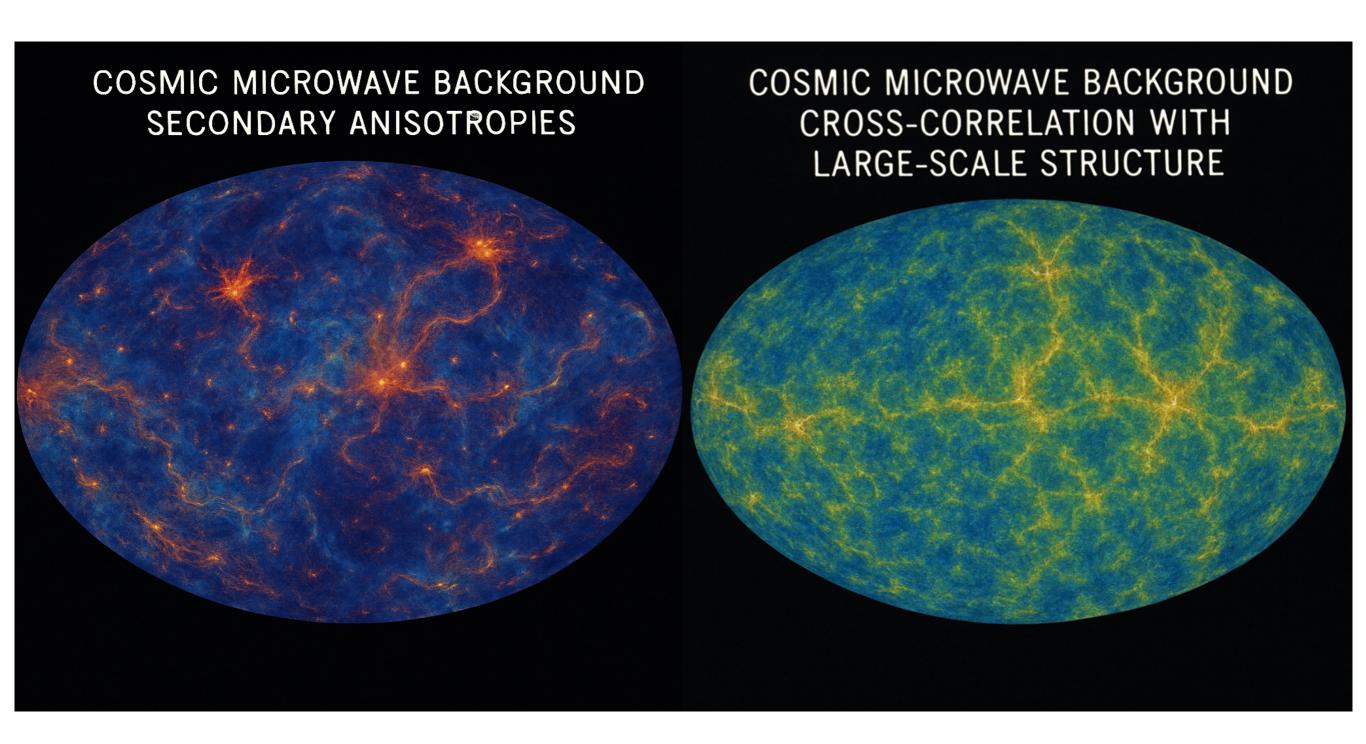
CMB secondary anisotropies and synergies with LSS probes



Giulio Fabbian Les Houches 2025

Outline (by ChatGPT)

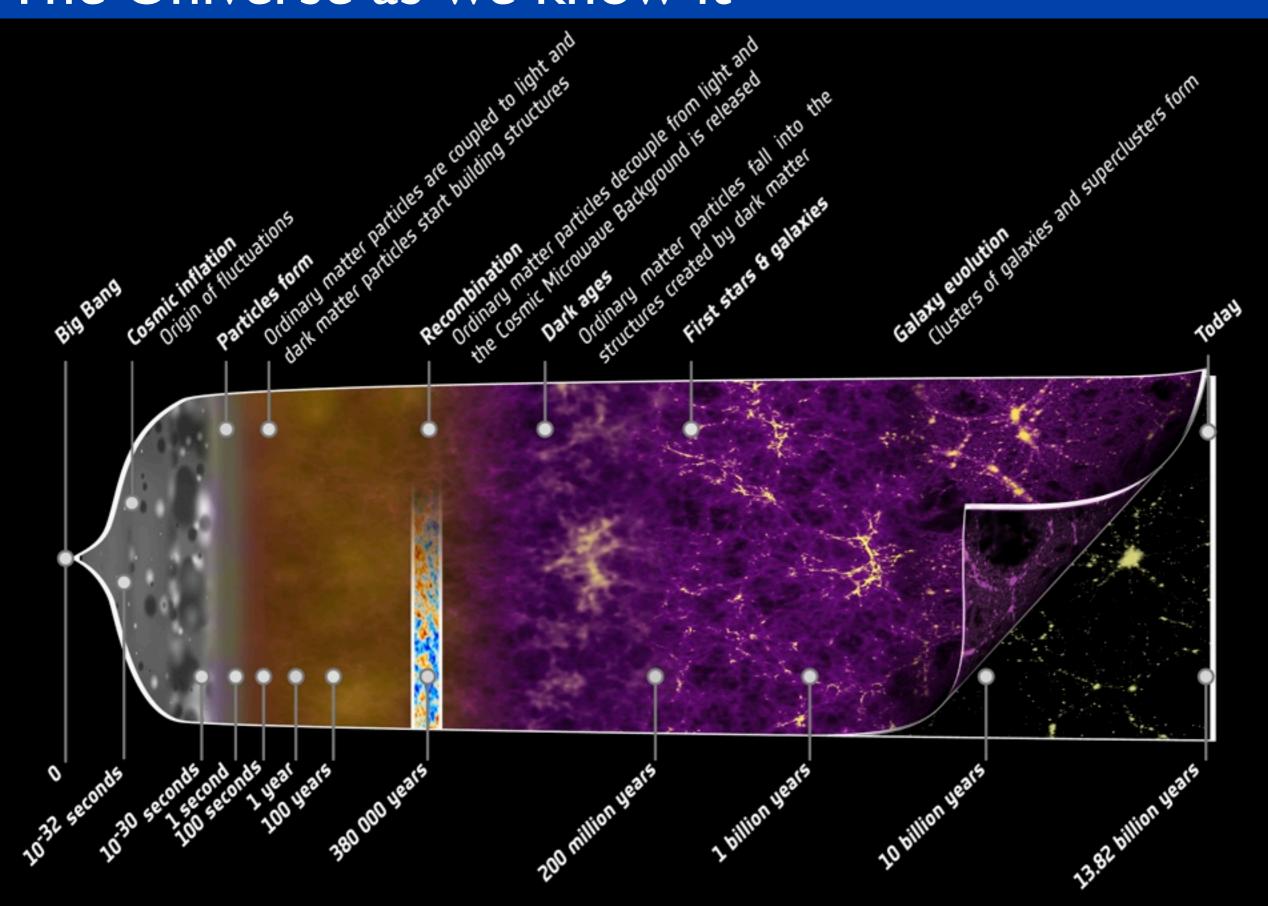


Outline (optimistic)

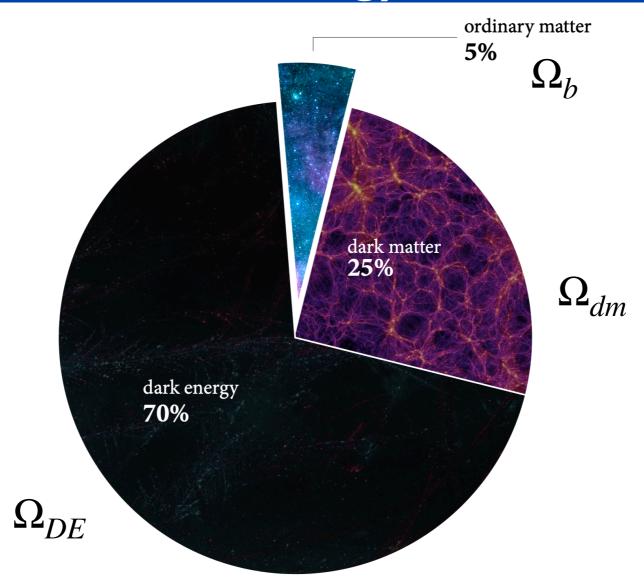
- Few practical concepts on experimental CMB.
- Secondary anisotropies
 - Deep dive on CMB lensing...
 - Quadratic estimators...
 - Cross-correlation with large-scale structure
 - Delensing: synergies between LSS, CMB and primordial universe.
 - Frank Thermal and kinetic Sunyaev Zeldovich
 - Integrated Sachs-Wolfe and CIB if time



The Universe as we know it

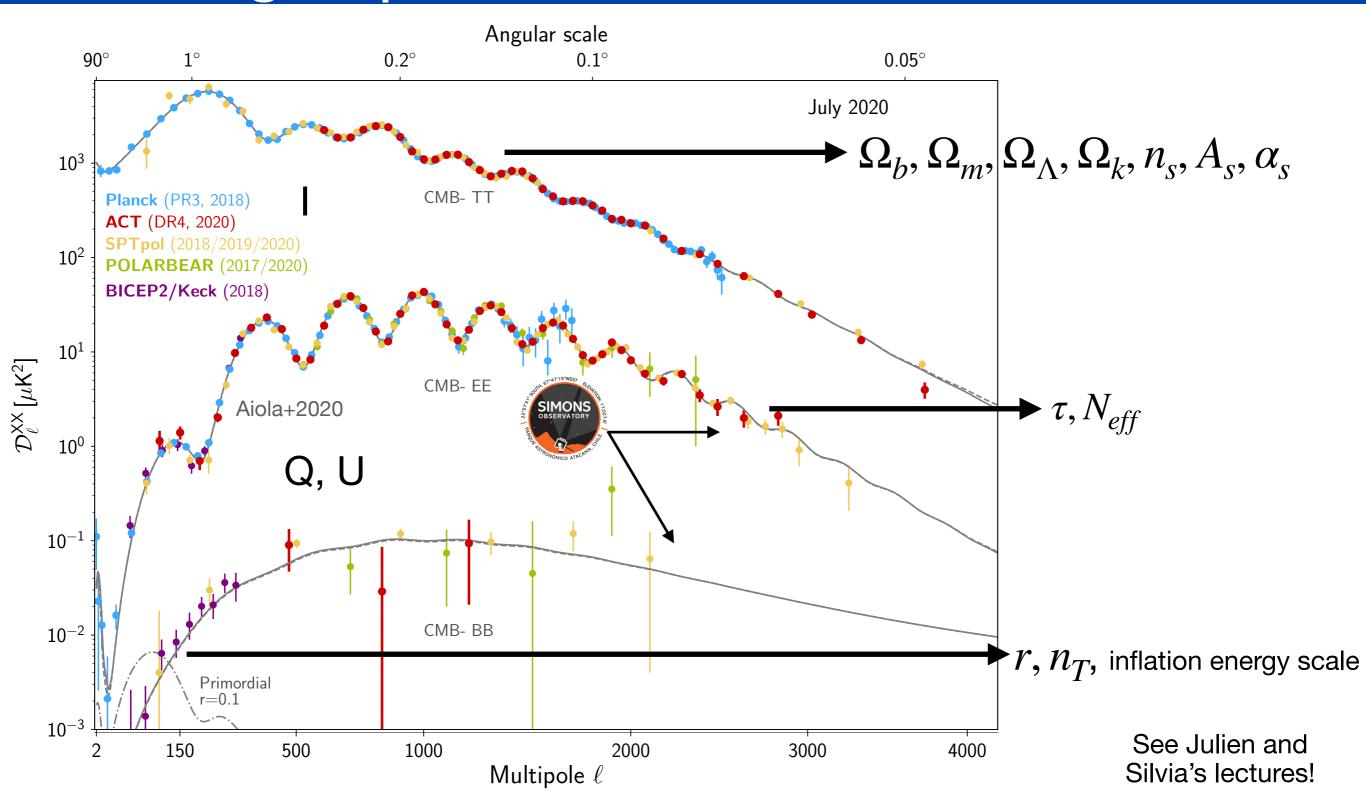


Open questions in cosmology as of 2025



- What is dark matter? Do massive neutrinos contribute?
- What is the nature of dark energy? Is General Relativity correct?
- Which mechanism drove primordial inflation?

