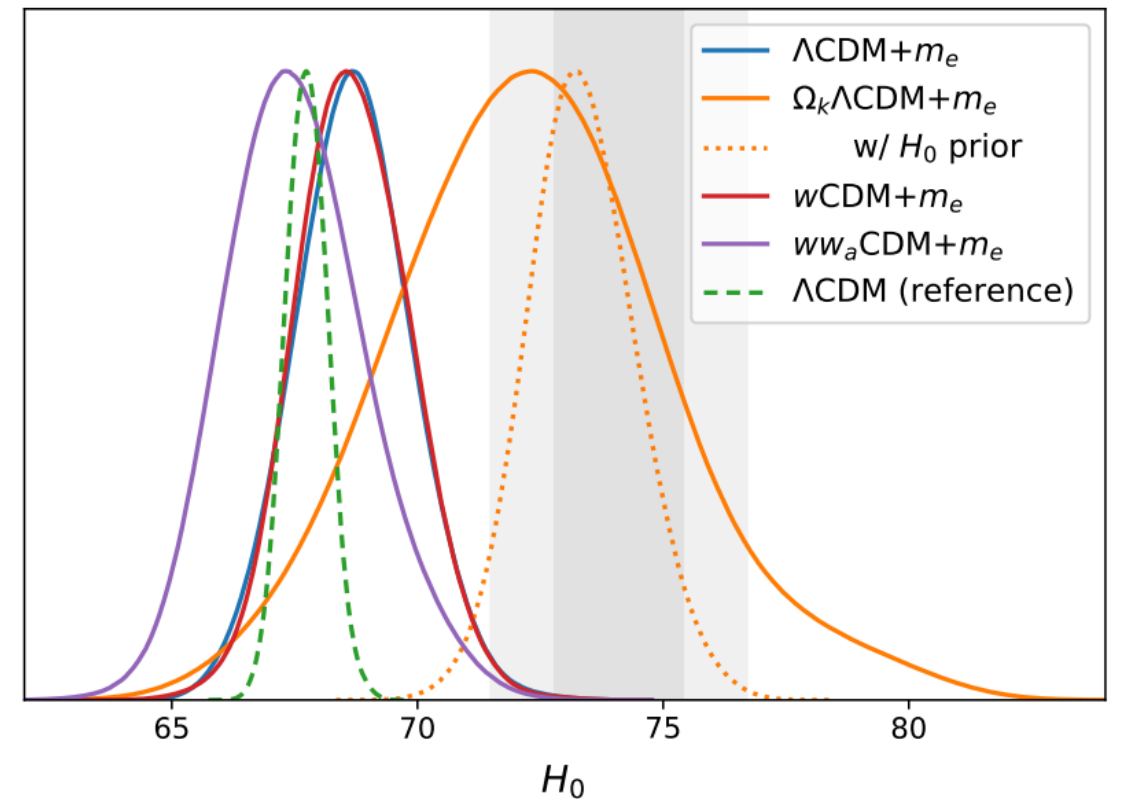
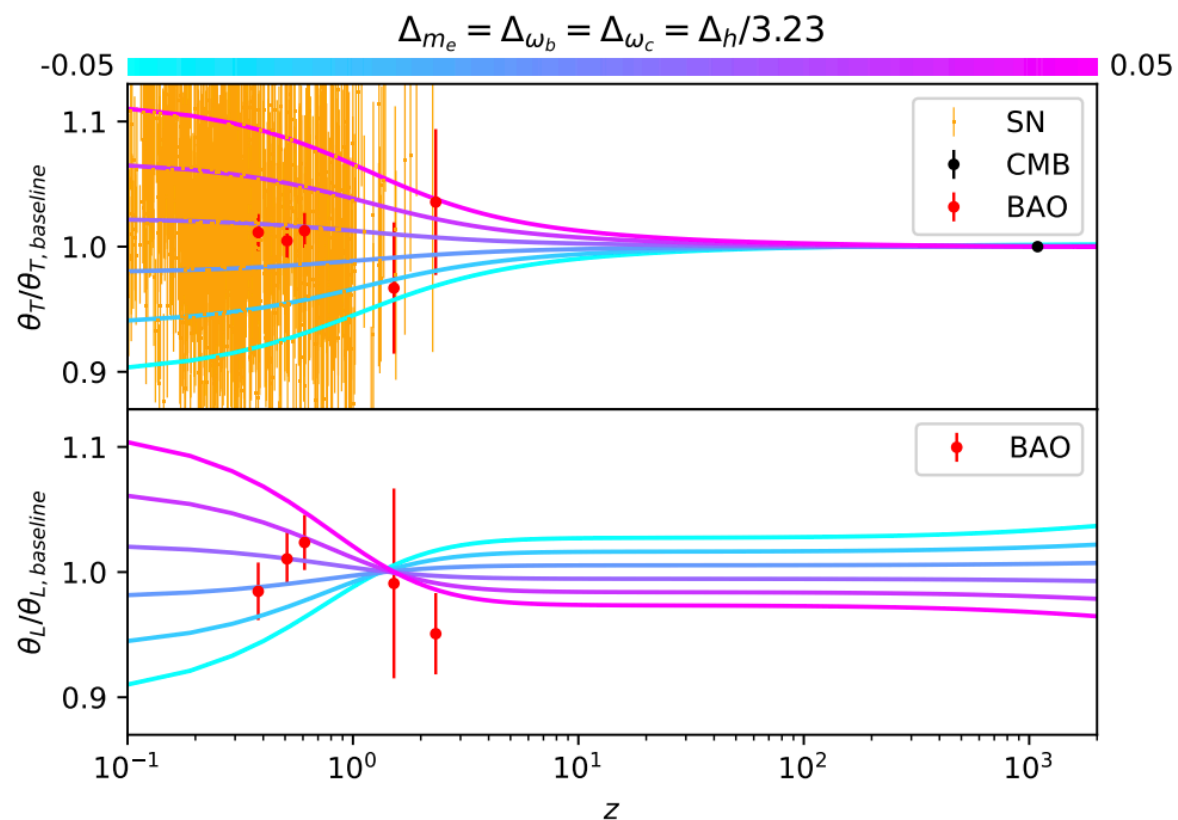
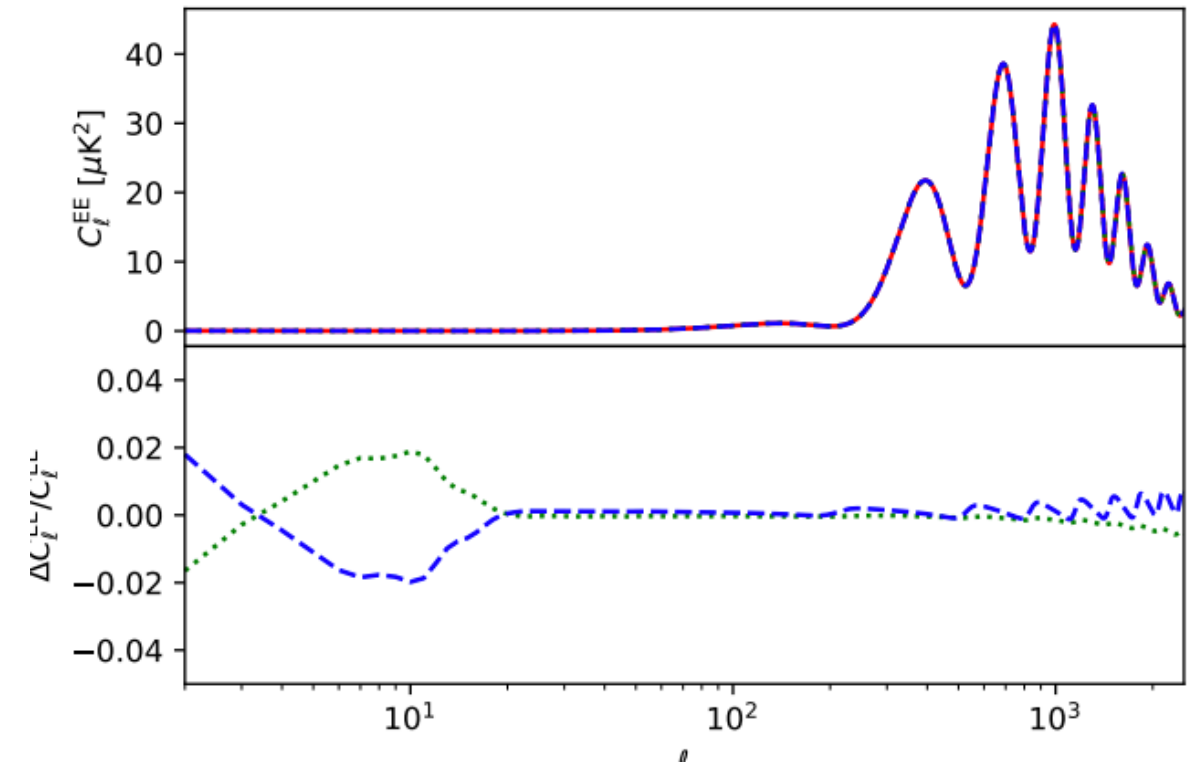
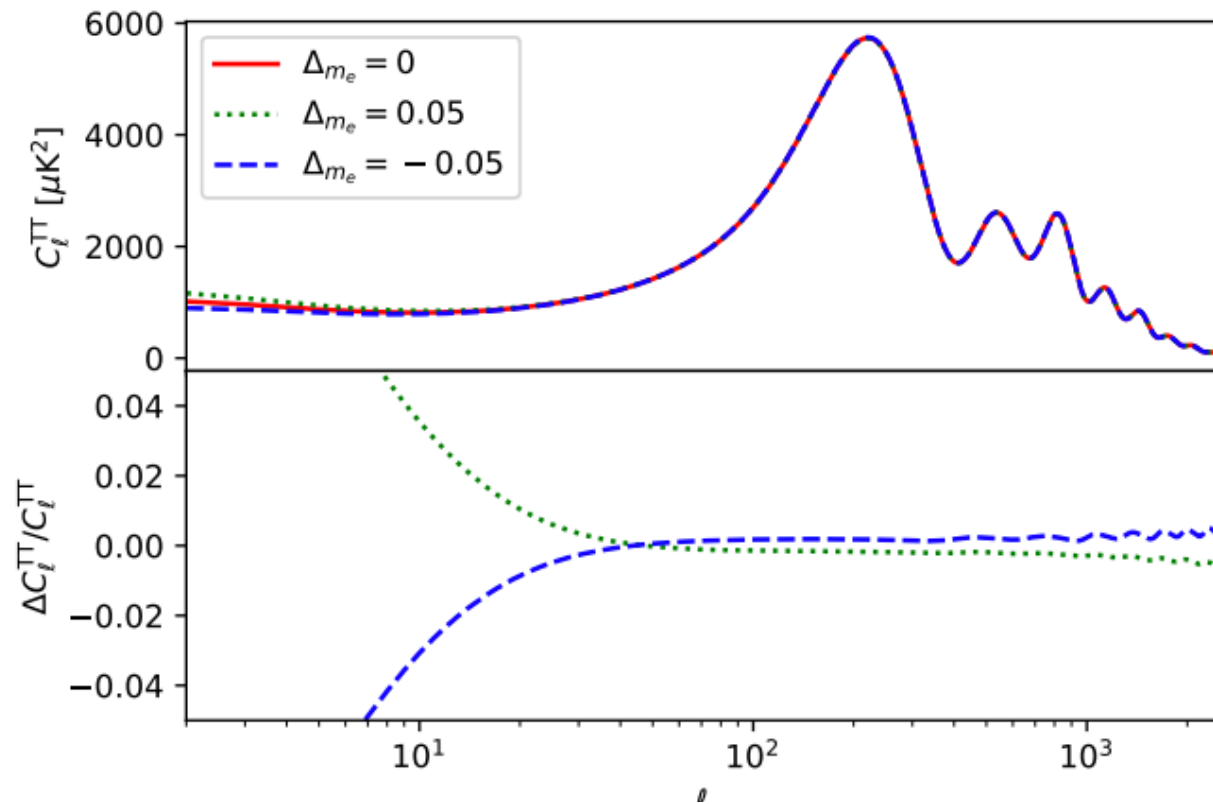
- Is there one field with a complicated potential or many fields with simple potentials?
- We know of Inflation, late-time Dark Energy: **could there be more of such era to be discovered?**



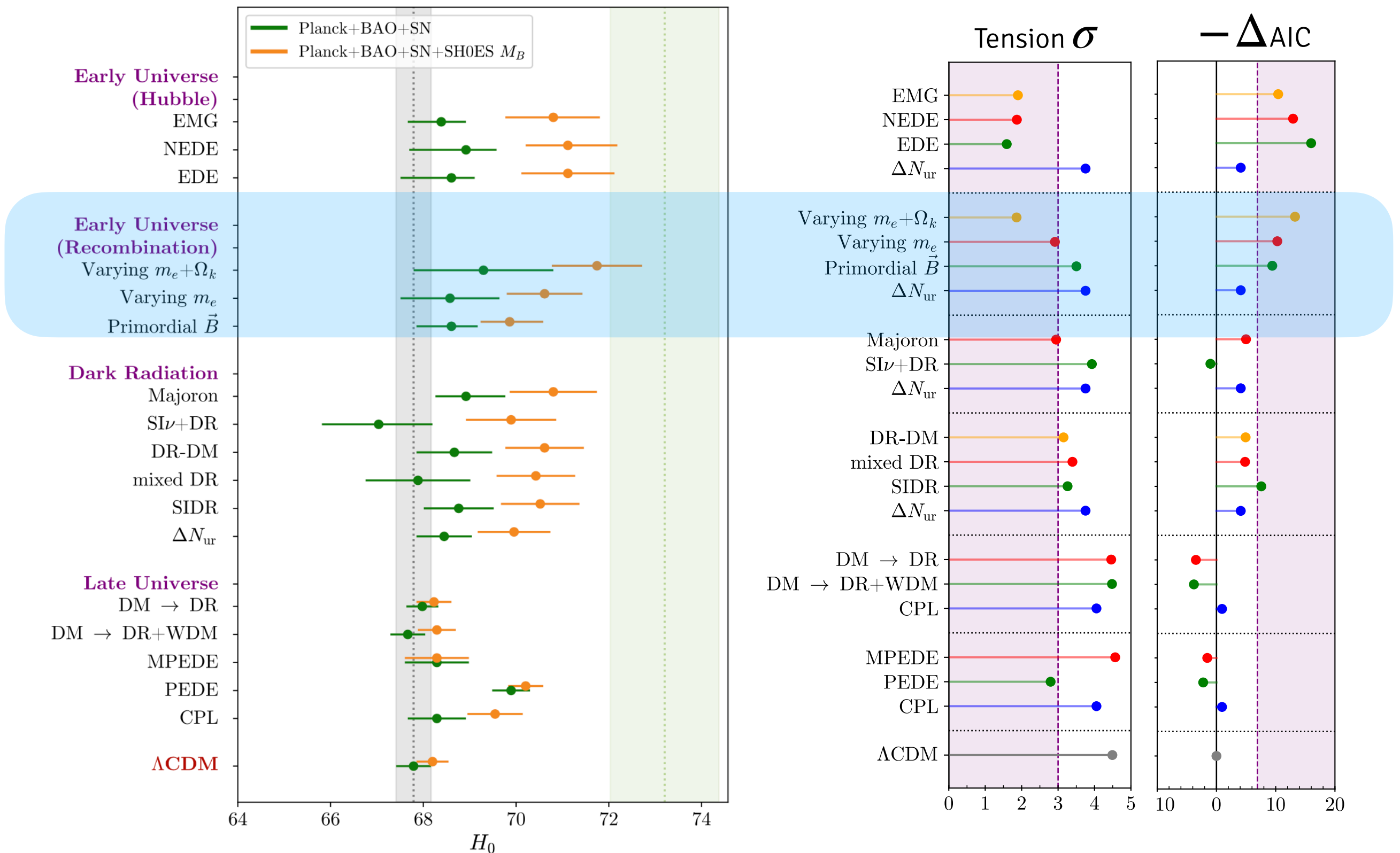
# Status of “Exotic Energy Injection” solutions



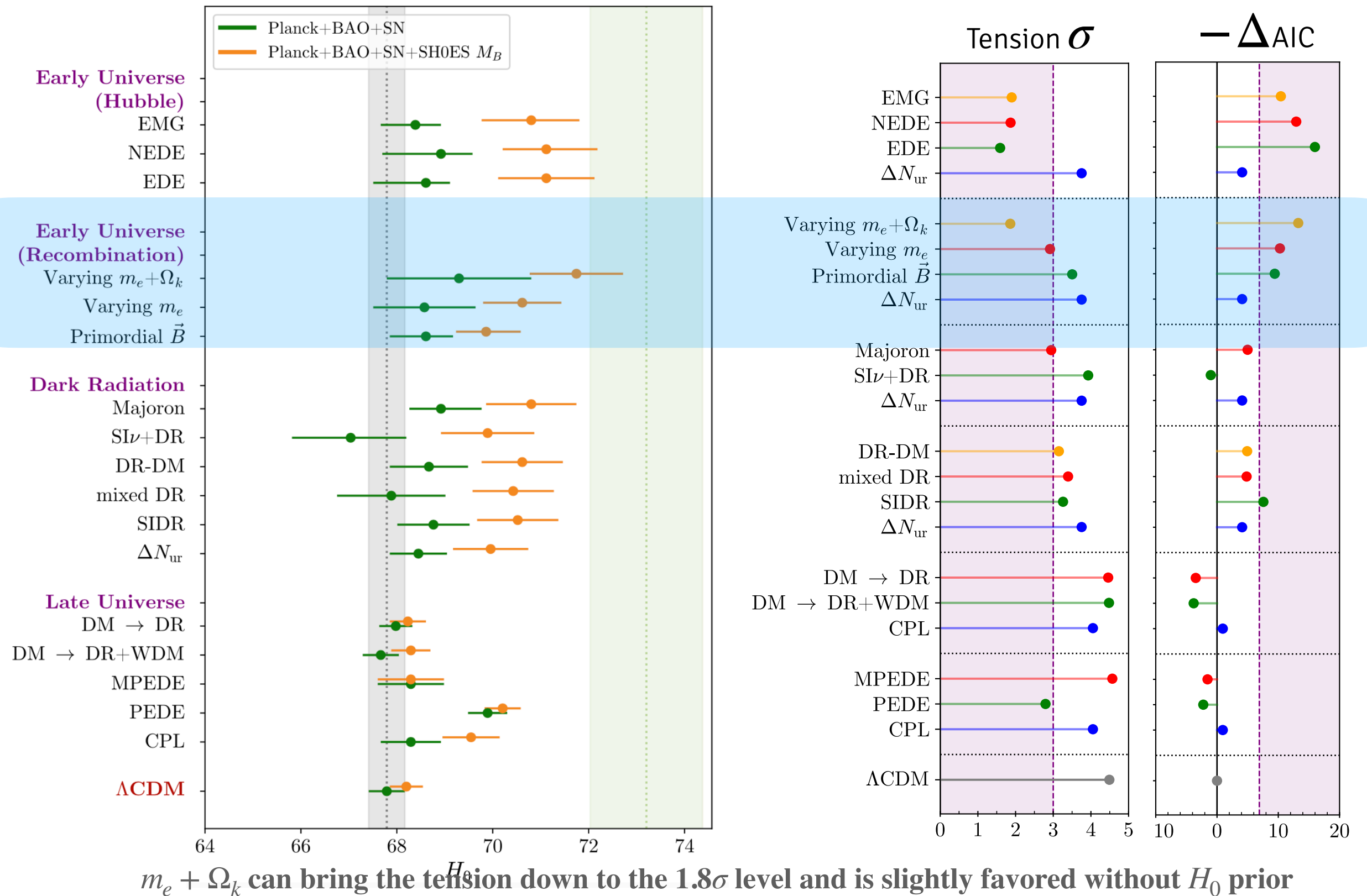
# A higher $m_e$ could resolve the $H_0$ tension



# Status of “modified recombination” solutions

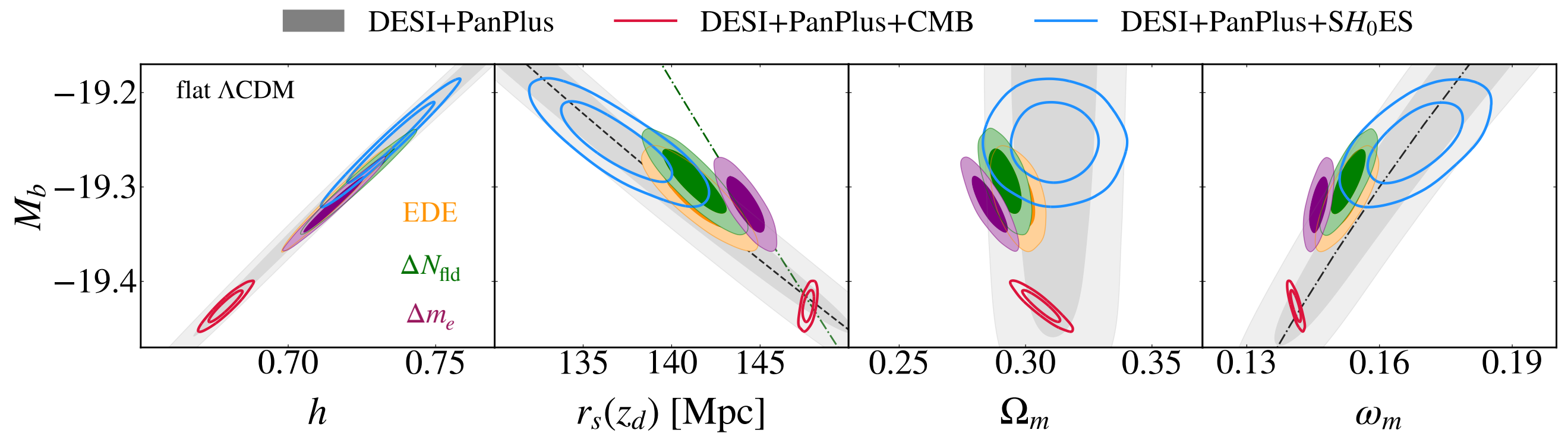


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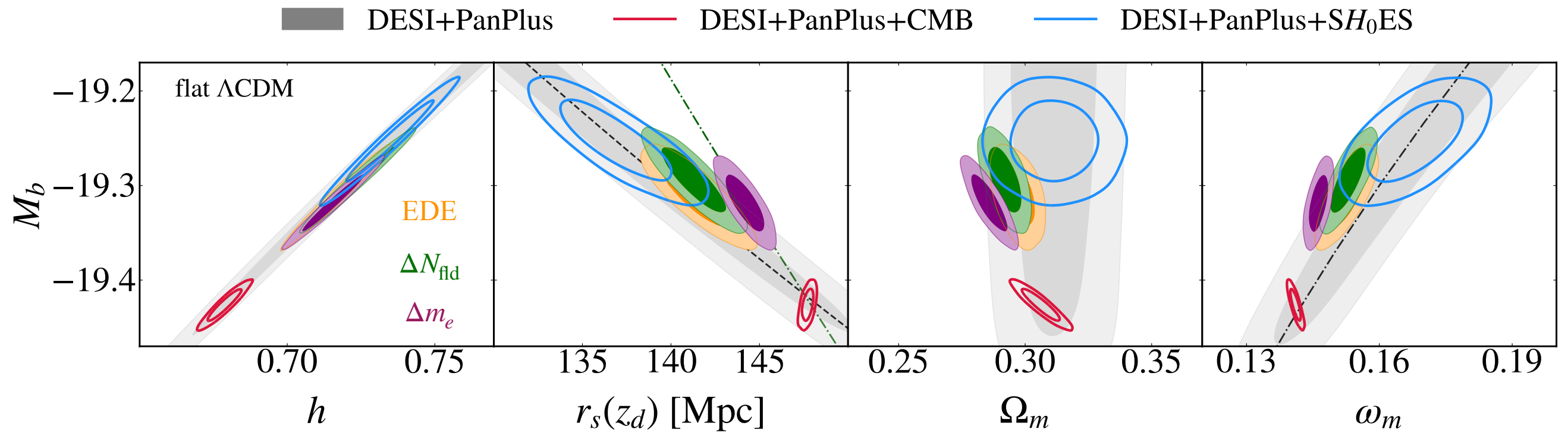




# Can models respect degeneracies imposed by the distance ladder?

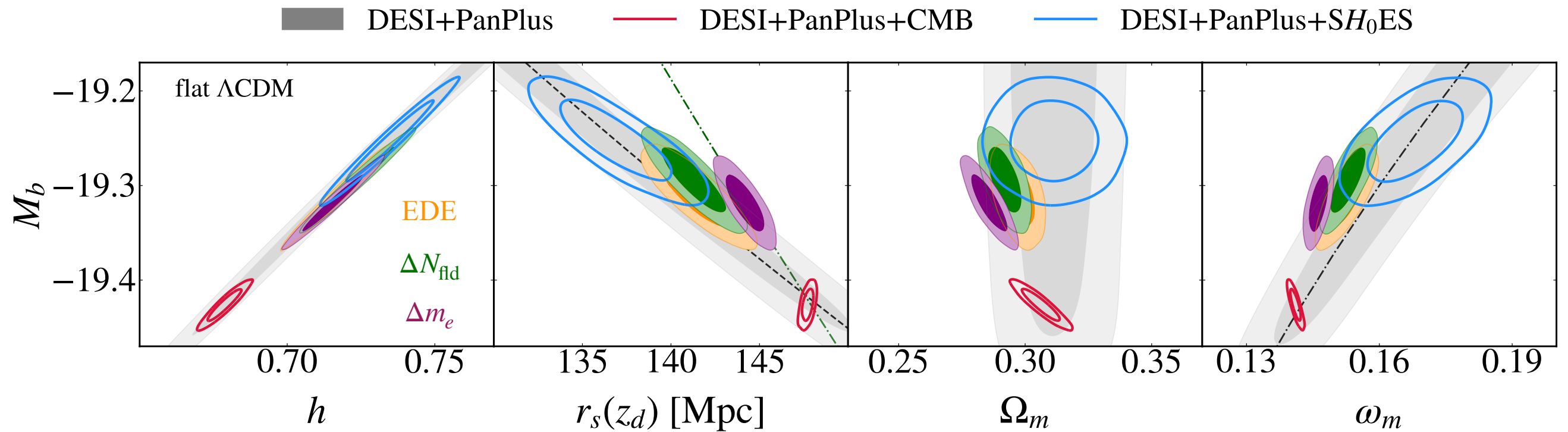


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- Models affecting expansion history can reduce tension to  $\sim 2 - 3\sigma$  level

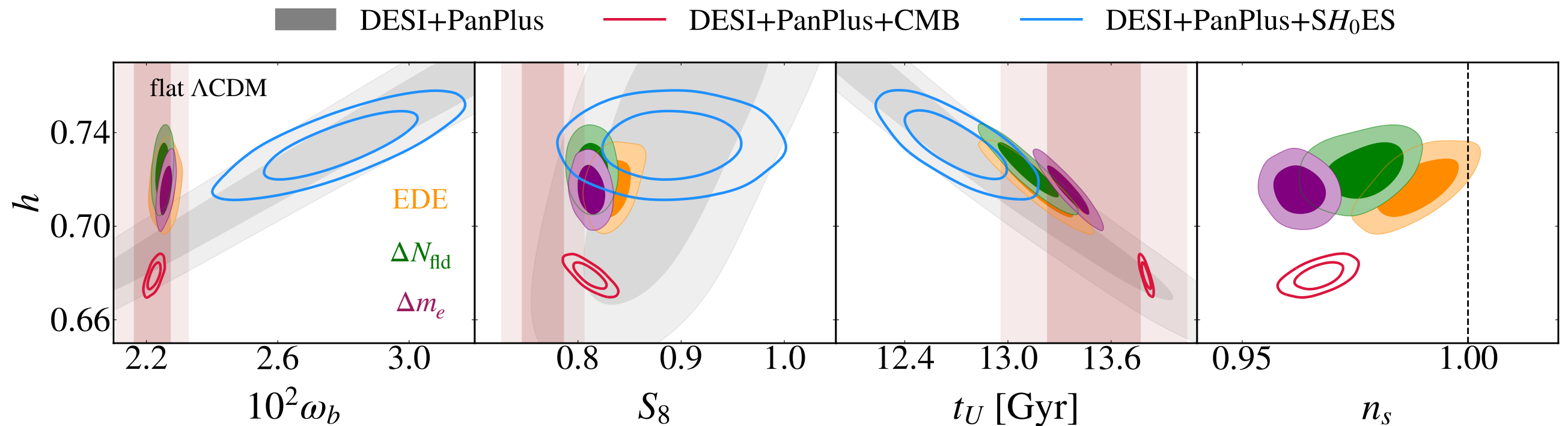
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- Models affecting solely the way recombination proceeds are disfavored: they lead to a low  $\Omega_m$

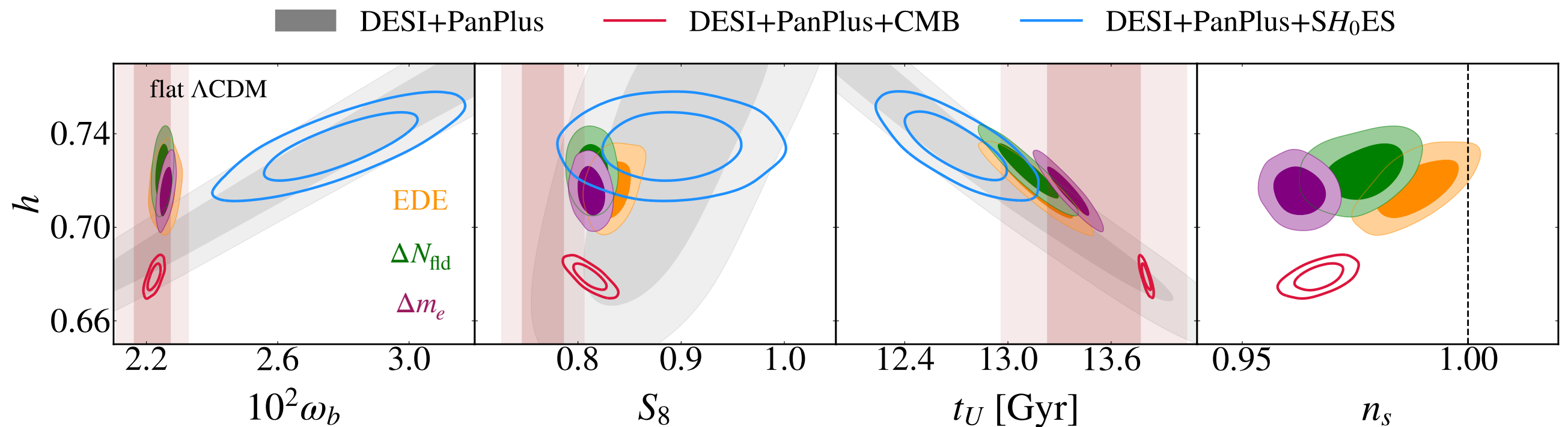
*Lee (VP)++ PRL 2022, Lynch++ 2404.05715*

# Can models resolve the other tensions?



- No more tension with BBN but **tension with weak lensing measurements at the  $3 - 3.5\sigma$  level**
- Age of the universe  **$\sim 0.7$  Gyr younger**: problem with old objects? JWST?

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- $n_s$  is degenerate with the **angular damping scale**  $\frac{\delta\theta_D}{\theta_D} \simeq 0.2 \frac{\delta n_s}{n_s}$ . *Smith&VP, 2309.03265*
- $\theta_D \sim \sqrt{H_0}$  while  $\theta_s \propto H_0$ :  **$n_s$  must increase** to compensate a higher  $H_0$ .



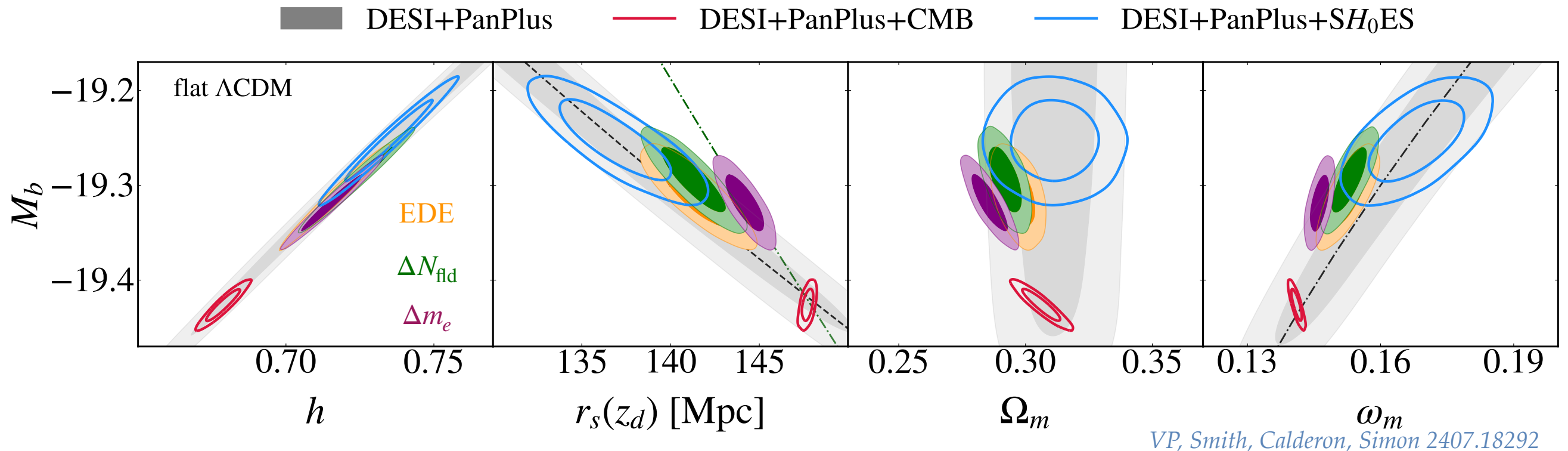
# Synergy between early and late-time?

- Constraints to  $\Omega_m$  are an important part of the problem: **how to relax them?**

- Hints of **dynamical dark energy**: could it **play a role** in the tensions?

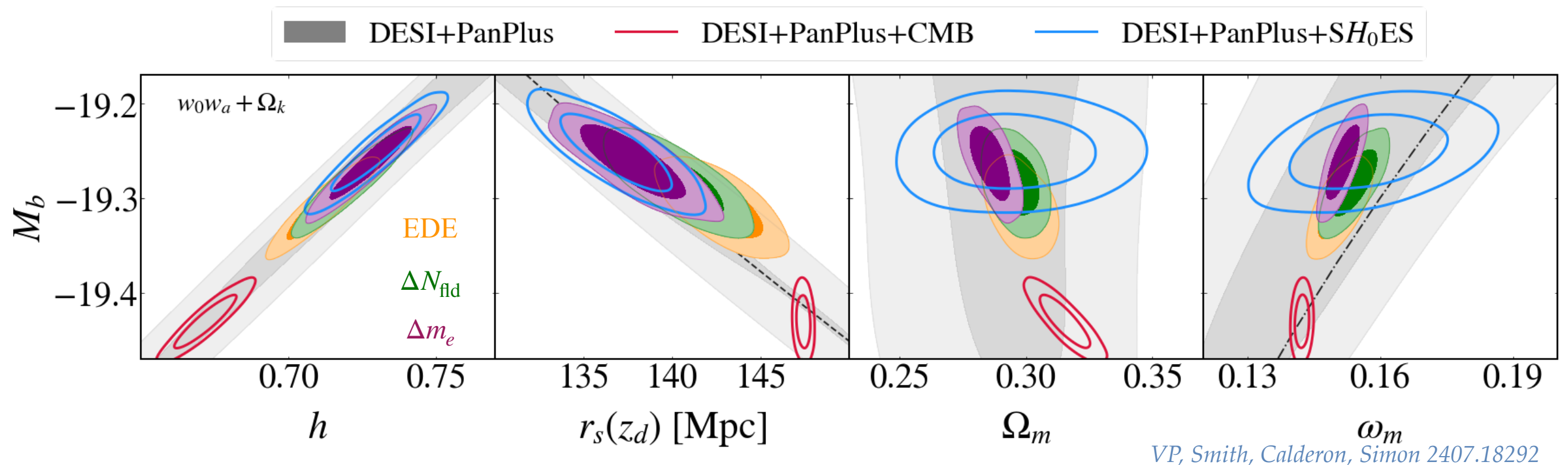
*DESI 2404.03002, Cortés&Liddle 2404.08056, Shlivko&Steinhardt 2405.03933, Berghaus++ 2404.14341, Efstathiou 2408.07175*

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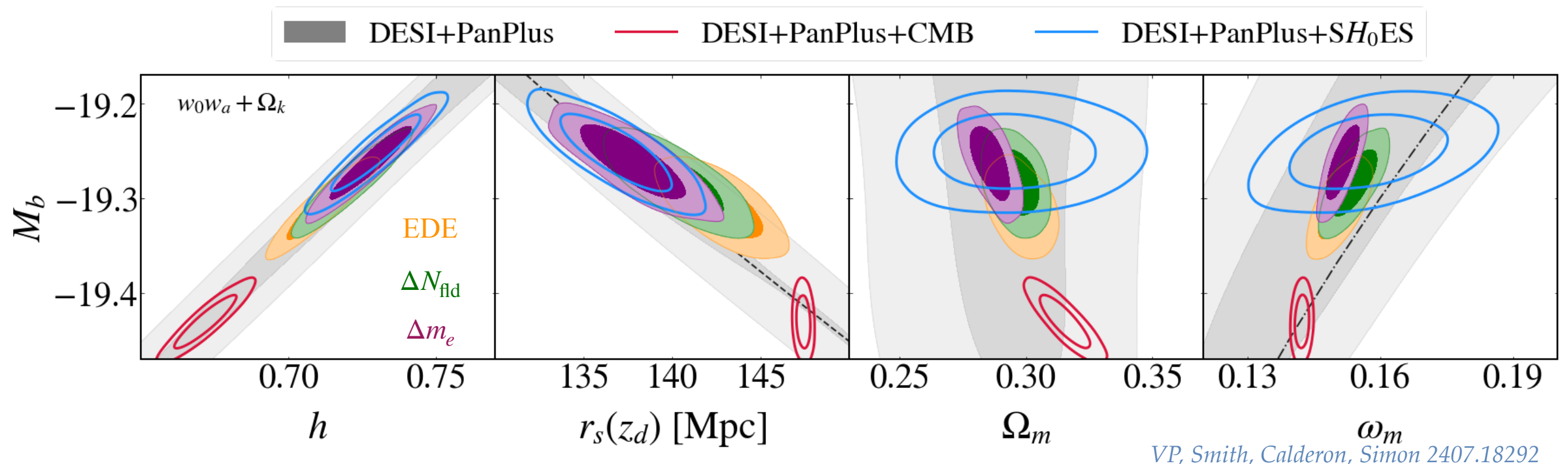
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*Sekiguchi++2007.03381*

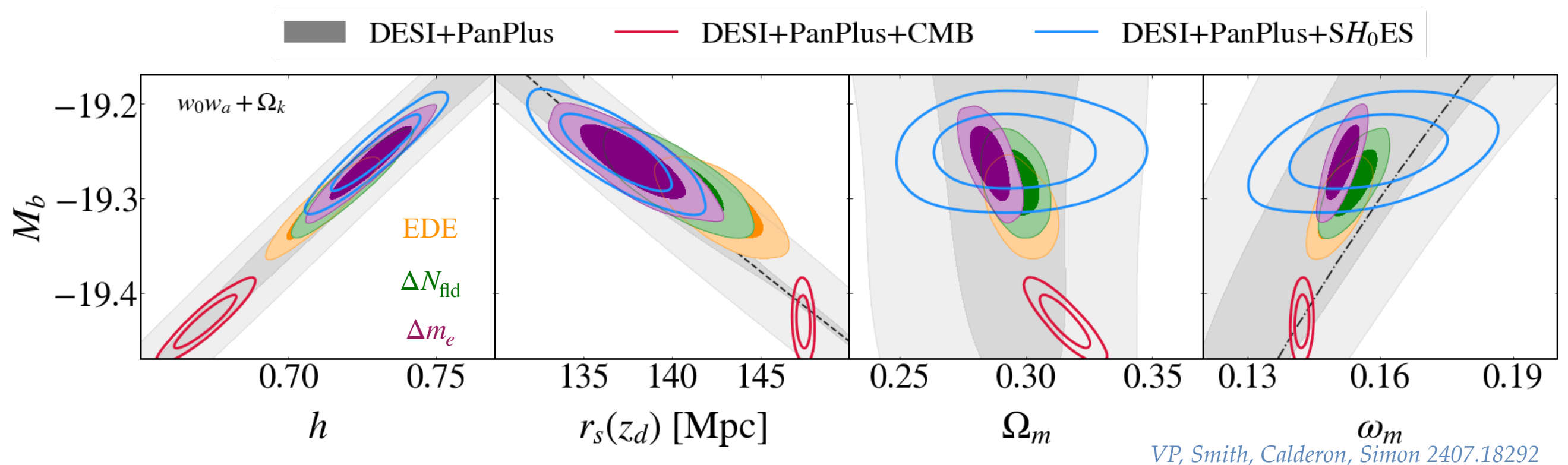
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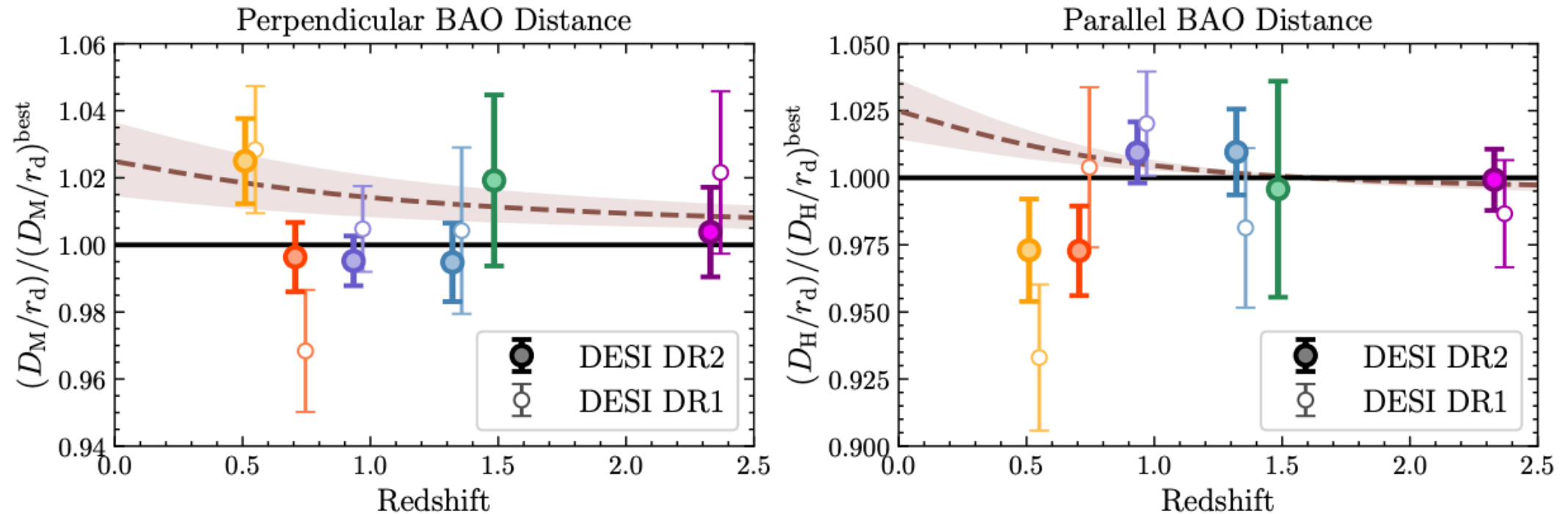
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*Sekiguchi++2007.03381*

- Localized energy injection boosting  $H(z)$  or a broad change affecting several cosmic epochs?

# DESI BAO measurements: hint of new physics?

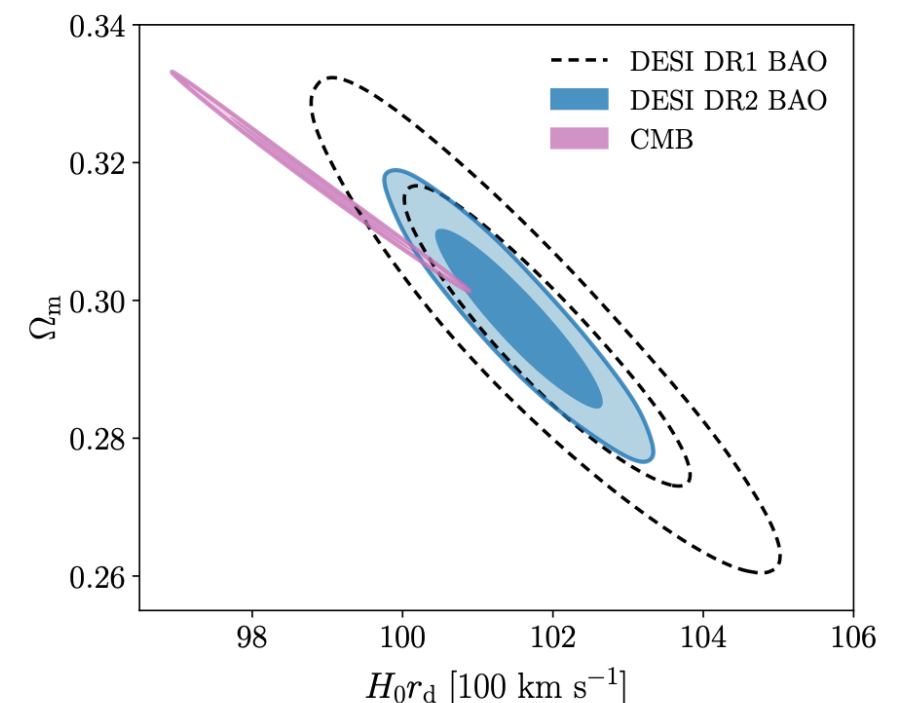
- Under  $\Lambda$ CDM, **2.3 $\sigma$  tension** between CMB and BAO data



- Under  $\Lambda$ CDM, the BAO allows to measure  $\Omega_m$  and  $H_0 r_d$ .

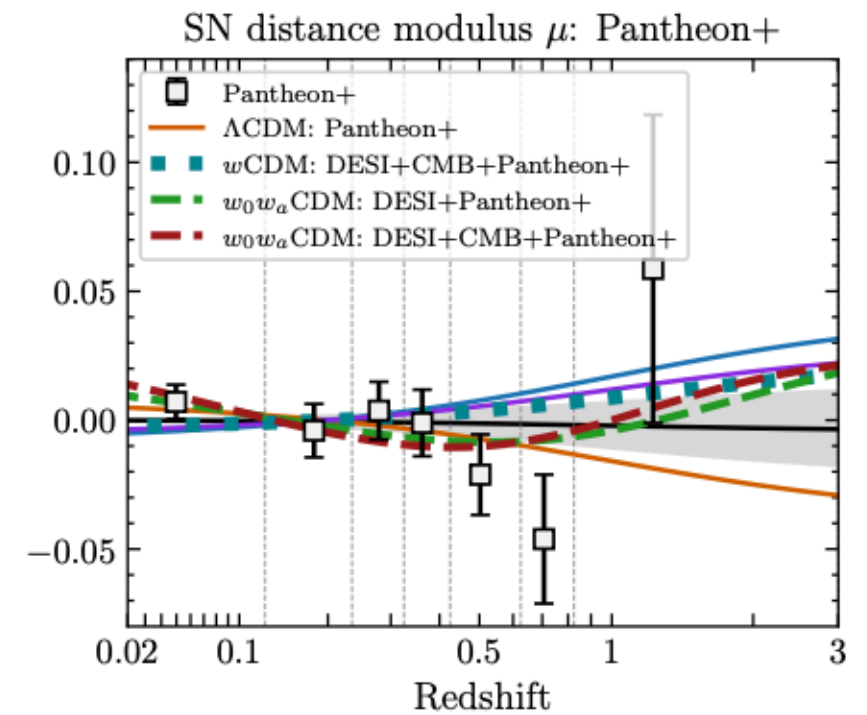
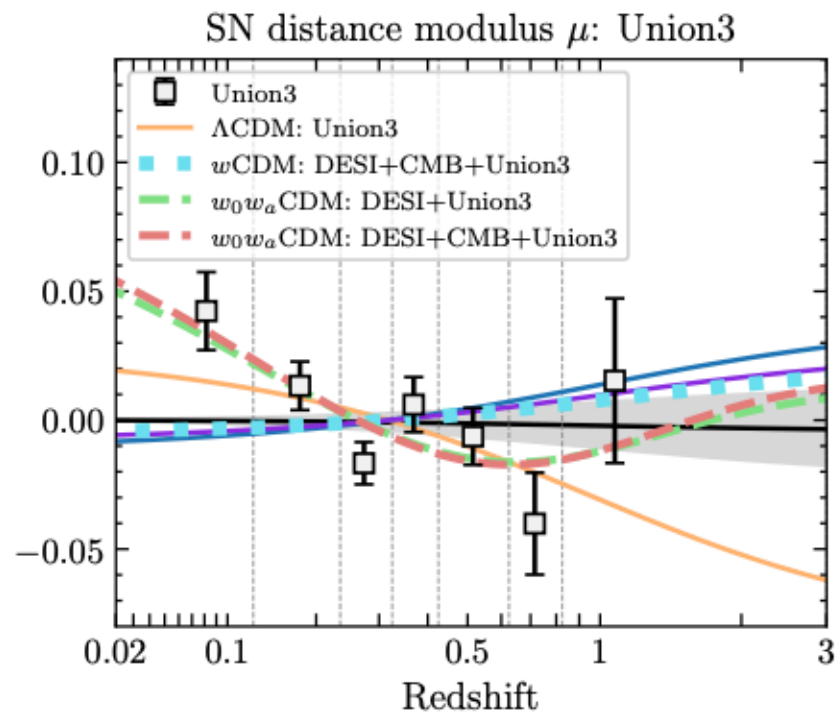
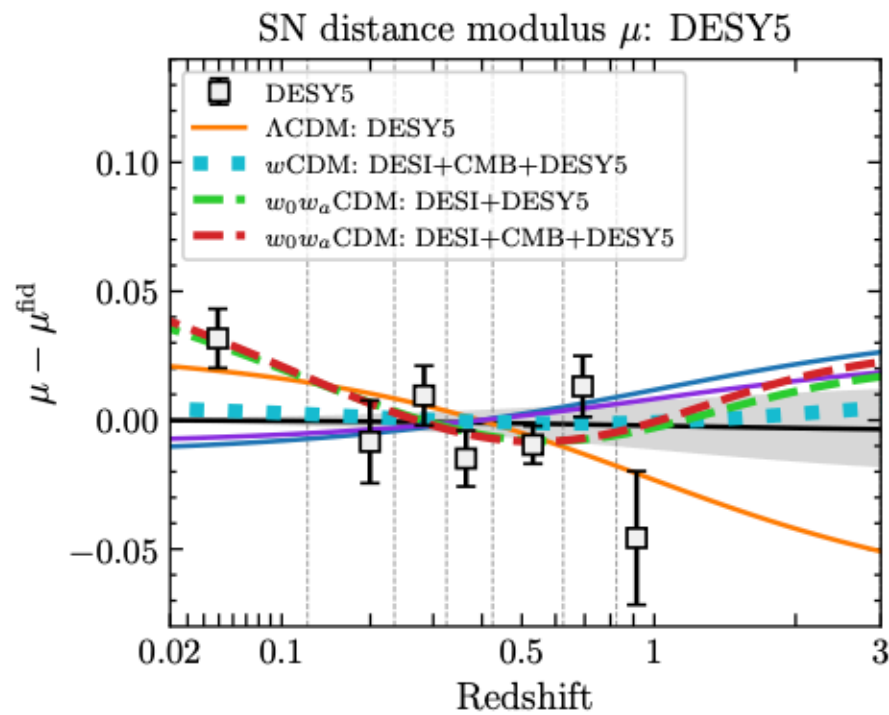
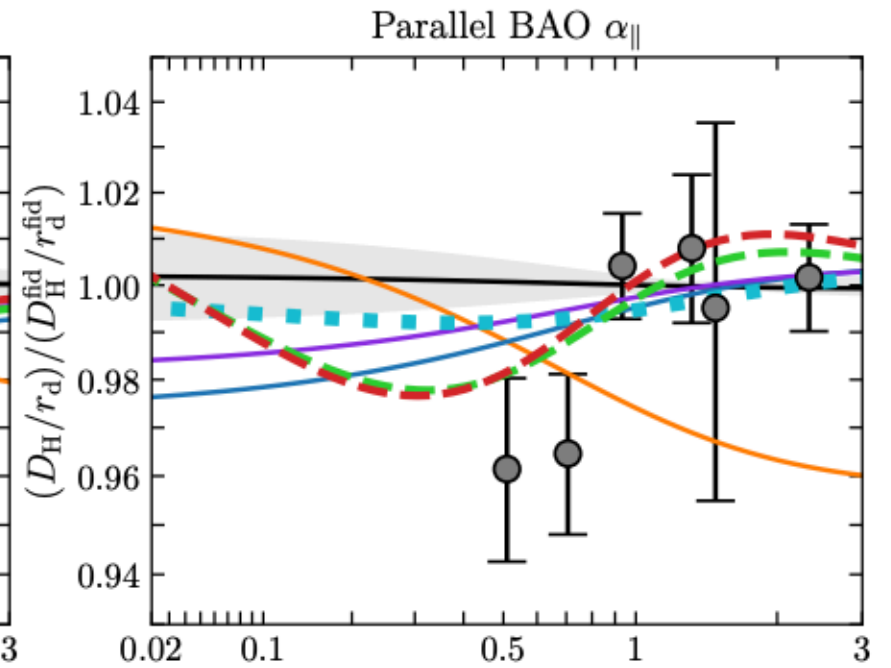
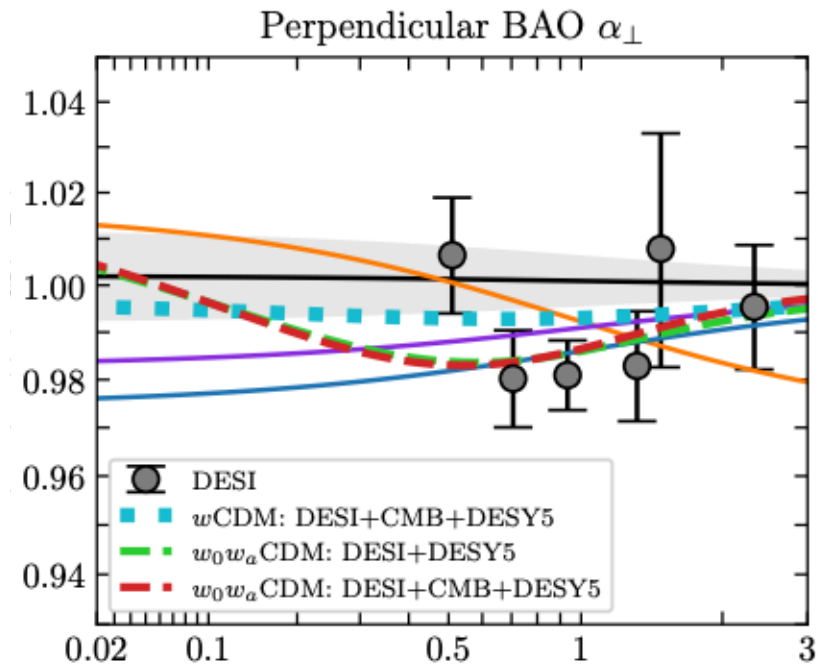
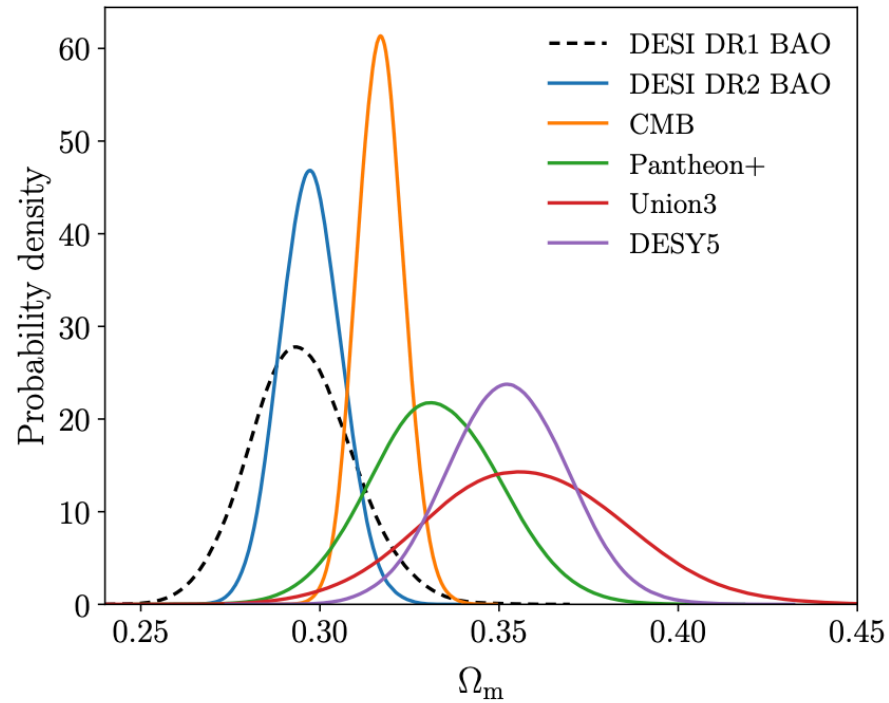
$$\frac{r_d}{D_M} \equiv \frac{H_0 r_s(z_d)}{\int_0^z dz (\Omega_m [(1+z)^3 - 1] + 1)^{-1/2}}$$

$$\frac{r_d}{D_H} \equiv H_0 r_s(z_d) \sqrt{\Omega_m [(1+z)^3 - 1] + 1}$$

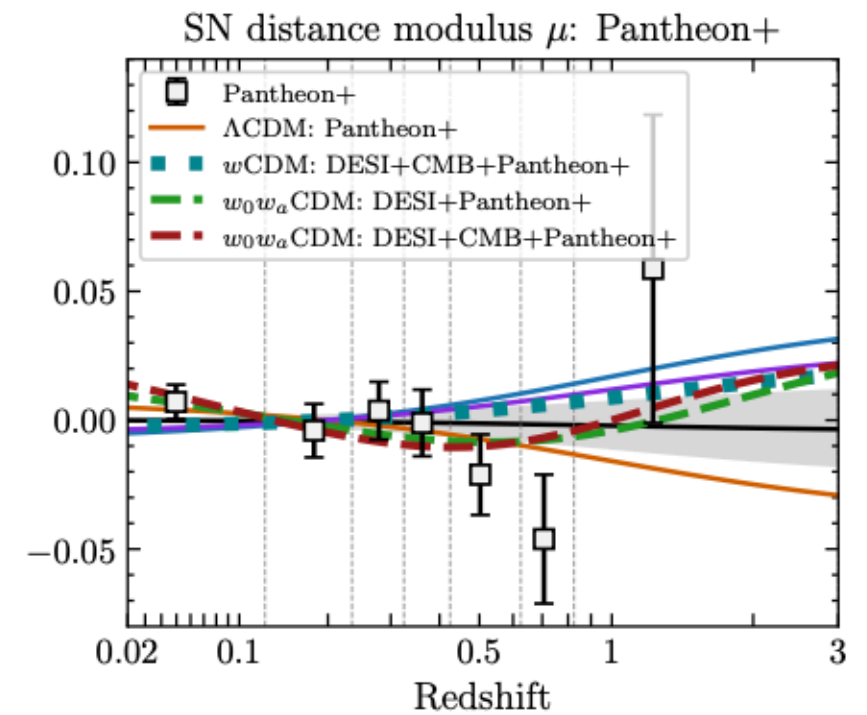
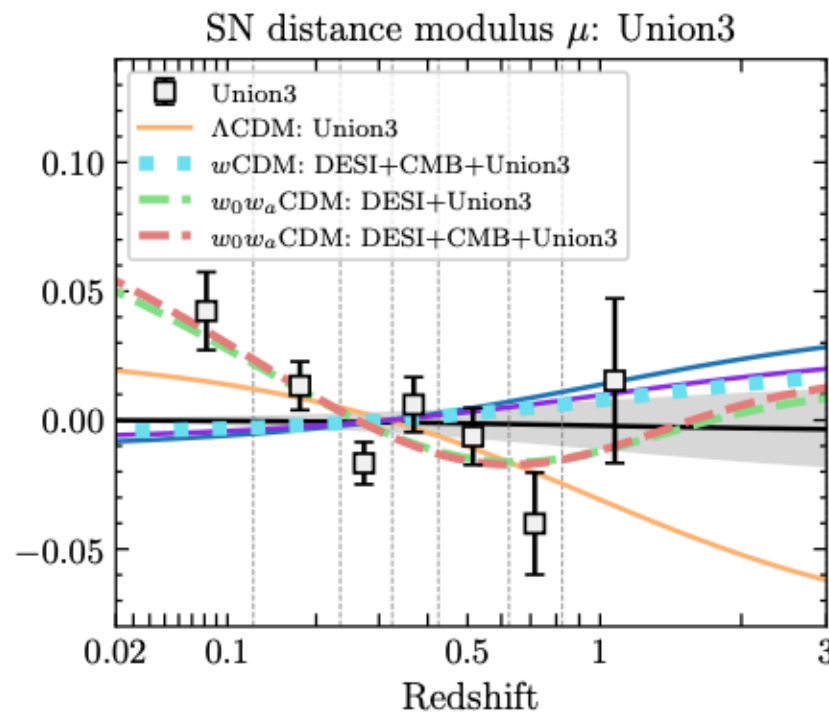
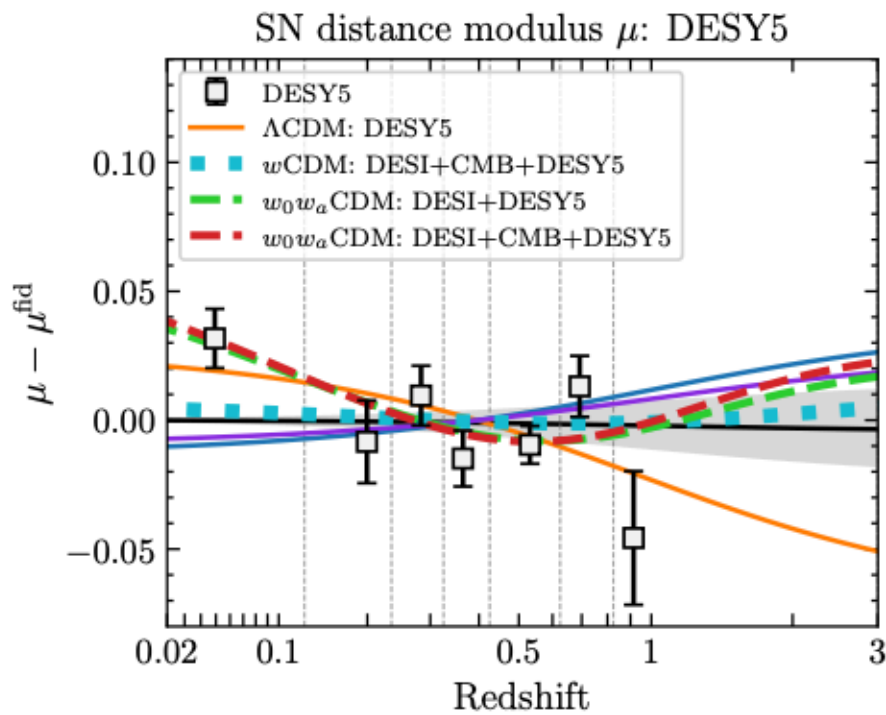
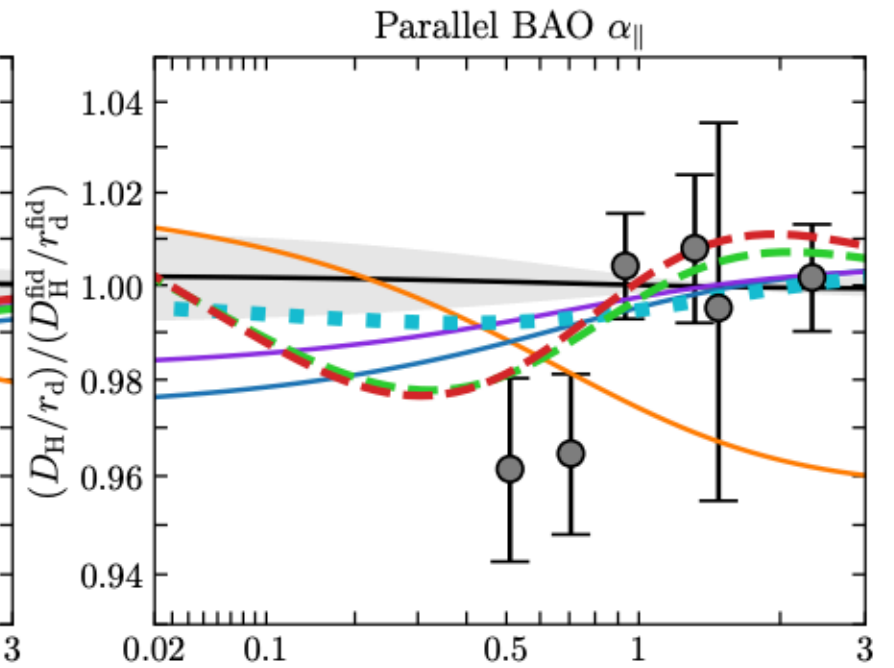
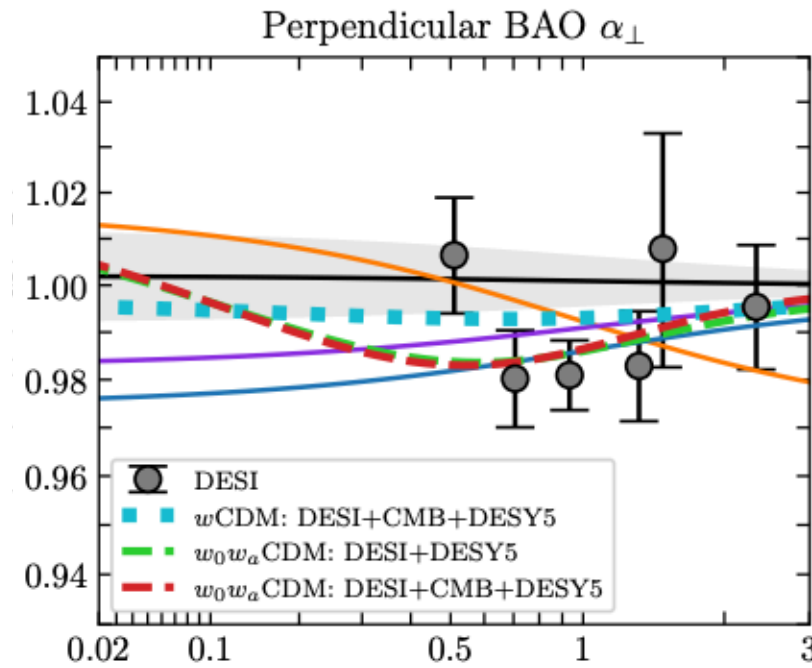
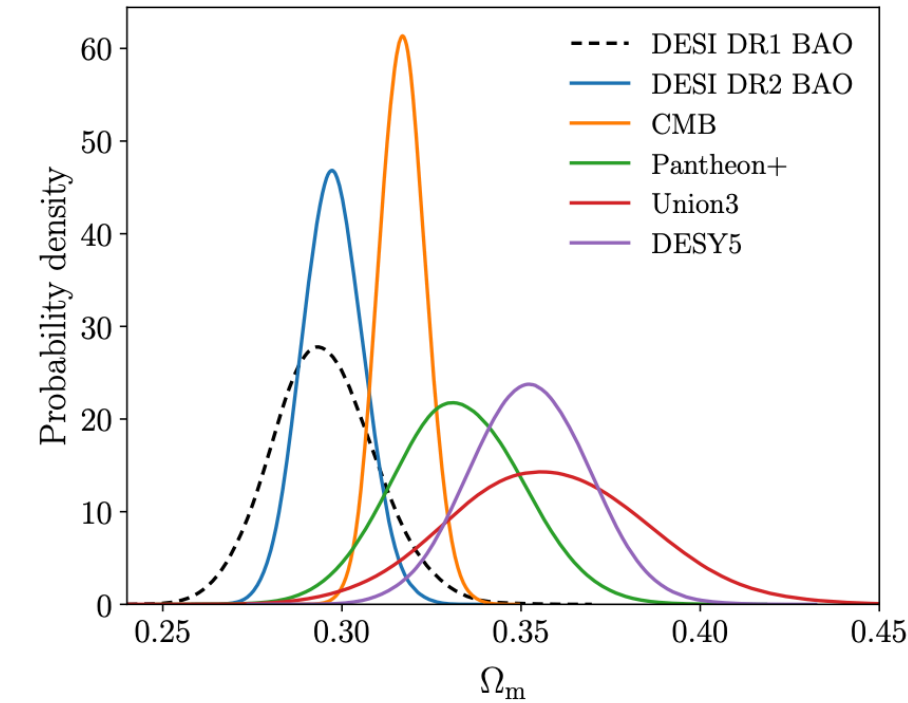




# DESI vs SNIa

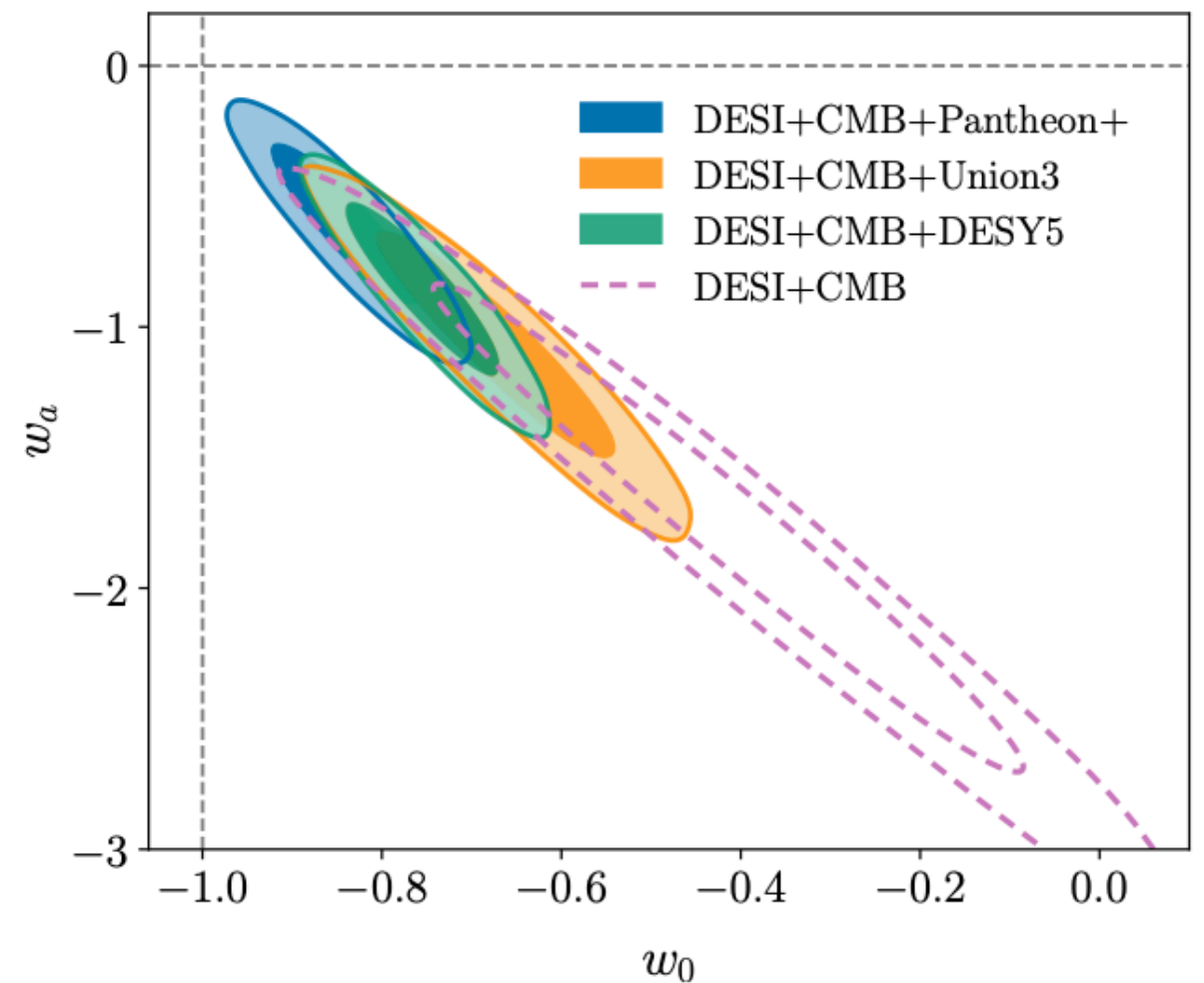
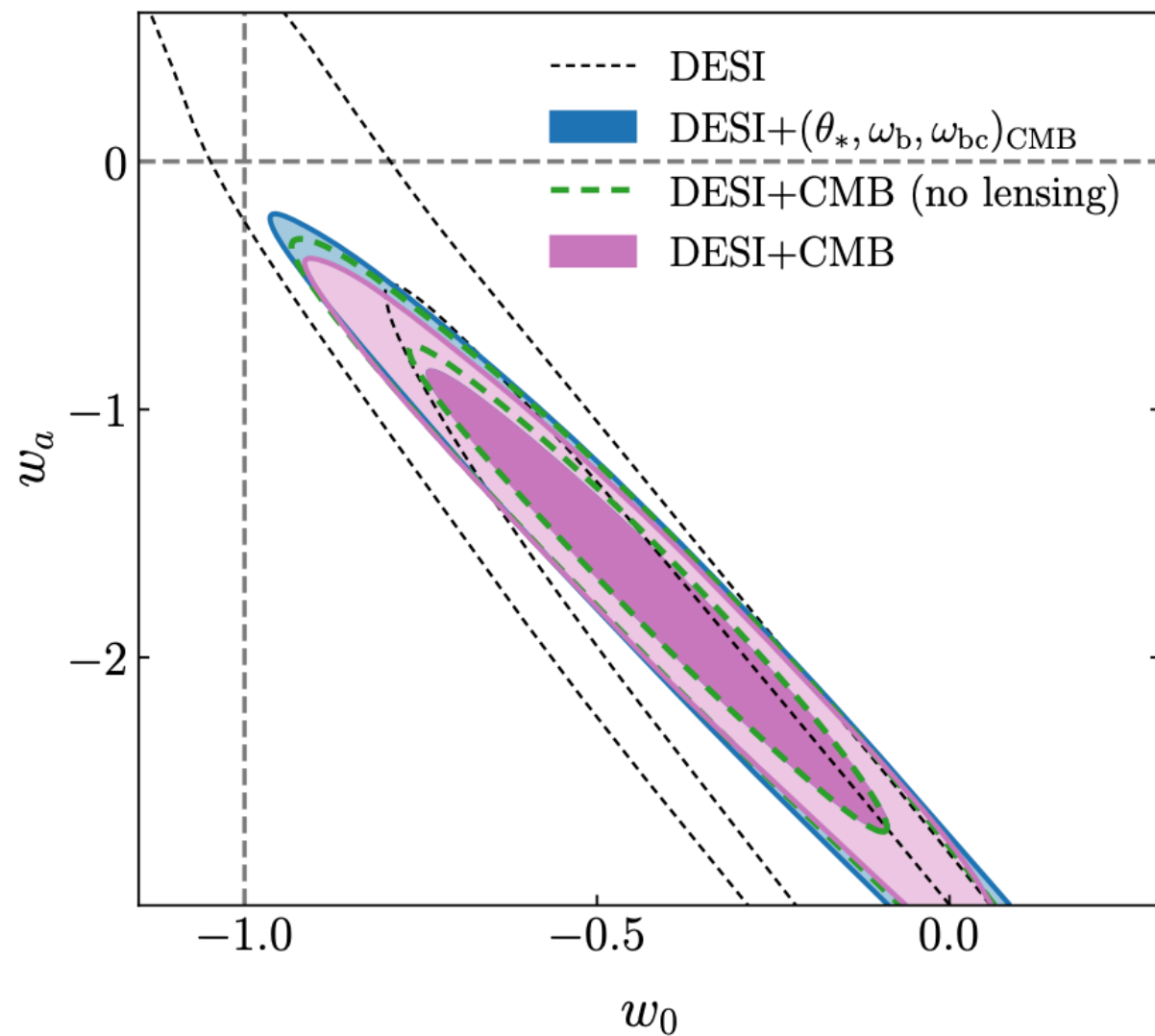


# DESI vs SNIa

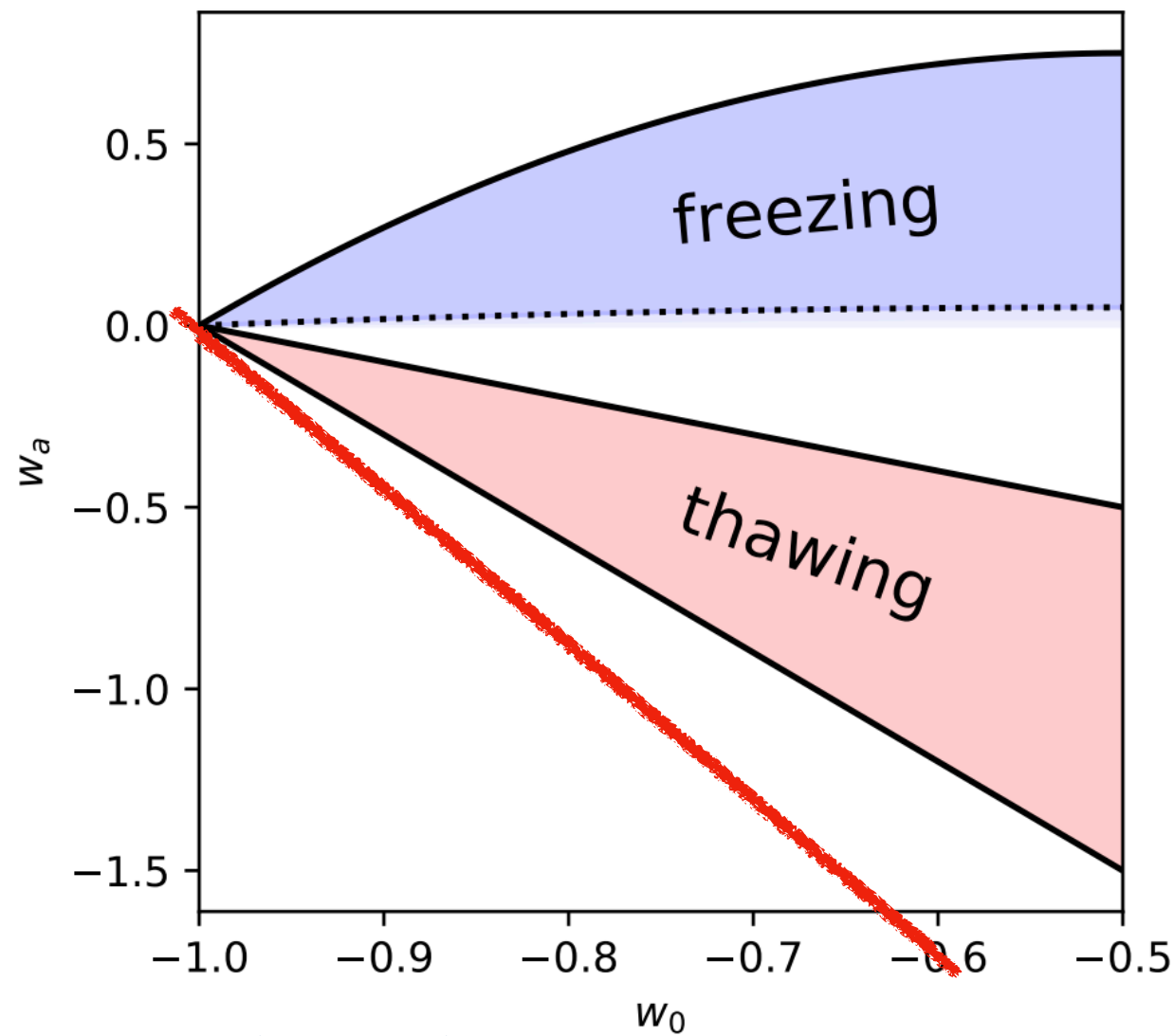


- DESI+CMB in tension at the  $\sim 2 - 3\sigma$  level with SNIa in the determination of  $\Omega_m$

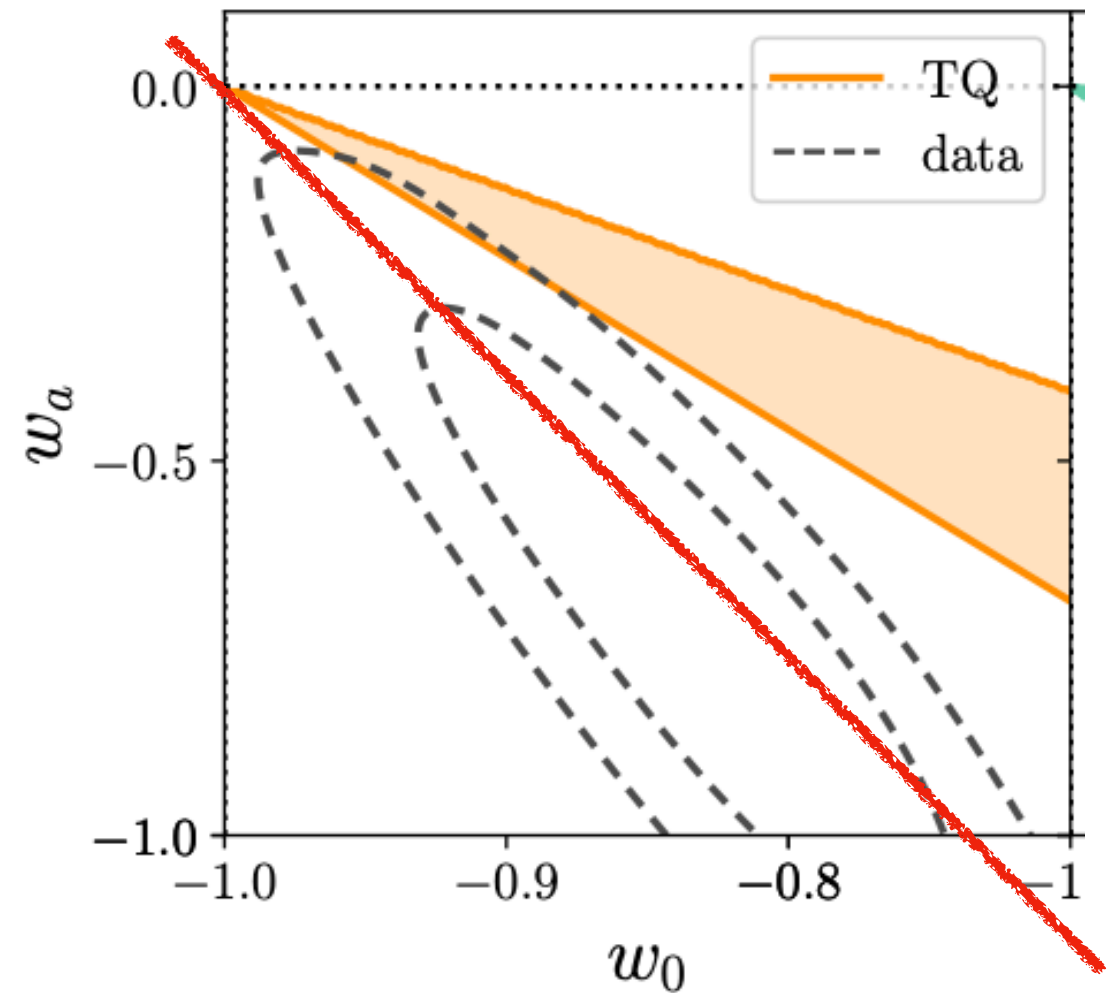
# Evidence for dynamical dark energy



# Evidence for non canonical quintessence



*Caldwell&Linder 2005*



*Wolf++ 2409.17019*

$$\langle w \rangle = -1 \Rightarrow w_a \approx -3.66(1 + w_0)$$

*Linder 0708.0024*

# A mirage of dynamical dark energy?

DEI+CMB: +PantheonPlus	+Union3	+DESY5
DE classes	$\Delta\text{DIC } (\Delta\chi^2)$	
Thaw. (Cal.)	+0.4 (−1.6)	−0.6 (−2.5) −5.8 (−7.1)
Thaw. (Alg.)	−1.0 (−2.9)	−4.6 (−6.9) −10.1 (−13.2)
Emergent	+2.1 (−0.05)	+1.8 (−0.1) +0.2 (−1.5)
Mirage	−9.1 (−10.5)	−13.8 (−16.2) −18.7 (−20.7)
$w_0 w_a$	−6.8 (−10.7)	−13.5 (−17.4) −17.2 (−21.0)

$$\langle w \rangle = -1 \Rightarrow w_a \approx -3.66(1 + w_0)$$

*Linder 0708.0024*

WEIRD??