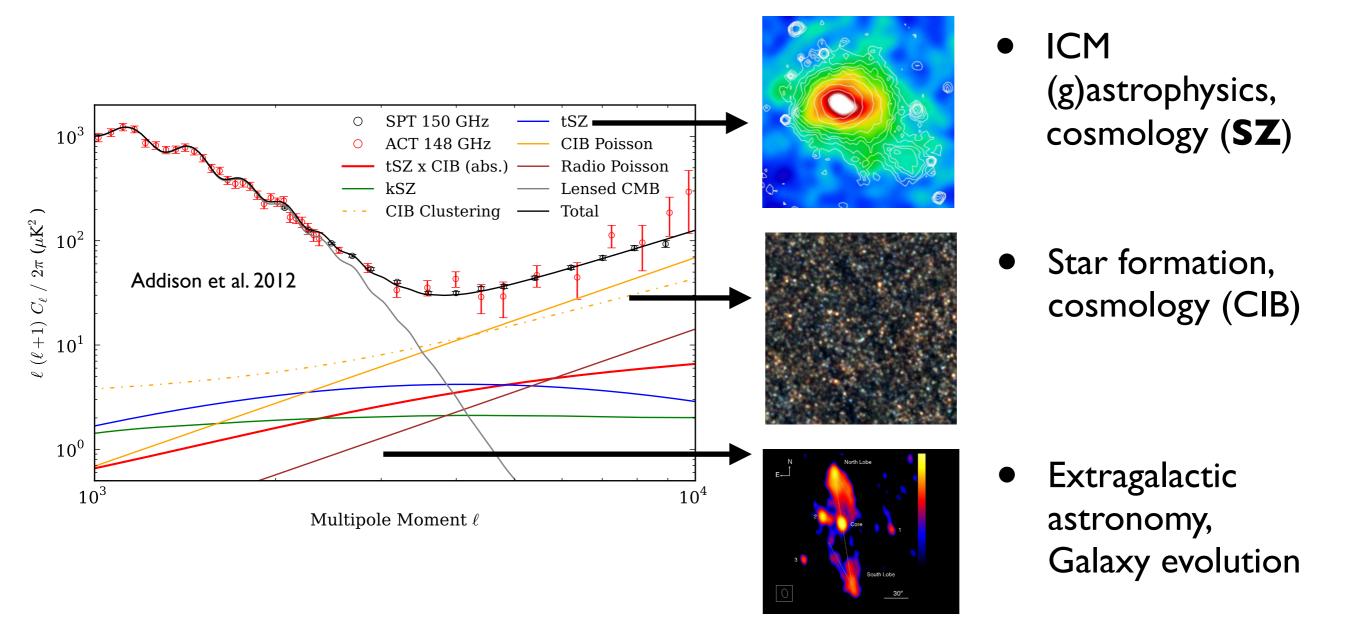
Cosmological probes: CMB



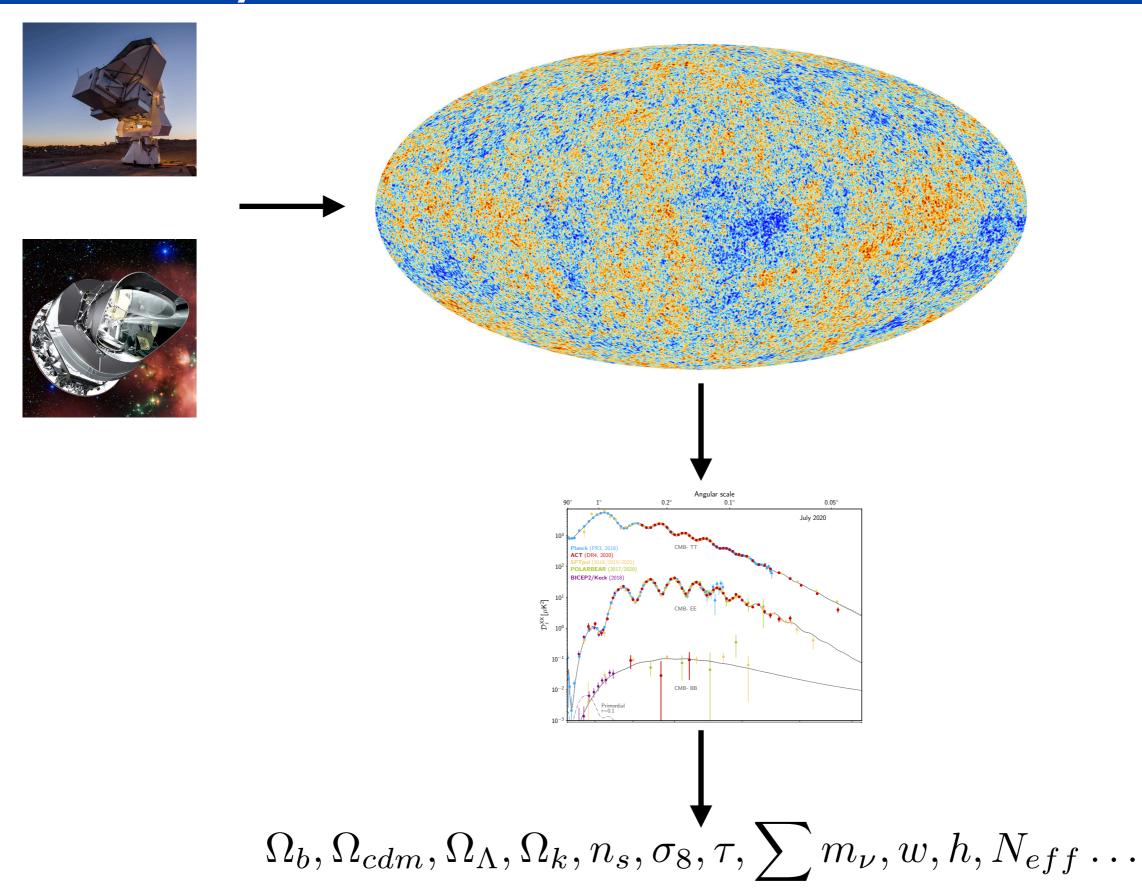
• Also improvements on $\sum m_{\nu}$ and others from new polarization measurements.

Is CMB "the" CMB?

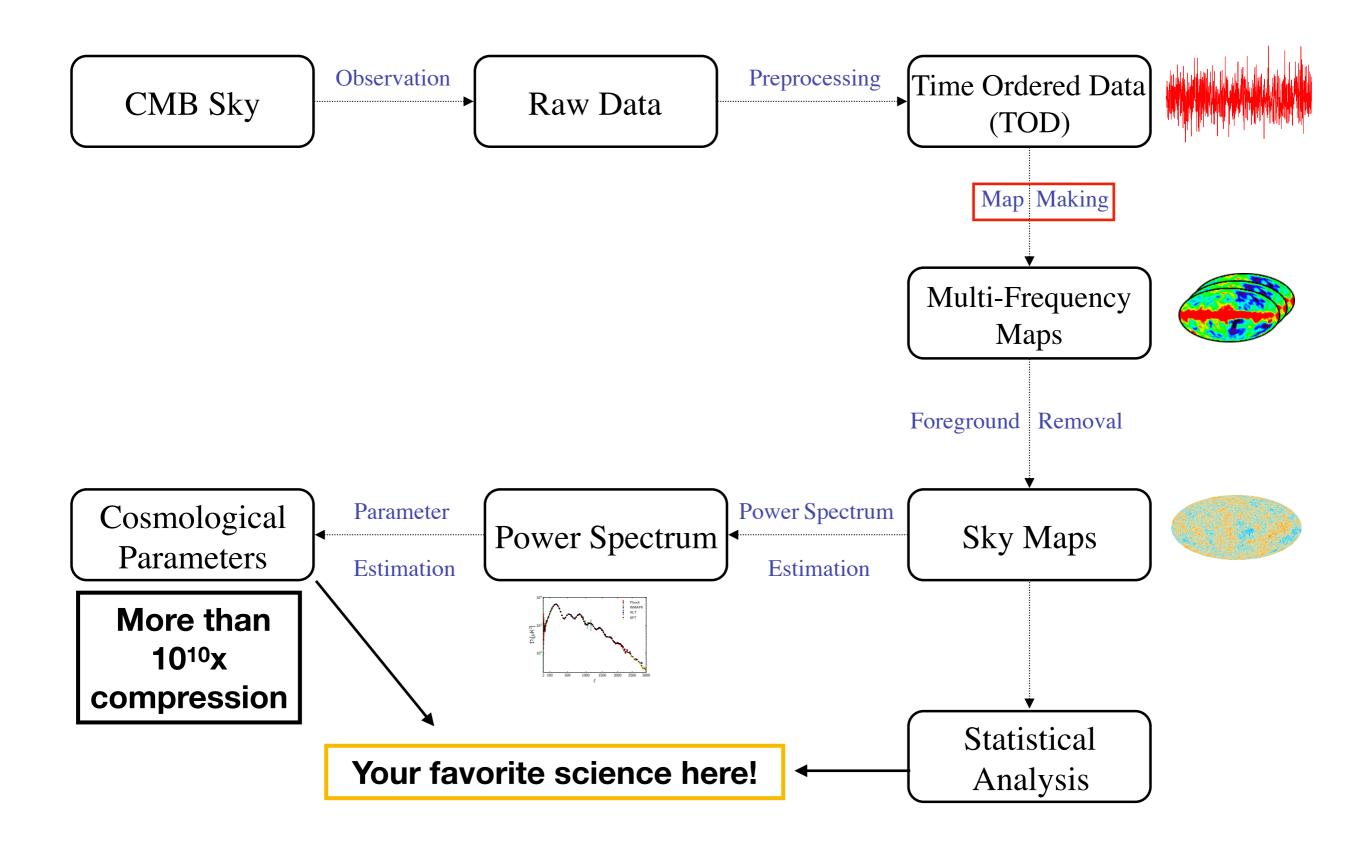
- CMB is a snapshot of the universe at z ~1100.... plus lots of other things!
 - Imprint of astrophysical emissions (galactic / extragalactic...)
 - Late time physics (e.g. Integrated Sachs-Wolfe effect, weak lensing)



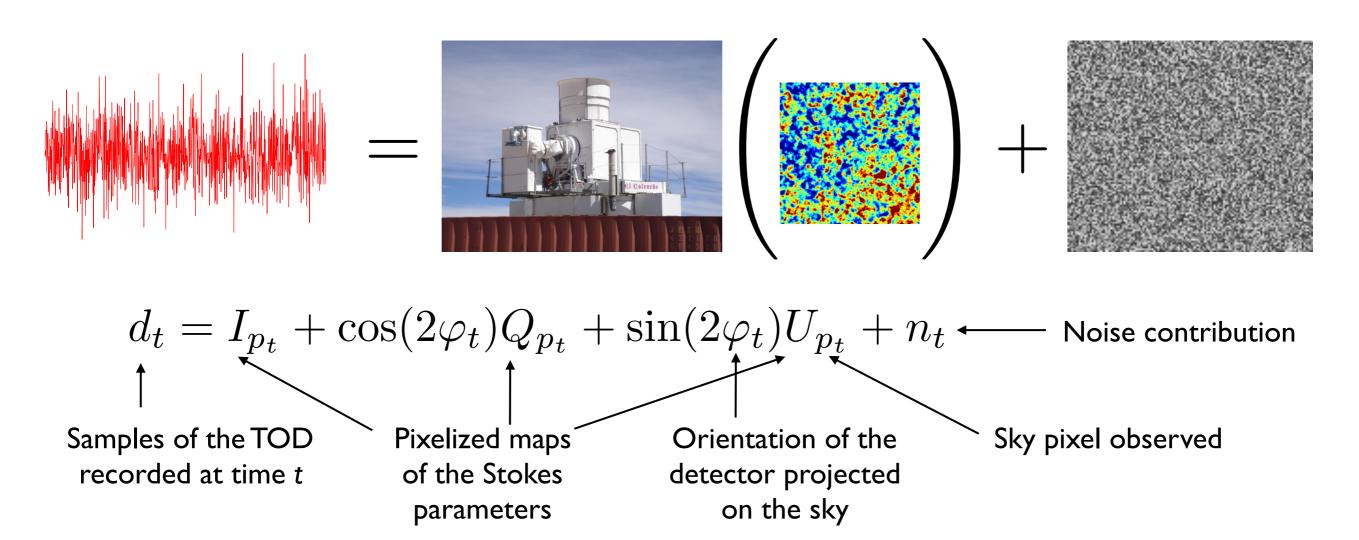
CMB analysis chain



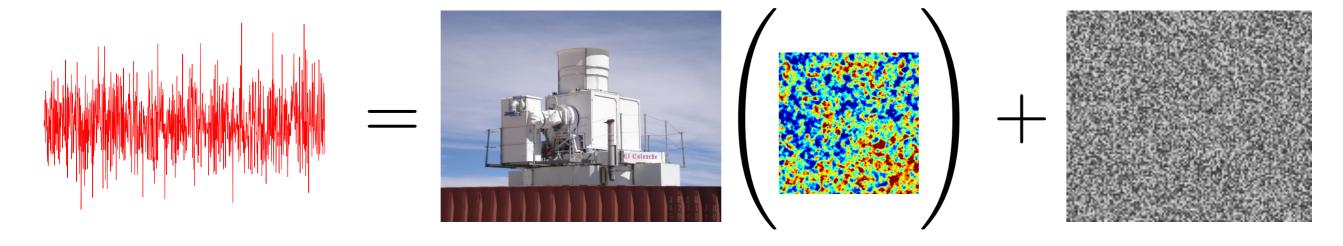
CMB analysis chain: a radical compression