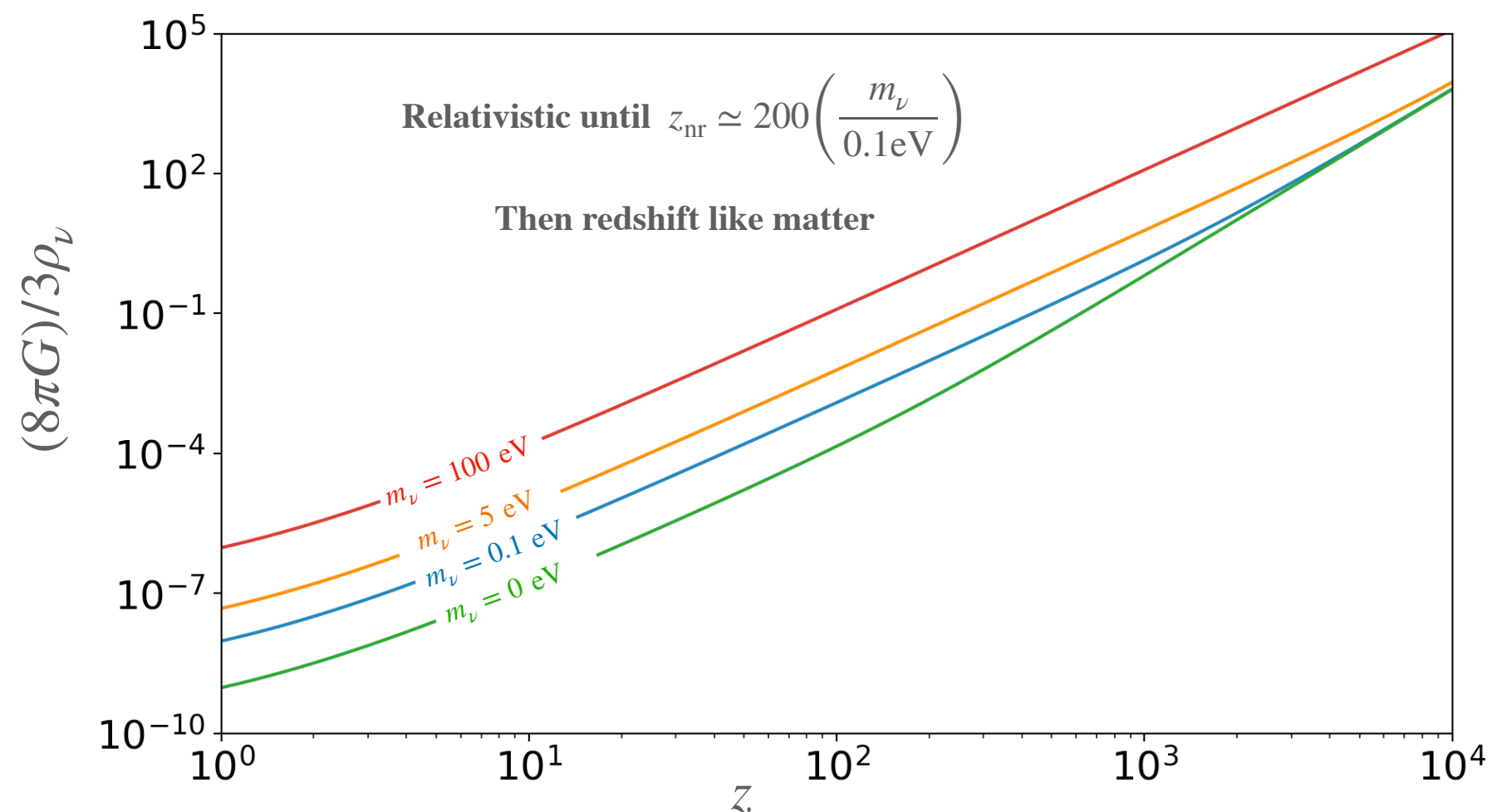
# $m_\nu$ can affect cosmological distances

- $\nu$  can affect the **homogeneous expansion**

$$H(z) \equiv \frac{\dot{a}}{a} = H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_r(1+z)^4 + \Omega_\Lambda + \dots}$$

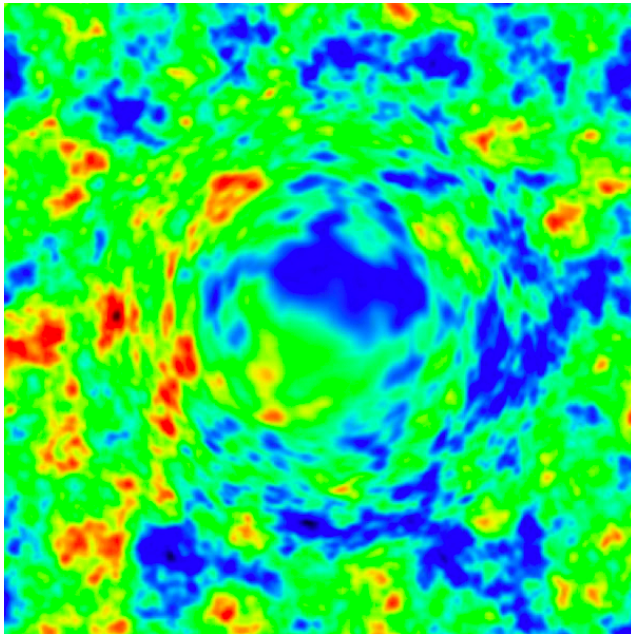
- Affect distance measurements via SN1a and BAO

$$D_M(z) = \int_0^z \frac{cdz}{H(z)}$$

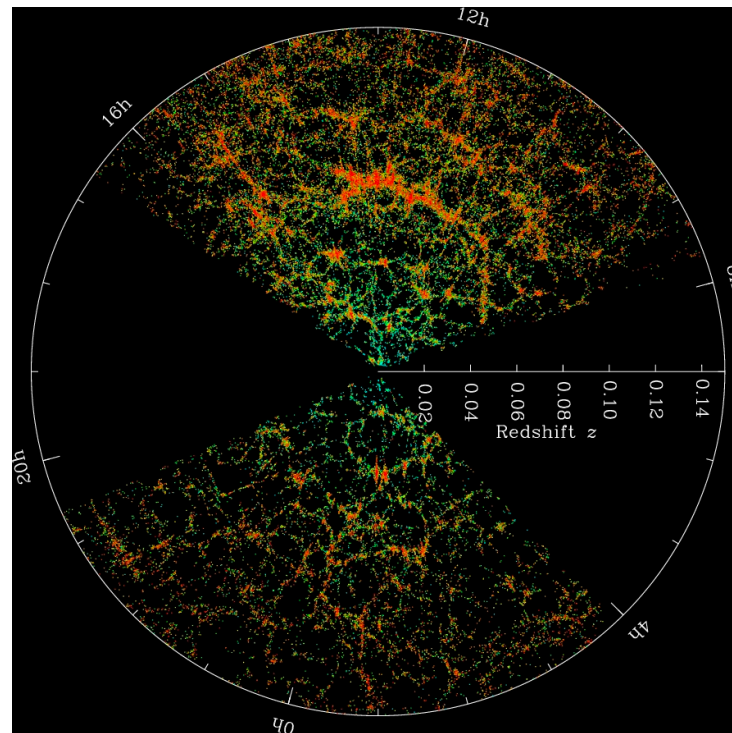


# $m_\nu$ can affect probes of matter structuring

CMB weak lensing



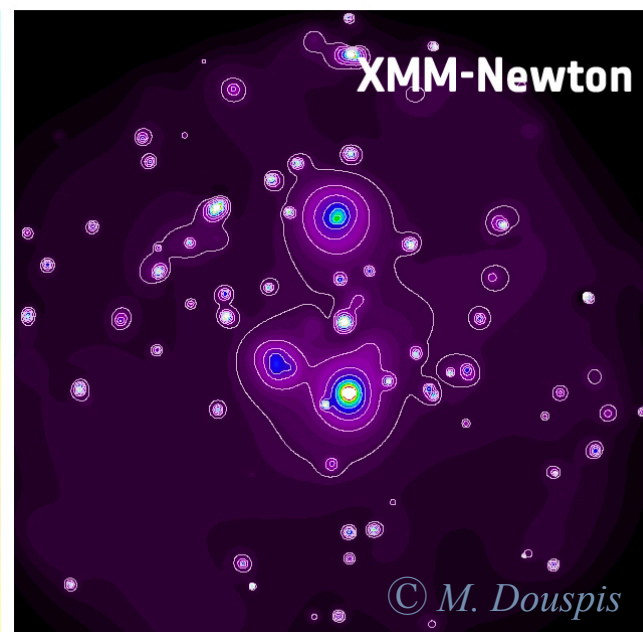
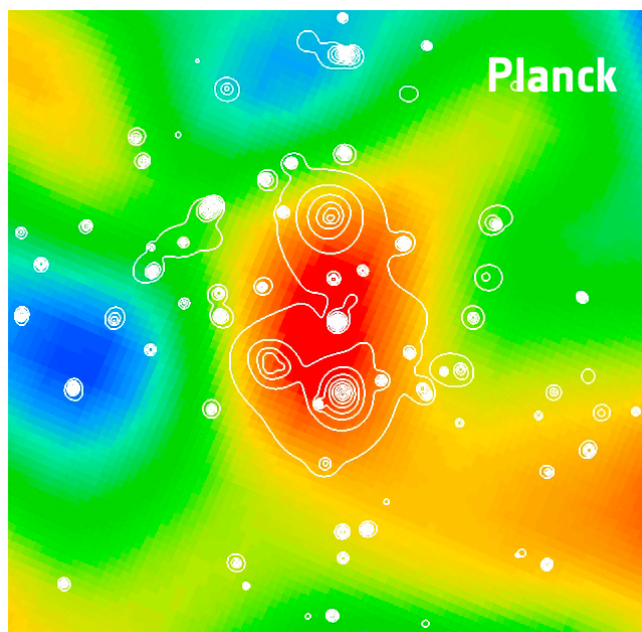
Galaxy correlation function (SDSS/BOSS)



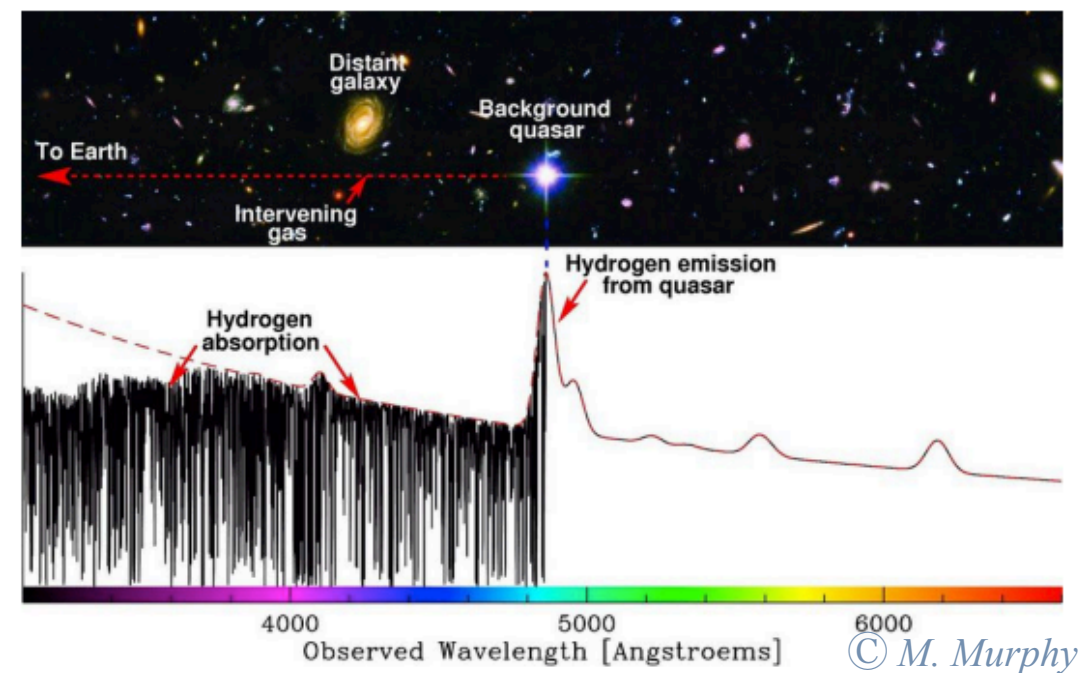
Galaxy weak lensing (KiDS / DES)



Galaxy cluster mass function



The Lyman- $\alpha$  forest (MIKE/HIRES)

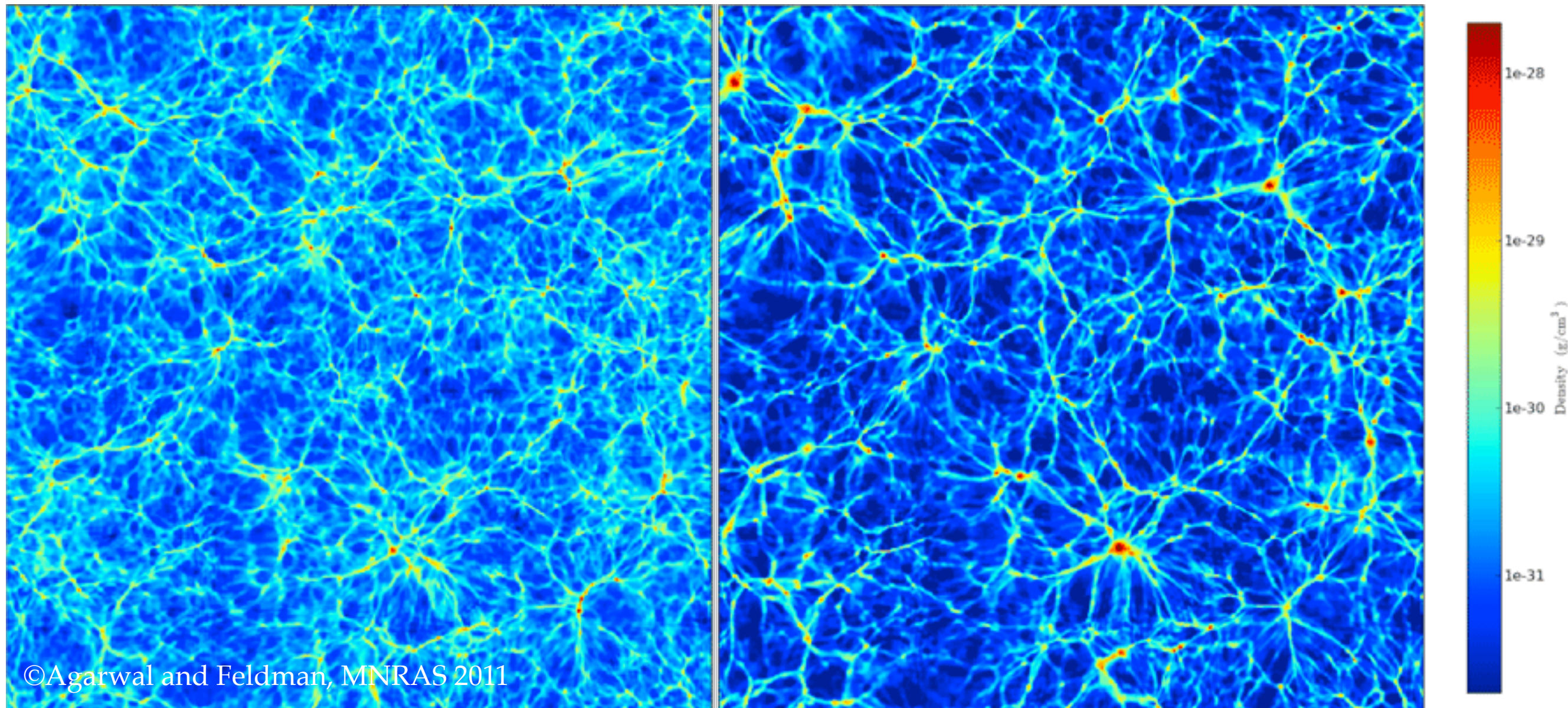




# $m_\nu$ suppresses the clustering of matter

$$M_\nu = 1.9 \text{ eV}$$

$$M_\nu = 0 \text{ eV}$$

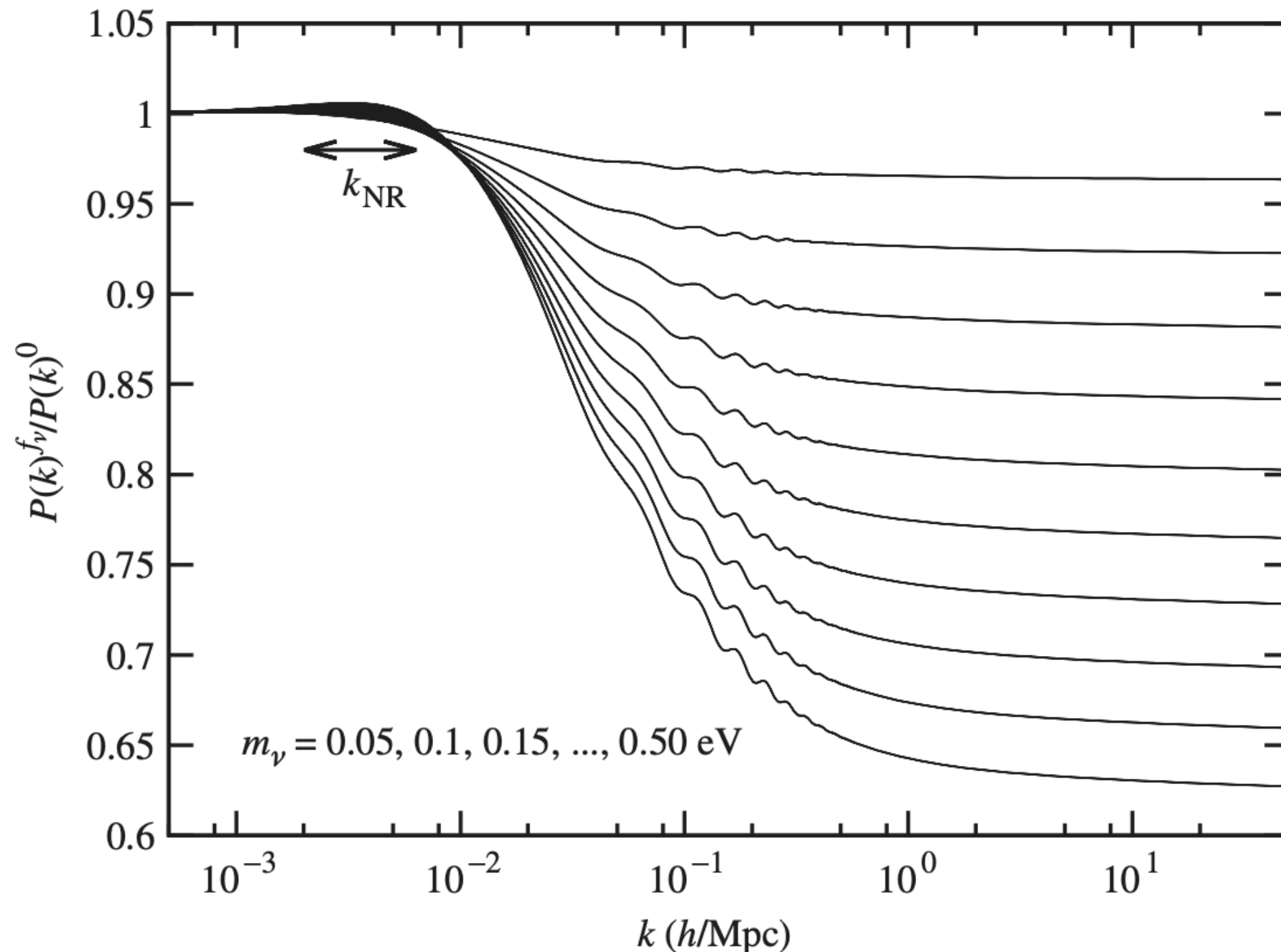


The density field is “smoother” on small scales



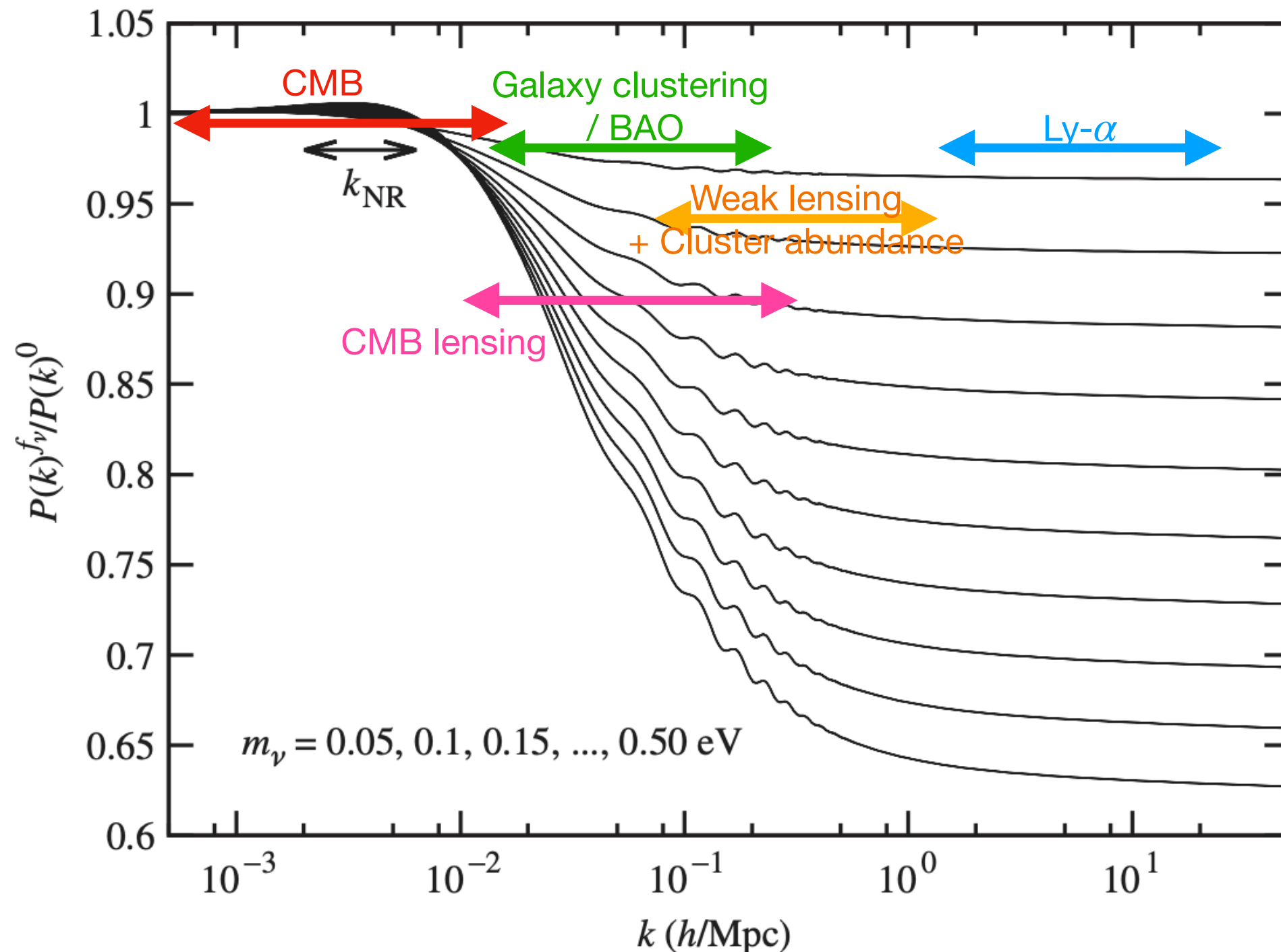
# $m_\nu$ suppresses the matter power spectrum

For  $\nu$ 's suppression at  $k \geq k_{\text{nr}} \equiv 0.01 \left( \frac{m_\nu}{1\text{eV}} \right)^{1/2} \left( \frac{\Omega_m}{0.3} \right)^{1/2} h\text{Mpc}^{-1}$  and amplitude  $\frac{\Delta P}{P} \simeq -8 \frac{\omega_\nu}{\omega_m}$



# $m_\nu$ suppresses the matter power spectrum

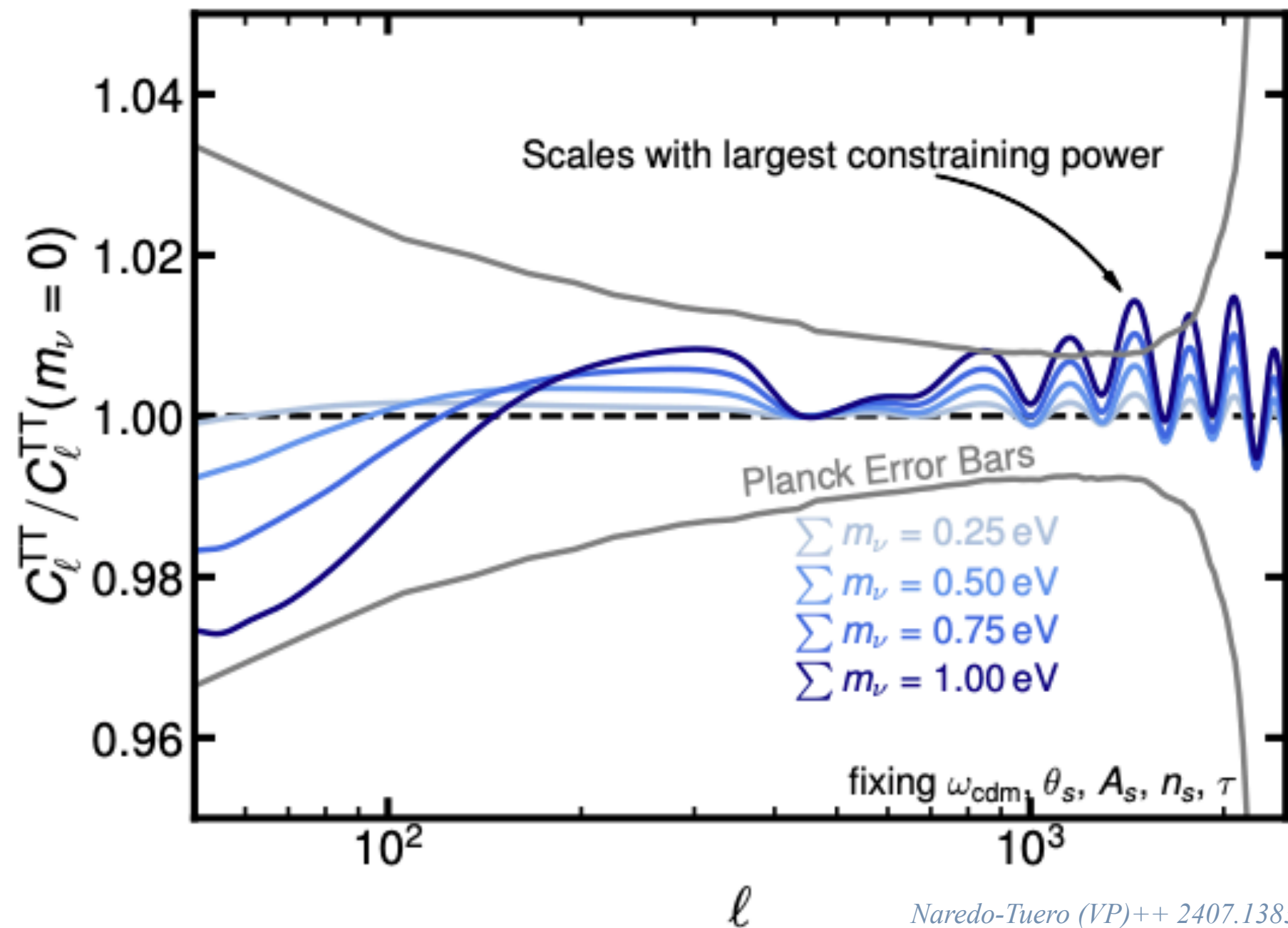
For  $\nu$ 's suppression at  $k \geq k_{\text{nr}} \equiv 0.01 \left( \frac{m_\nu}{1\text{eV}} \right)^{1/2} \left( \frac{\Omega_m}{0.3} \right)^{1/2} h\text{Mpc}^{-1}$  and amplitude  $\frac{\Delta P}{P} \simeq -8 \frac{\omega_\nu}{\omega_m}$



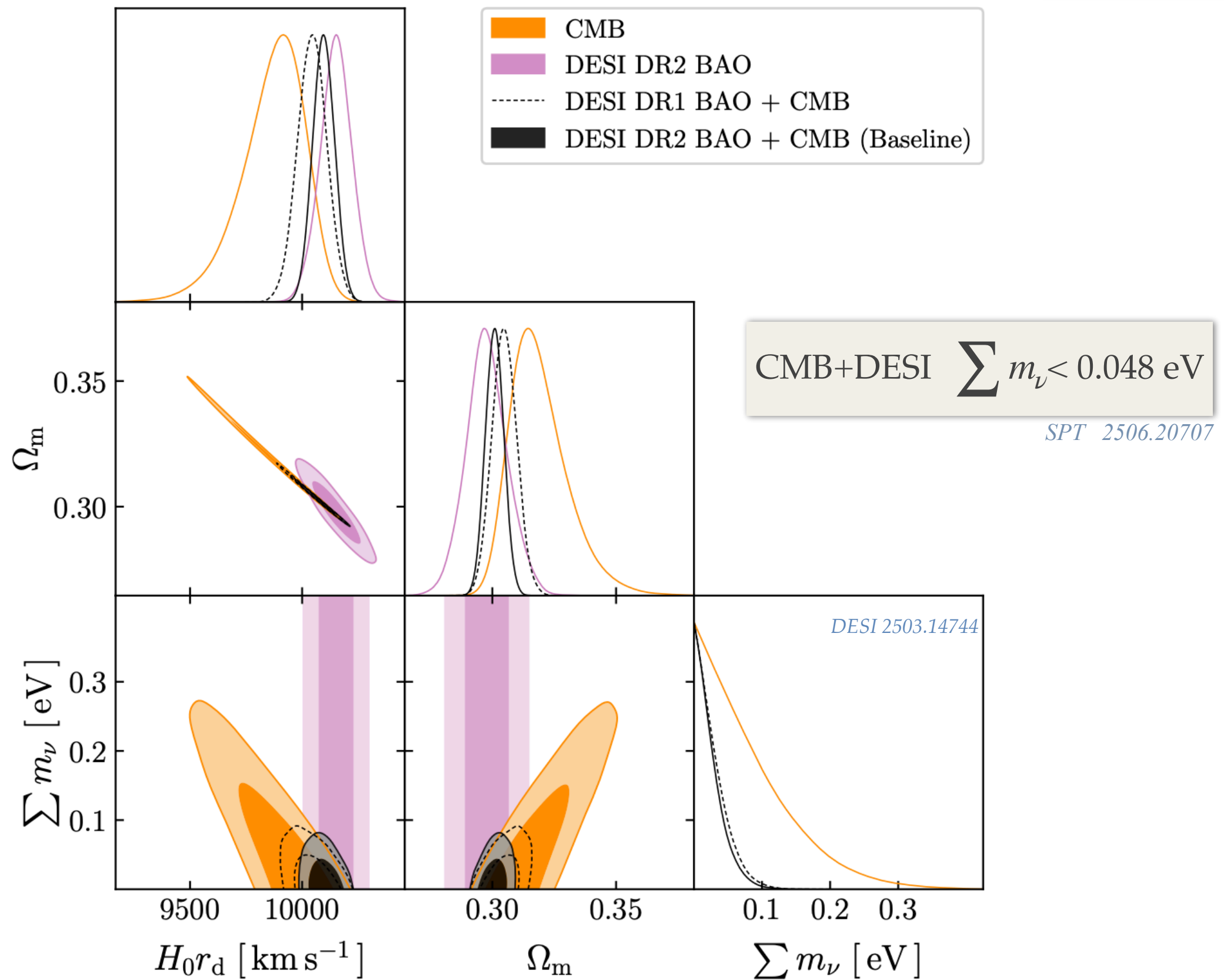


# $m_\nu$ affects the CMB power spectrum

For  $\sum m_\nu < 1$  eV, the main effect of neutrinos is to **alter the lensing** in the CMB



# Strong constraints to $M_\nu$ from background effect

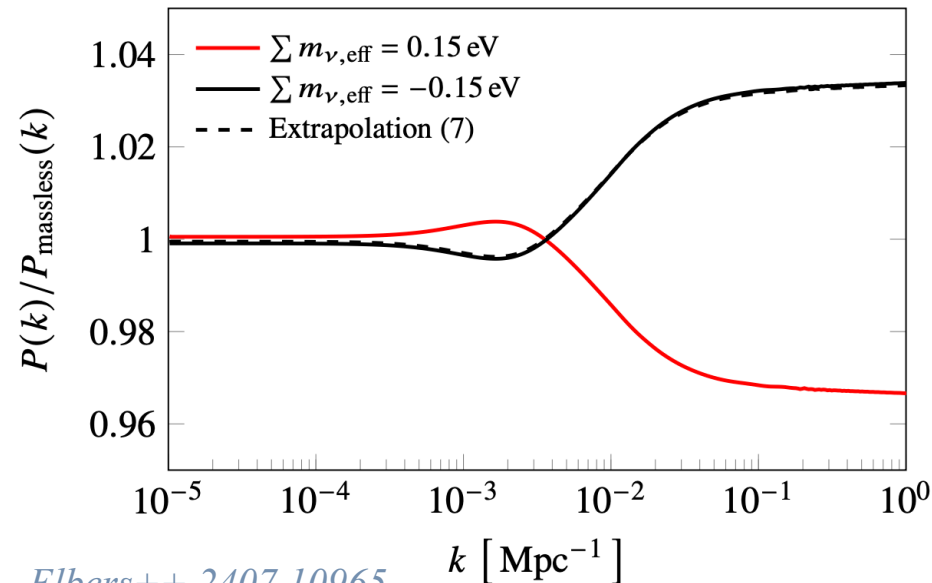


# No $\nu$ 's is good news?

Craig++ 2405.00836

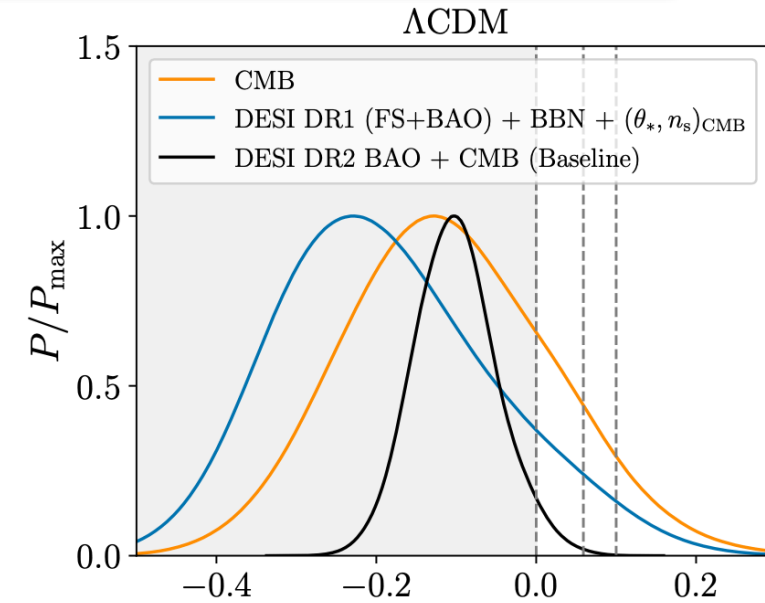
- When allowing for (effective)  $m_\nu < 0$  eV

$$\sum m_{\nu,\text{eff}} = -0.101^{+0.047}_{-0.056} \text{ eV}$$

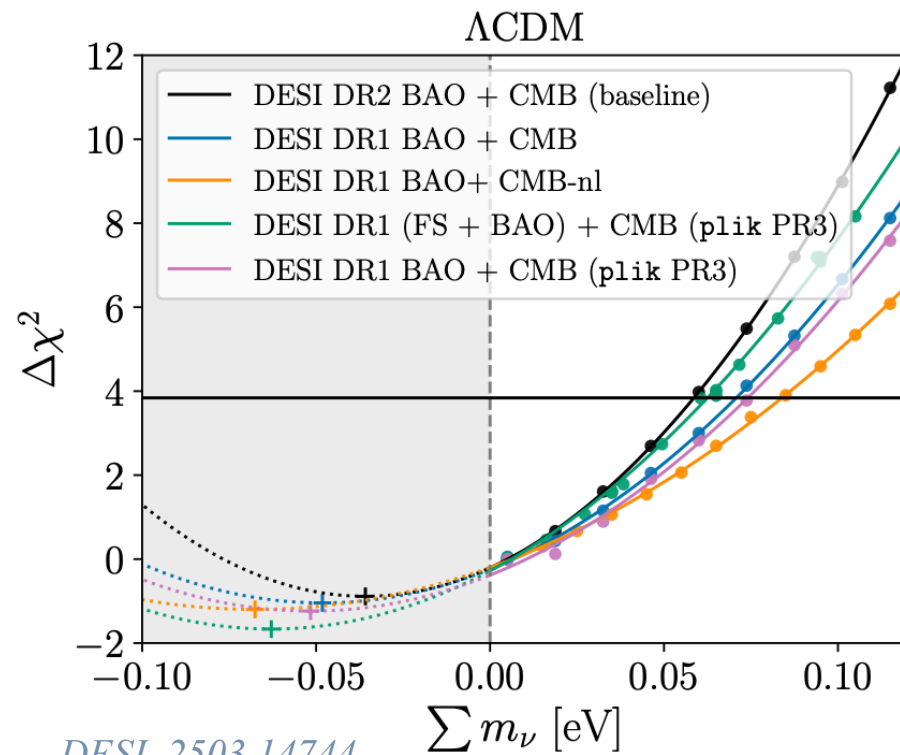


Elbers++ 2407.10965

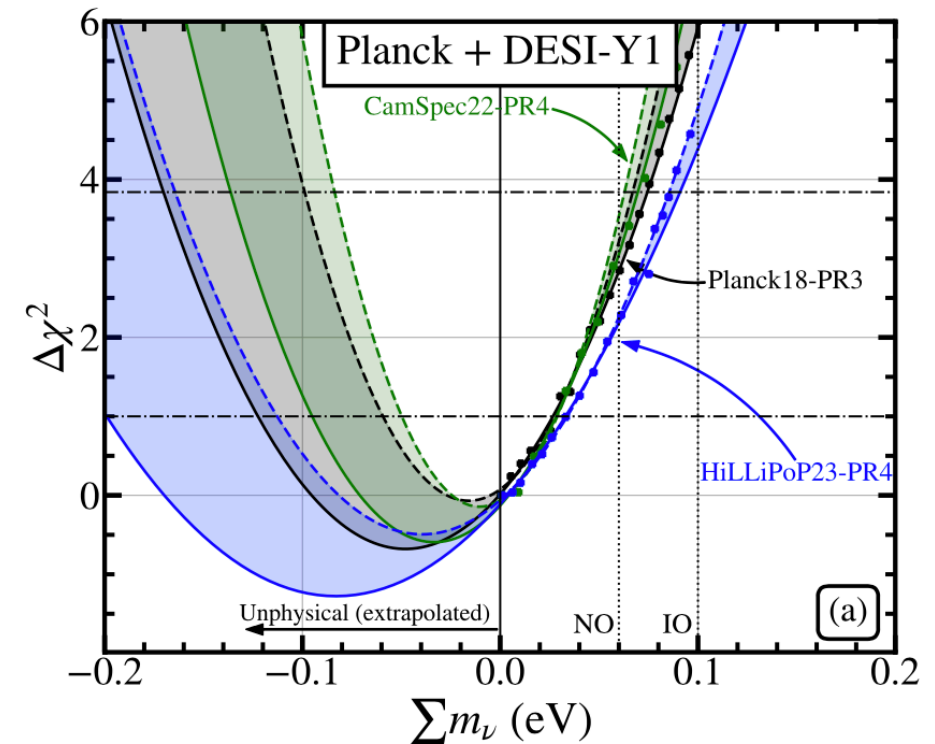
- Also seen in Frequentist analyses



DESI 2503.14744  $\sum m_{\nu,\text{eff}}$  [eV]



DESI 2503.14744



Naredo-Tuero (VP)++ 2407.13831

# A statistical fluke?

The screenshot shows the top of a Science journal article page. At the top left is the 'Science' logo. To its right are links for 'Current Issue', 'First release papers', 'Archive', and 'About'. Further right is a 'Submit manuscript' button. Below this is a breadcrumb trail: 'HOME > SCIENCE > VOL. 388, NO. 6743 > DIRECT NEUTRINO-MASS MEASUREMENT BASED ON 259 DAYS OF KATRIN DATA'. Below the breadcrumb is a row of social media icons (Facebook, X, Twitter, LinkedIn, etc.). The article title 'Direct neutrino-mass measurement based on 259 days of KATRIN data' is prominently displayed. Below the title is the author list: 'KATRIN COLLABORATION, MAY AKER, DOMINIC RATZ, ERIC ARMENBERG, ADRIAN IAN REHDENS, JUSTUS REISENKÖTTER, MATTEO RIASSONNI, RENÉDIKT RIEBINGER'.

Science

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HOME > SCIENCE > VOL. 388, NO. 6743 > DIRECT NEUTRINO-MASS MEASUREMENT BASED ON 259 DAYS OF KATRIN DATA

RESEARCH ARTICLE | PARTICLE PHYSICS

Direct neutrino-mass measurement based on 259 days of KATRIN data

KATRIN COLLABORATION, MAY AKER, DOMINIC RATZ, ERIC ARMENBERG, ADRIAN IAN REHDENS, JUSTUS REISENKÖTTER, MATTEO RIASSONNI, RENÉDIKT RIEBINGER

## Abstract

That neutrinos carry a nonvanishing rest mass is evidence of physics beyond the Standard Model of elementary particles. Their absolute mass holds relevance in fields from particle physics to cosmology. We report on the search for the effective electron antineutrino mass with the KATRIN experiment. KATRIN performs precision spectroscopy of the tritium  $\beta$ -decay close to the kinematic endpoint. On the basis of the first five measurement campaigns, we derived a best-fit value of  $m_\nu^2 = -0.14^{+0.13}_{-0.15} \text{ eV}^2$ , resulting in an upper limit of  $m_\nu < 0.45 \text{ eV}$  at 90% confidence level. Stemming from 36 million electrons collected in 259 measurement days, a substantial reduction of the background level, and improved systematic uncertainties, this result tightens KATRIN's previous bound by a factor of almost two.

- Within Katrin, it is attributed to under fluctuations compatible with statistical fluke
- There are **two main reasons** driving this preference in CMB data, both still **compatible with fluke**

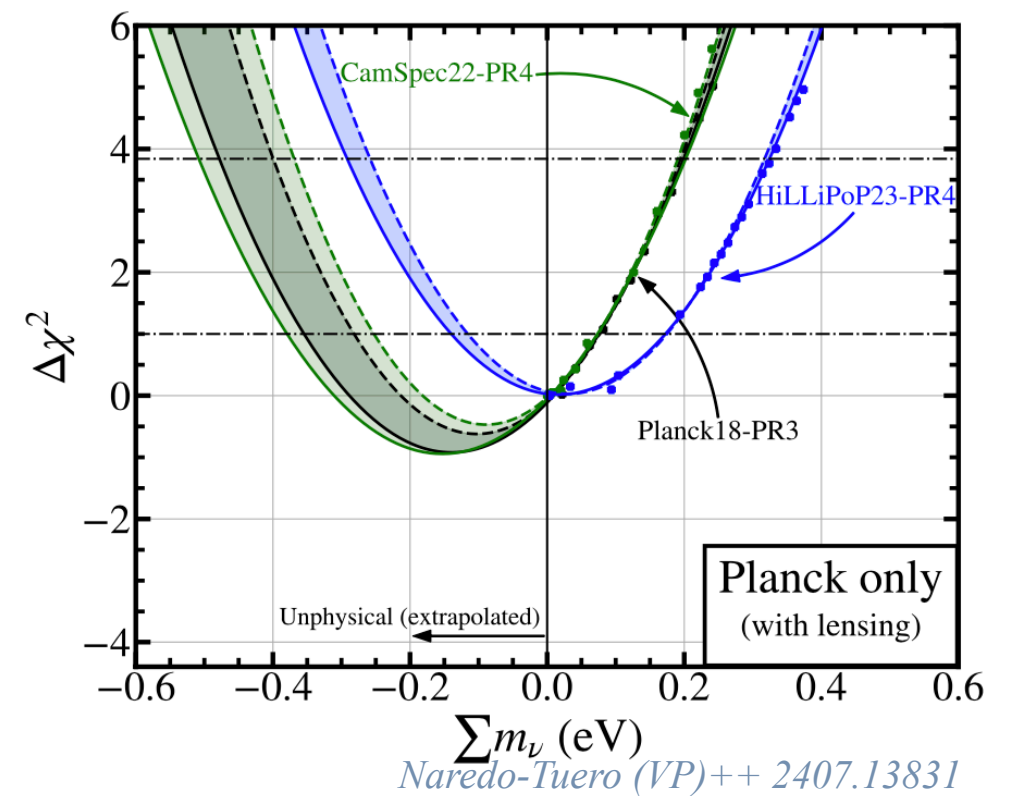
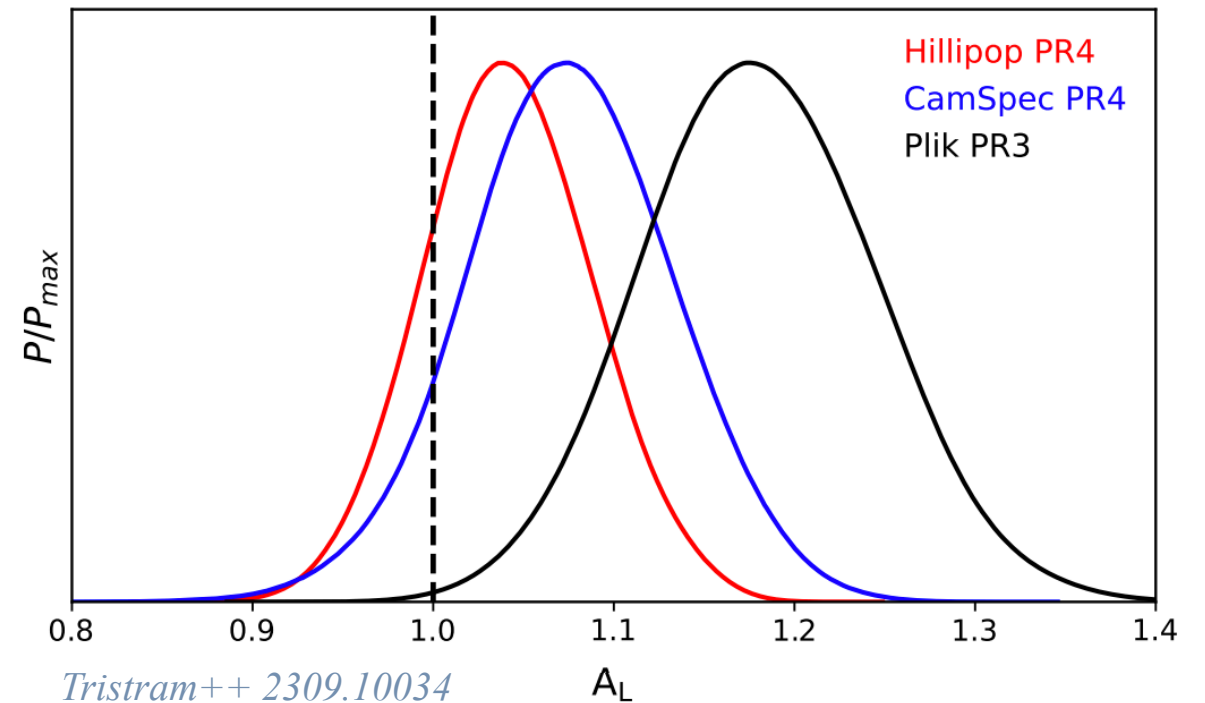
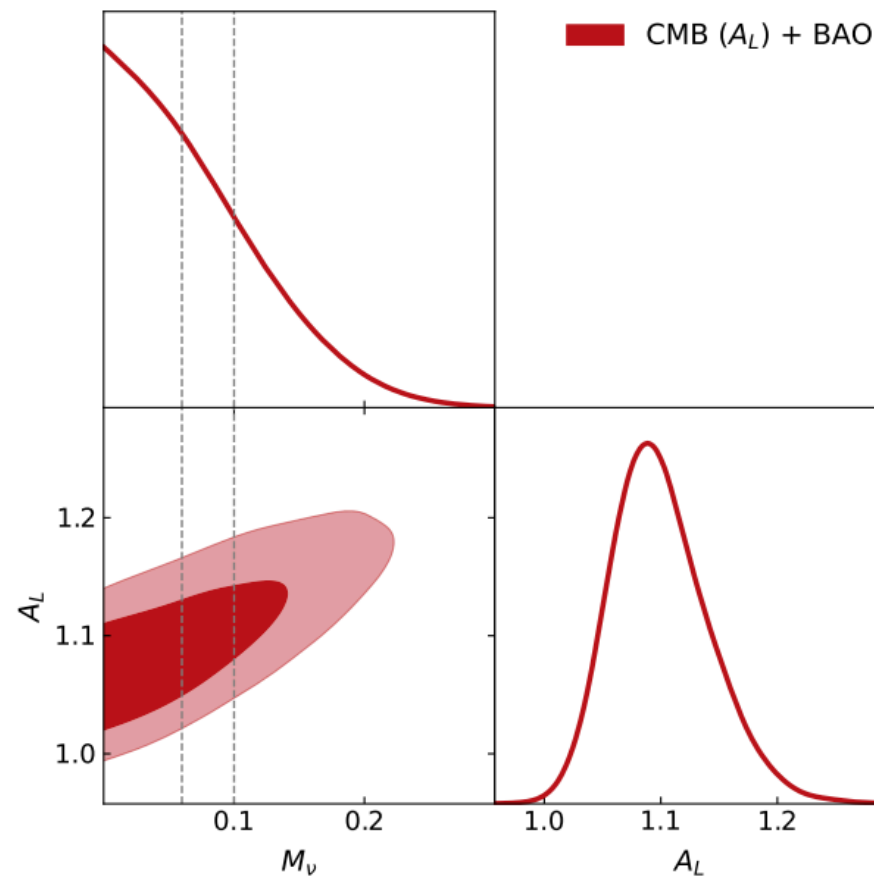
# $m_\nu < 0$ is due to a “lensing anomaly” in Planck

- Planck 2018 has an anomalous amount of lensing

$$C_\ell^{\phi\phi} \rightarrow A_L C_\ell^{\phi\phi}, \quad A_L = 1.180 \pm 0.065$$

- This anomaly went down with PR4

$$A_L = 1.039 \pm 0.052$$



- The preference for  $m_\nu < 0$  goes away when using a newer version *Planck* data (NPIPE)



# The role of the optical depth $\tau$

- The amplitude is correlated with the optical depth to reionization  $\tau$

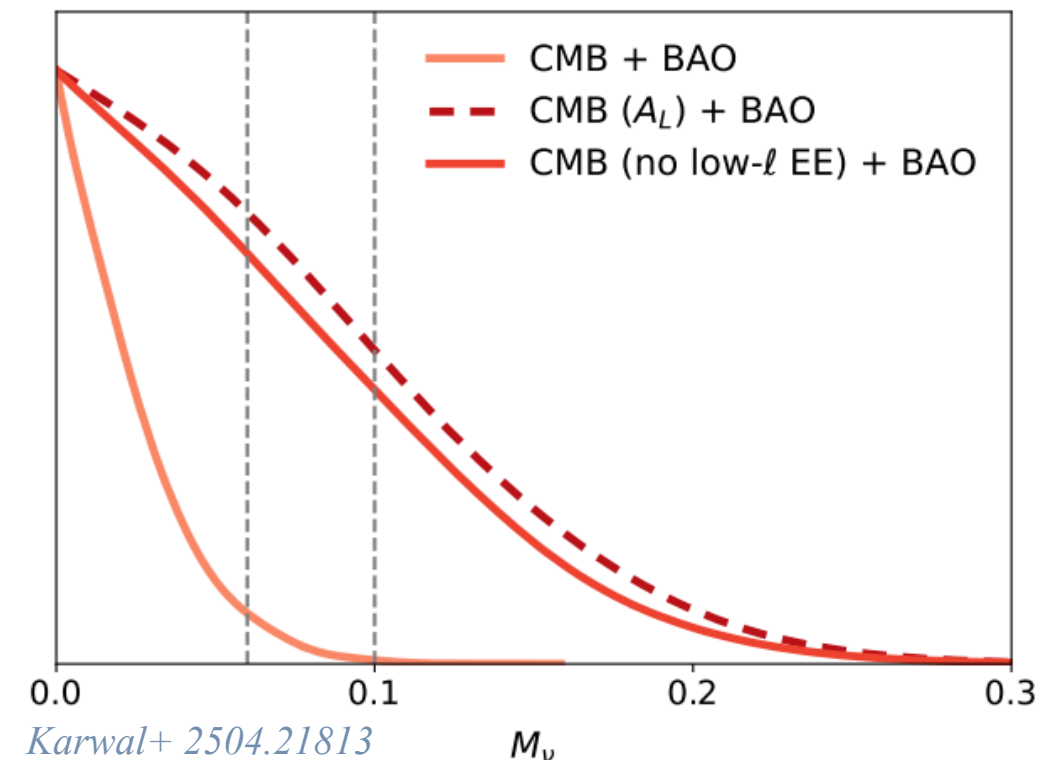
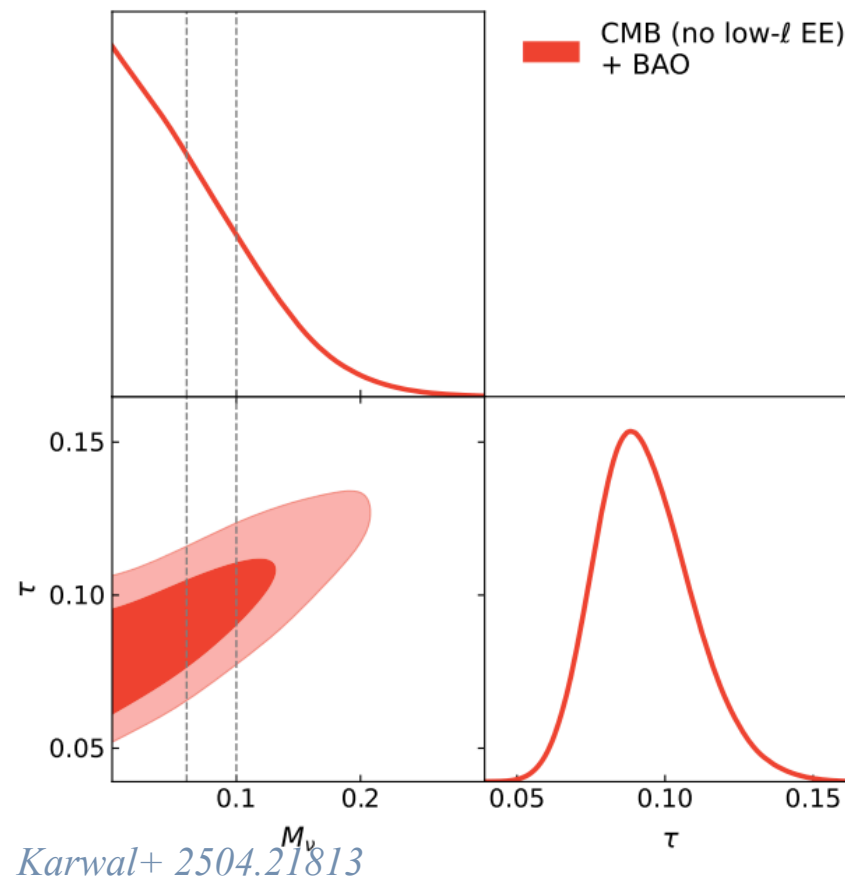
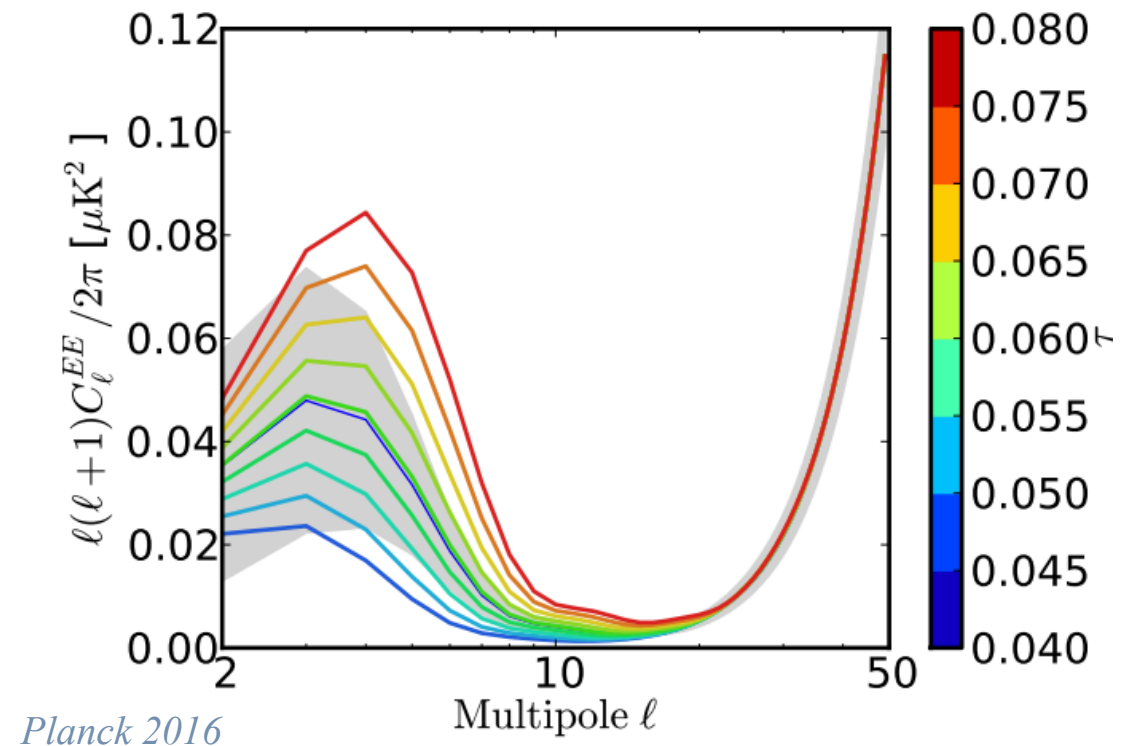
$$C_\ell \propto A_s \exp(-2\tau)$$

- The low- $\ell$  EE spectrum constrains

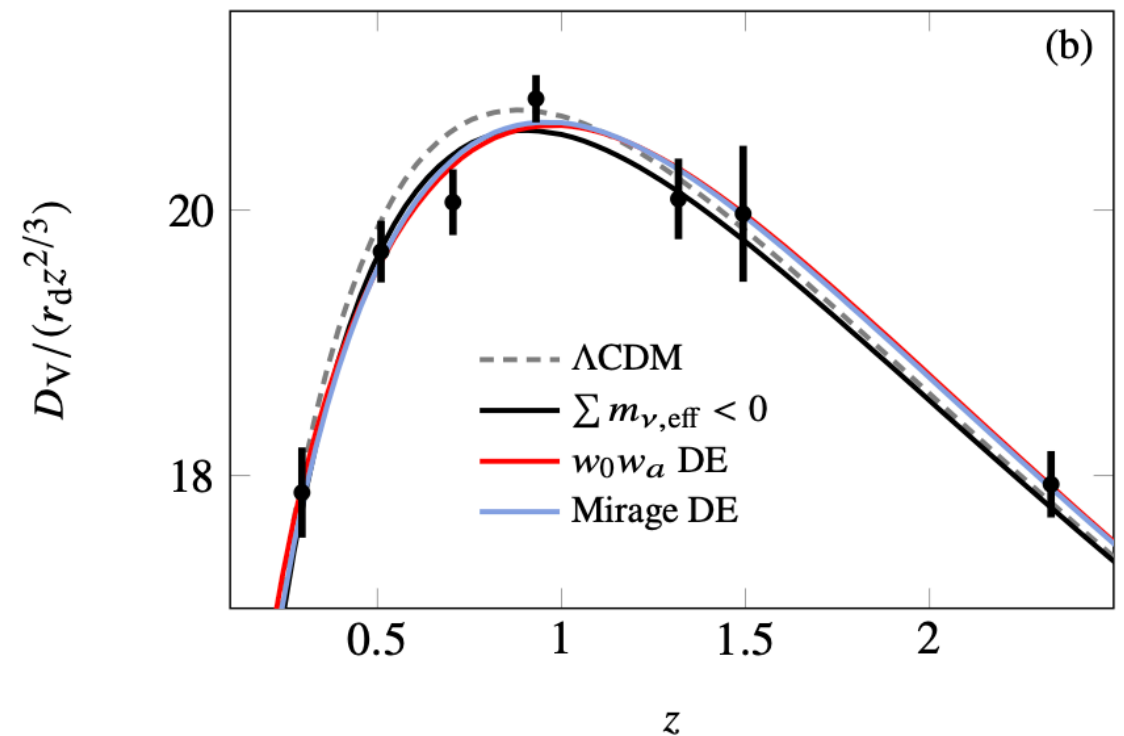
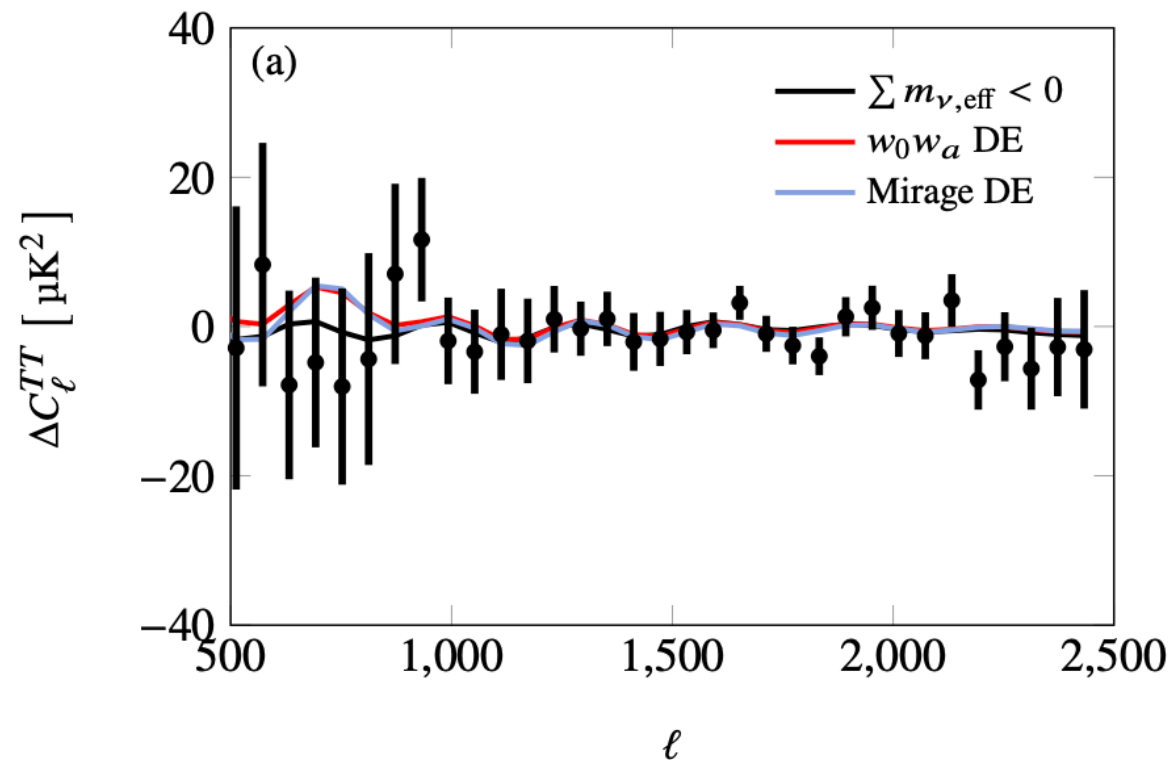
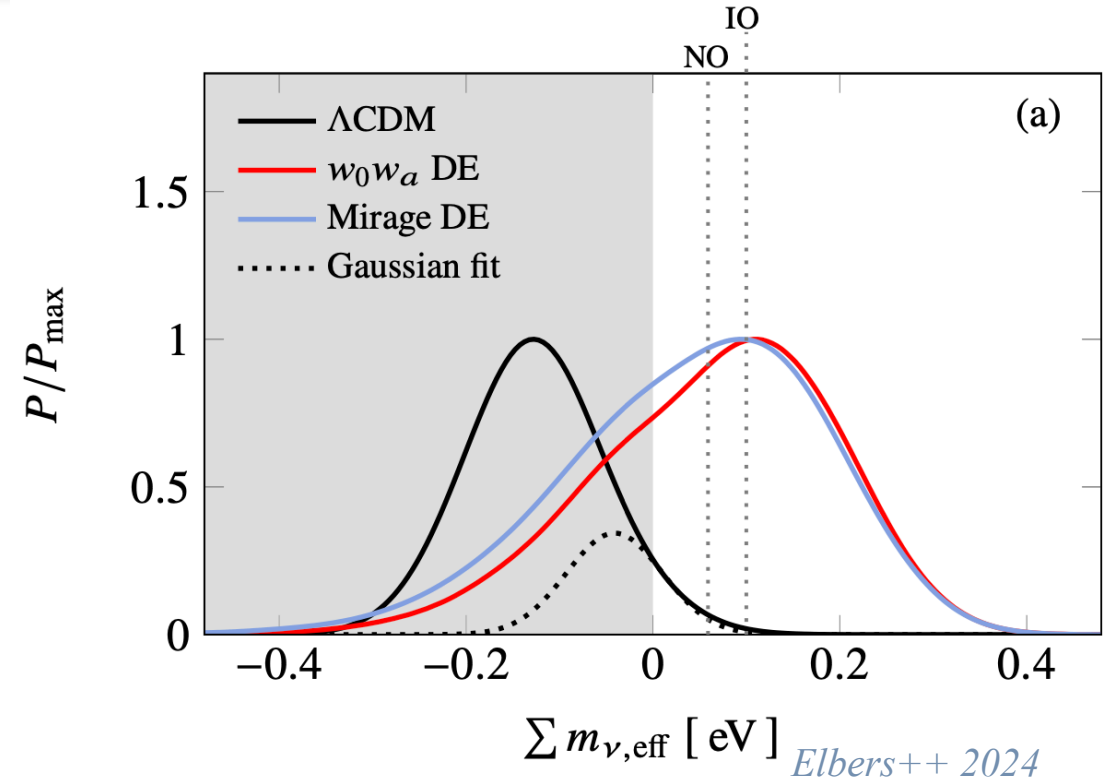
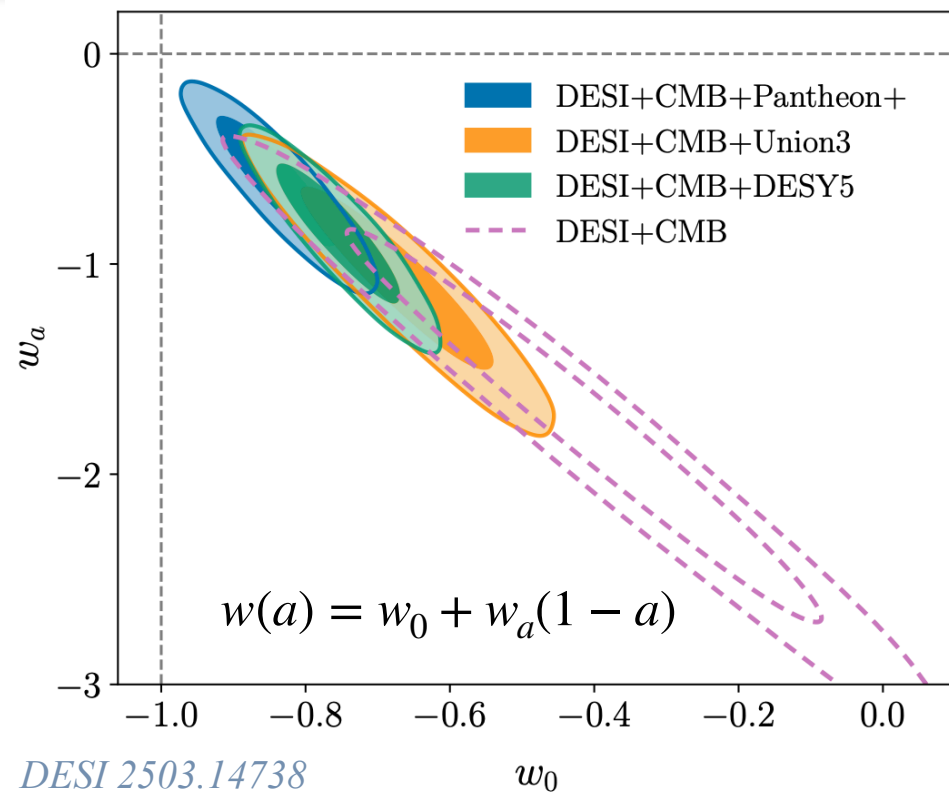
$$\tau = 0.0592 \pm 0.0062$$

- Without low- $\ell$  EE information,

$$\tau = 0.09 \pm 0.012, \quad \sum m_\nu < 0.2 \text{ eV}$$



# $m_\nu$ is degenerate with the effect of dark energy



# Summary of neutrino mass bounds

DESI 2503.14744, 2504.18464

- Despite anomalies, it is hard to get rid of the neutrino mass bound from cosmology

Flat  $\Lambda$ CDM (3 deg  $\nu$ 's)

$$\text{Planck+DESI} \quad \sum m_\nu < 0.064 \text{ eV}$$

$$\text{Planck+ ACT +DESI} \quad \sum m_\nu < 0.06 \text{ eV}$$

$$\text{P+ ACT +SPT +DESI} \quad \sum m_\nu < 0.048 \text{ eV}$$

$w_0 w_a$ CDM (3 deg  $\nu$ 's)

$$\text{Planck+DESI} \quad \sum m_\nu < 0.163 \text{ eV}$$

$$\text{Planck+ ACT +DESI} \quad \sum m_\nu < 0.152 \text{ eV}$$

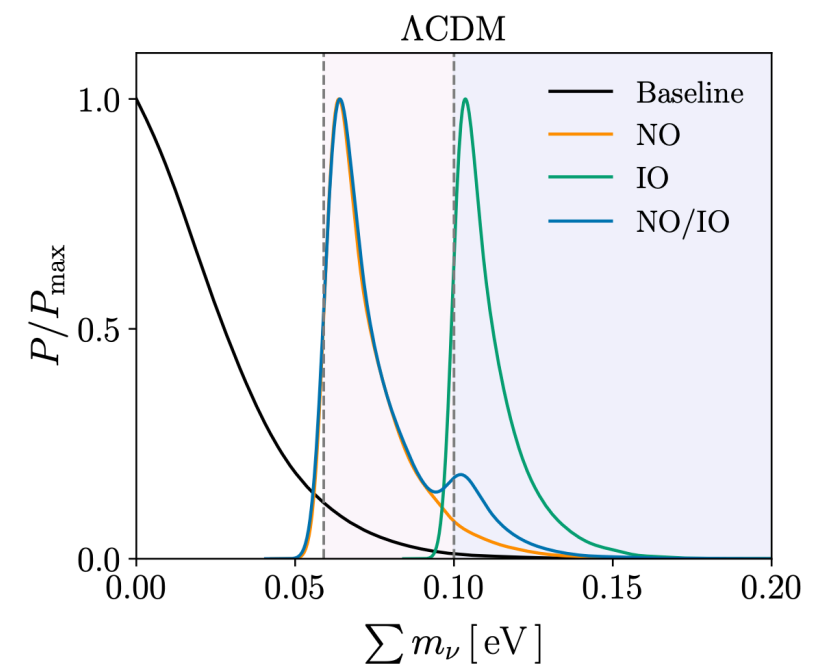
$$\text{Planck+ ACT + SN1a} \quad \sum m_\nu < 0.117\text{-}0.139 \text{ eV}$$

- Enforcing neutrino mass ordering leads to a preference for NO over IO at 10 : 1

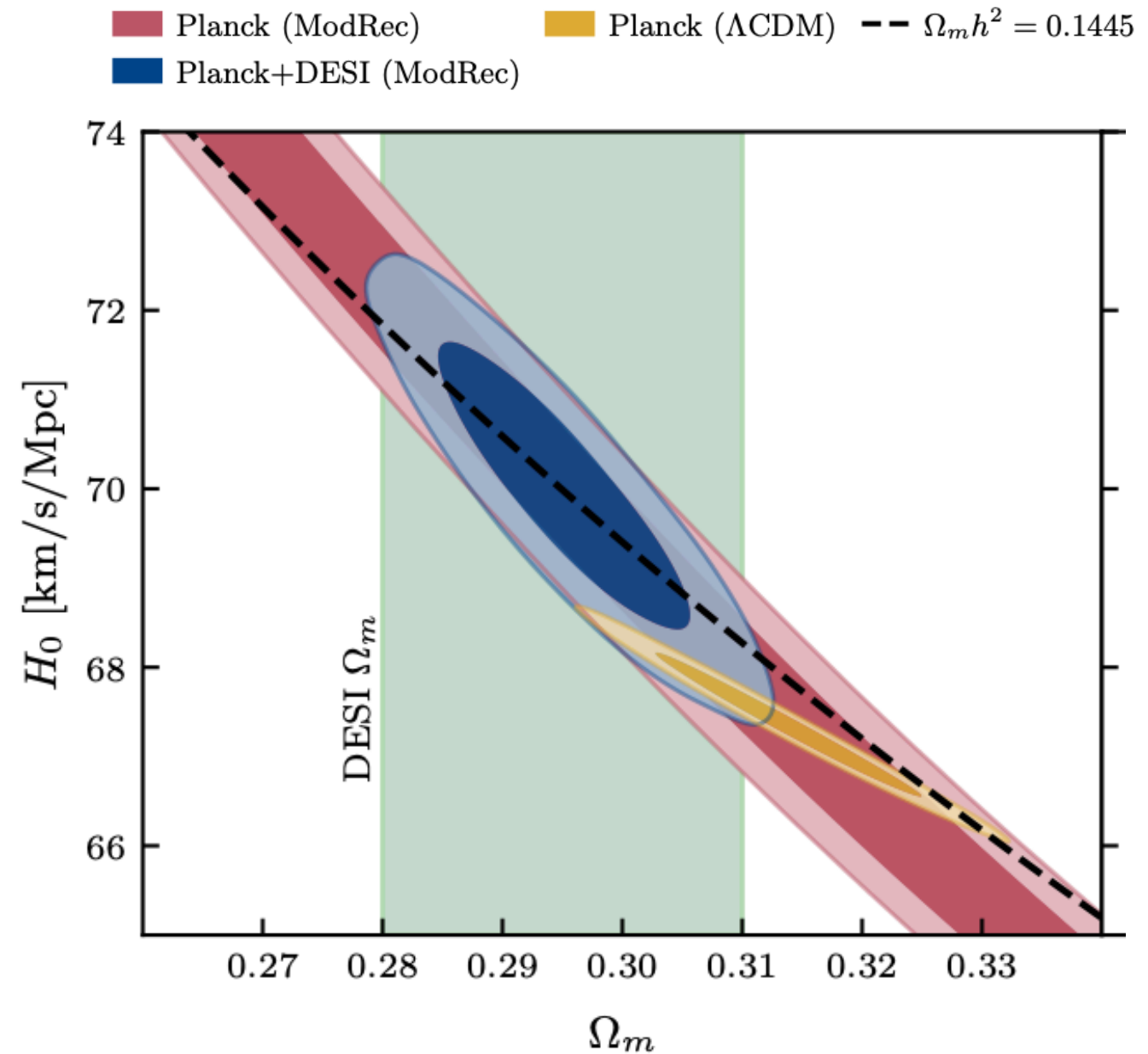
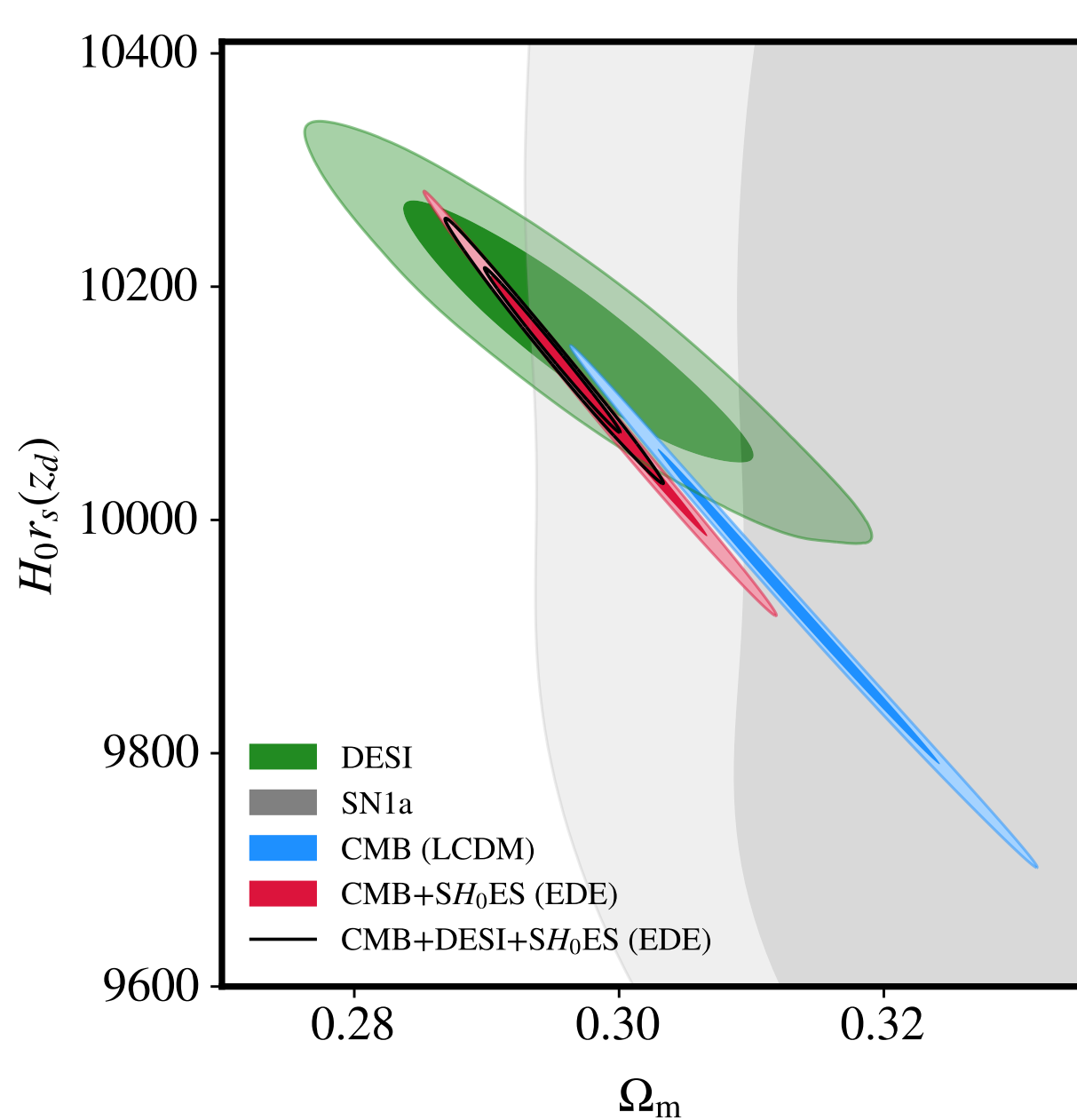
Planck + DESI + NuFIT6.0 ( $\Lambda$ CDM)

$$\text{NO} \quad \sum m_\nu < 0.101 \text{ eV} \Rightarrow m_l < 0.023 \text{ eV}$$

$$\text{IO} \quad \sum m_\nu < 0.133 \text{ eV} \Rightarrow m_l < 0.024 \text{ eV}$$