Mapmaking: the most challenging inverse problem



Mapmaking: the most challenging inverse problem

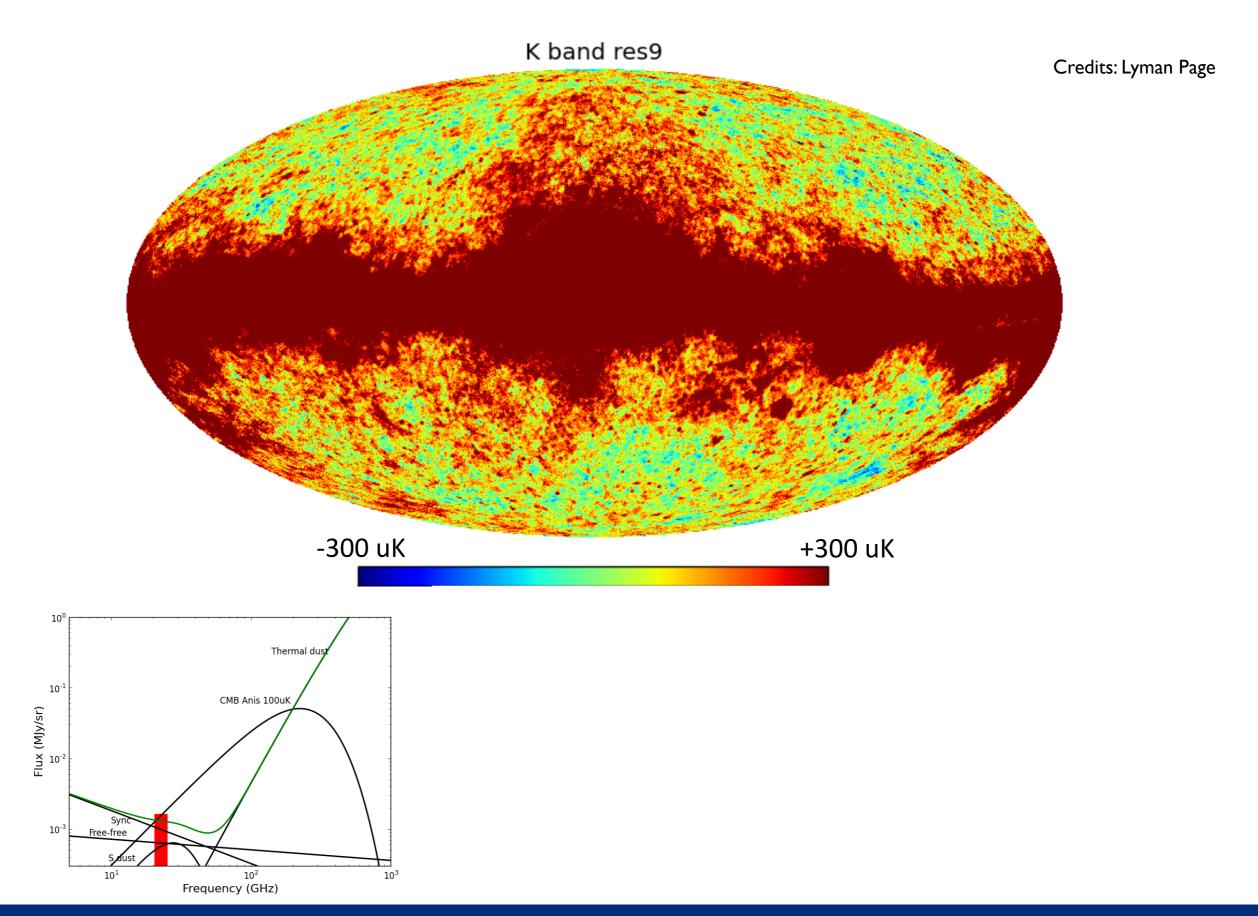


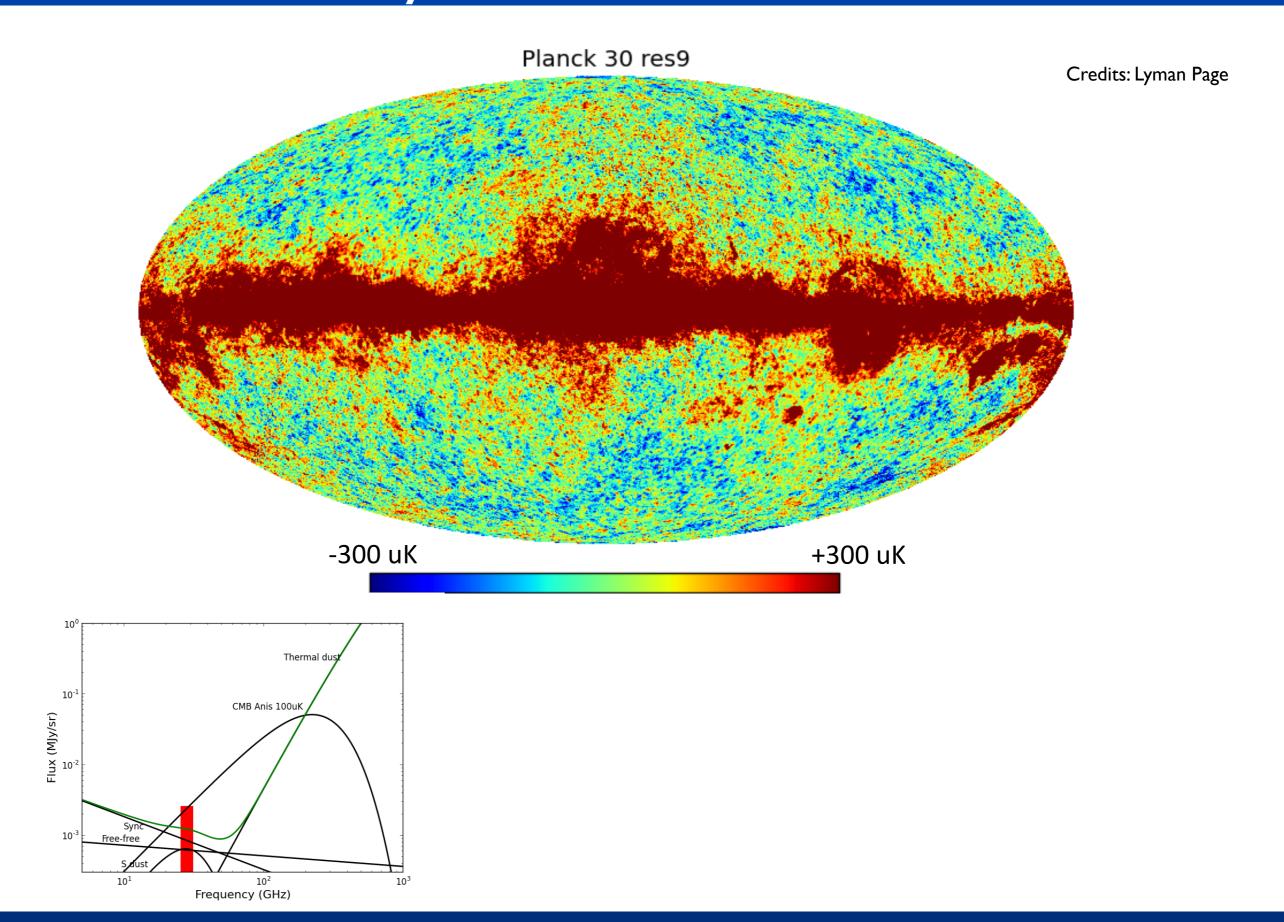
$$\mathbf{d} = \mathbf{A} \cdot \mathbf{s} + \mathbf{n}$$

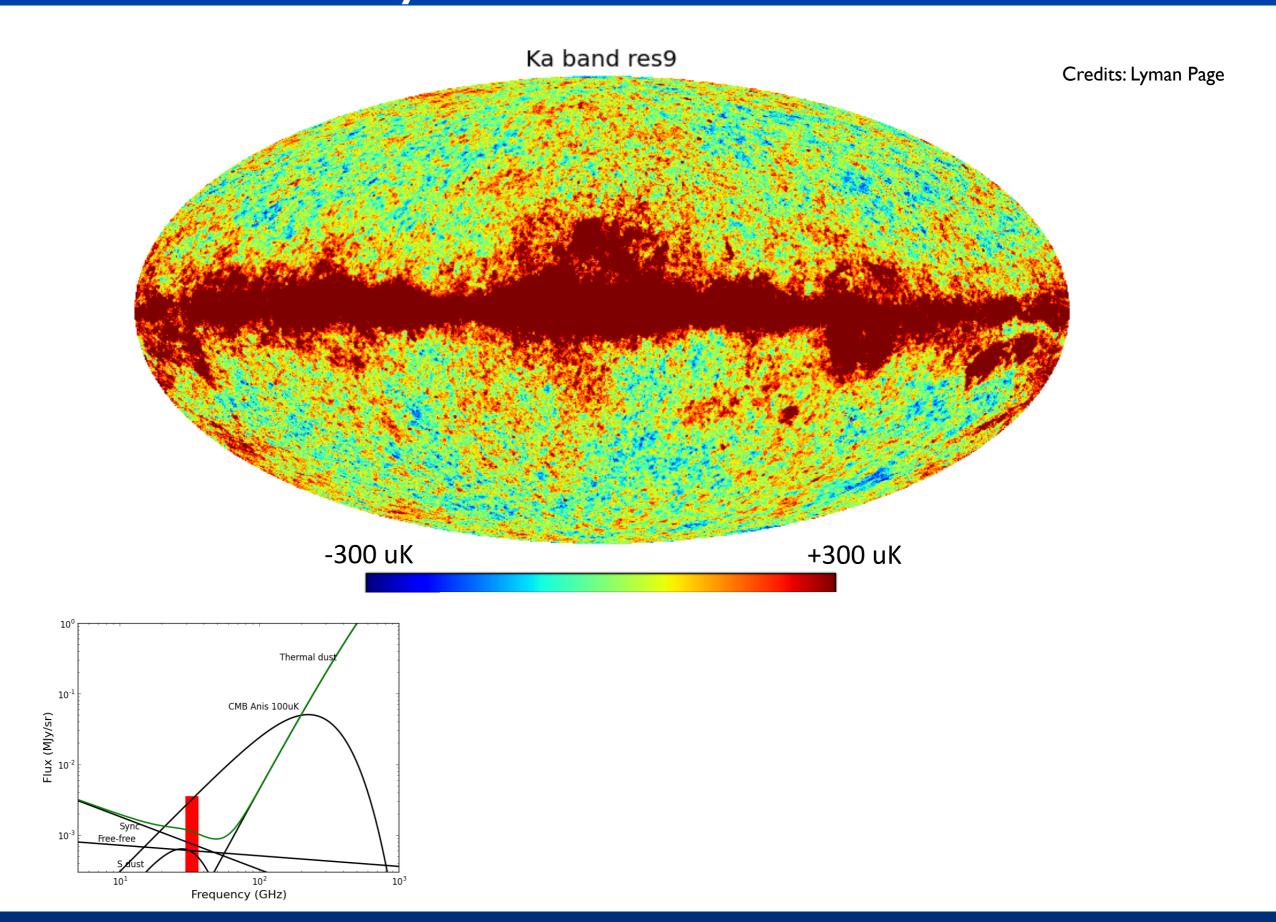
- Unbiased GLS solution
- $\hat{\mathbf{s}} = (\mathbf{A}^{\mathsf{T}} \mathbf{N}^{-1} \mathbf{A})^{-1} \mathbf{A}^{\mathsf{T}} \mathbf{N}^{-1} \mathbf{d} \quad \mathbf{N} \equiv \langle \mathbf{n}^{\mathsf{T}} \mathbf{n} \rangle$
- Challenging, advanced algebraic techniques mandatory

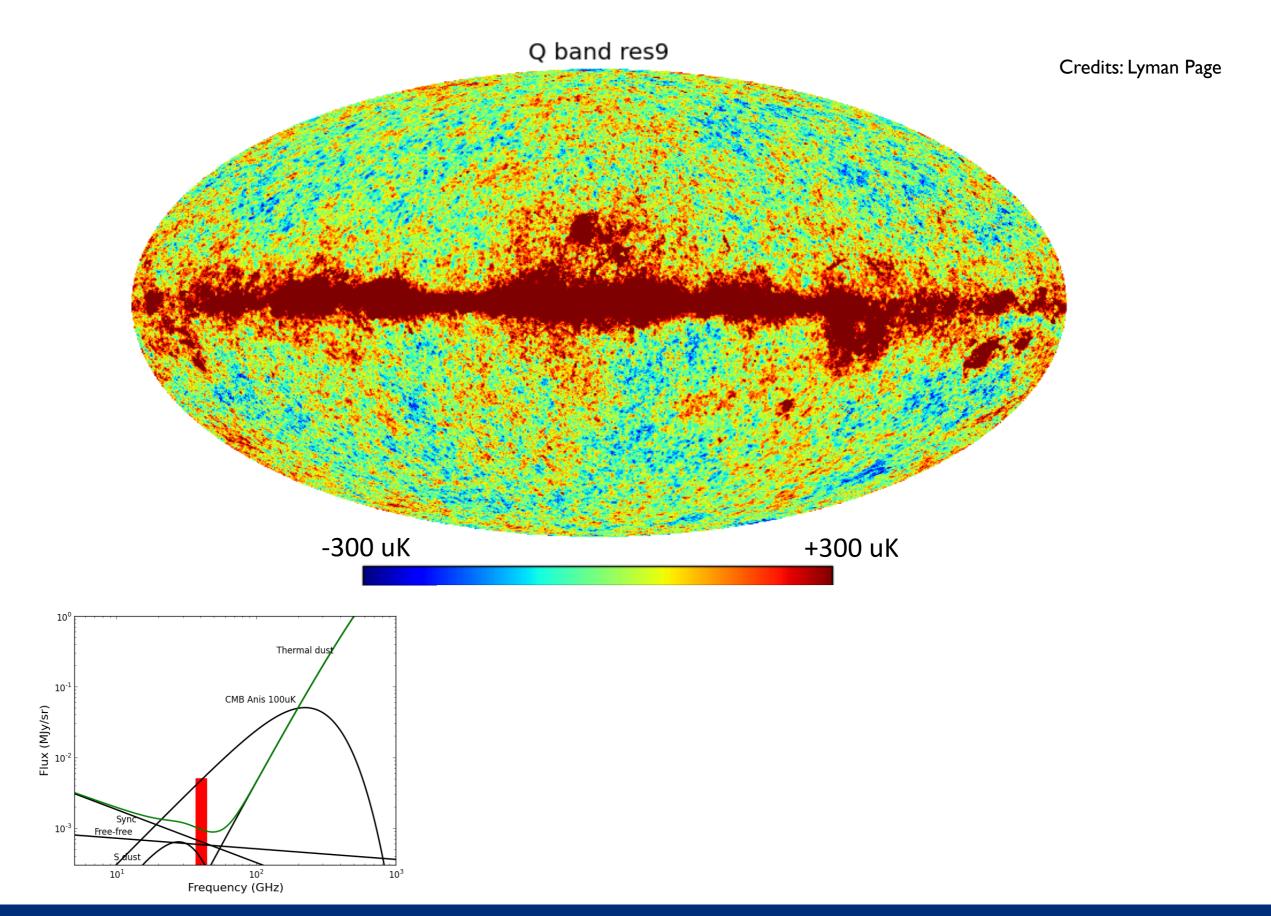
$$\mathcal{N}_p = 10^6 \ \mathcal{N}_t = 10^{12}$$

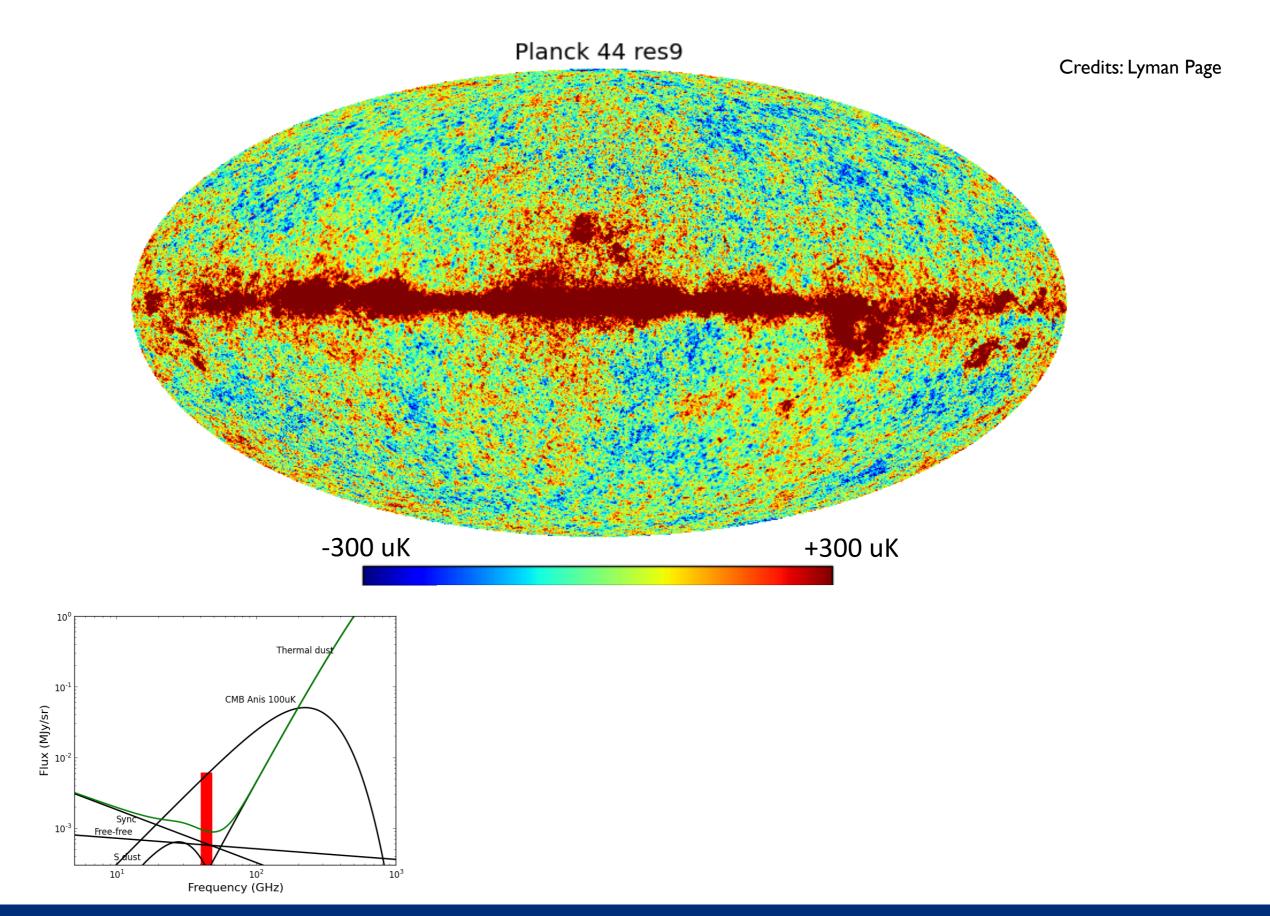
$$\mathbf{\hat{s}} = egin{bmatrix} \mathcal{N}_p imes \mathcal{N}_p & \mathcal{N}_t \end{bmatrix} lacktriangle \mathcal{N}_t imes \mathcal{N}_t \end{bmatrix} lacktriangle \mathcal{N}_t$$