# Early universe solution to the BAO tension

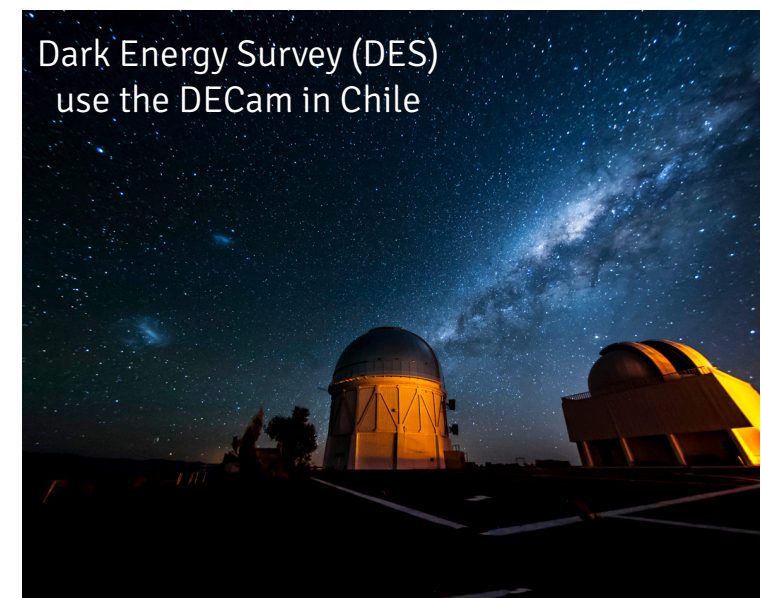
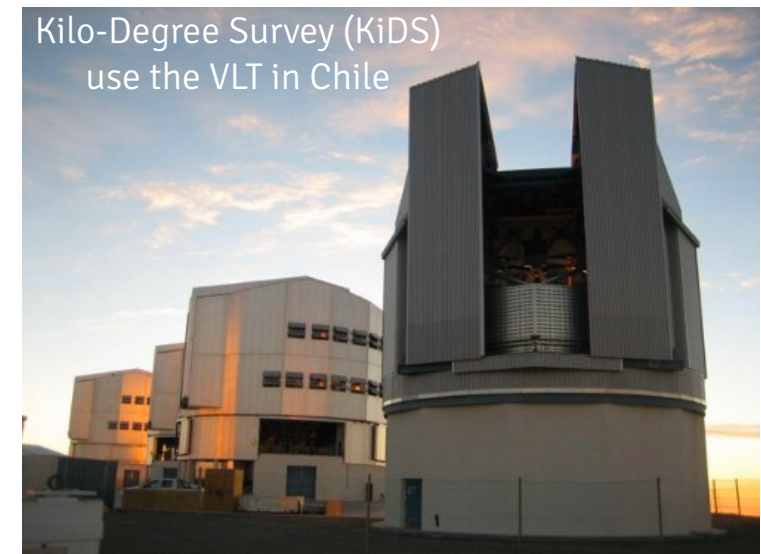
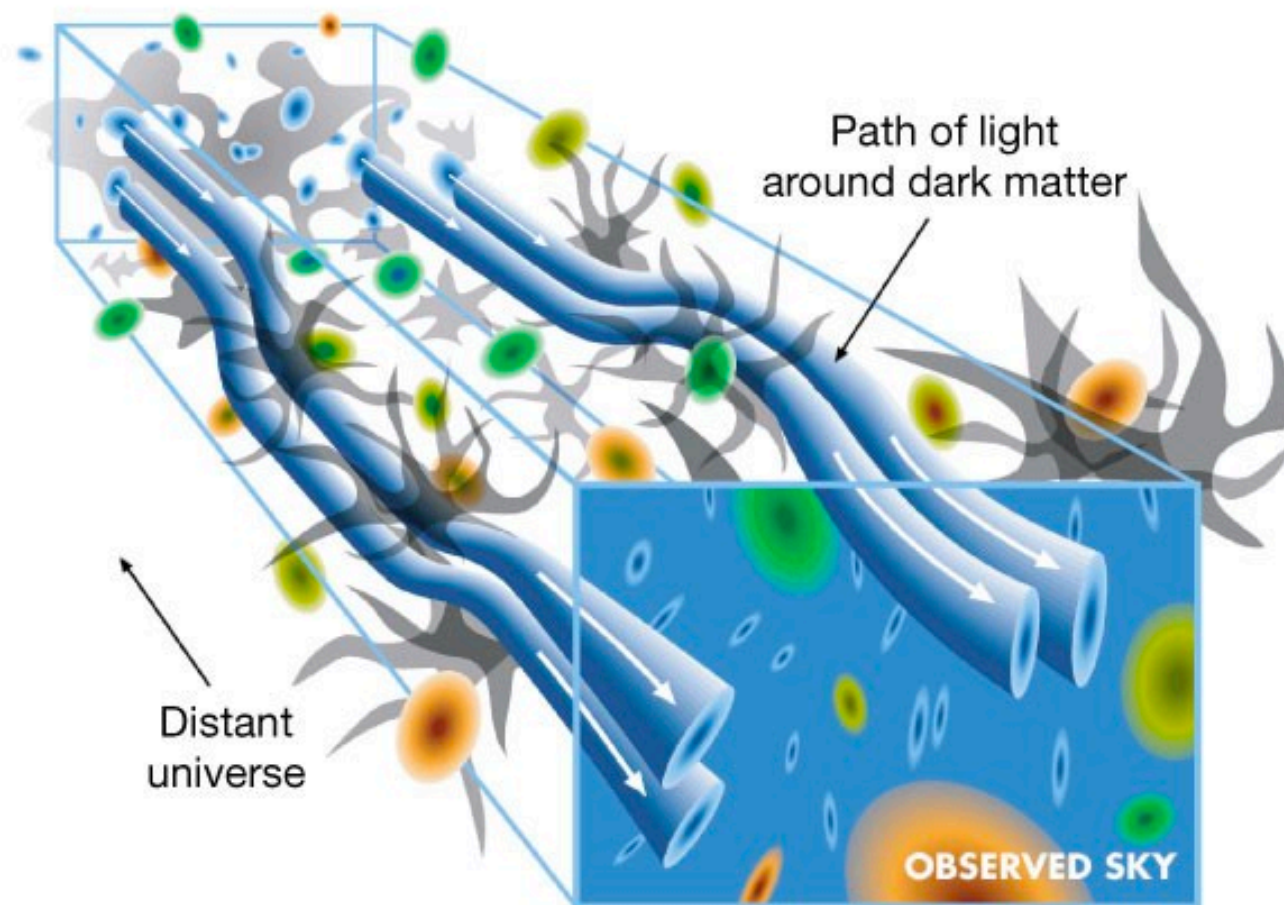


- Early universe solution can **reduce  $H_0 r_d$  and  $\Omega_m$**
- An alternative explanation to DESI results? [Lynch&Chluba 2406.10202](#), [Chaussidon++ 2503.24343](#)



# Galaxy weak lensing

- “Weak gravitational lensing” observations **measure the distortions in the shape of galaxies**

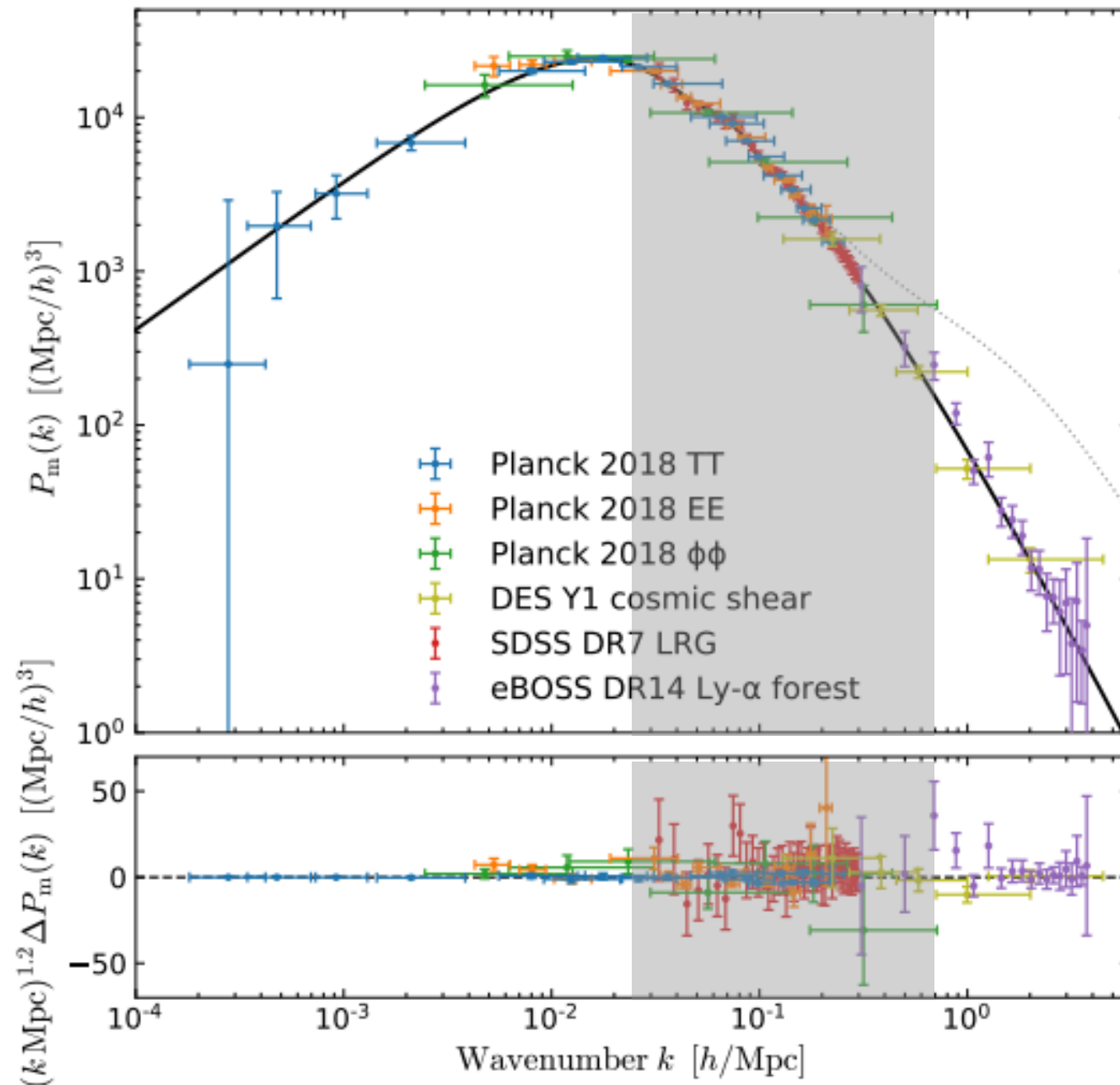


- There are three main WL observatory: DES, KiDS and HSC (Hawaii)
- New: Euclid!



# The $S_8$ parameter

- WL observations are mostly sensitive to the ‘ $S_8$  parameter’.



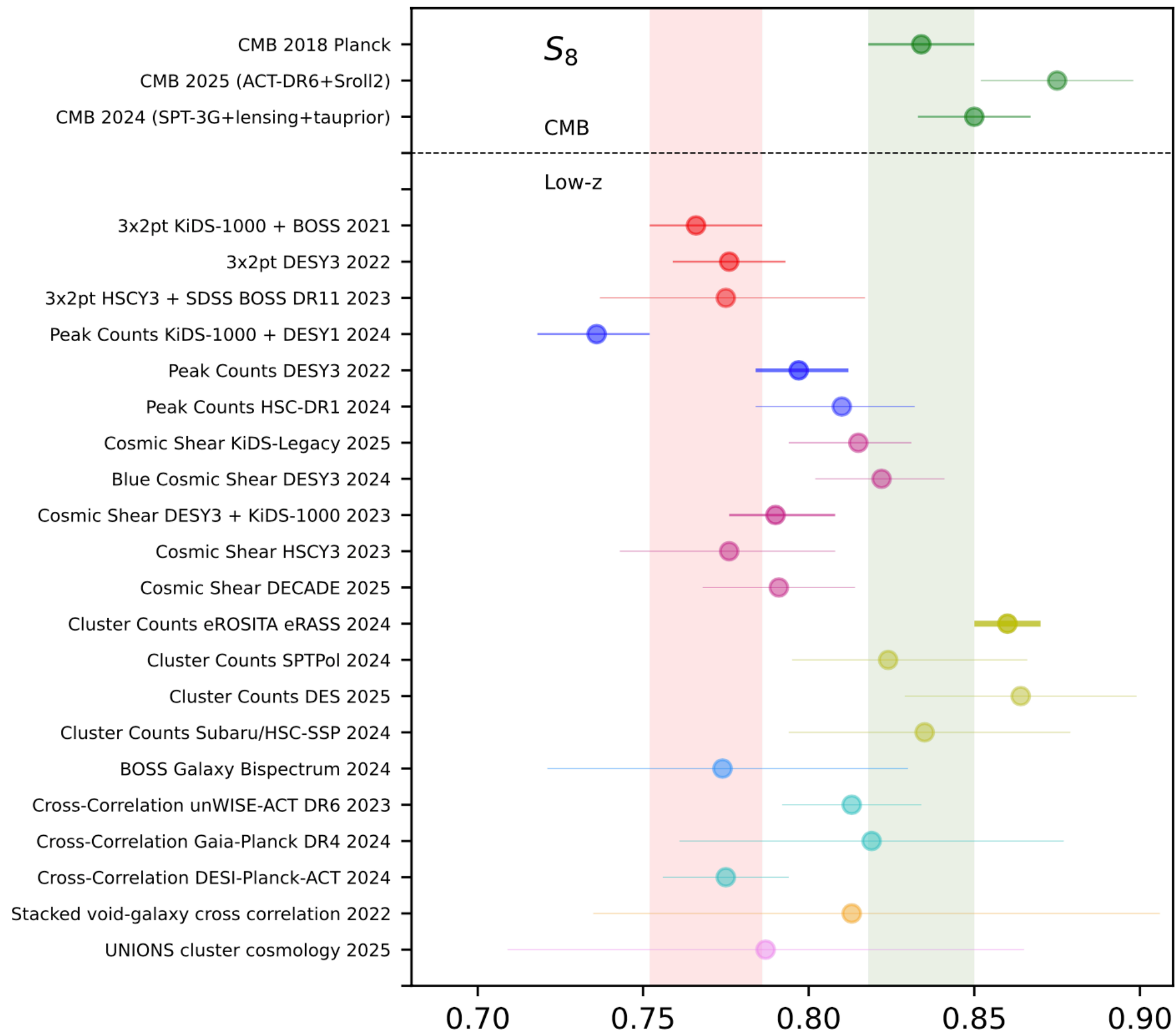
*Chabanier 1905.08103*

$$S_8 \equiv \sigma_8 \left( \frac{\Omega_m}{0.3} \right)^{0.5}$$

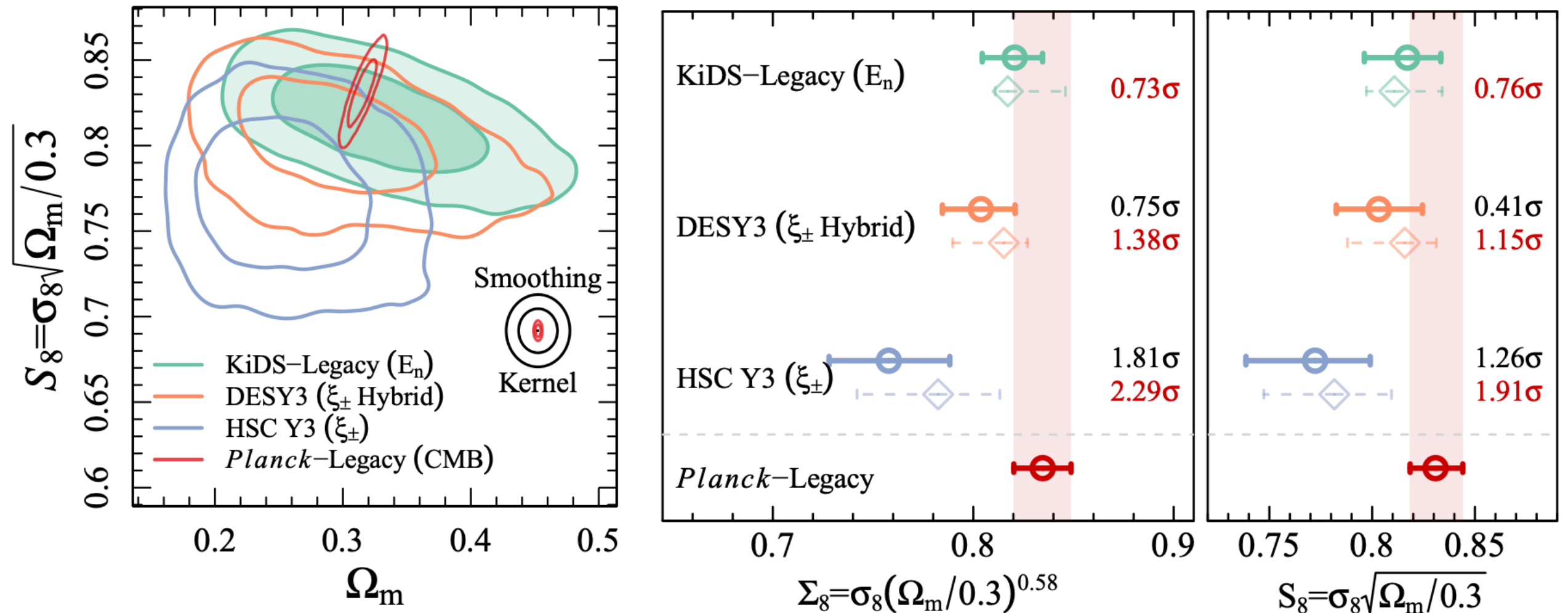
$$\sigma_8^2 = \int_0^\infty \frac{k^3}{2\pi^2} P_{\text{lin}}(k) W^2(kR) d\ln k$$

- The  $S_8$  parameter quantifies how “clumpy” the universe is on scales of  $\sim 30$  million-ly

# The S8 tension

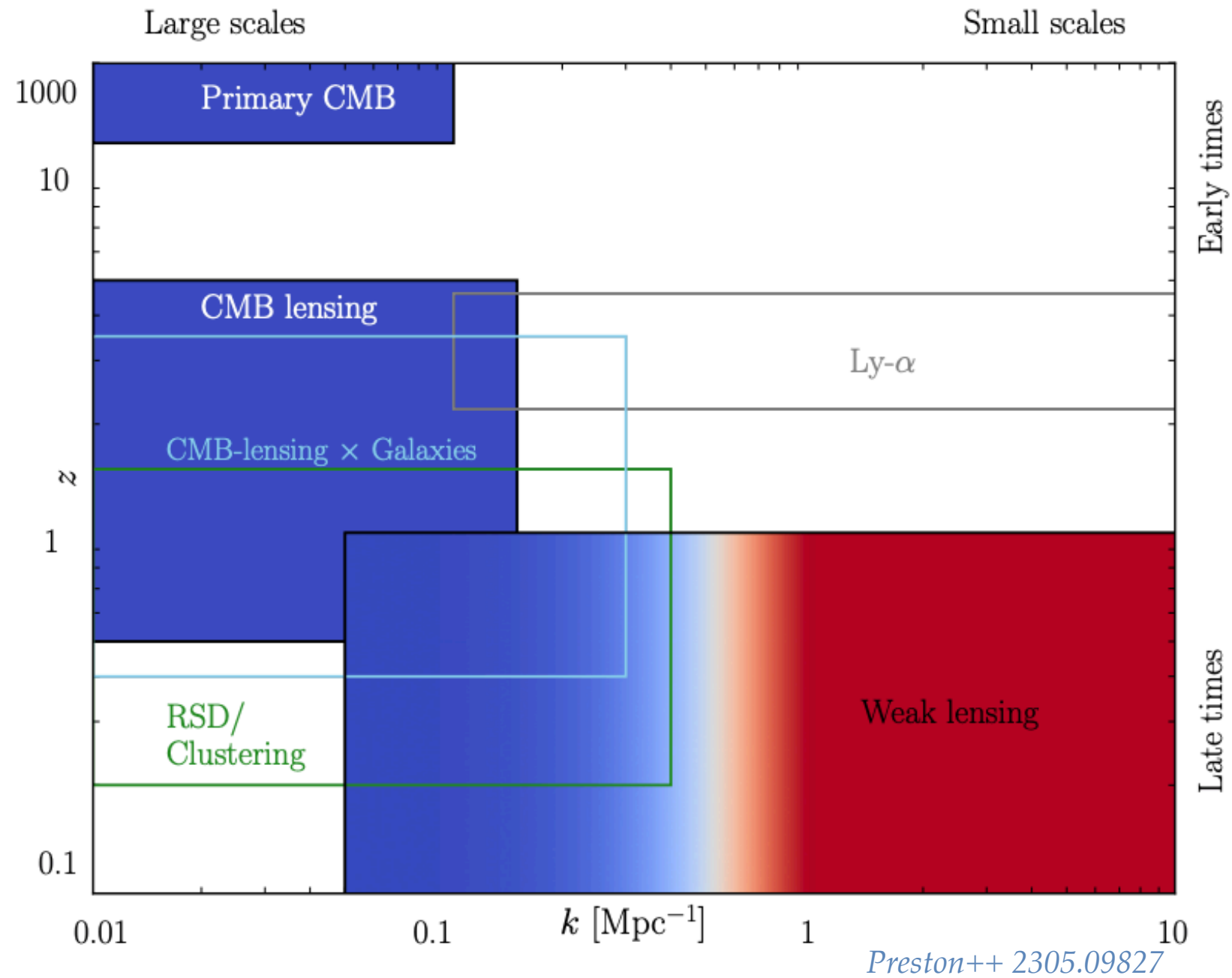


# The $S_8$ tension revisited



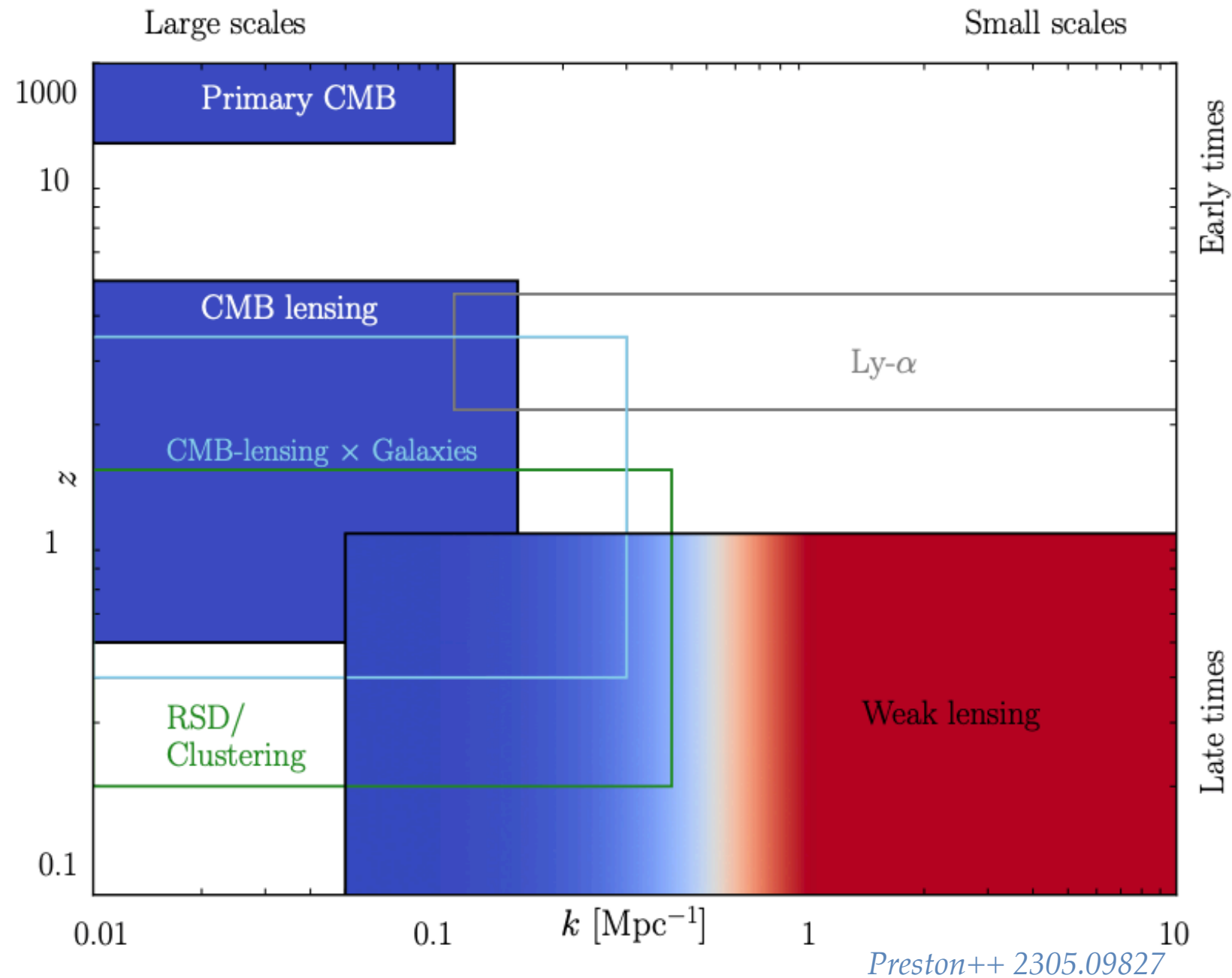
- Latest results from KIDS Legacy: improved redshift calibration has resolved the tension

# The general picture: what do we know about $P(k,z)$ ?



*Goldstein++ 2303.00746 , K. Rogers & VP 2311.16377*

# The general picture: what do we know about $P(k,z)$ ?



- Weak lensing measure smaller scales than galaxy cluster number counts! Power suppression at  $k \gtrsim 0.5 \text{ h/Mpc}$
- Lyman- $\alpha$  data may or may not favor a power suppression at  $z \sim 3$  and  $k \sim 0.7 \text{ Mpc}^{-1}$

*Goldstein++ 2303.00746 , K. Rogers & VP 2311.16377*

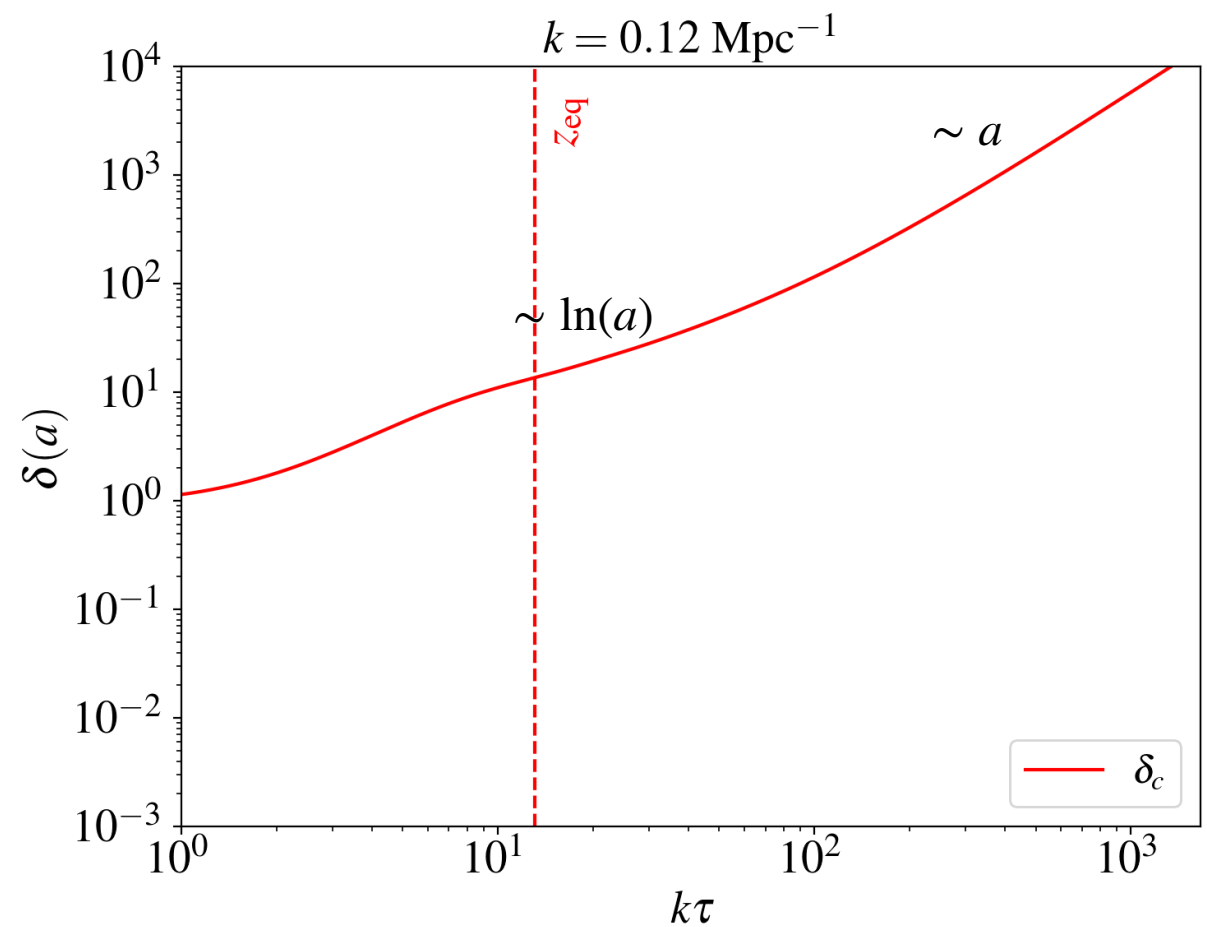
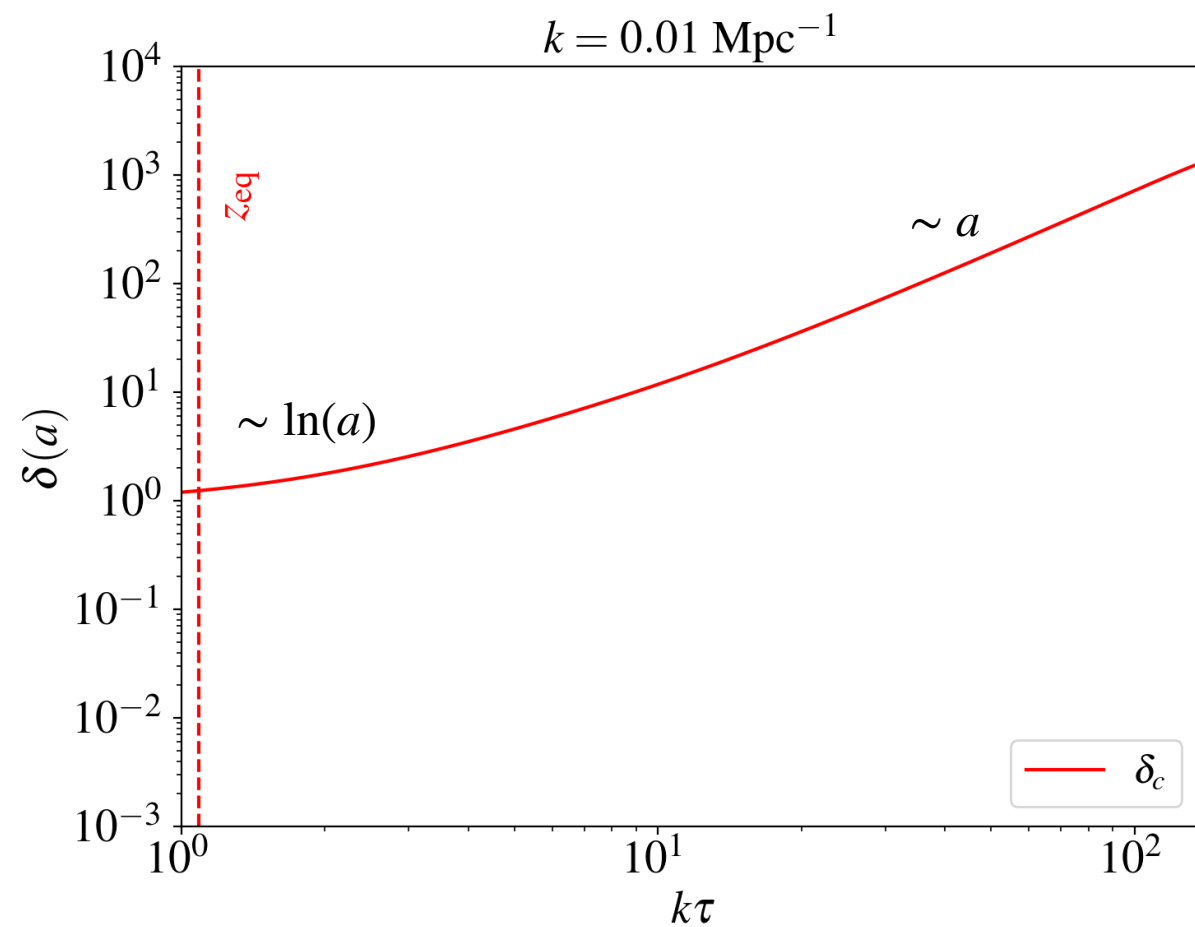


# The growth of CDM density perturbations

- Continuity & Euler equations for CDM perturbations (synchronous gauge):

$$\delta'_c = -\theta_c - \frac{1}{2}h', \quad \theta'_c = -\frac{a'}{a}\theta_c \quad \delta \equiv \delta\rho/\rho, \quad \theta \equiv kv \equiv 0$$

- For pressure-less, collision-less fluid: within the horizon, scale-independent growth.



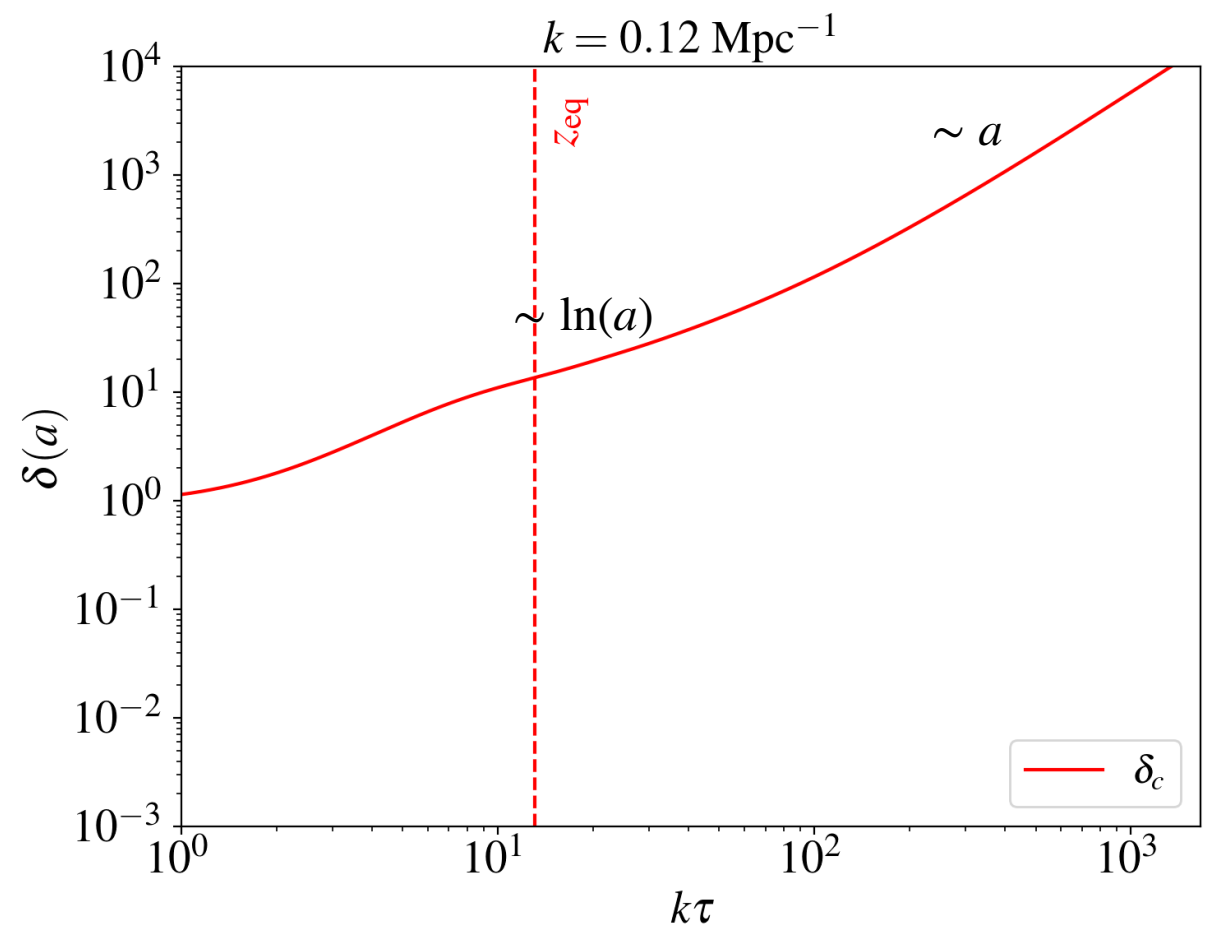
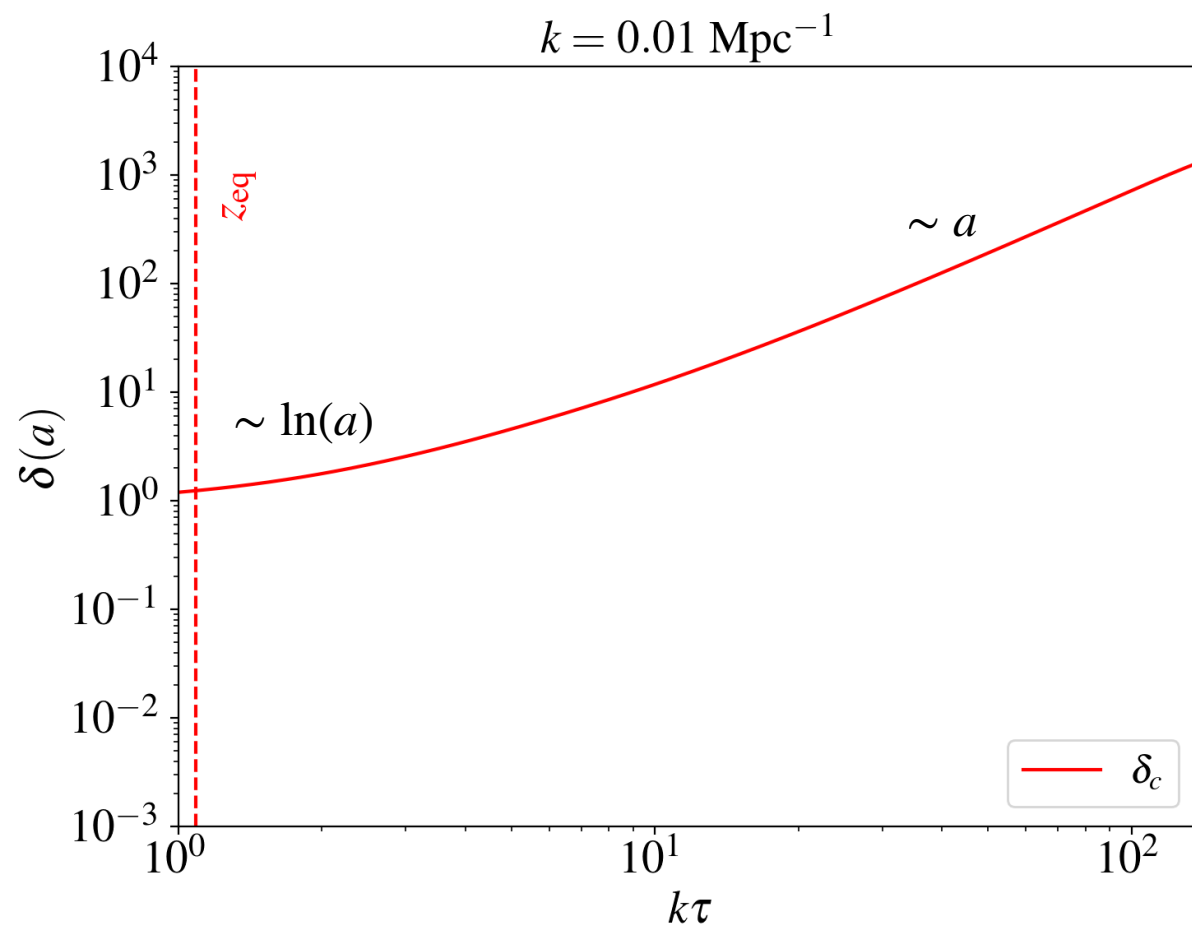
# How to decrease power at small scales

- If non-zero pressure:  $w = \frac{p}{\rho}$ ,  $c_a^2 = \frac{p'}{\rho'}$ ,  $c_s^2 = \frac{\delta p}{\delta \rho}$  can be non-zero

$$\delta'_{\text{ncdm}} = -(1+w) \left( \theta_{\text{ncdm}} - \frac{1}{2} h' \right) - 3 \frac{a'}{a} (c_s^2 - w) \delta_{\text{ncdm}}, \quad \theta'_{\text{ncdm}} = -\frac{a'}{a} (1 - 3c_a^2) \theta_{\text{ncdm}} + \frac{c_s^2}{1+w} - k^2 \sigma_{\text{ncdm}}$$

- One can write a formal equation driving the growth of perturbation on small scales:

$$k\tau \gg 1 \Rightarrow \delta''_{\text{ncdm}} + \frac{a'}{a} \delta'_{\text{ncdm}} + (k^2 - k_J^2) c_s^2 \delta_{\text{ncdm}} = 0 \quad k_J \equiv \sqrt{\frac{3(a'/a)}{c_s^2}}$$



# The case of neutrinos

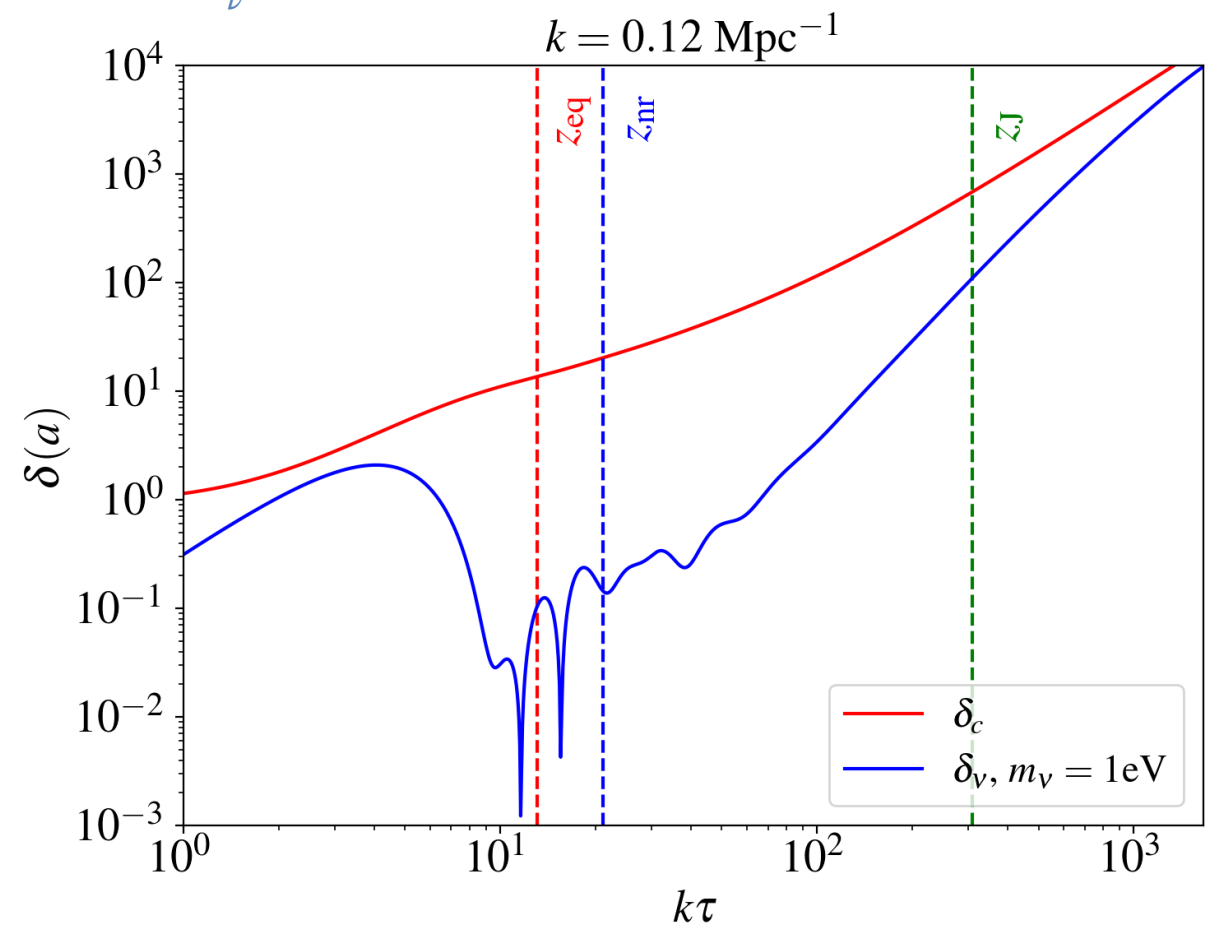
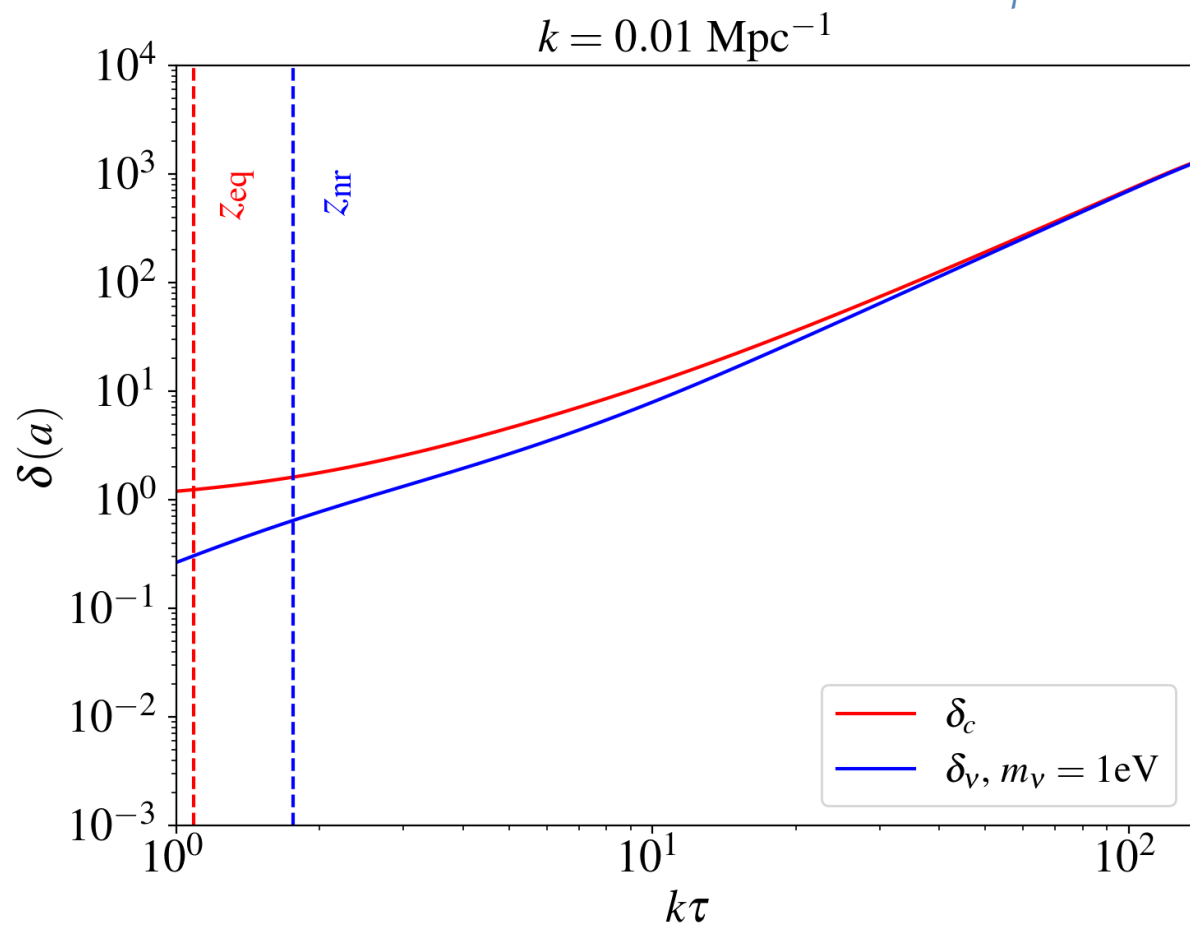
- If non-zero pressure:  $w = \frac{p}{\rho}$ ,  $c_a^2 = \frac{p'}{\rho'}$ ,  $c_s^2 = \frac{\delta p}{\delta \rho}$  can be non-zero

$$\delta'_{\text{ncdm}} = -(1+w) \left( \theta_{\text{ncdm}} - \frac{1}{2} h' \right) - 3 \frac{a'}{a} (c_s^2 - w) \delta_{\text{ncdm}}, \quad \theta'_{\text{ncdm}} = -\frac{a'}{a} (1 - 3c_a^2) \theta_{\text{ncdm}} + \frac{c_s^2}{1+w} - k^2 \sigma_{\text{ncdm}}$$

- One can write a formal equation driving the growth of perturbation on small scales:

$$k\tau \gg 1 \Rightarrow \delta''_{\text{ncdm}} + \frac{a'}{a} \delta'_{\text{ncdm}} + (k^2 - k_J^2) c_s^2 \delta_{\text{ncdm}} = 0 \quad k_J \equiv \sqrt{\frac{3(a'/a)}{c_s^2}}$$

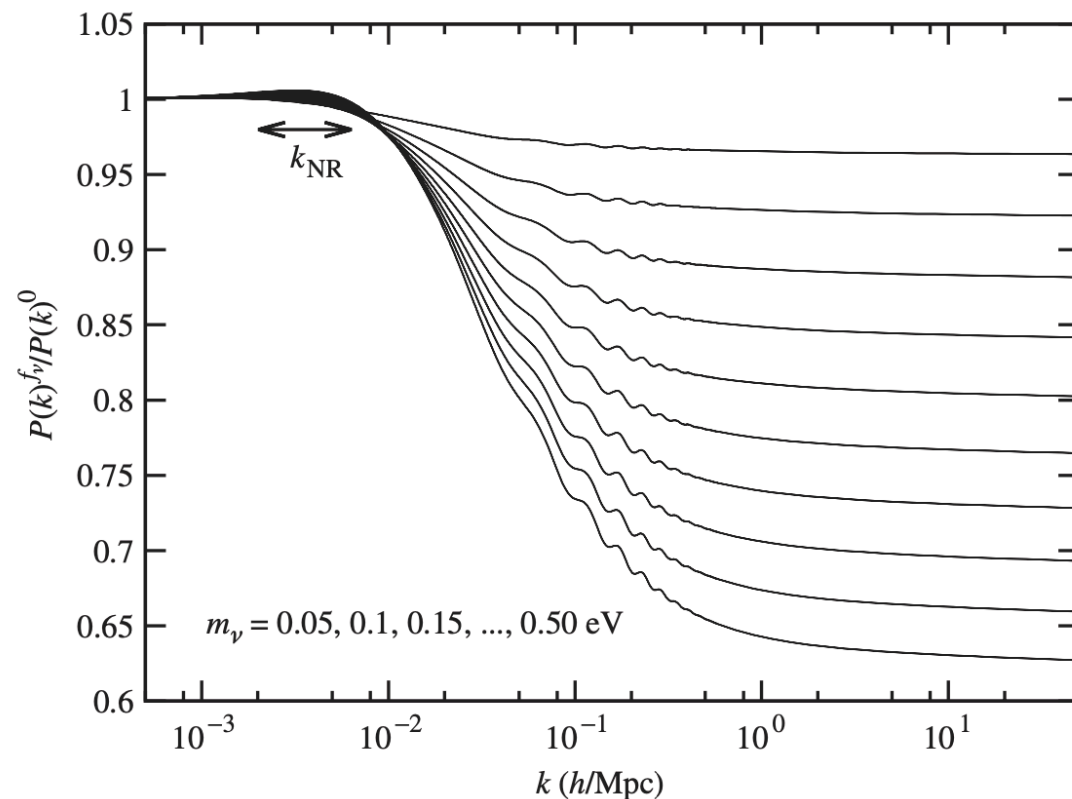
*Example: thermal neutrinos with  $m_\nu = 1 \text{ eV}$*



# Could $\nu$ 's explain the $S_8$ tension?

Power suppression:  $k \geq k_{\text{nr}} \equiv 0.01 \left( \frac{m_\nu}{1\text{eV}} \right)^{1/2} \left( \frac{\Omega_m}{0.3} \right)^{1/2} h \text{Mpc}^{-1}$  with amplitude  $\frac{\Delta P}{P} \simeq -8 \frac{\omega_\nu}{\omega_m}$

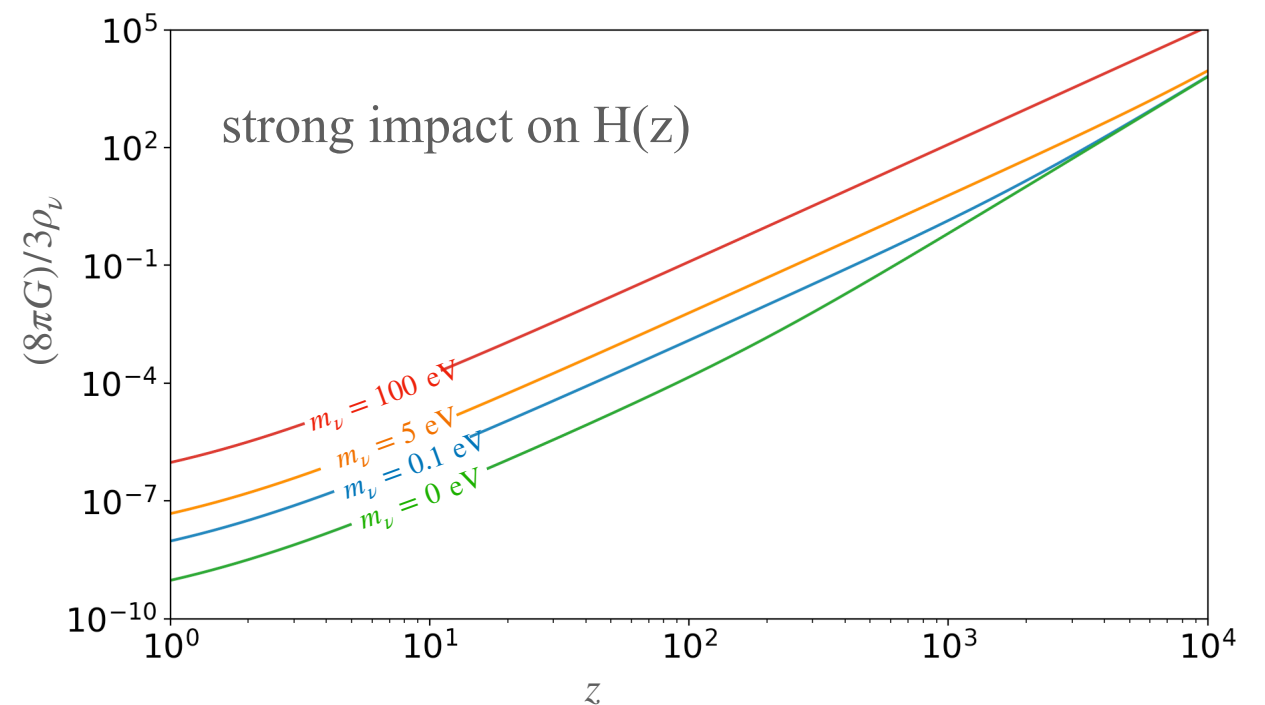
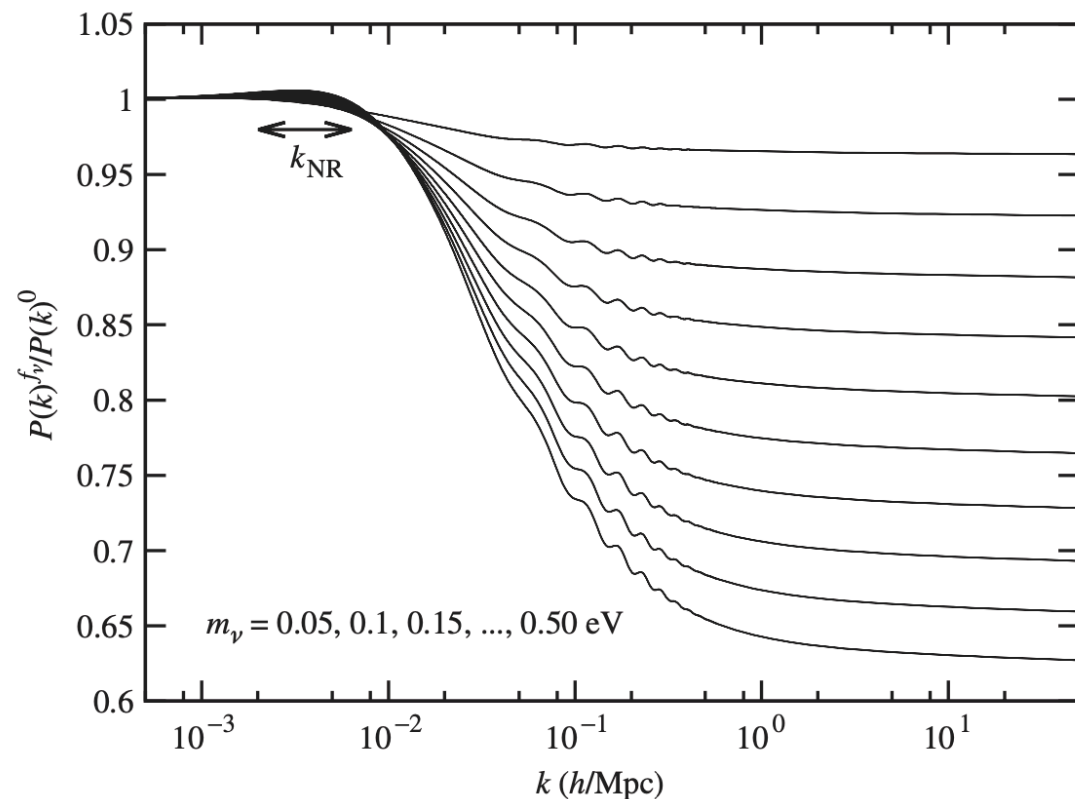
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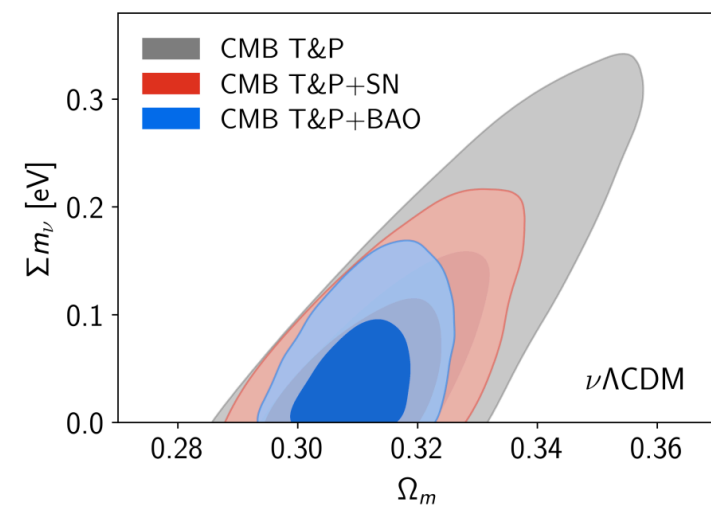
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Planck 2018 + BAO  $< 0.12 \text{ eV}$

Planck 1807.06205

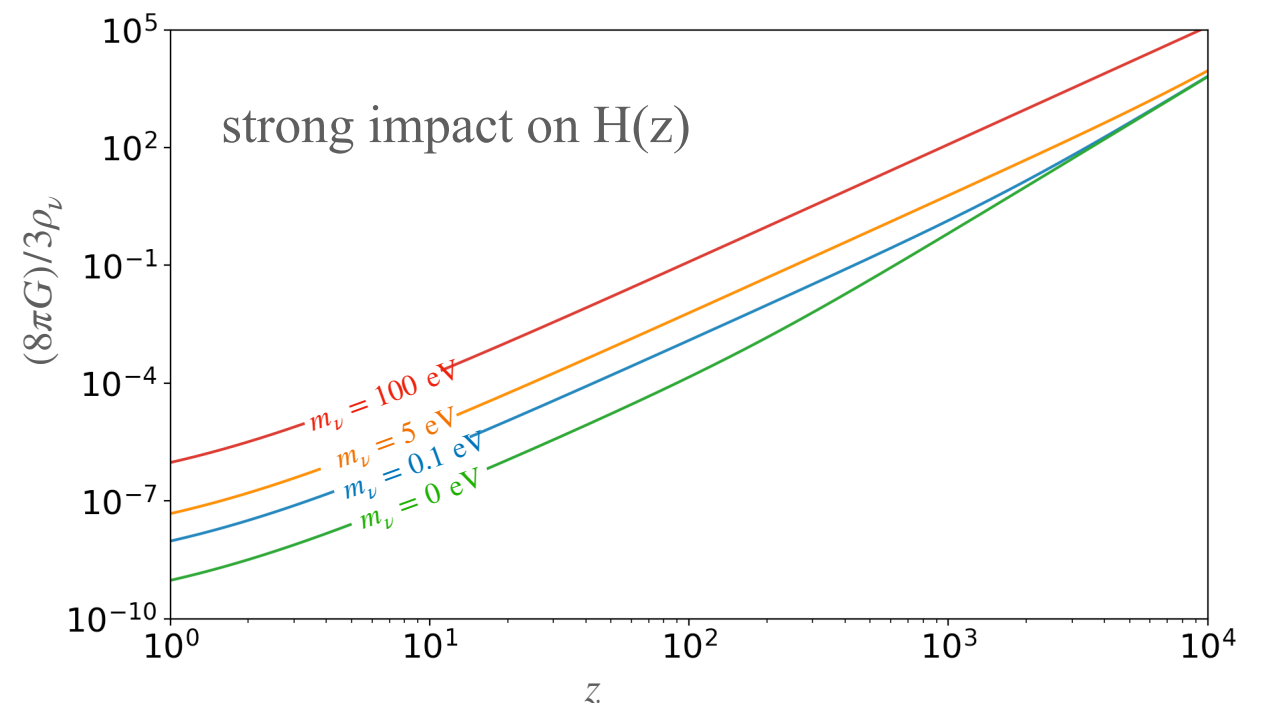
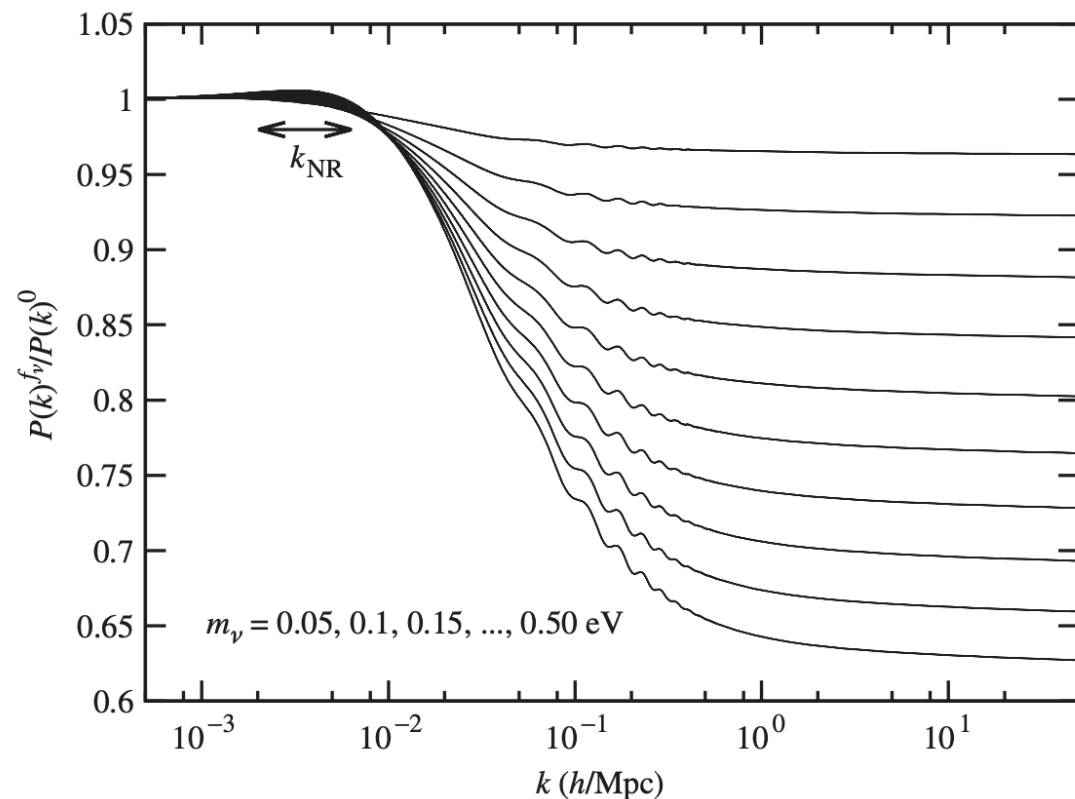




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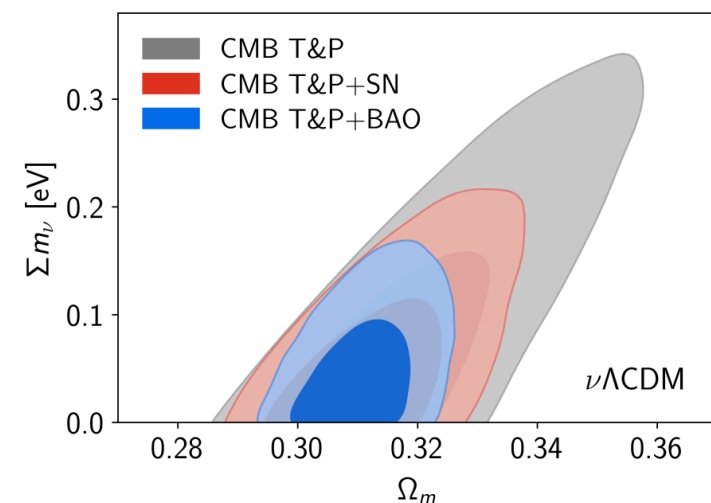
*Planck* 1807.06205

*Planck* 2018 + BAO + Ly- $\alpha$   $< 0.089\text{eV}$

*Palanque-Delabrouille++* 1911.09073

*Planck* 2018 + BOSS + eBOSS  $< 0.082\text{eV}$

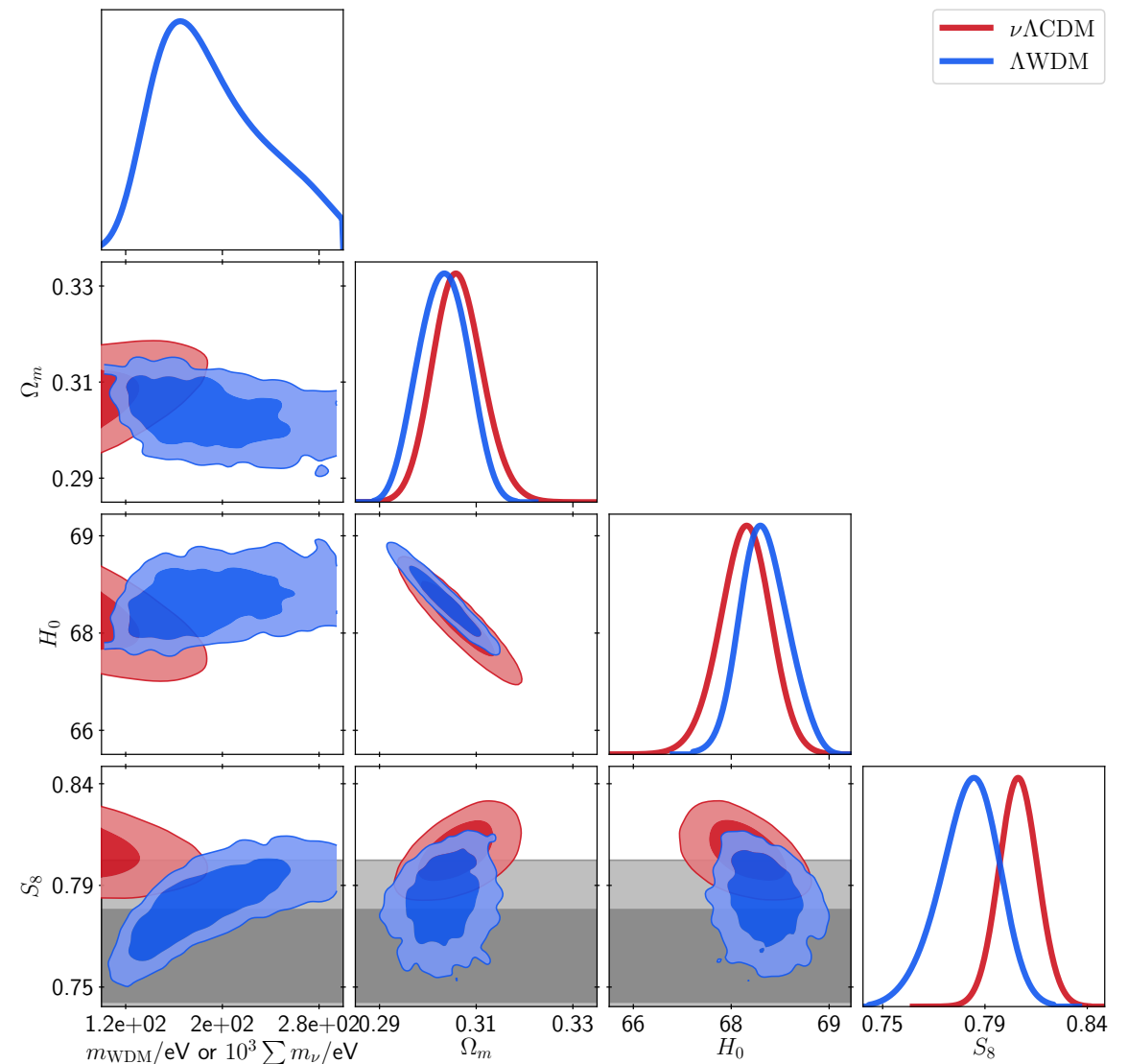
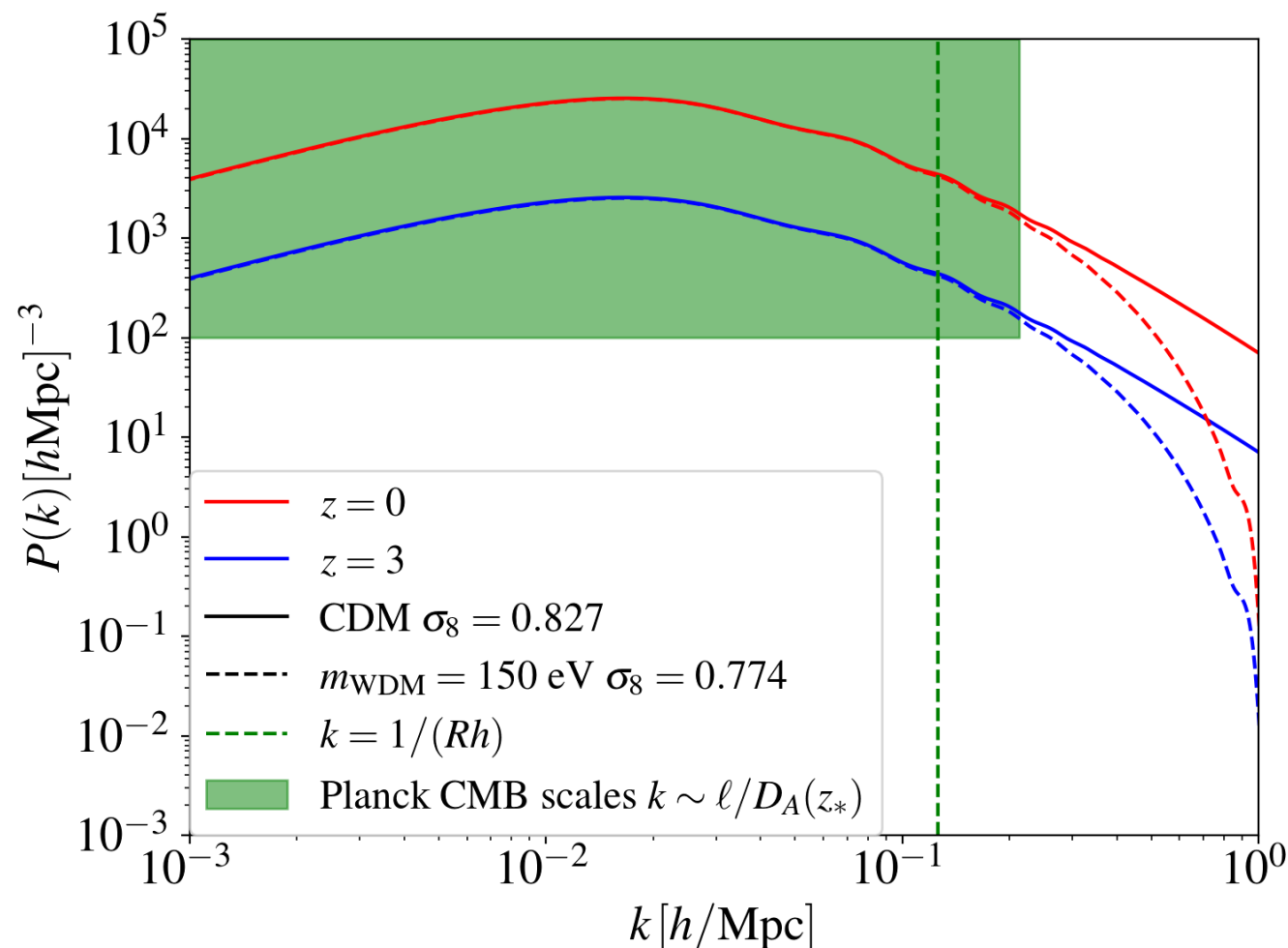
*Brieden++* 2204.11868, *Simon++* 2210.14931



# The case of warm dark matter

- For WDM: suppression at  $k \geq k_{\text{FS}} \sim 5 \text{ Mpc}^{-1} \left( \frac{m_{\text{WDM}}}{1 \text{ keV}} \right) \left( \frac{T_\nu}{T_{\text{WDM}}} \right)$
- Requiring  $k_{\text{FS}} \geq 0.1 h/\text{Mpc}$  and  $\omega_{\text{nCDM}} = \omega_{\text{CDM}}$  leads to  $m_{\text{WDM}} \sim 100 \text{ eV}$ .

*Viel++ astro-ph/0501562*



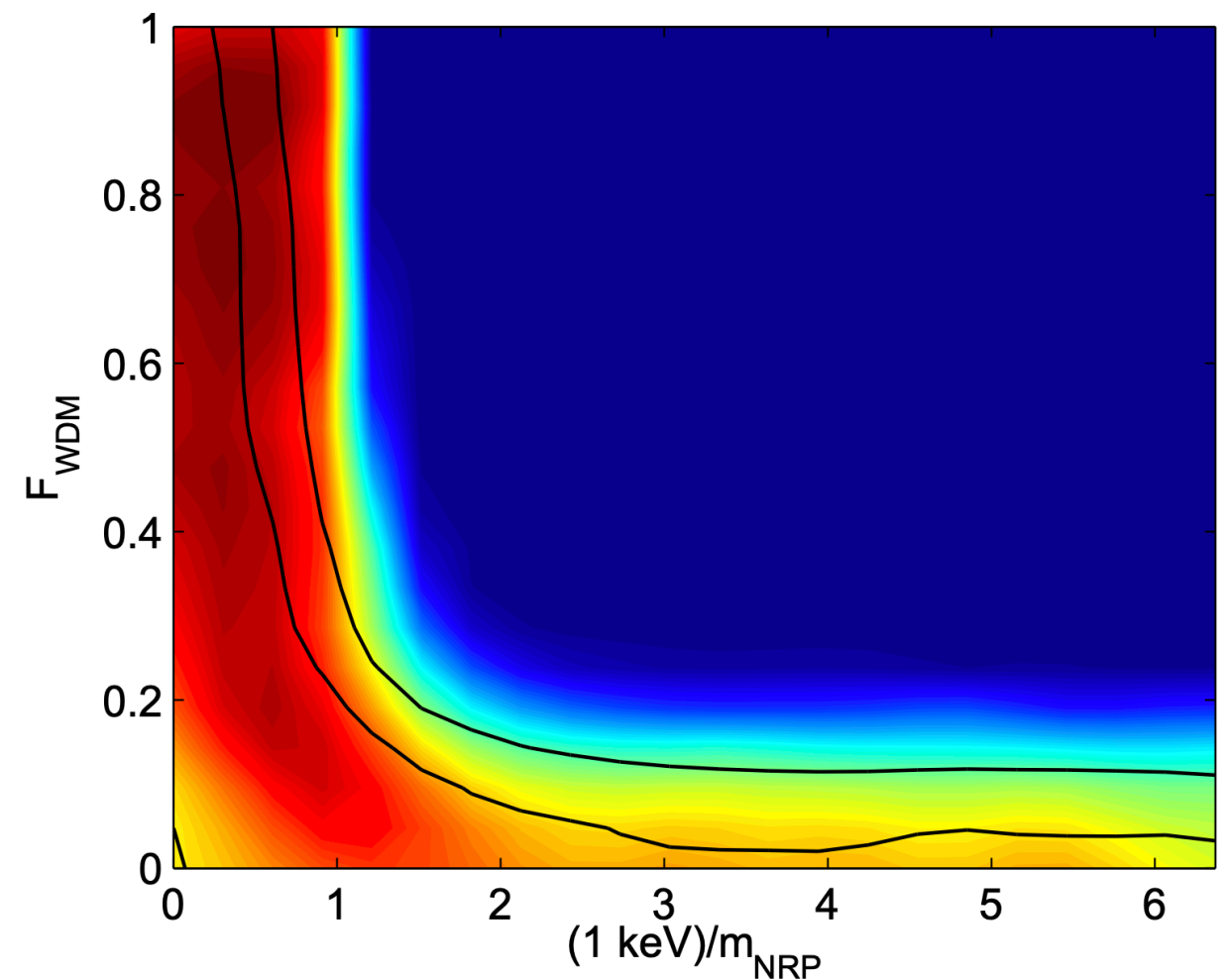
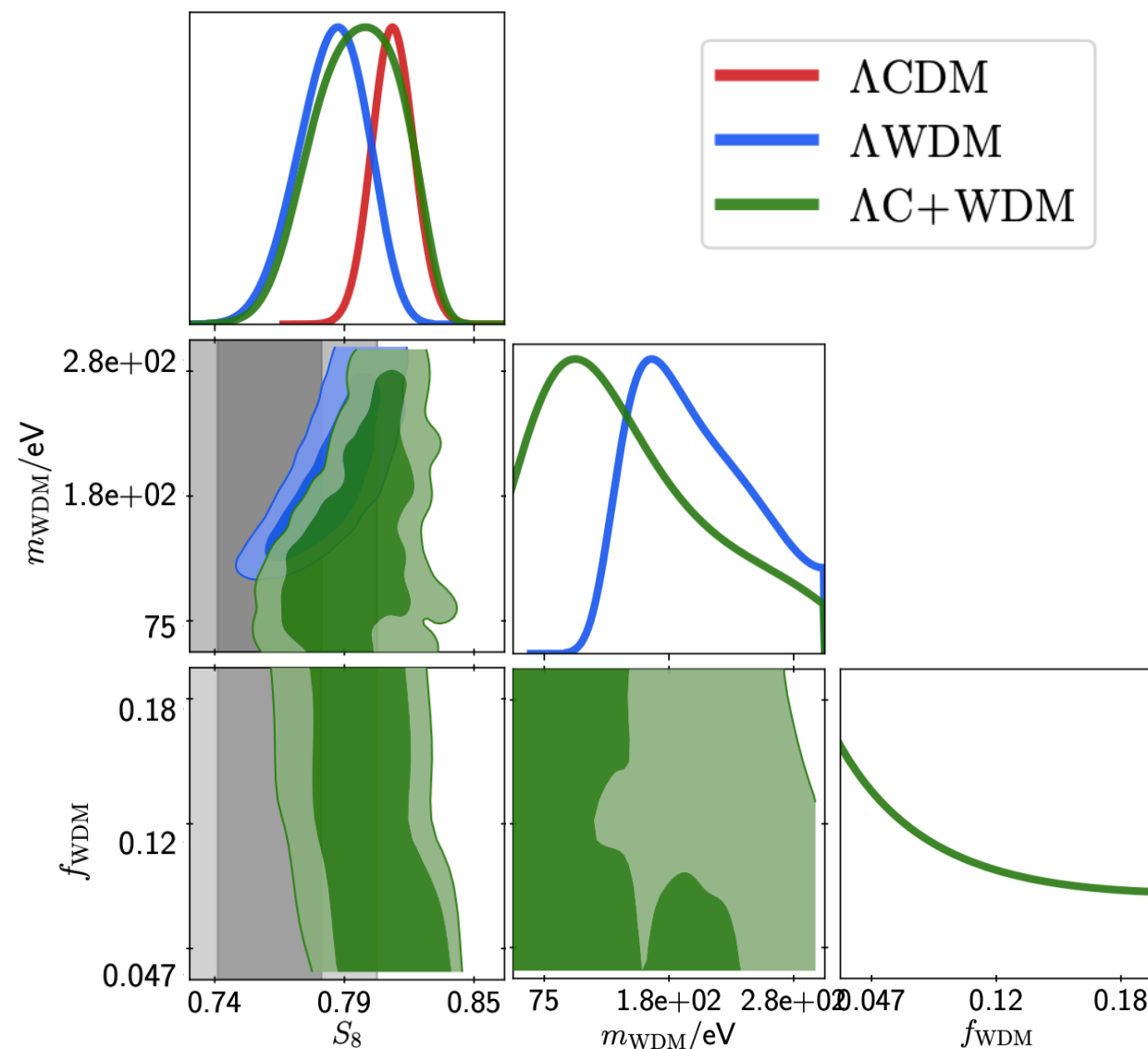
- CMB + BAO +  $S_8$   $m_{\text{WDM}} \simeq 192.2^{+31}_{-60} \text{ eV}$ .

- Yet, exponential cutoff ‘a la WDM’ are excluded:  $m_{\text{WDM}} > 5 \text{ keV}$ .

*Palanque-Delabrouille++ 1911.09073*

# Fraction of Warm Dark Matter and $S_8$

Boyarski, Lesgourgues ++ 0812.0010



- A fraction of thermal WDM with  $m \sim \mathcal{O}(100\text{eV})$  could explain low  $S_8$ : Ly- $\alpha$  restricts  $f_{\text{WDM}} \lesssim 0.2$

See also Gariazzo++ [1704.02991](#)

- How to generate a fraction of WDM?