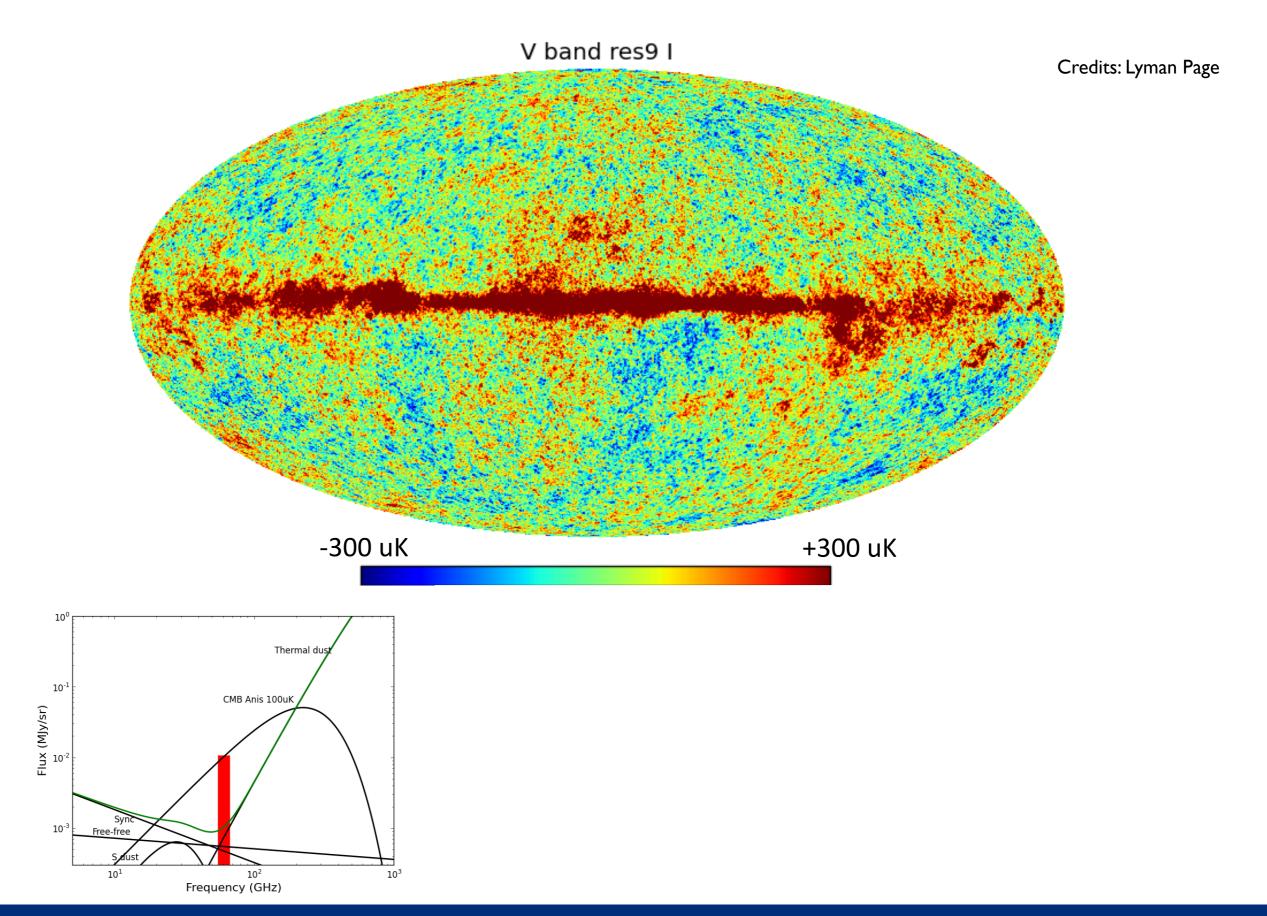


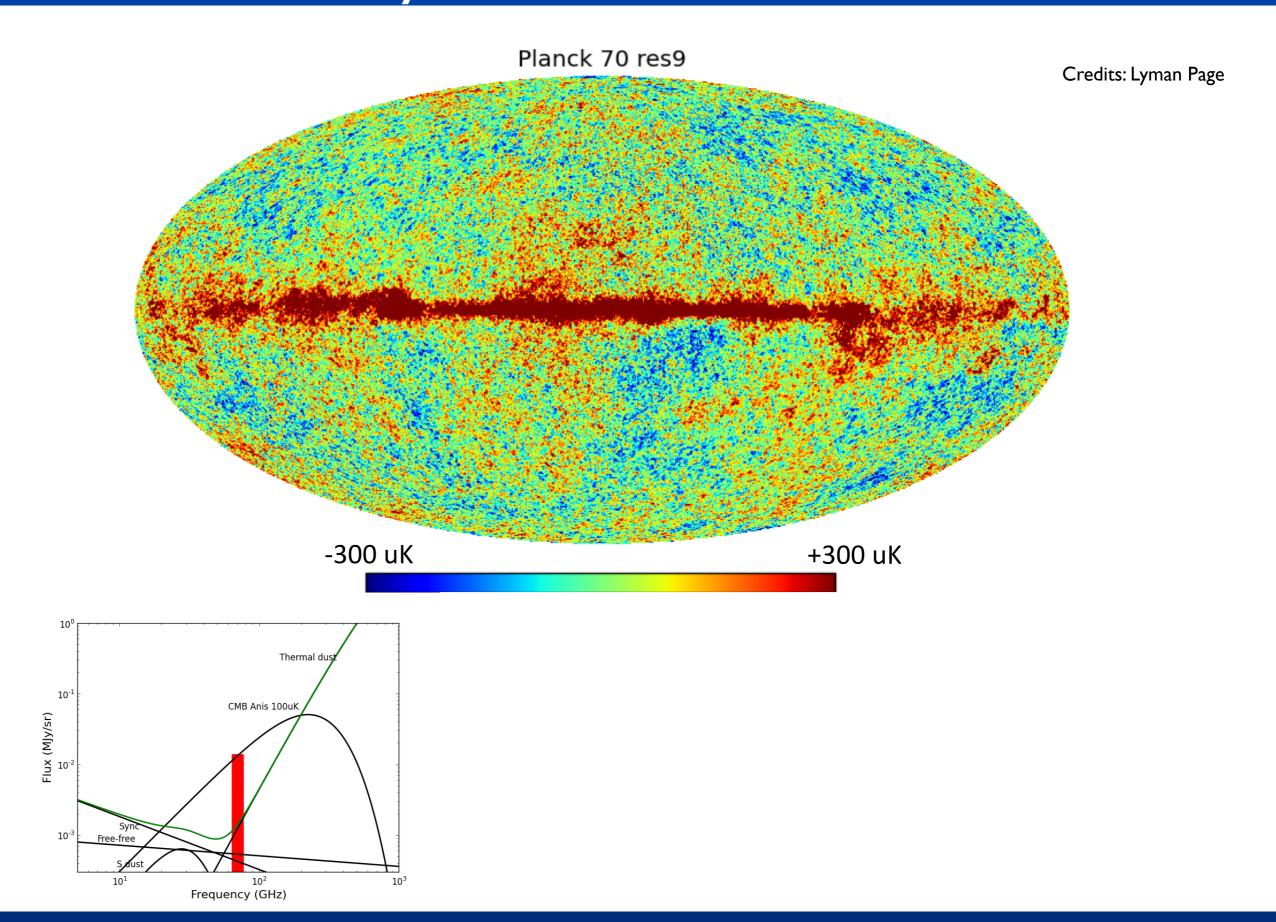


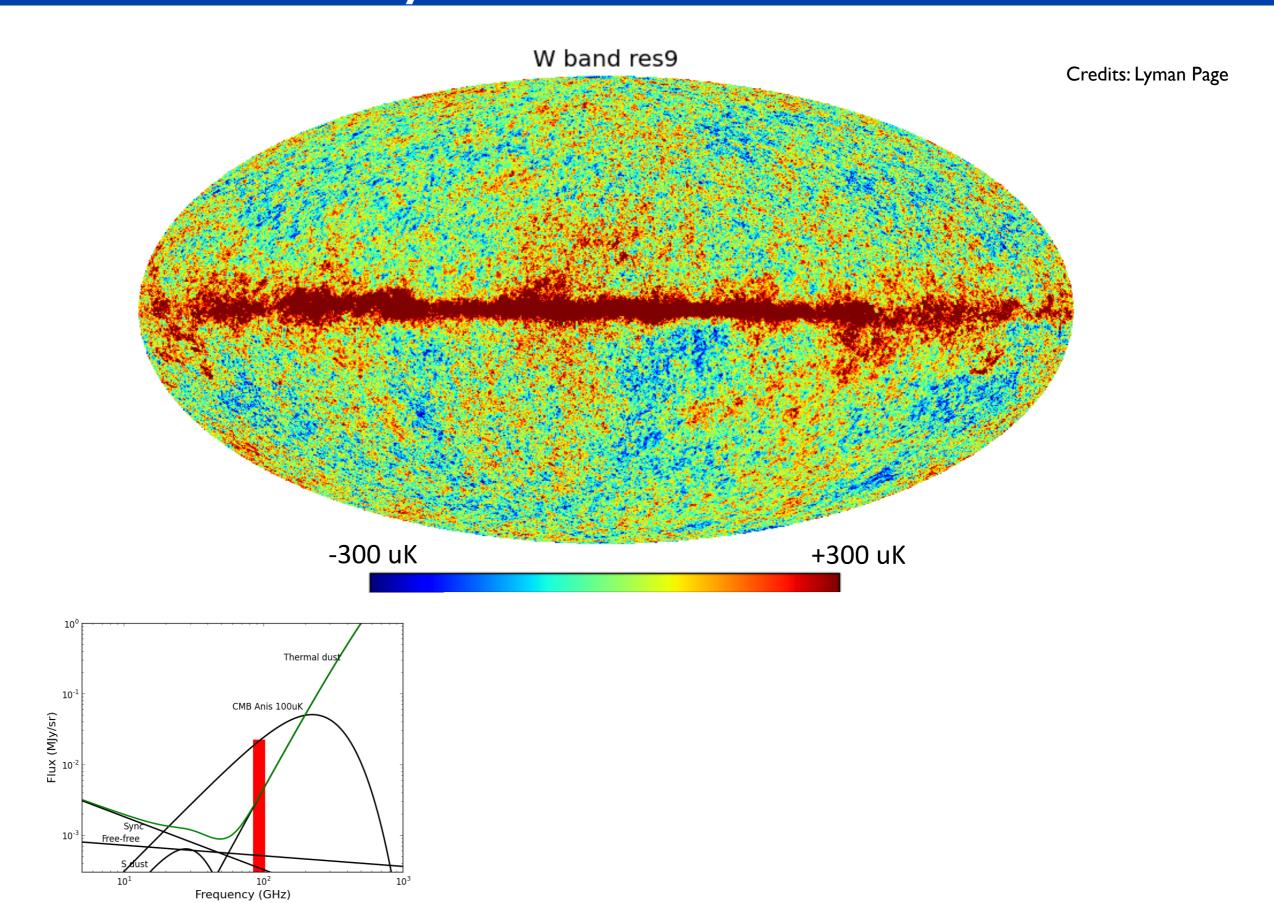


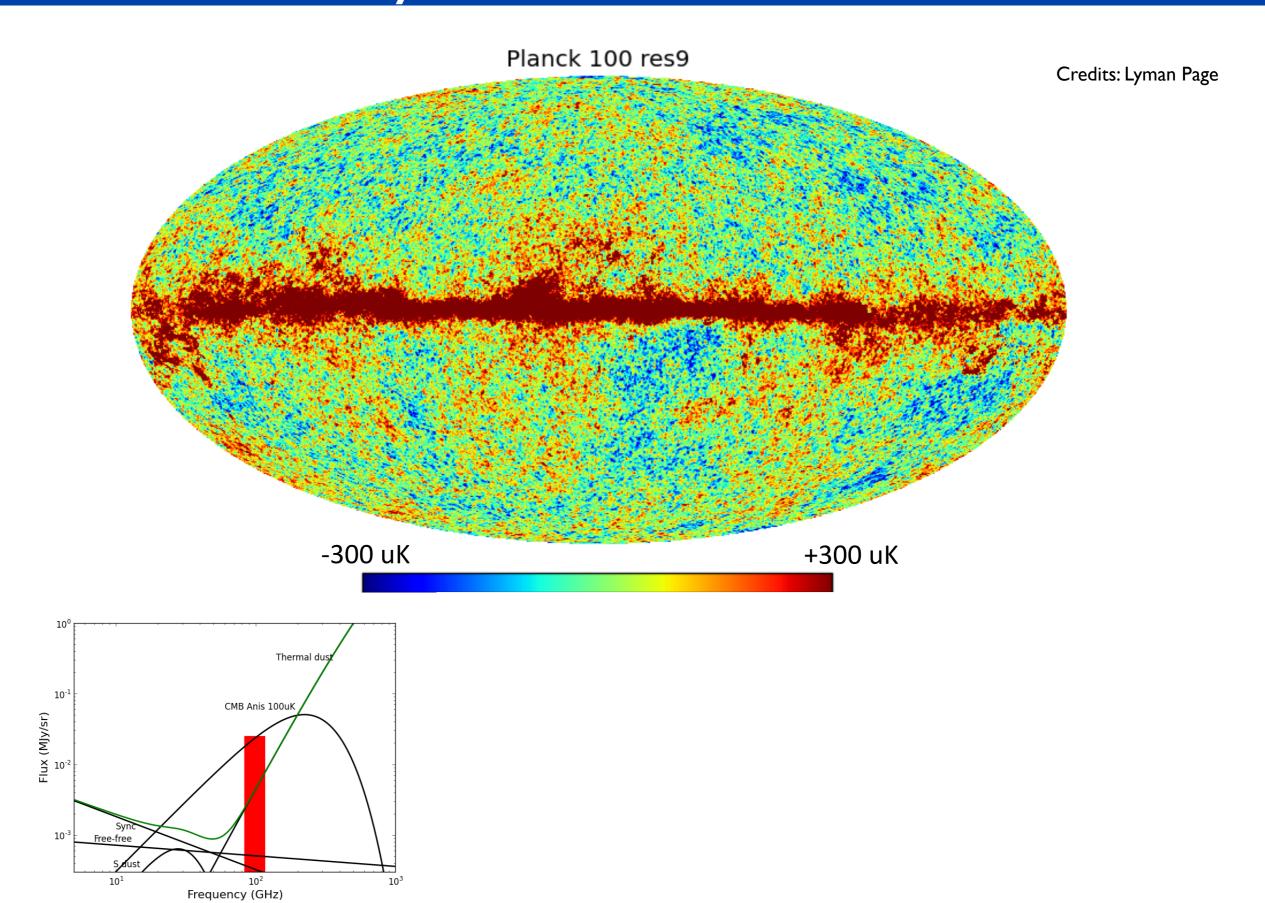




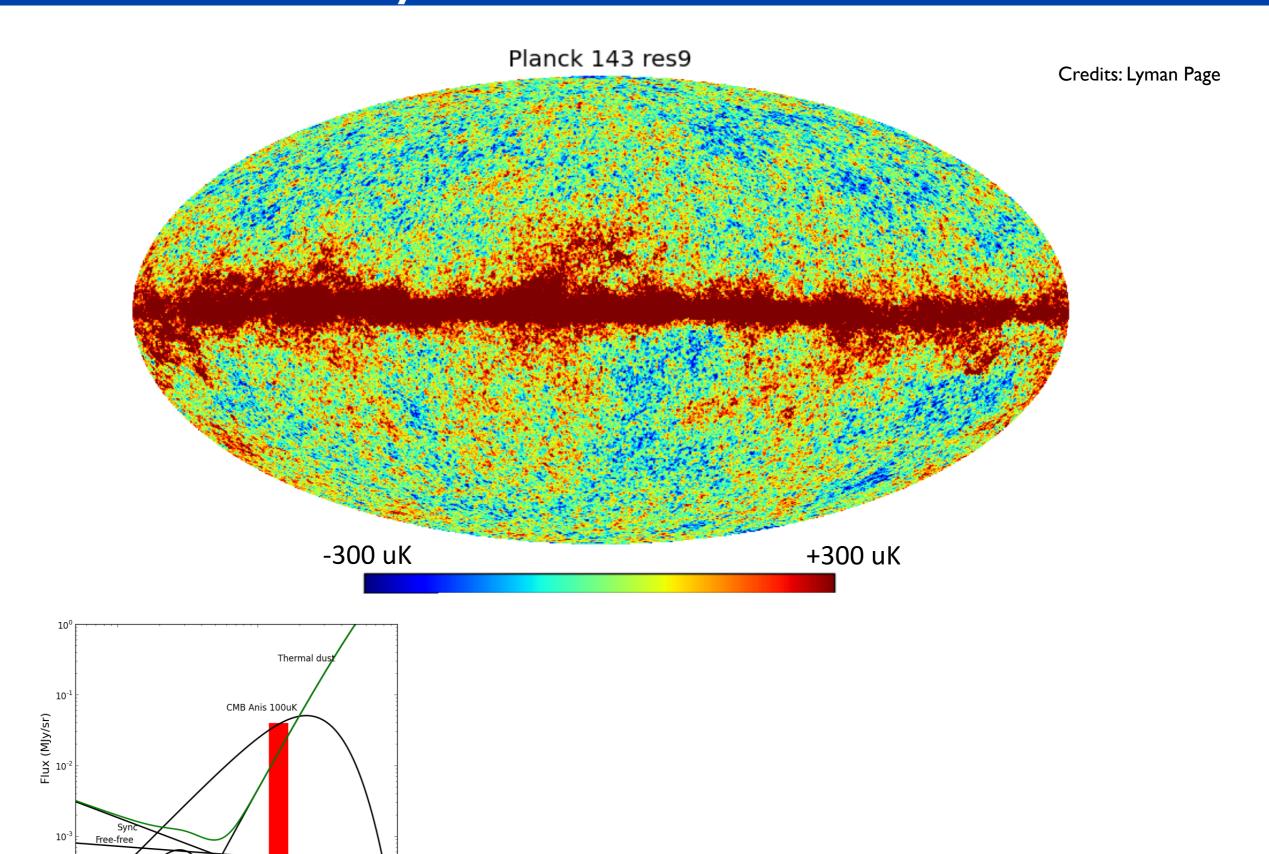


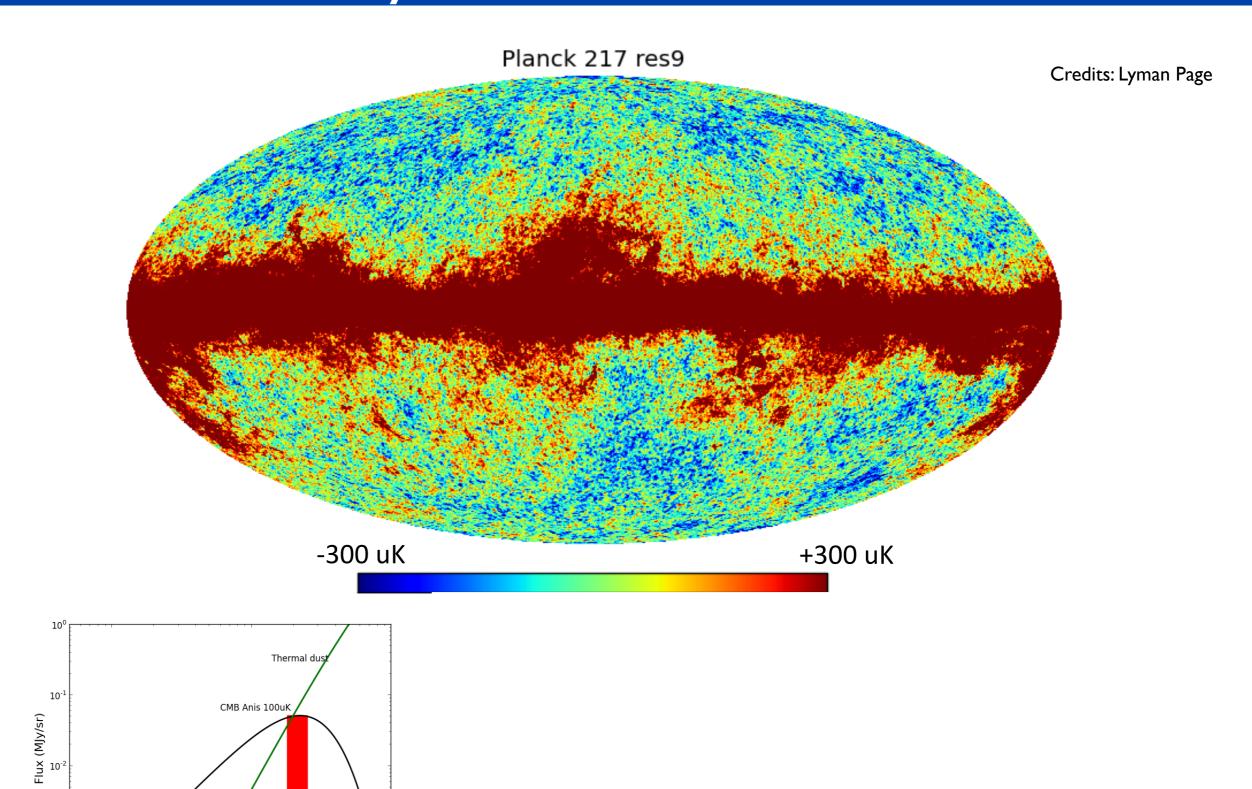


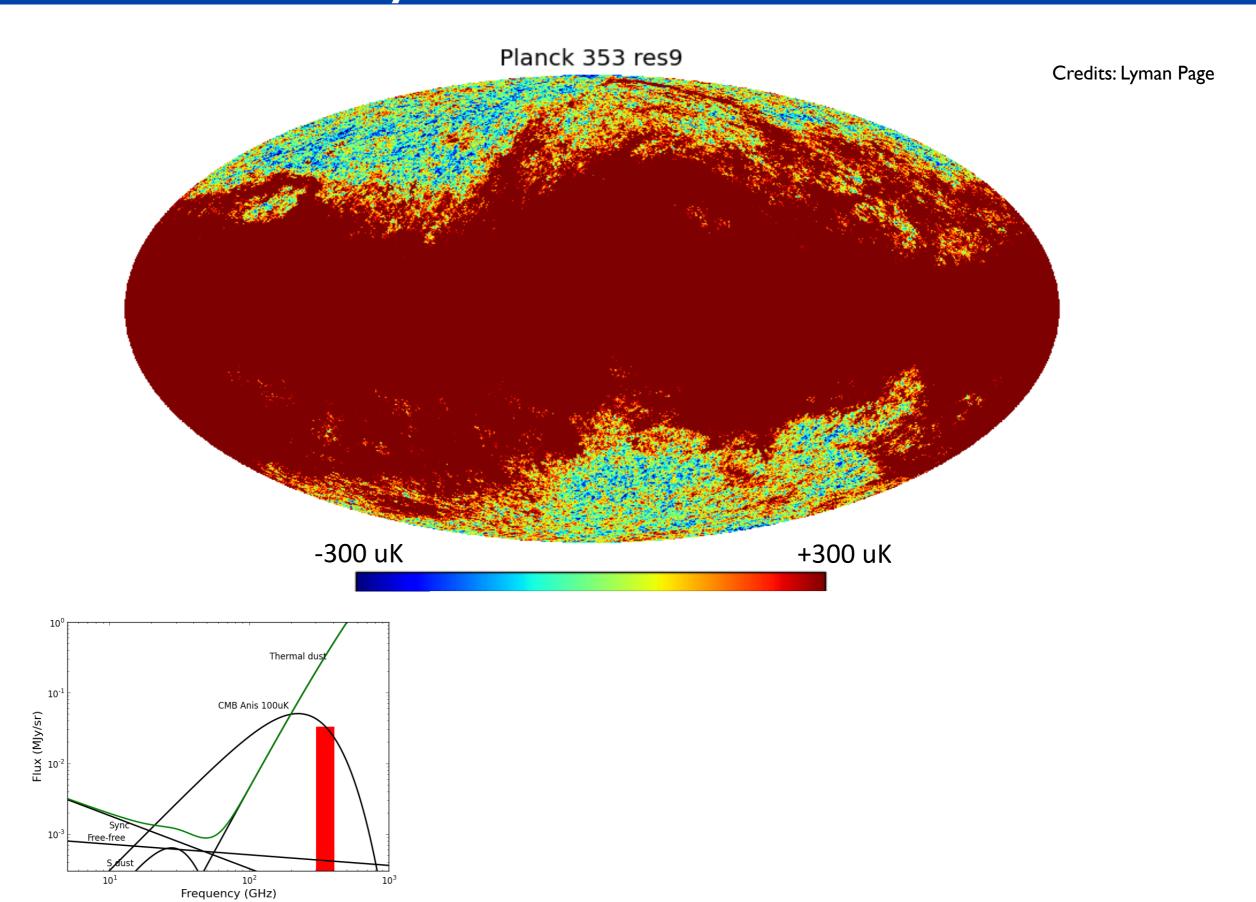




10² Frequency (GHz)

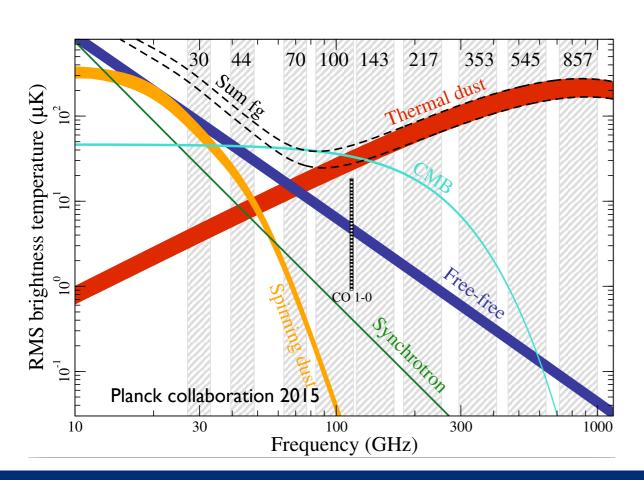


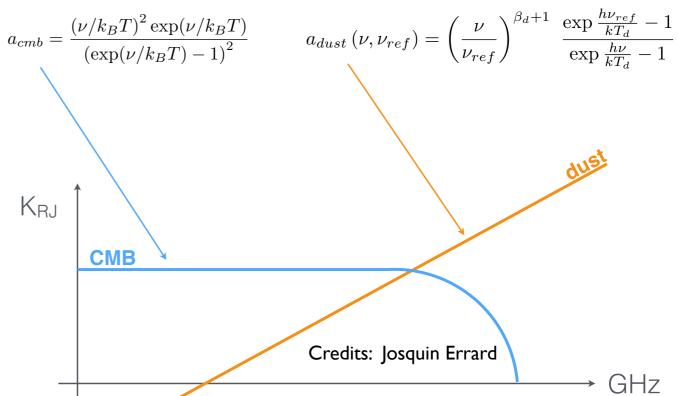


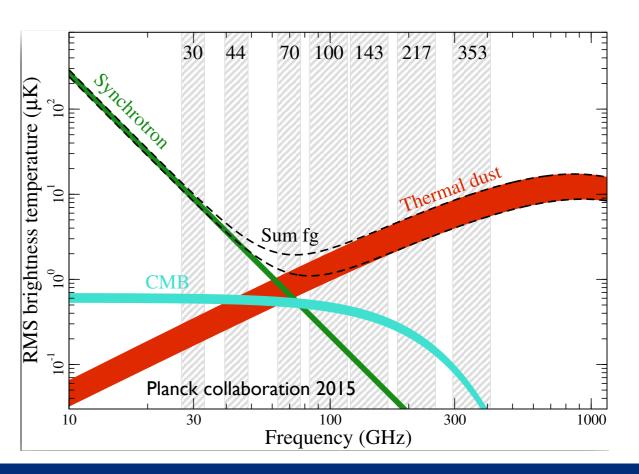


Component separation principle

- How to disentangle CMB and foregrounds?
- Different emission laws, different scaling with frequency
- Multifrequency observations







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Component separation: a concrete example

1- Component separation generalities

a map at a given frequency is a sum of cmb, dust and noise

(1)
$$map(\nu) = a_{cmb}(\nu)s_{cmb} + a_{dust}(\nu)s_{dust} + n(\nu)$$
 for three frequency channels,
$$s \equiv \left[\begin{array}{c} Q \\ U \end{array}\right]$$
 using matrix form

(2)
$$\begin{bmatrix} map(\nu_1) \\ map(\nu_2) \\ map(\nu_3) \end{bmatrix} = \mathbf{A}(\nu_1, \nu_2, \nu_3) \begin{bmatrix} s_{cmb} \\ s_{dust} \end{bmatrix} + \begin{bmatrix} n(\nu_1) \\ n(\nu_2) \\ n(\nu_3) \end{bmatrix}$$
 it's like map-making!

Component separation is performed in two steps:

- 1- Estimation of the mixing matrix **A** method specific
- 2- Solving the linear system (2), with **A** estimated above general to any method

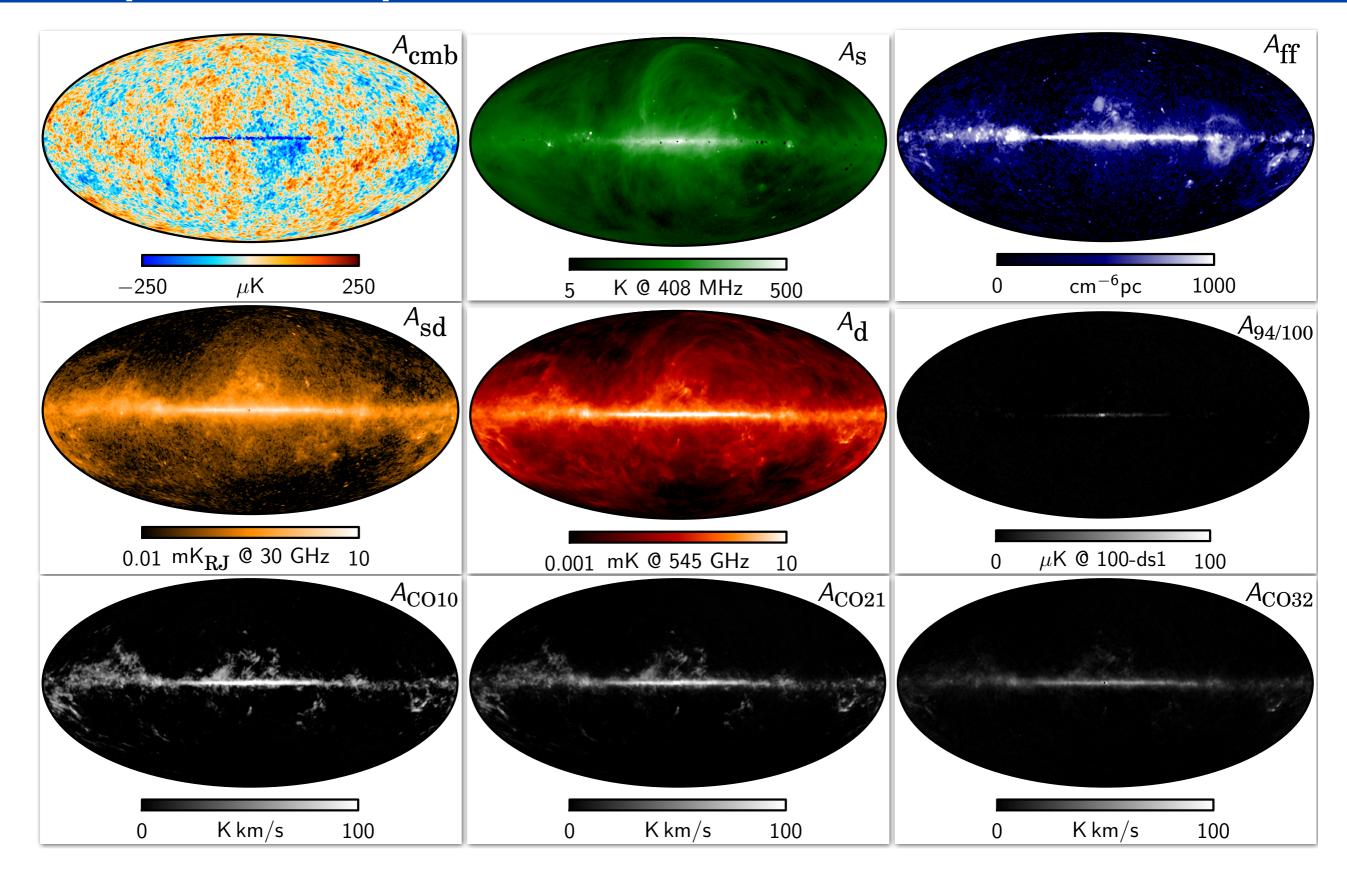
GLS solution

(3)
$$\begin{bmatrix} s_{cmb} \\ s_{dust} \end{bmatrix} = \underbrace{\left(\mathbf{A}^T \mathbf{N}^{-1} \mathbf{A}\right)^{-1}}_{\mathbf{N}} \mathbf{A}^T \mathbf{N}^{-1} \begin{bmatrix} map(\nu_1) \\ map(\nu_2) \\ map(\nu_3) \end{bmatrix}$$

Planck collaboration 2015

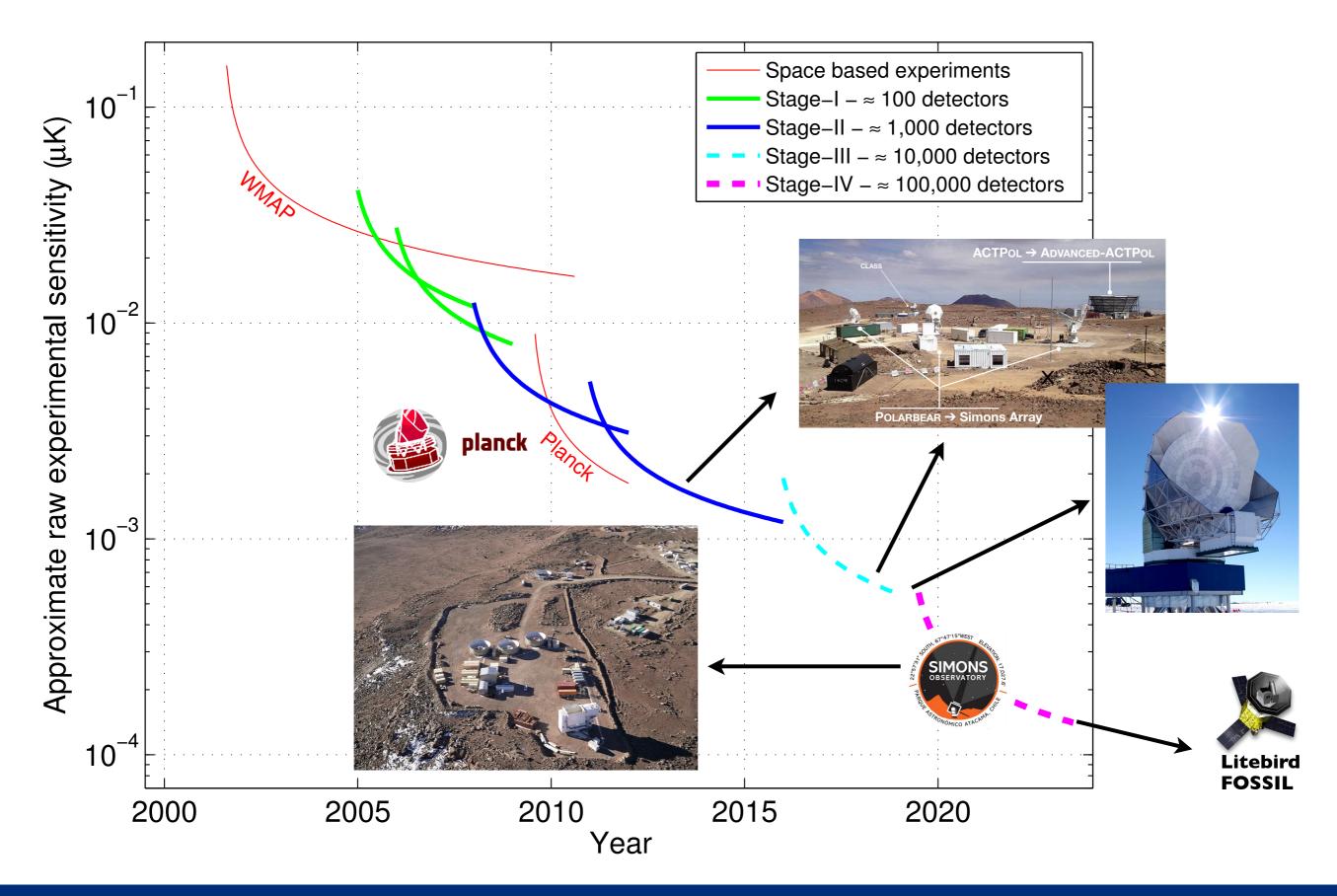
Credits: J. Errard

Component separation: results



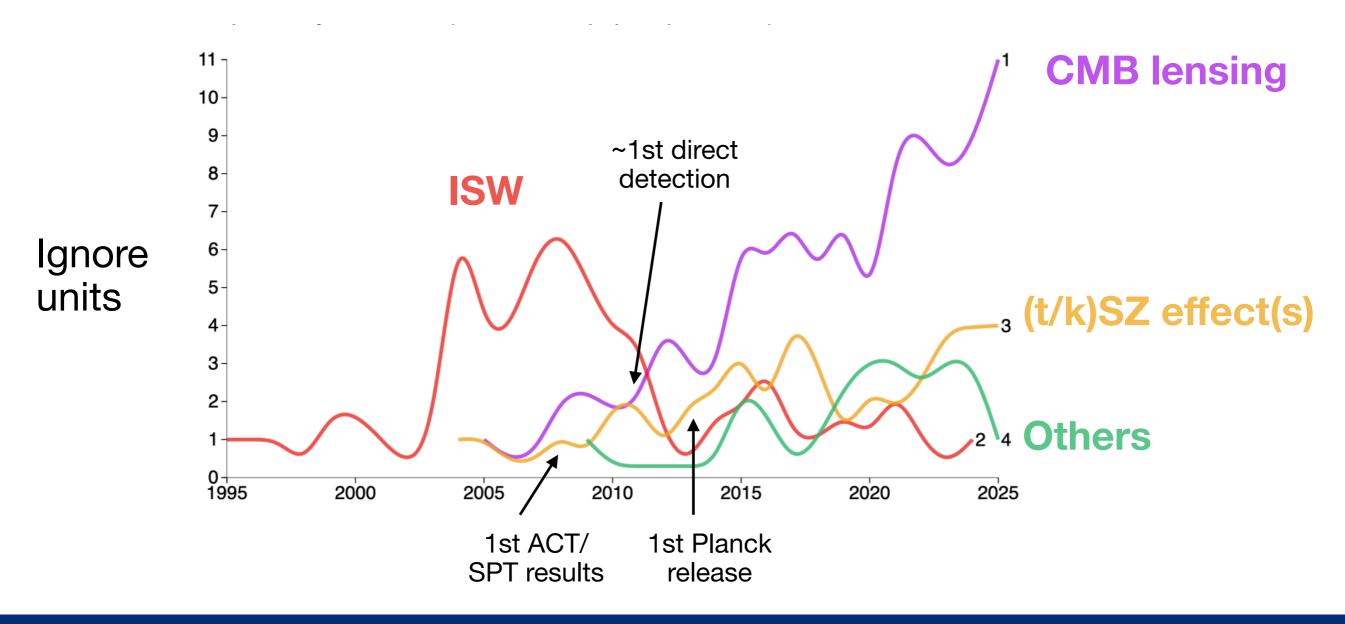
Planck collaboration 2015

Experimental CMB landscape

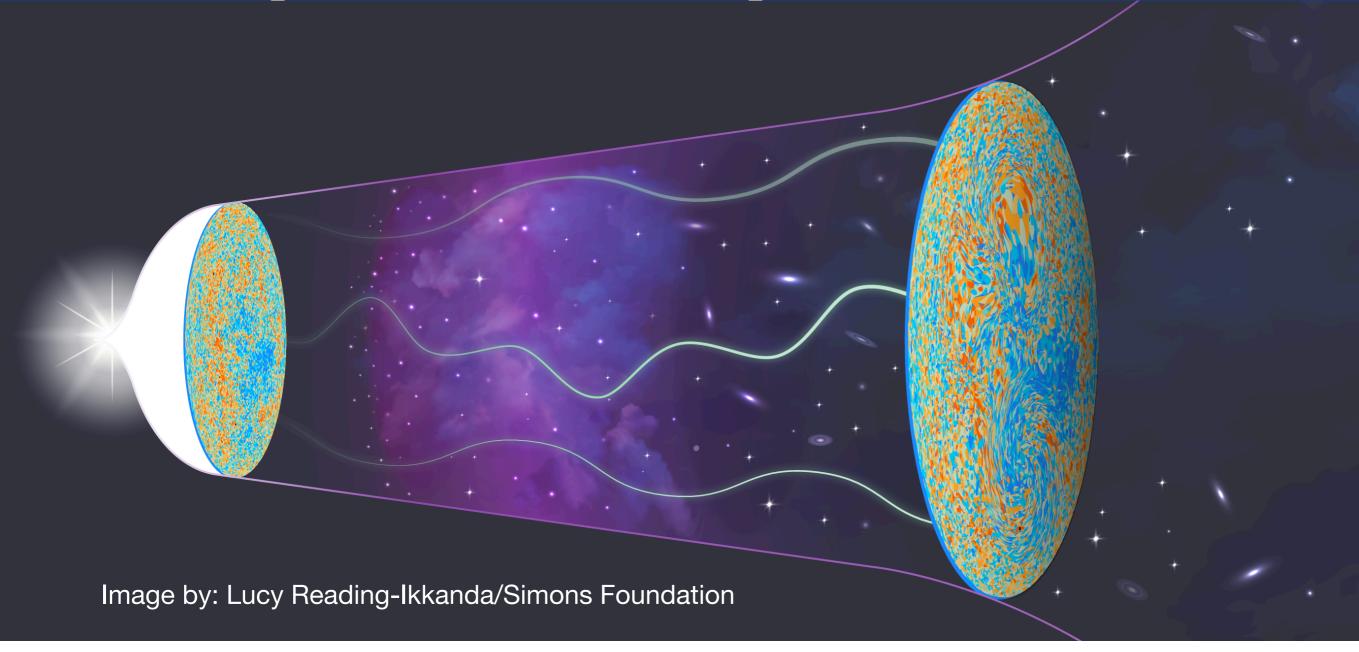


State of the art of the CMB secondaries

- ISW "oldest" probe, becoming less competitive because of limited achievable precision (cosmic variance...)
- CMB lensing hints in early 2000s, first detections 2010, now booming!
- SZ picking up after first Planck data release....