- Nb: similar results with fraction of fuzzy dark matter / tightly coupled fraction of DM

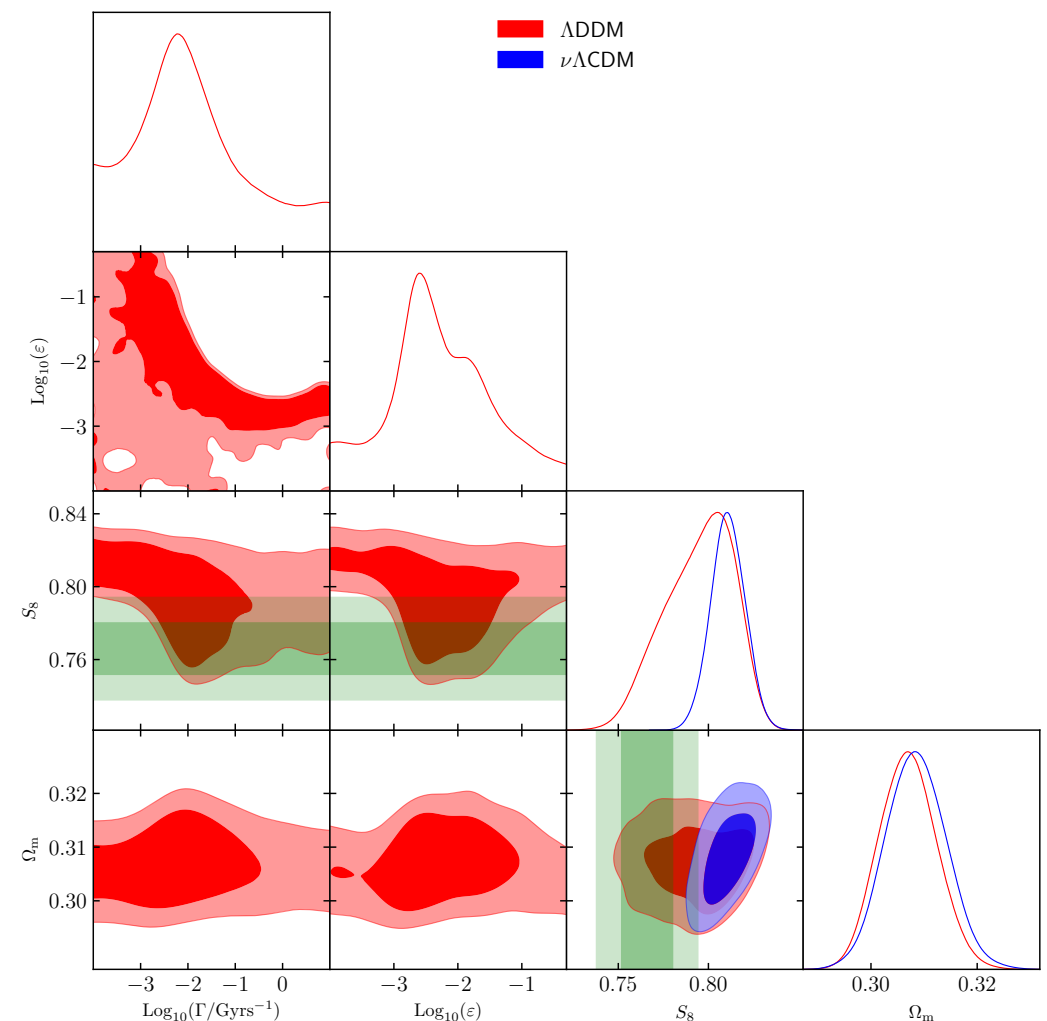
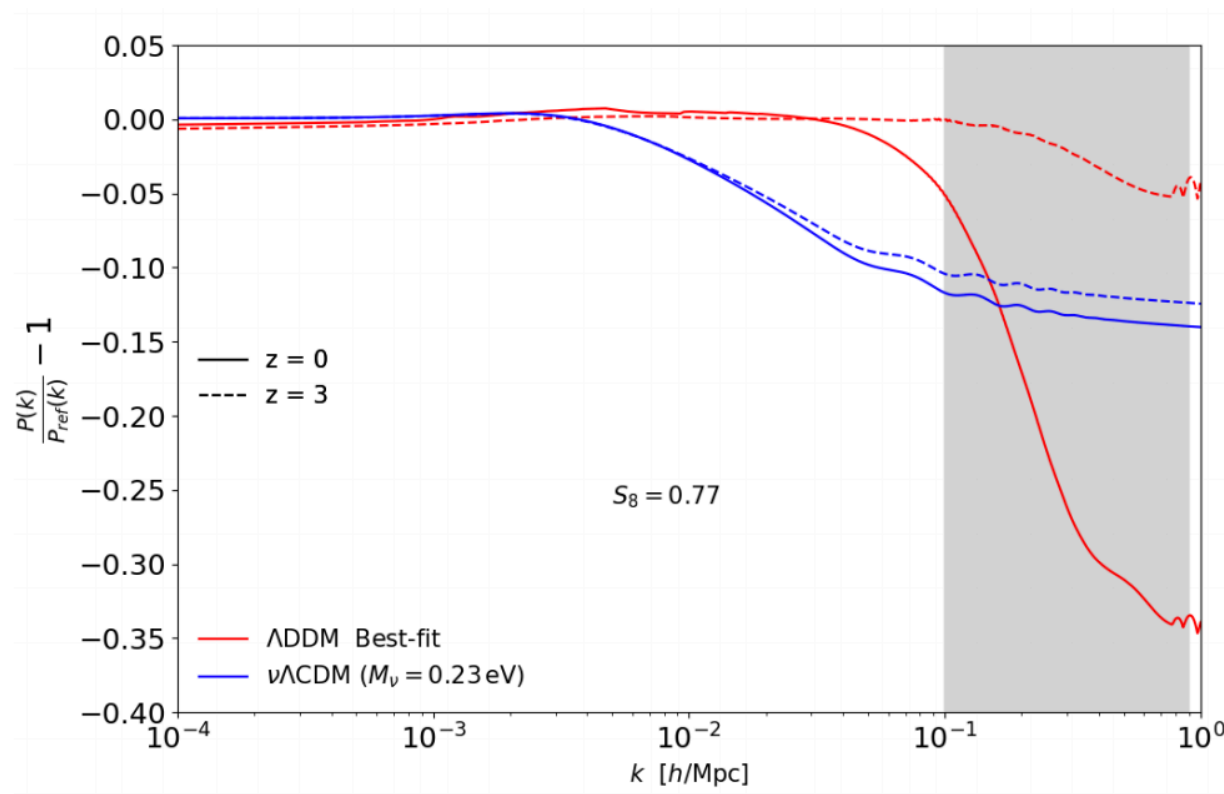
Chacko++ [1609.03569](#), Allali++ [2104.12798](#), Laguë++ [2104.07802](#)

# DM decays generate a late-time suppression

- Standard neutrinos are largely excluded as a solution: need  $M_\nu \simeq 0.23$  eV but  $M_\nu \lesssim 0.08 - 0.12$  eV  
*Palanque-Delabrouille++ 1911.09073 ; Brieden++ 2204.11868 ; Simon (VP)++ 2210.14931*

- $\Lambda$ CDM + two free parameters: the CDM decay rate  $\Gamma$  and the branching ratio to DR  $\varepsilon \equiv \left( \frac{1}{2} - \frac{m_{\text{WDM}}^2}{m_{\text{DCDM}}^2} \right) \simeq v_{\text{wdm}}/c$

$$\begin{aligned}\dot{\bar{\rho}}_{\text{dcdm}} &= -3\mathcal{H}\bar{\rho}_{\text{dcdm}} - a\Gamma\bar{\rho}_{\text{dcdm}}, \\ \dot{\bar{\rho}}_{\text{dr}} &= -4\mathcal{H}\bar{\rho}_{\text{dr}} + \varepsilon a\Gamma\bar{\rho}_{\text{dcdm}}, \\ \dot{\bar{\rho}}_{\text{wdm}} &= -3(1+w)\mathcal{H}\bar{\rho}_{\text{wdm}} + (1-\varepsilon)a\Gamma\bar{\rho}_{\text{dcdm}}.\end{aligned}$$



- DM with  $\Gamma^{-1} \simeq 55(\varepsilon/0.007)^{1.4}$  Gyrs can explain low  $S_8$  ( $1.3\sigma$  agreement)

*Abellan++ 2008.09615 & 2104.03329*

See also *Davari&khosravi 2203.09439, Clark++ 2110.09562*

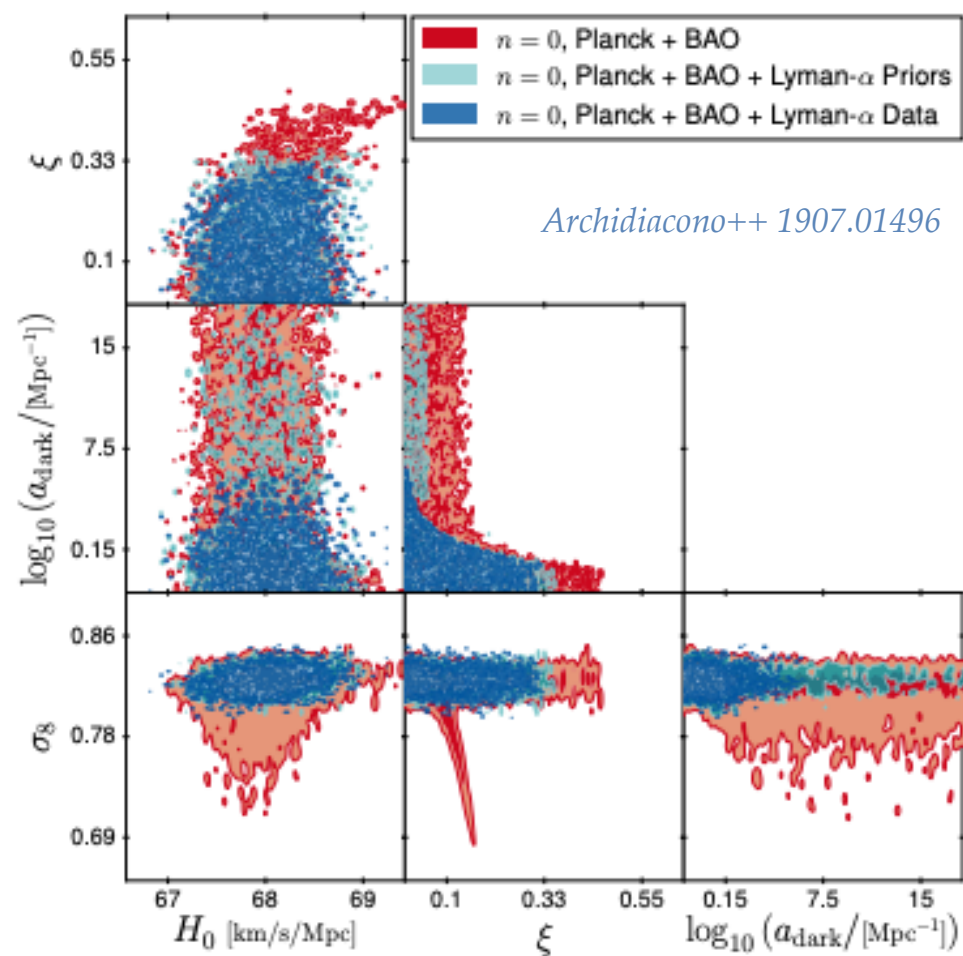
# The $S_8$ tension is a drag...

DM<=>DR

$$\dot{\delta}_{\text{DM}} + \theta_{\text{DM}} - 3\dot{\phi} = 0,$$

$$\dot{\theta}_{\text{DM}} - k^2 c_{\text{DM}}^2 \delta_{\text{DM}} + \mathcal{H} \theta_{\text{DM}} - k^2 \psi = \Gamma_{\text{DM-DR}} (\theta_{\text{DM}} - \theta_{\text{DR}}),$$

$$\Gamma_{\text{DR-DM}} = -\Omega_{\text{DM}} h^2 a_{\text{dark}} \left( \frac{1+z}{1+z_d} \right)^n, \quad \xi = T_{\text{DR}}/T_{\gamma}$$

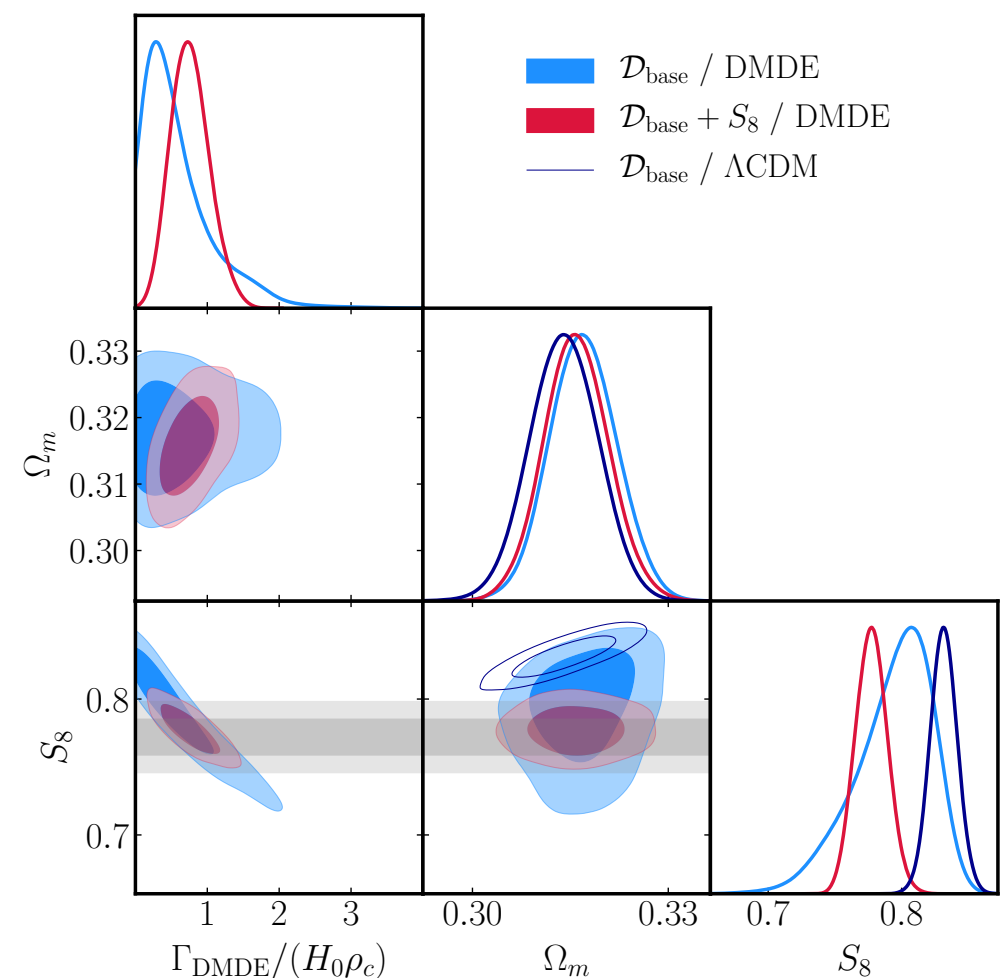


DM<=>DE

*VP, Bernal, Kovetz, Kamionkowski 2209.06217*

$$\theta'_{\text{DM}} = -\frac{a'}{a} \theta_{\text{DM}} + k^2 \psi + \Gamma_{\text{DMDE}}(a) (\theta_{\text{DE}} - \theta_{\text{DM}}),$$

$$\theta'_{\text{DE}} = -(1 - 3c_{s,\text{DE}}^2) \frac{a'}{a} \theta_{\text{DE}} + \frac{k^2 c_{s,\text{DE}}^2}{(1 + w_{\text{DE}})} \delta_{\text{DE}} + k^2 \psi - \Gamma_{\text{DMDE}}(a) R (\theta_{\text{DE}} - \theta_{\text{DM}}),$$

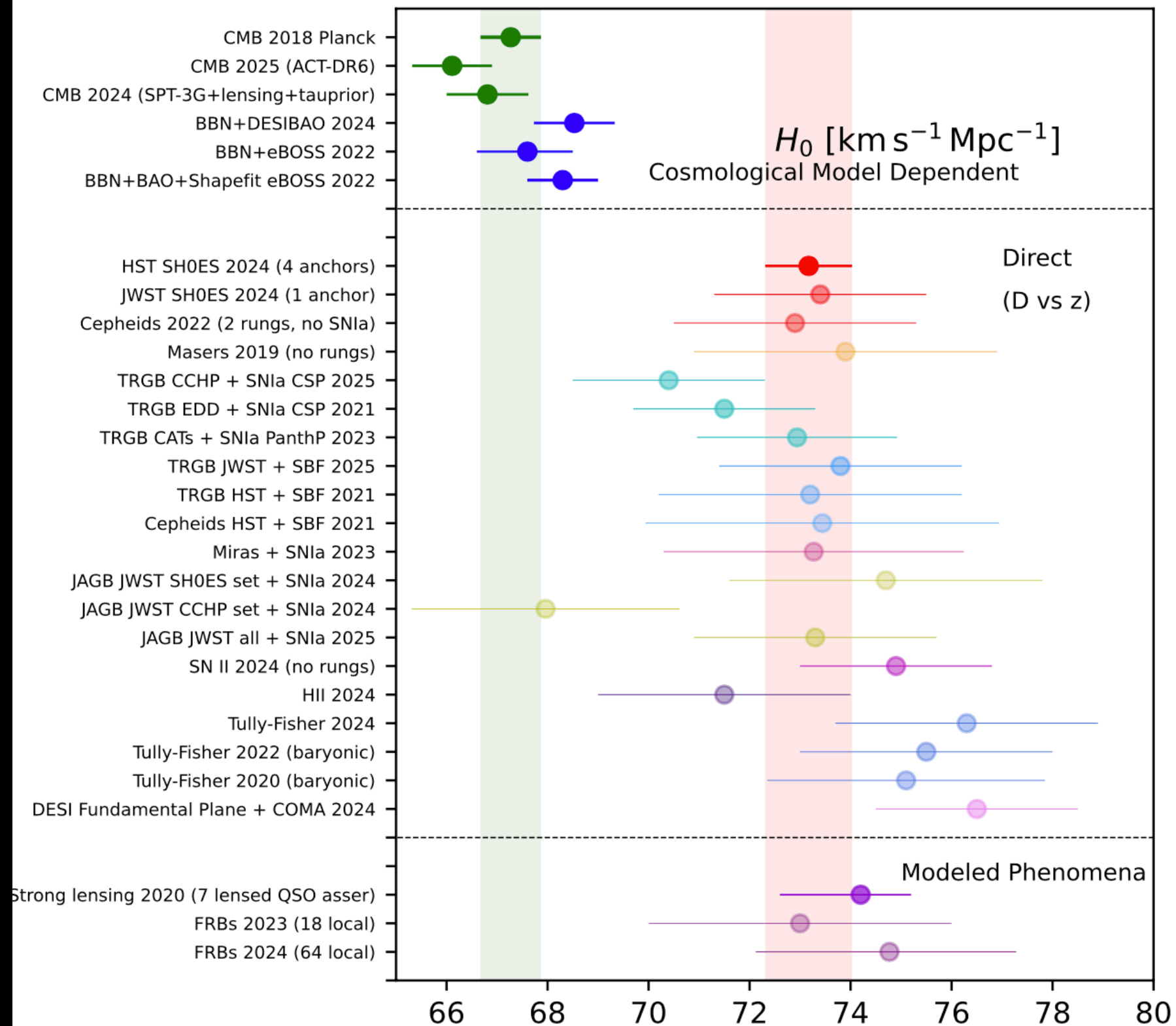


- Non-Abelian dark matter model, Cannibal dark matter, also with sub-component of strongly interacting DM

*Buen-Abad++1505.03542, Lesgourgues++1507.04351, Heimersheim++ 2008.08486, Chacko++1609.03569, Buen-Abad++ 1708.09406, Raveri++ 1709.04877*



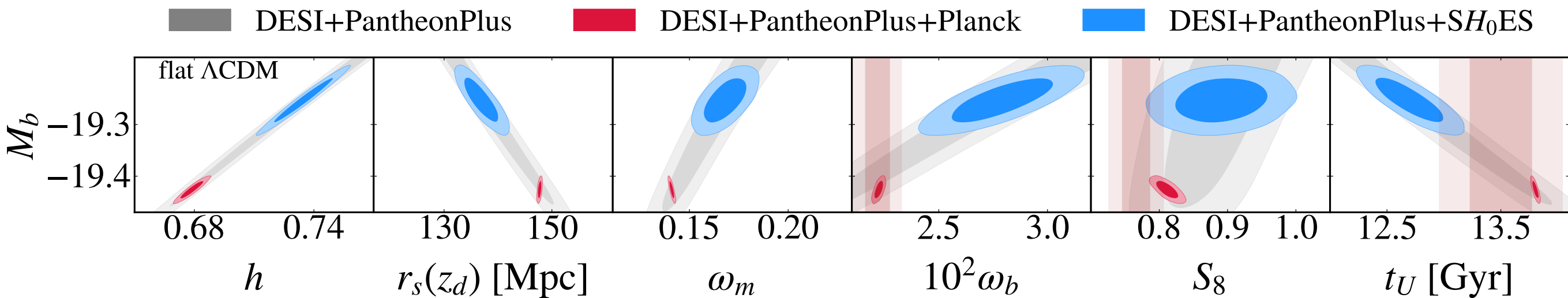
# The Hubble tension



- We are still tracking “unknown unknowns”

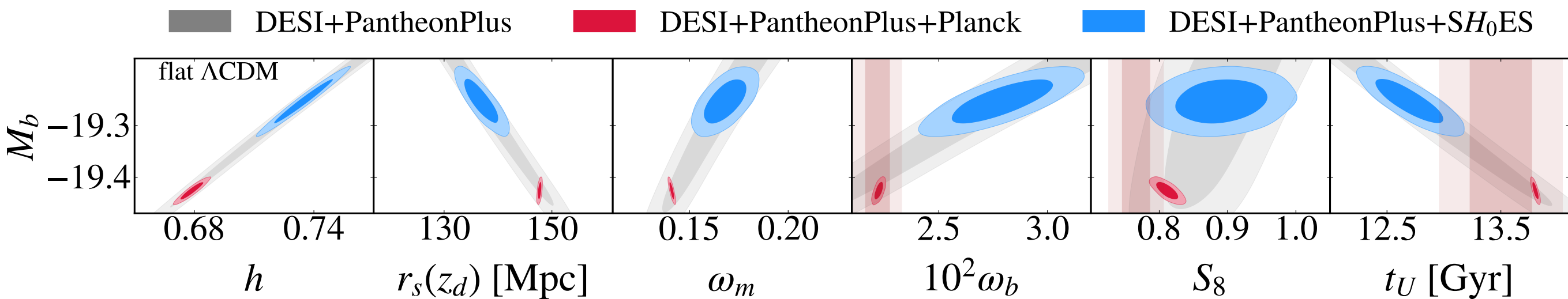
# Stop calling it $H_0$ tension!

- The “ $H_0$  tension” should really be called **cosmic calibration tension**
- Calibrating the ladder has implications beyond the value of  $H_0$ : **smaller  $t_U$ , larger  $\omega_m$ ,  $\omega_b$  and  $S_8$**



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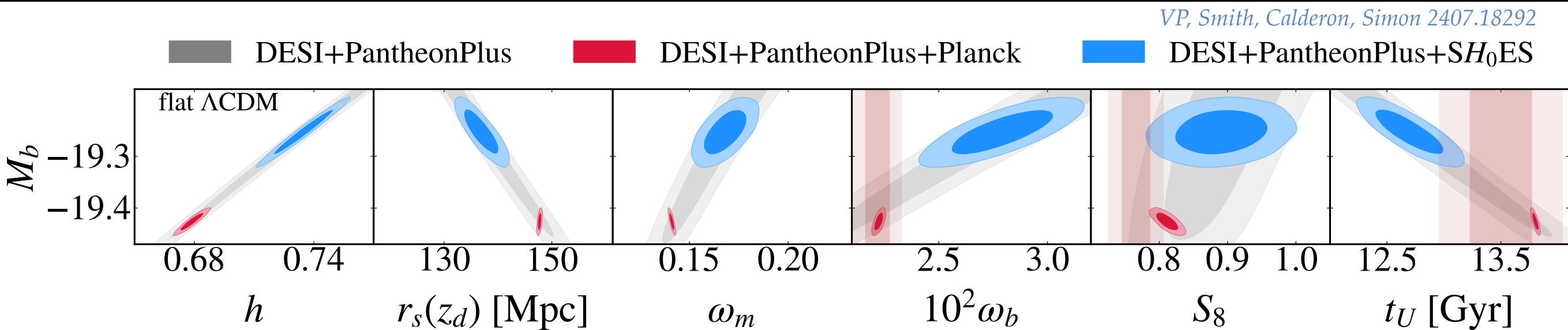
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- New physics must reduce the sound horizon  $r_s$  and accommodate larger  $\omega_m$ .
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- Or maybe need **new degrees of freedom** at both early- and late-times?

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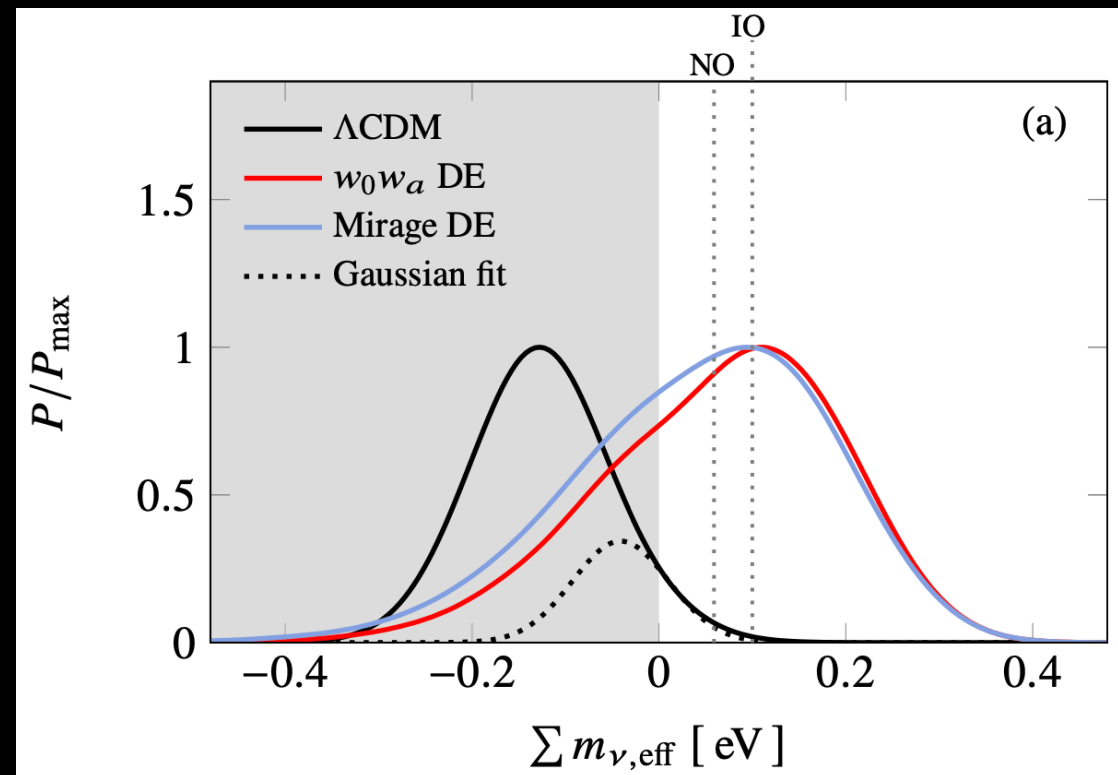
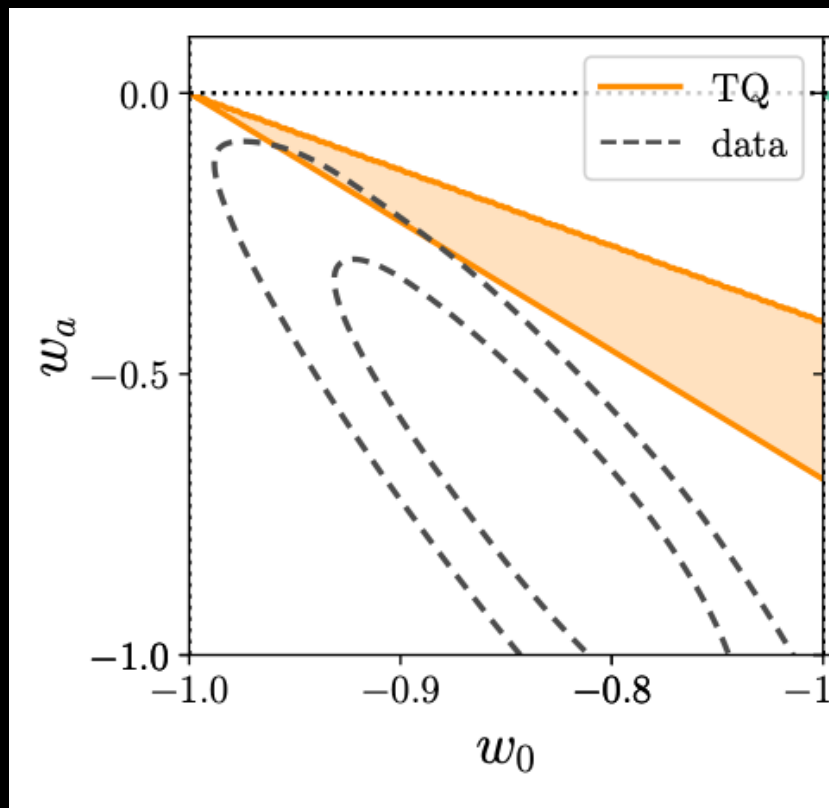


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- Or maybe need **new degrees of freedom at both early- and late-times?**

• We haven't found the solution yet, but there is a lot we understand!

# A new DESI tension?

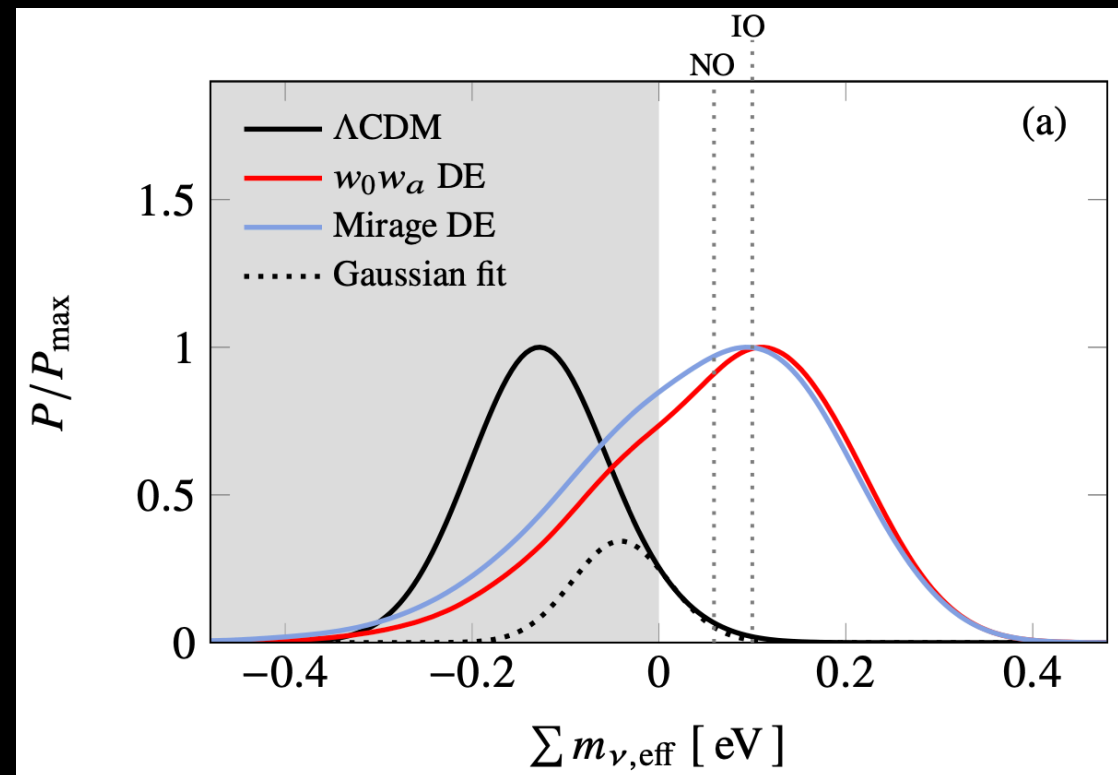
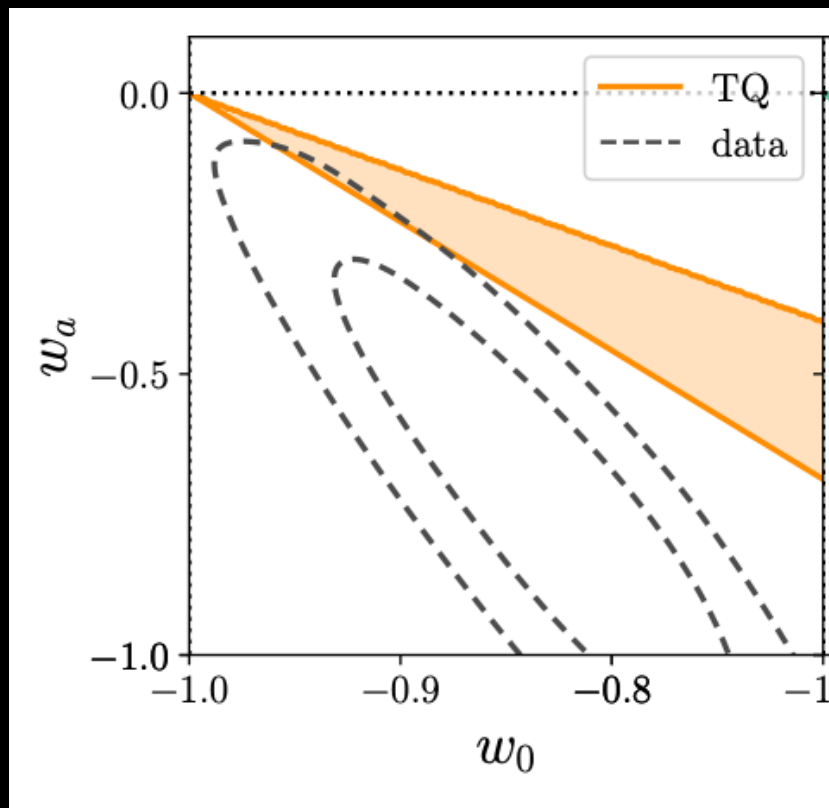
- DESI + CMB in  $2.3\sigma$  tension, DESI+CMB in tension with SN1a at  $2-3\sigma$
- This can be explained by Dynamical Dark Energy ==> non-canonical quintessence
- Mirage Dark Energy is favored: weird?





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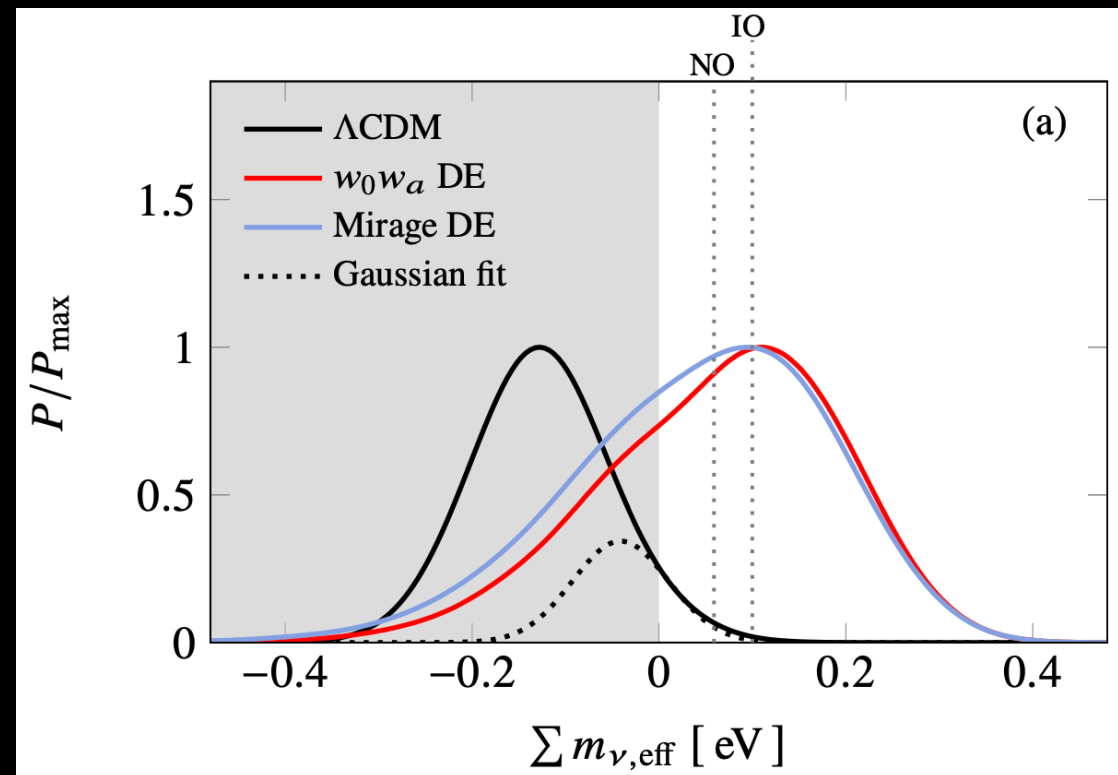
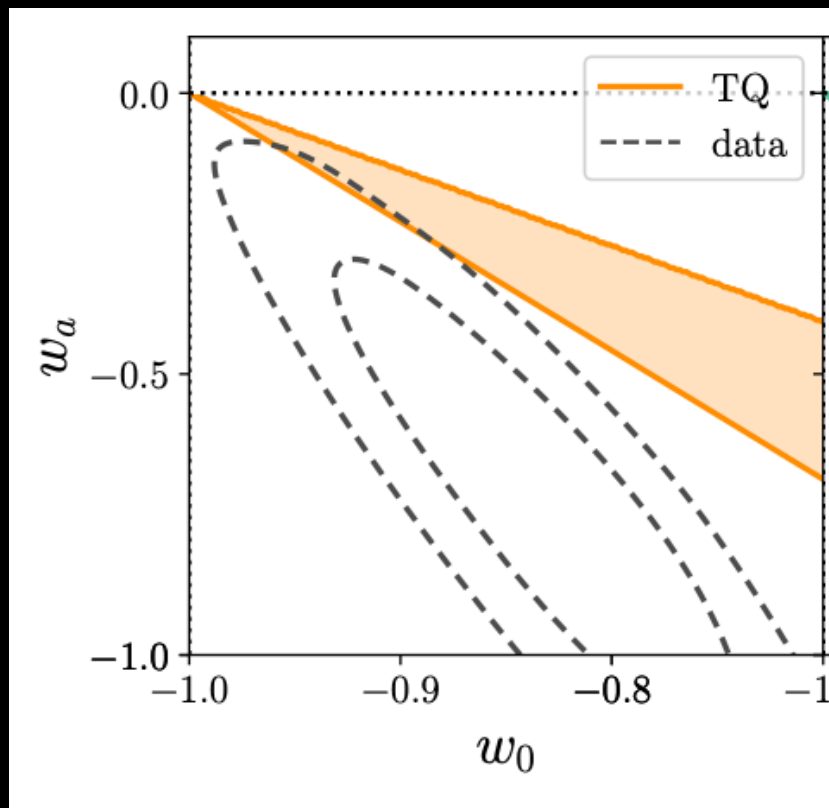
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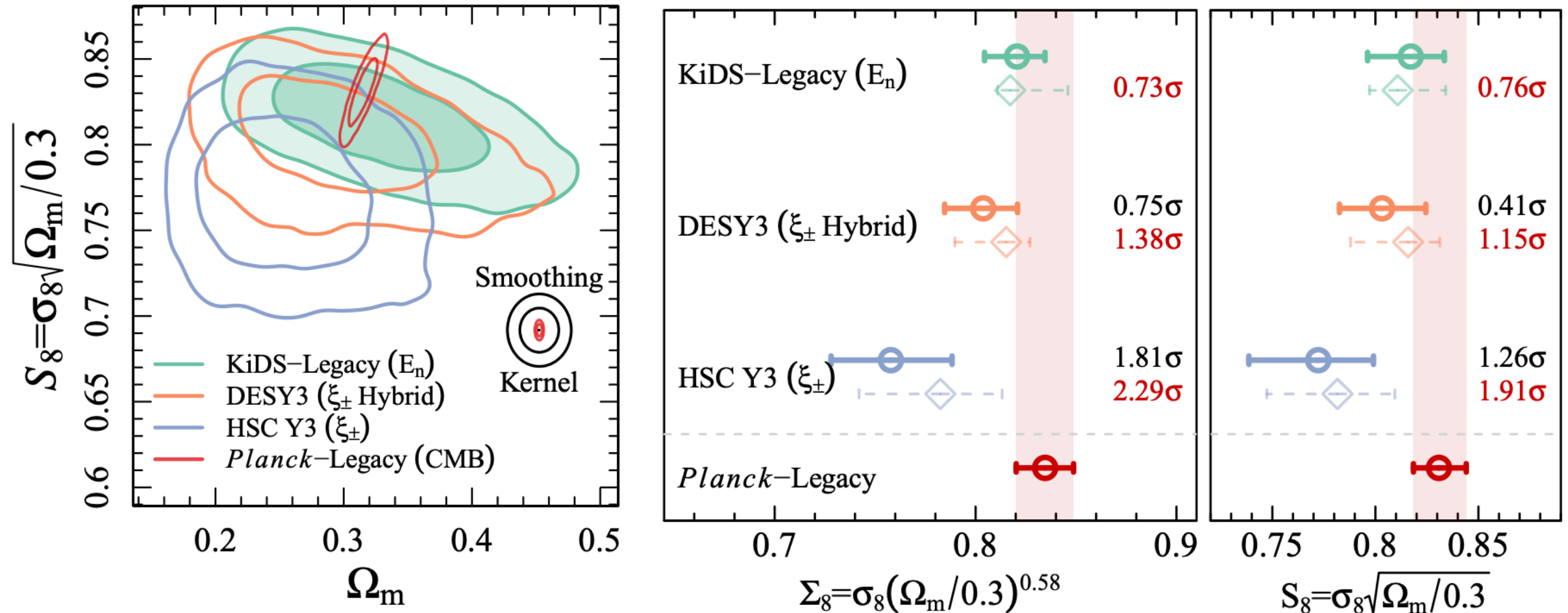
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- Early universe models could explain BAO data but not large  $\Omega_m$  from SNe

# The $S_8$ tension is gone?

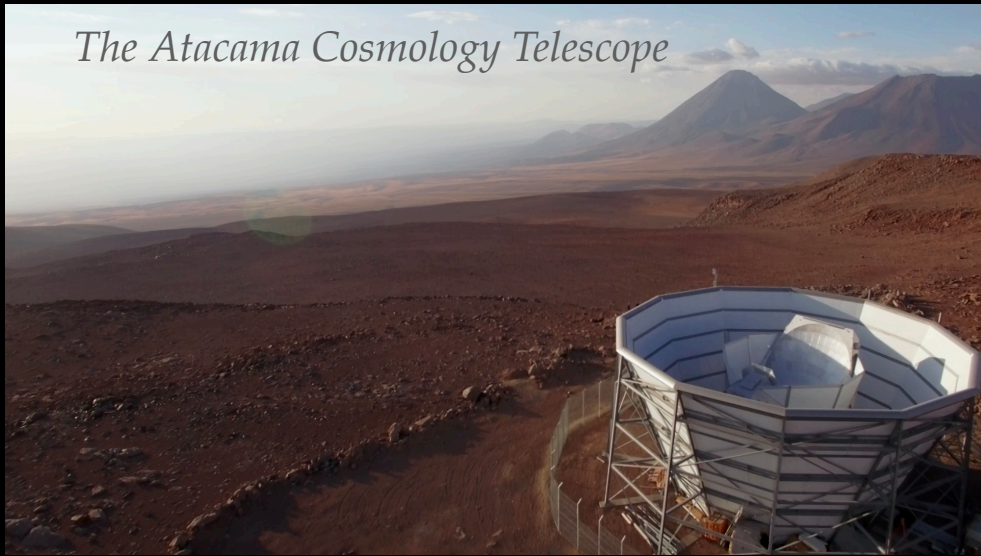


- But remember that the  $H_0$  tension may imply some residual tension ...
- See DM talks for more ideas for solutions



# Cosmic tension: where are we going next?

*The Atacama Cosmology Telescope*



*The South Pole Telescope*



*DESI*



*Euclid*

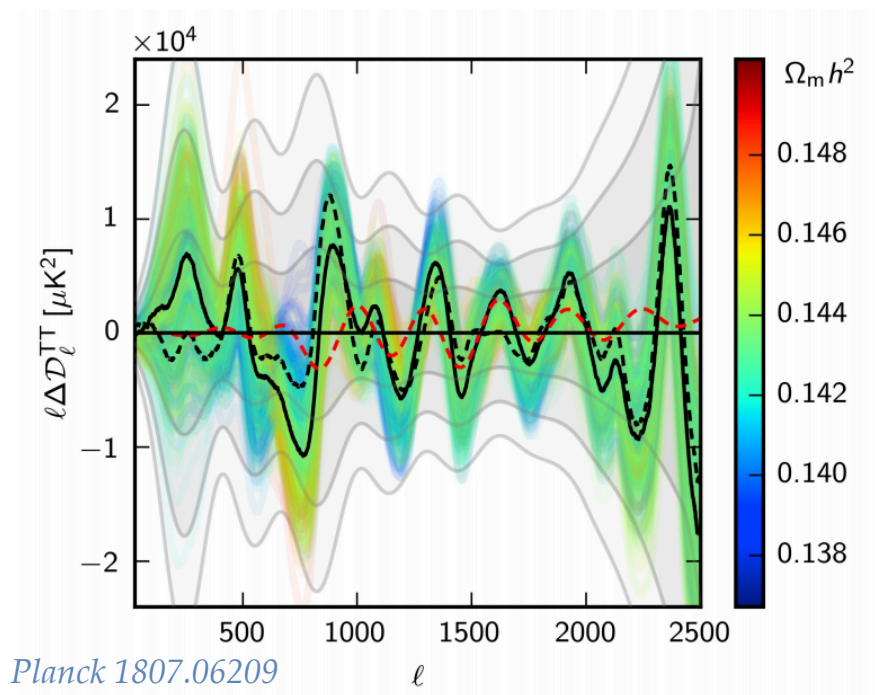


*LSST/Vera Rubin Observatory*



- **New CMB data are coming:** very sensitive to new physics around recombination!
- **New LSS data are coming:** measure  $P(k, z)$ , constrain baryonic feedback, neutrino masses?
- **New JWST data + age of the universe? + gravitational wave** measurements of  $H_0$ .