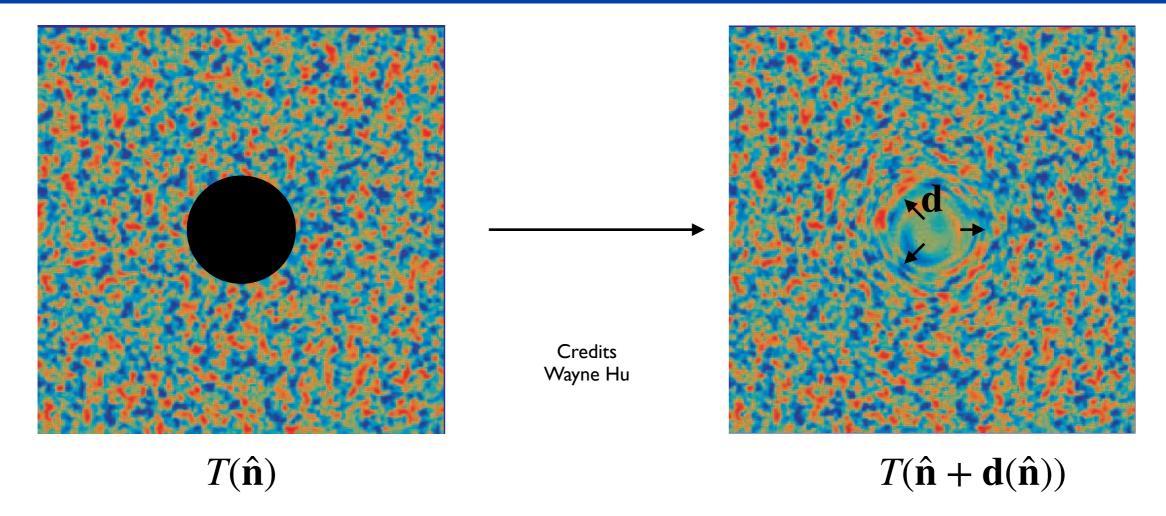


CMB and gravitational lensing



- CMB is the most distant and oldest source of radiations: photons cross potential wells of LSS as they form.
- Preserves surface brightness: no effect if CMB is fully homogeneous.

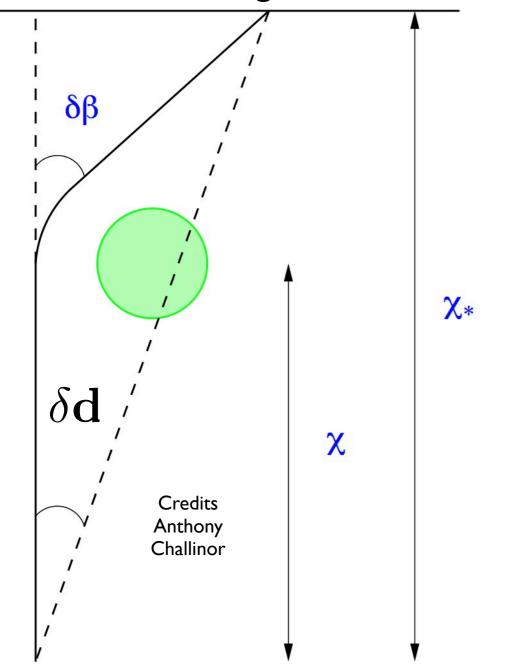
Lensing cartoon



- WARNING: exaggerated cartoon
- Dark matter introduces features in the CMB anisotropies pattern causing shearing and magnification
- The properties of lensing are encoded in the deflection field: can we estimate this?

The lensing geometry

Last scattering surface



ÉCOLE DE PHYSIQUE DES HOUCHES

According to GR photon obey the geodesic equation

$$\frac{dp^{\mu}}{d\lambda} + \Gamma^{\mu}_{\nu\rho} p^{\nu} p^{\rho} = 0$$

• Exercise: $\delta\beta = -2\delta\chi\nabla_\perp\Phi$

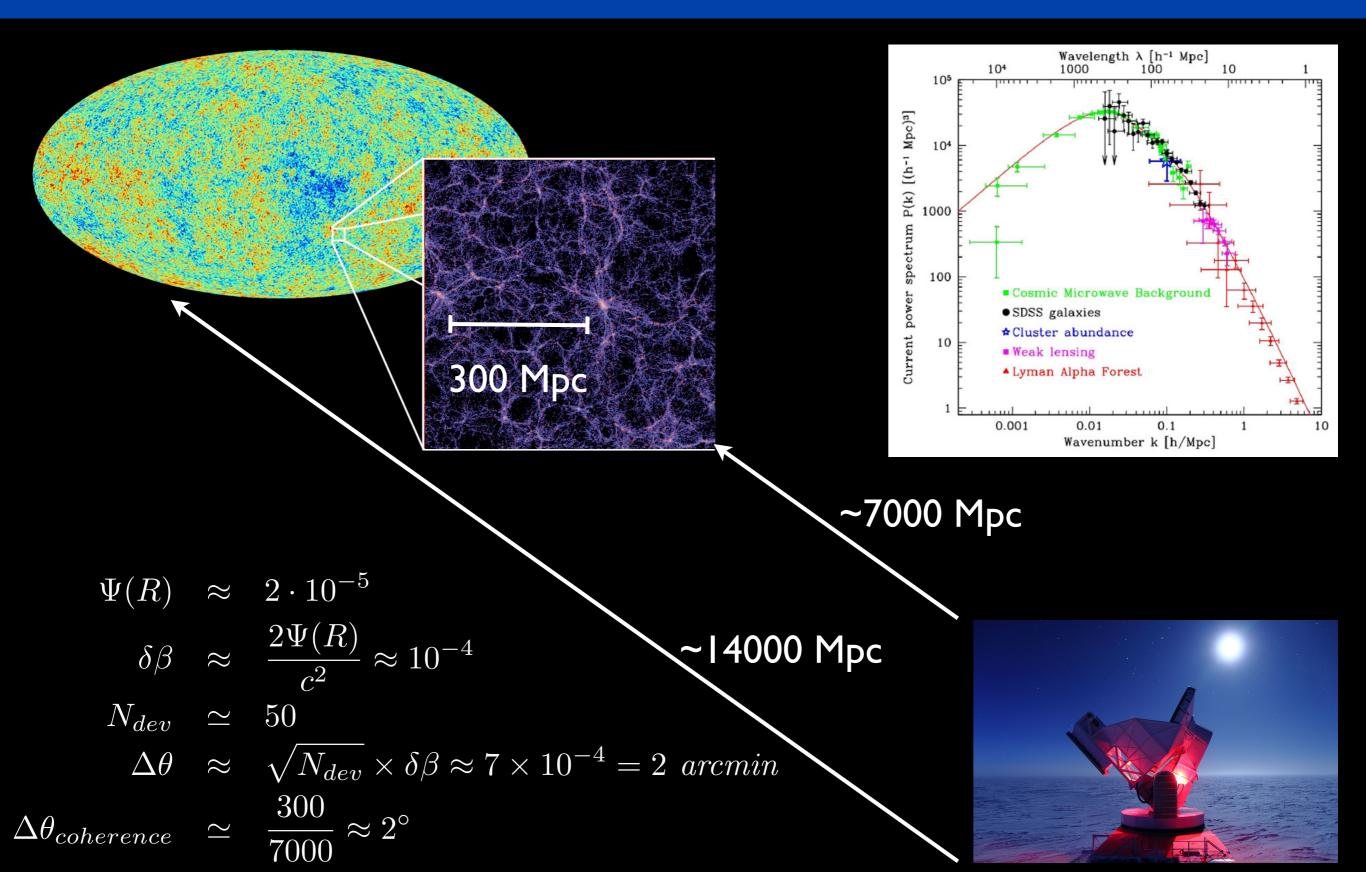
• By pure geometric considerations then

$$\delta \mathbf{d} = -2 \frac{\chi_* - \chi}{\chi_*} \delta \chi \nabla_{\perp} \Phi$$

Total effect then given by

$$\mathbf{d}(\mathbf{\hat{n}}) = -\int_0^{\chi_*} 2d\chi \frac{\chi_* - \chi}{\chi_*} \delta\chi \nabla_{\perp} \Phi(\chi \mathbf{\hat{n}}, \eta_0 - \chi)$$

0-th order calculation

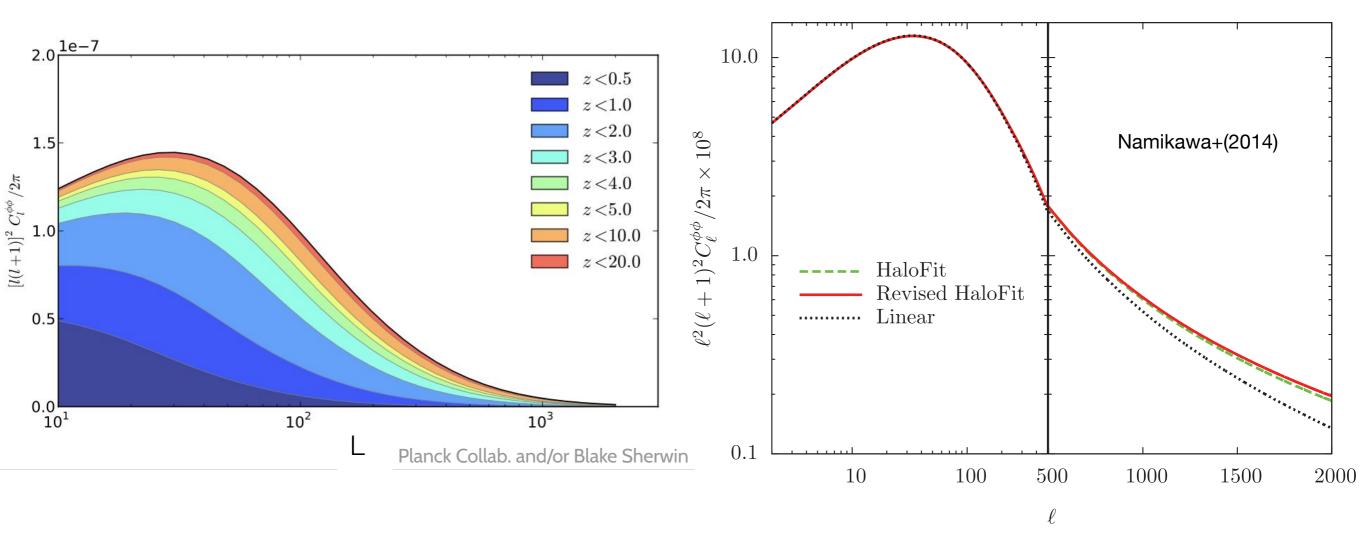


The CMB lensing potential

Unbiased tracers of the whole integrated matter distribution along the line of sight.

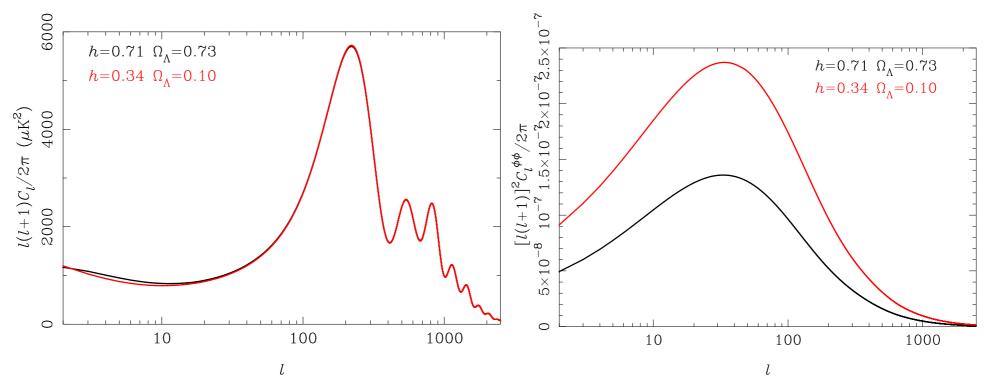
$$\phi(\boldsymbol{\theta}) = -2 \int_0^{\chi_s} \frac{D_A(\chi_s - \chi')}{D_A(\chi_s) D_A(\chi')} \Psi\left(\boldsymbol{\theta}, \chi'\right) \mathrm{d}\chi' \qquad \mathbf{d} = \nabla \phi \qquad \text{Warning!} \\ \kappa \propto -\nabla^2 \phi \to \delta$$

• Sensitive to total matter distribution $\sigma_8\Omega_m^{0.25}$ at z~0.6-5 on mildly non-linear scales.