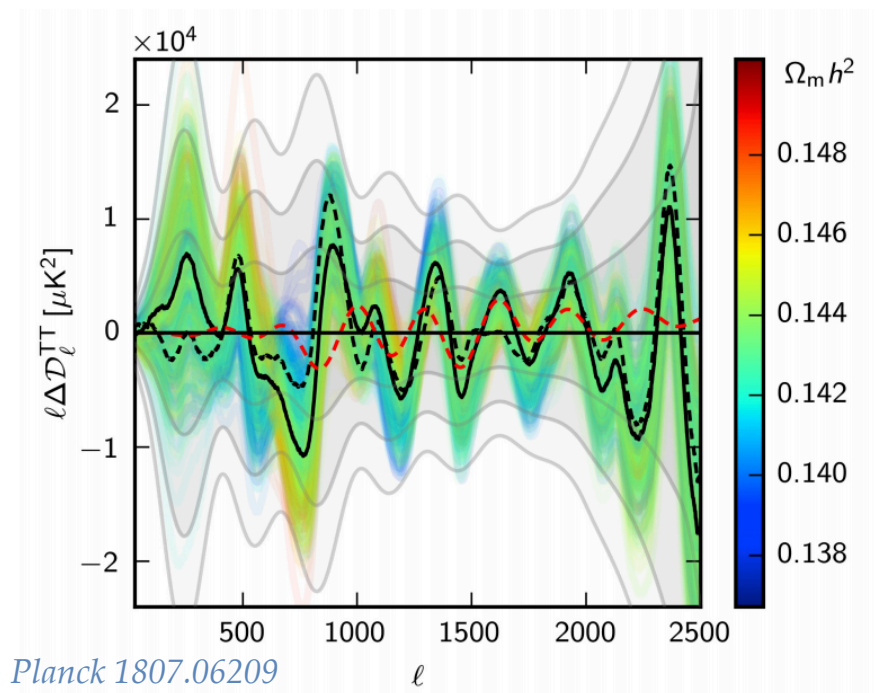




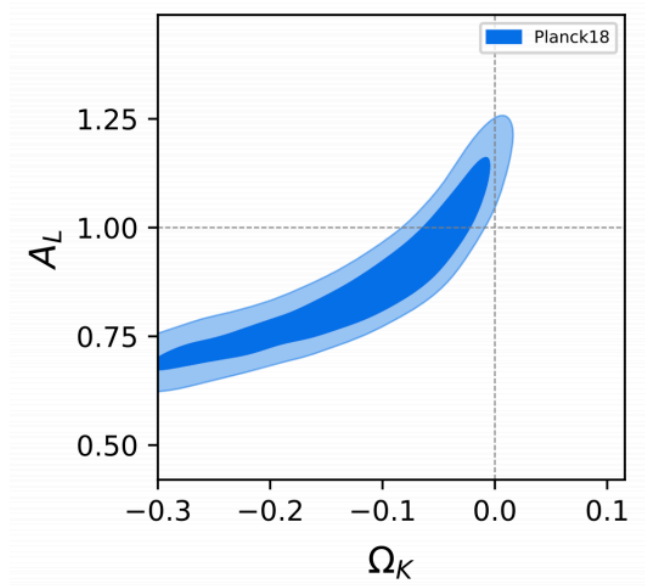
$$C_{\ell}^{\phi\phi} \rightarrow A_L C_{\ell}^{\phi\phi}$$

Unless specified, Figs. from Di Valentino++ 1911.02087

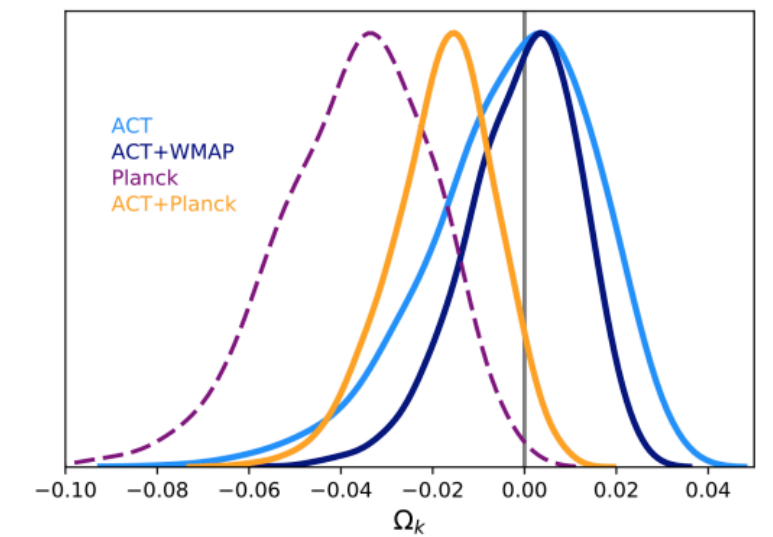


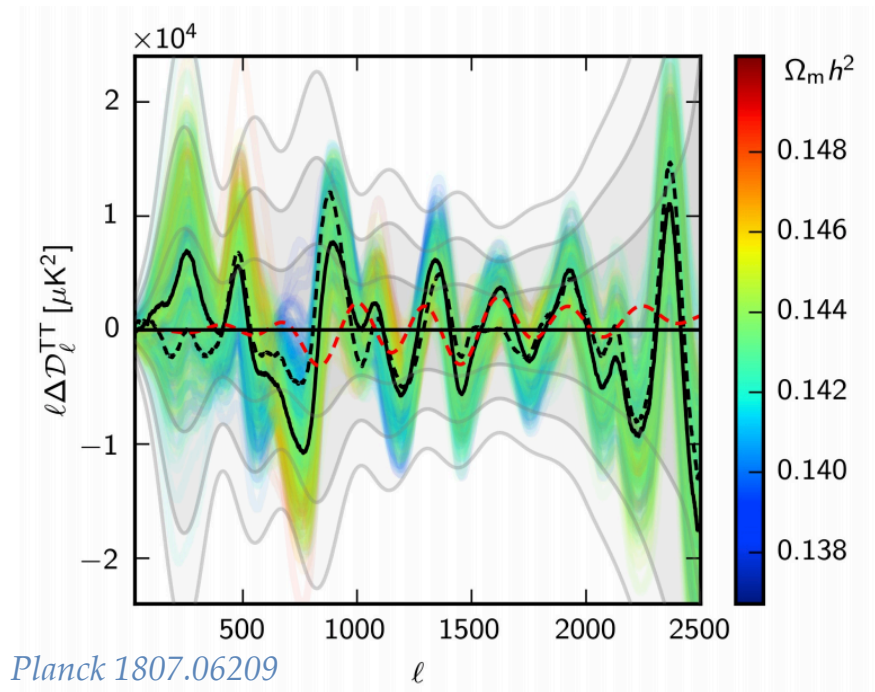


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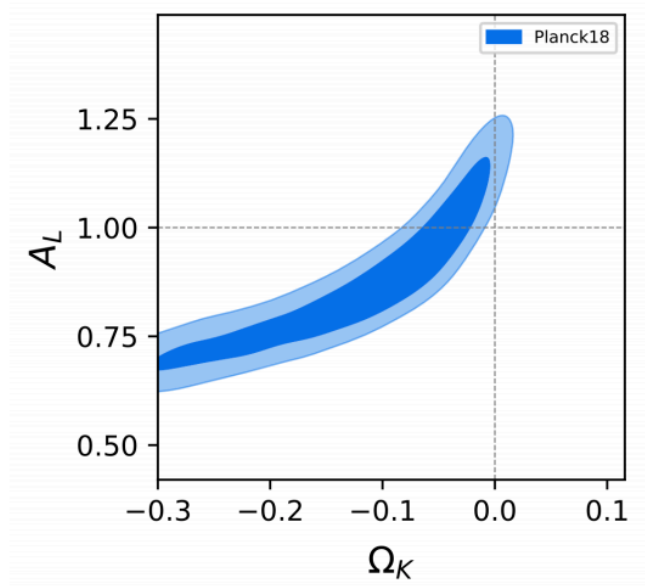


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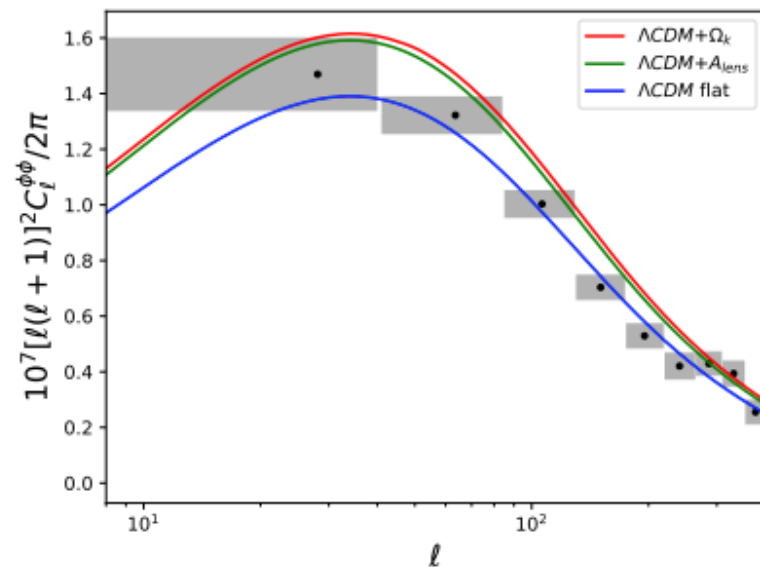
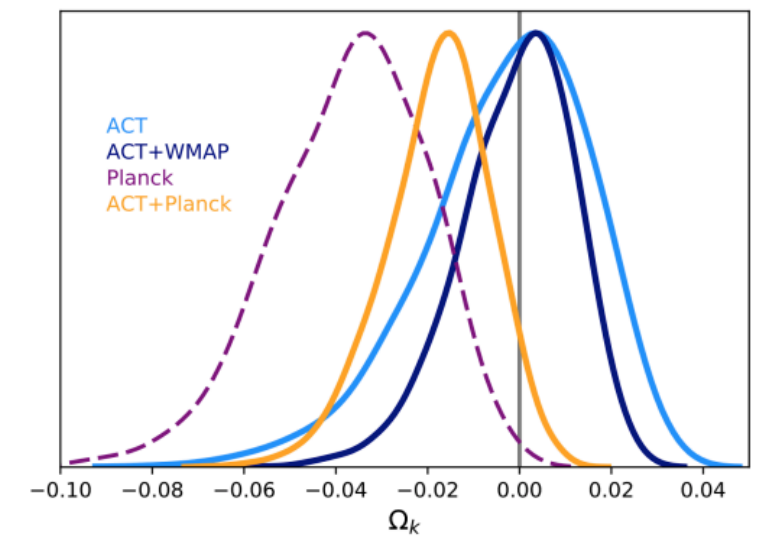


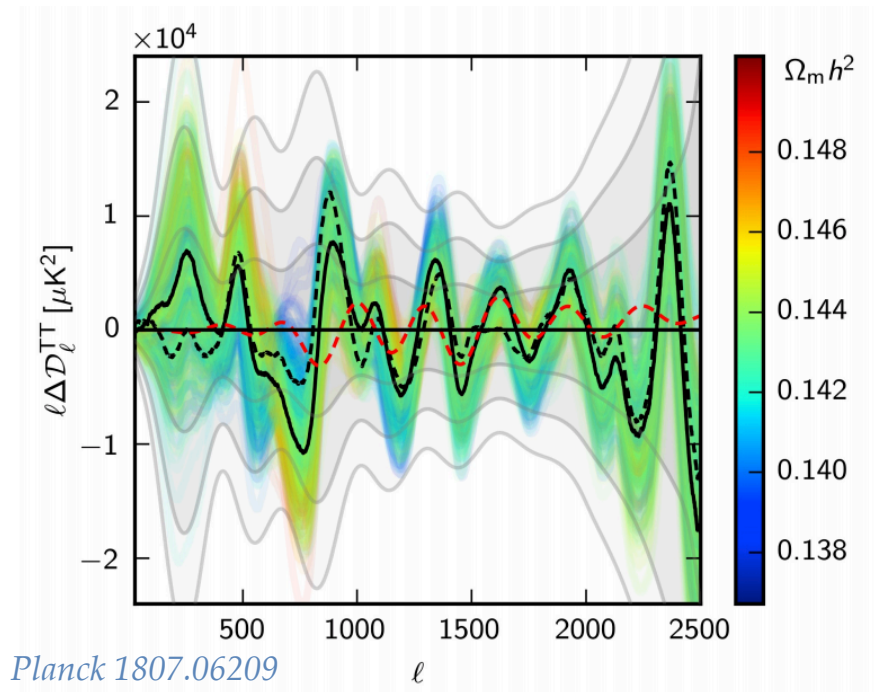


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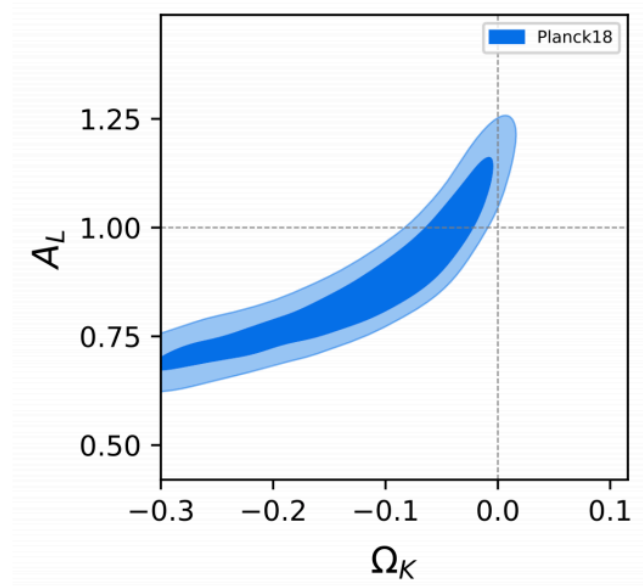


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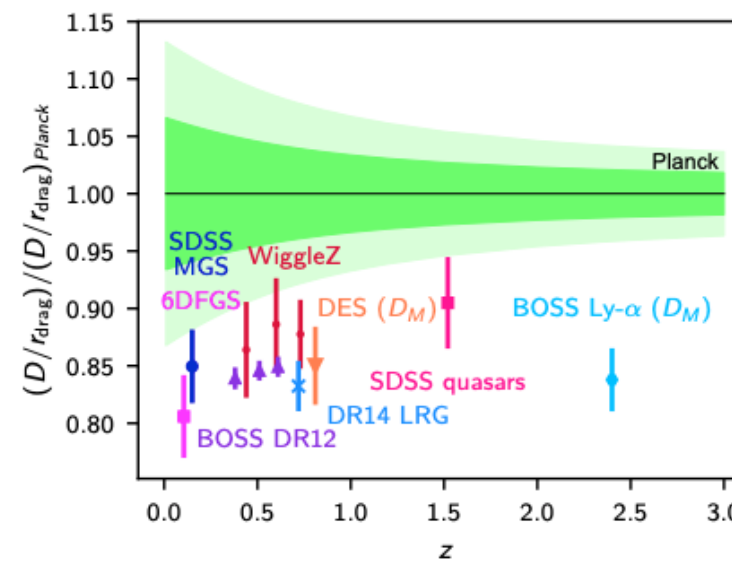
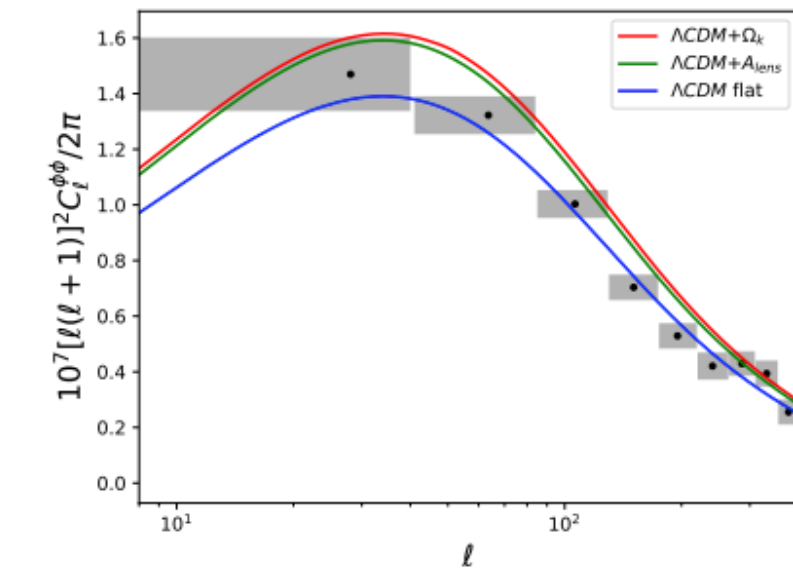
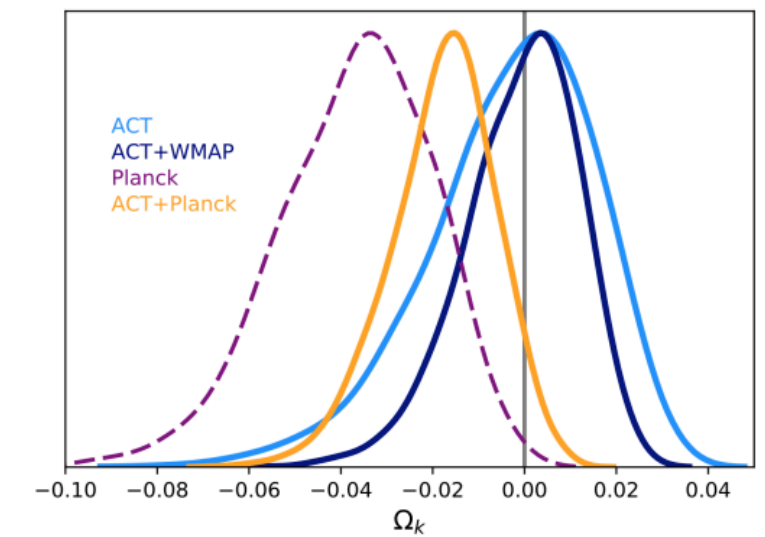


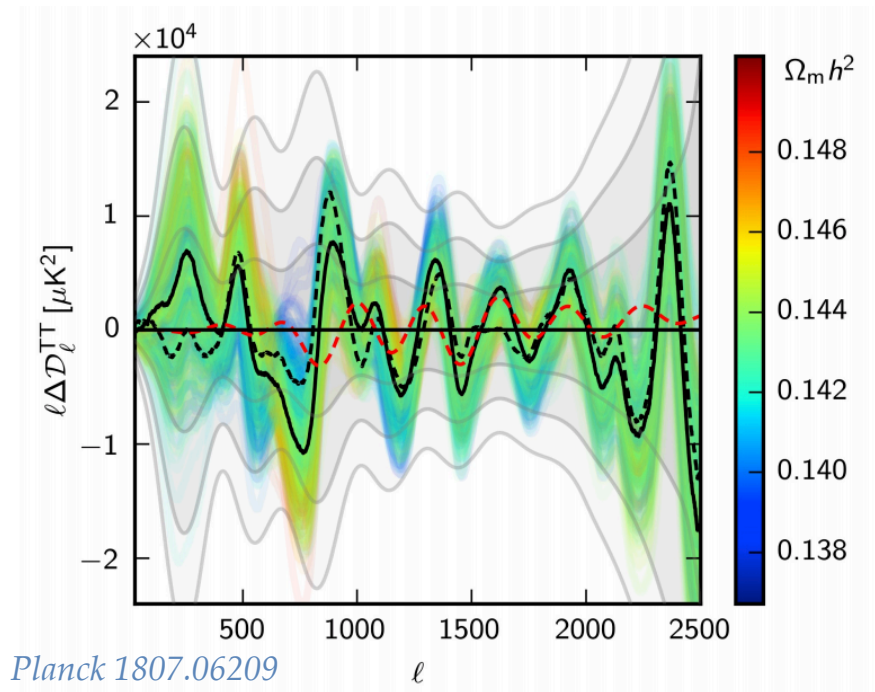


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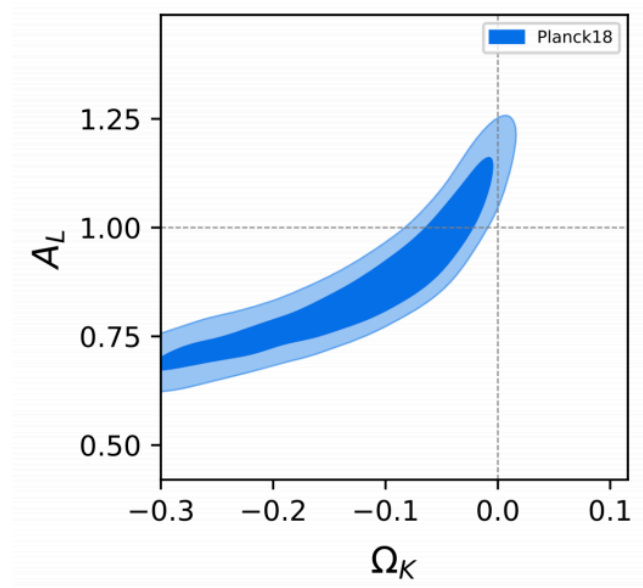


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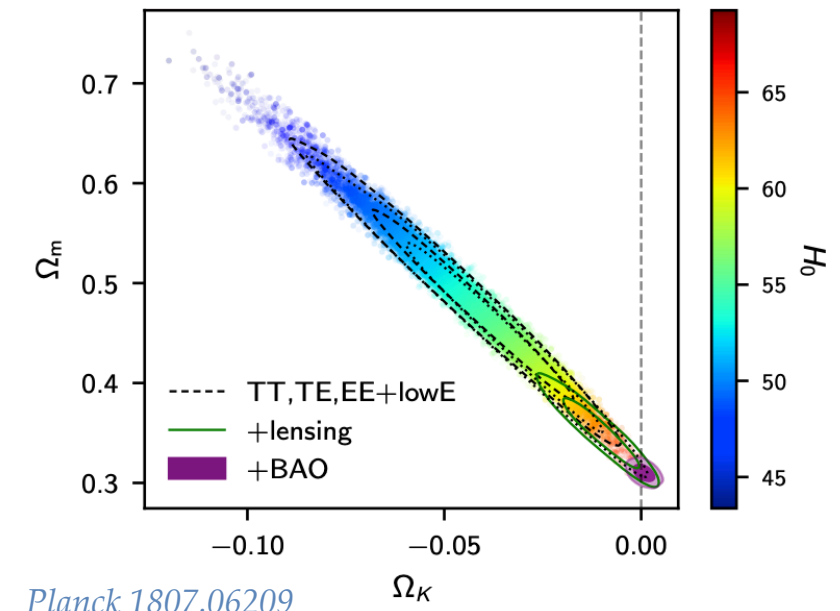
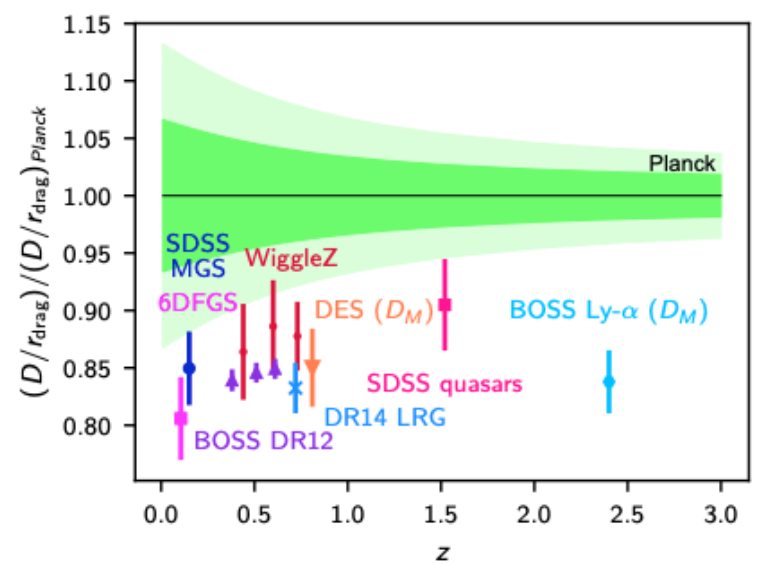
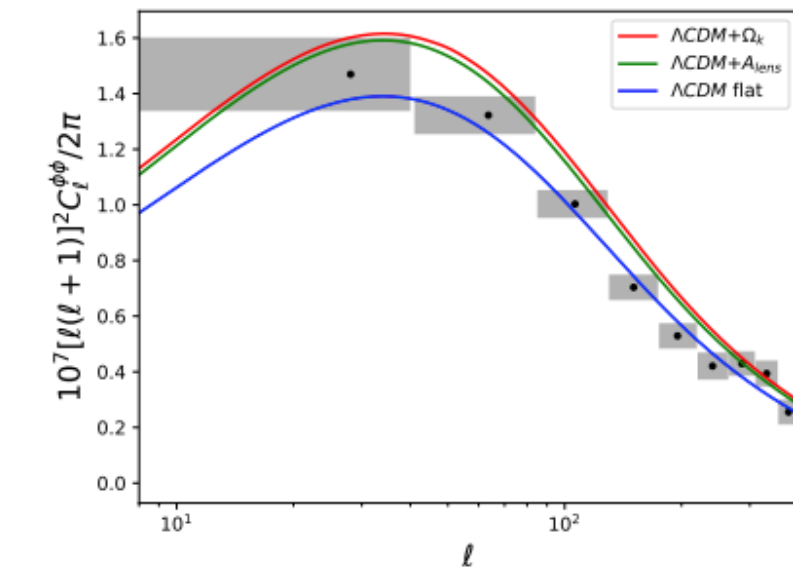
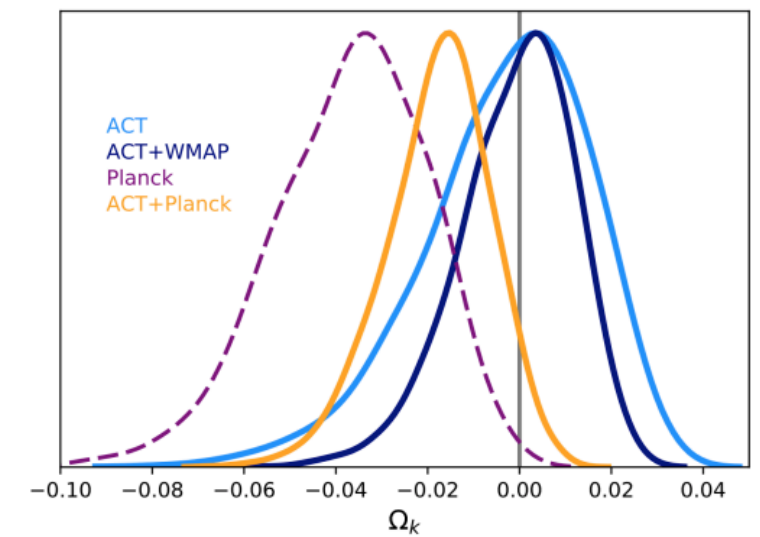




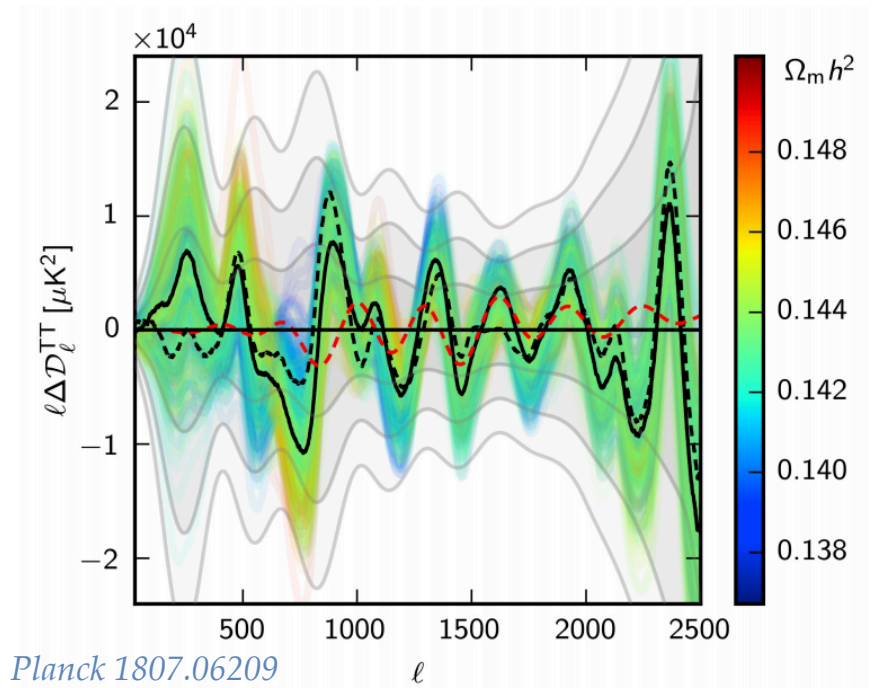
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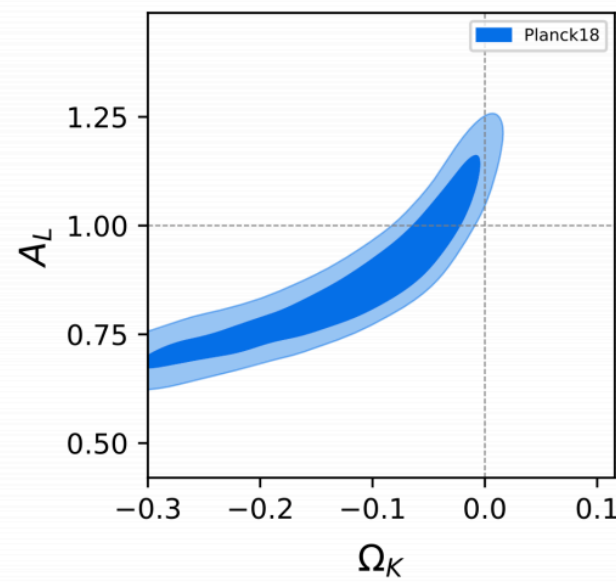
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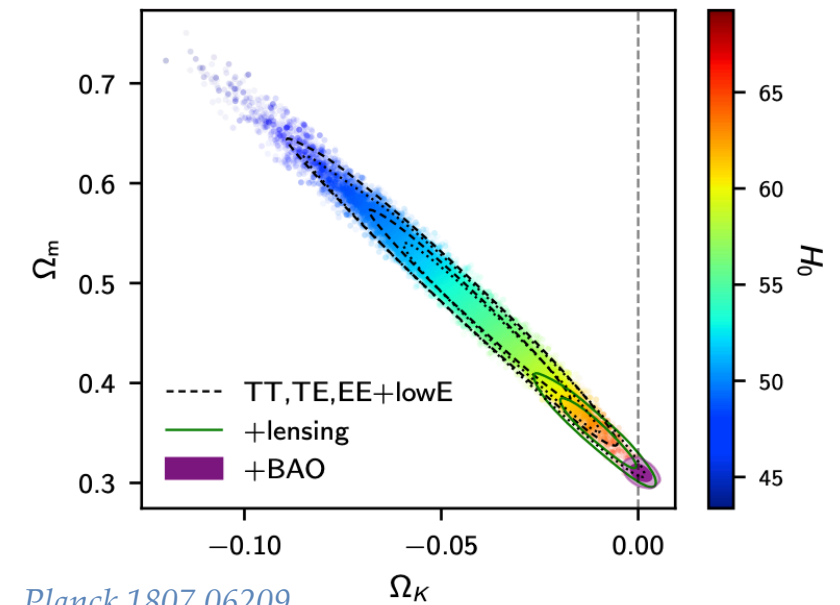
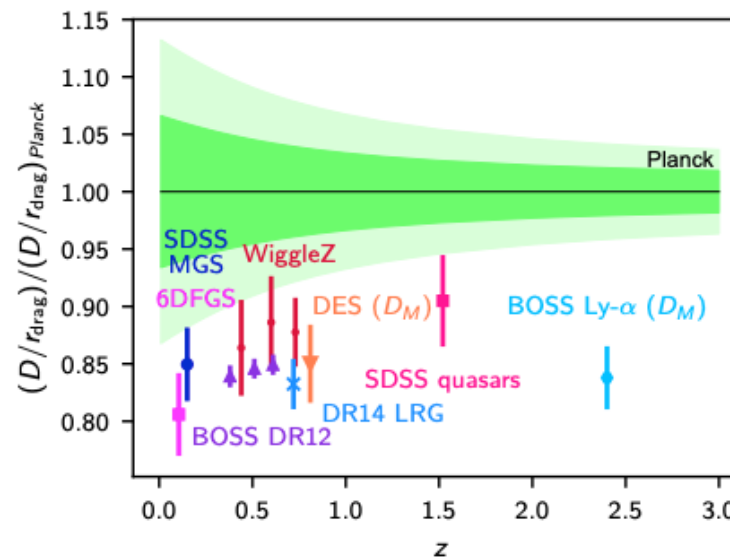
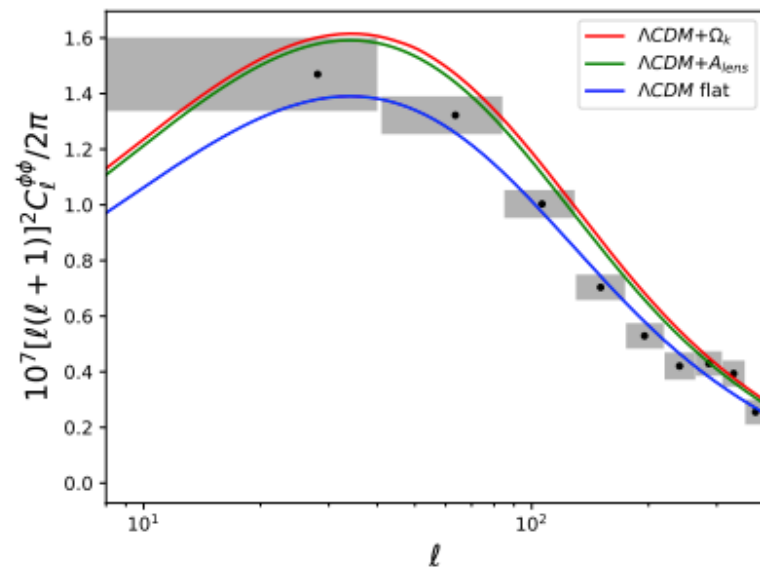
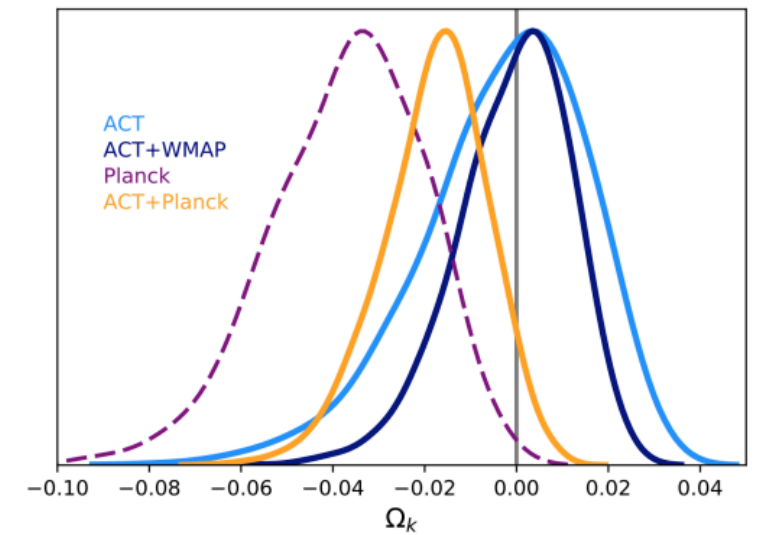




$$C_\ell^{\phi\phi} \rightarrow A_L C_\ell^{\phi\phi}$$



Unless specified, Figs. from Di Valentino++ 1911.02087



- The Universe is flat unless of a true ‘cosmological crisis’.
- Flat universe is also supported by BOSS and Cosmic Chronometers. [Vagnozzi++2010.02230](#), [2011.11645](#)
- Nb:  $A_L$  could also be explained in modified gravity framework, it suffers from the same issues.