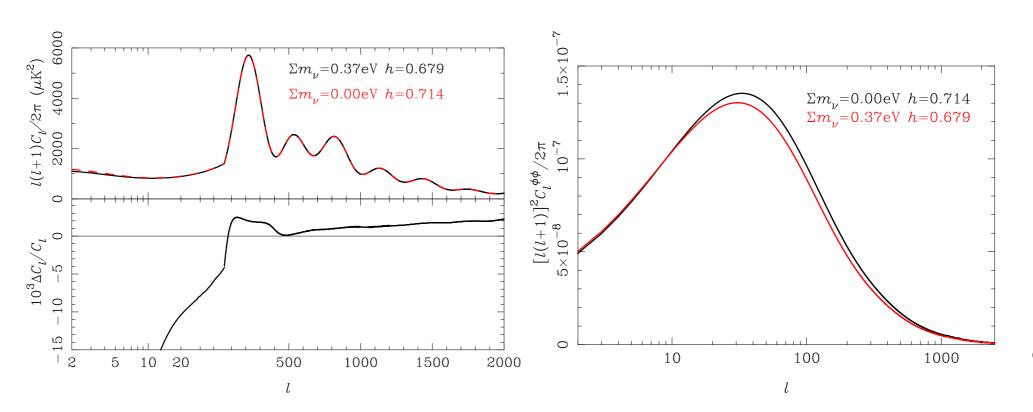


Breaking degeneracies with CMB lensing

Lensing sensitive to geometry and late-time growth of structure: curvature

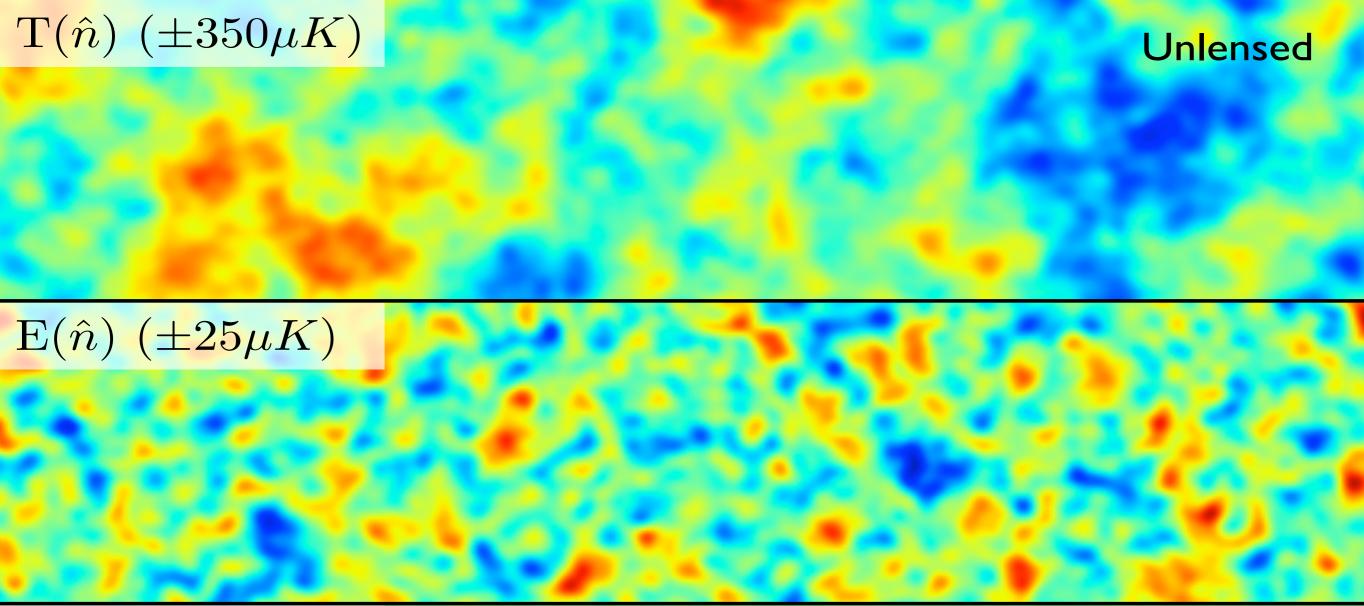


Neutrino masses:



Credits Anthony Challinor





$$B(\hat{n}) \ (\pm 2.5 \mu K)$$

(no primordial B-modes)

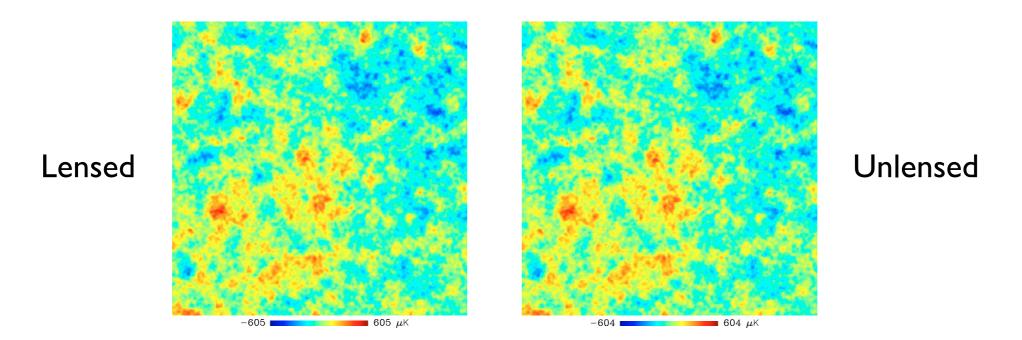
credits D. Hanson

Lensing on CMB maps $T(\hat{n}) \ (\pm 350 \mu K)$ Lensed $E(\hat{n}) (\pm 25 \mu K)$ $B(\hat{n}) (\pm 2.5 \mu K)$ (no primordial B-modes)

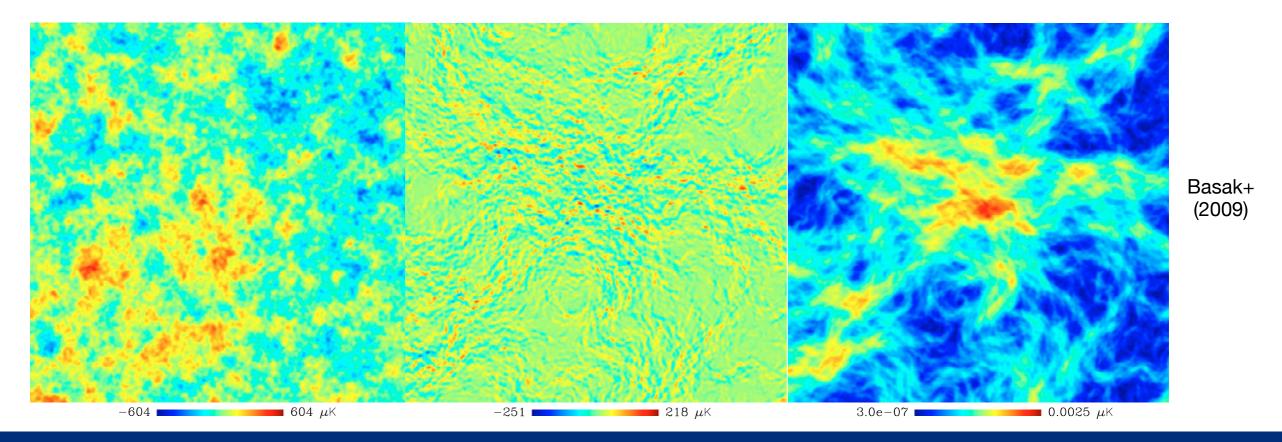
credits D. Hanson

Effects on maps

Lensed and unlensed maps are practically indistinguishable by eye



Their difference shows a pattern similar to the LSS which lensed the signal



A sketch of the effect of lensing

Expanding in 2D Fourier modes

$$\Theta(\mathbf{x}) = \int \frac{d^2l}{(2\pi)^2} \Theta(\mathbf{l}) e^{i\mathbf{l}\cdot\mathbf{x}}$$
Hu+(2000)
Lewis & Challinor (2006)

Expanding in Taylor series and Fourier transforming

$$\tilde{\Theta}(\mathbf{x}) = \Theta(\mathbf{x} + \mathbf{d}) = \Theta(\mathbf{x}) + \nabla \phi \cdot \nabla \Theta + \cdots$$

$$\tilde{\Theta}(\mathbf{l}) = \Theta(\mathbf{l}) + \int \frac{d^2 L}{(2\pi)^2} [\mathbf{L}\phi(\mathbf{L})] \cdot [(\mathbf{l} - \mathbf{L})\Theta(\mathbf{l} - \mathbf{L})] + \cdots$$

The power spectrum reads

$$\langle \Theta(\mathbf{l})\Theta^*(\mathbf{l'})\rangle = (2\pi)^2 C_{\mathbf{l}}\delta(\mathbf{l}-\mathbf{l'})$$

$$\langle \tilde{\Theta}(\mathbf{l}) \tilde{\Theta}^*(\mathbf{l}') \rangle = (2\pi)^2 C_{\mathbf{l}} \delta(\mathbf{l} - \mathbf{l}') + \langle \delta^{(1)} \Theta(\mathbf{l}) \delta^{(1)} \Theta(\mathbf{l}') \rangle + \langle \Theta(\mathbf{l}) \delta^{(2)} \Theta(\mathbf{l}') \rangle + \langle \Theta(\mathbf{l}') \delta^{(2)} \Theta(\mathbf{l}) \rangle + \cdots + \langle \Theta(\mathbf{l}') \delta^{(2)} \Theta(\mathbf{l}) \rangle + \cdots$$

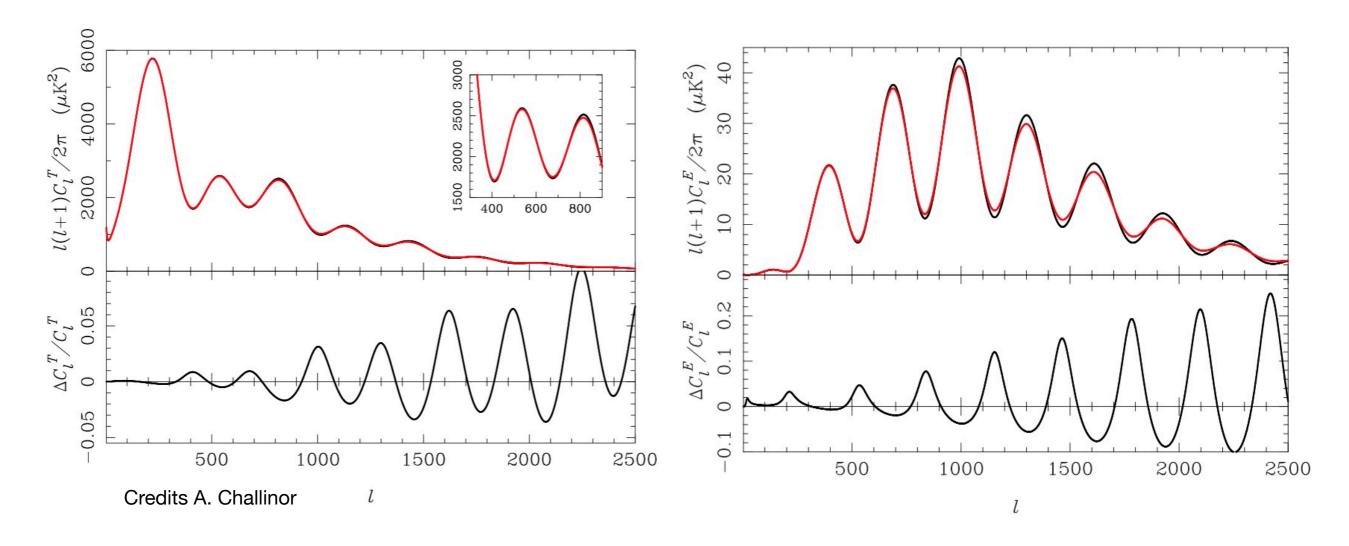
Effect of CMB angular power spectra

Effective smoothing of peaks measured at 1% error and routinely accounted for

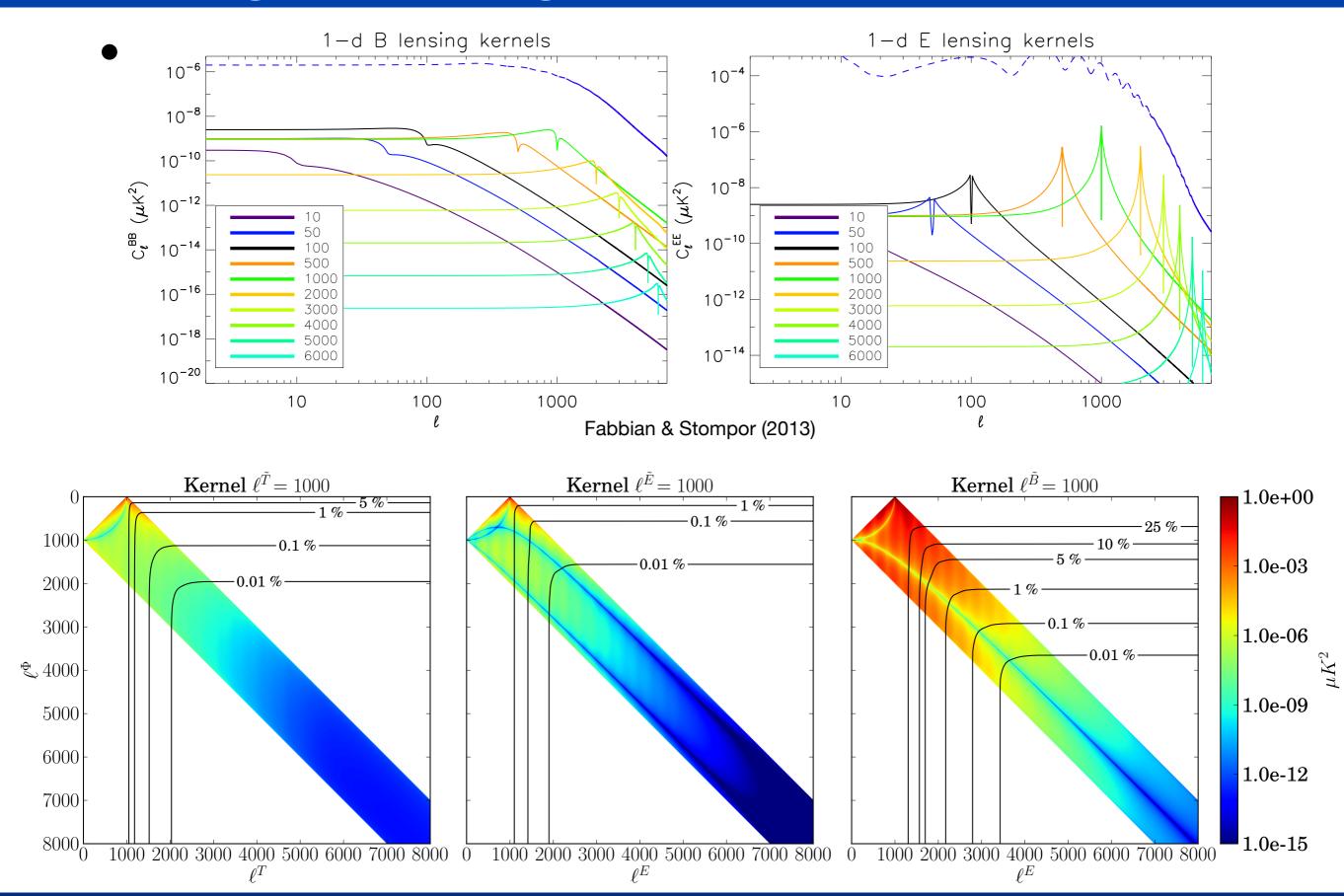
$$\tilde{C}_{\mathbf{l}} = \left[1 - \frac{1}{2} l^2 \langle d^2 \rangle \right] C_{\mathbf{l}} + \int \frac{d^2 L}{(2\pi)^2} C_{|\mathbf{l} - \mathbf{L}|} C_{\mathbf{L}}^{\phi} [\mathbf{L} \cdot (\mathbf{l} - \mathbf{L})]^2$$

Hu (2000), Lewis & Challinor (2000)

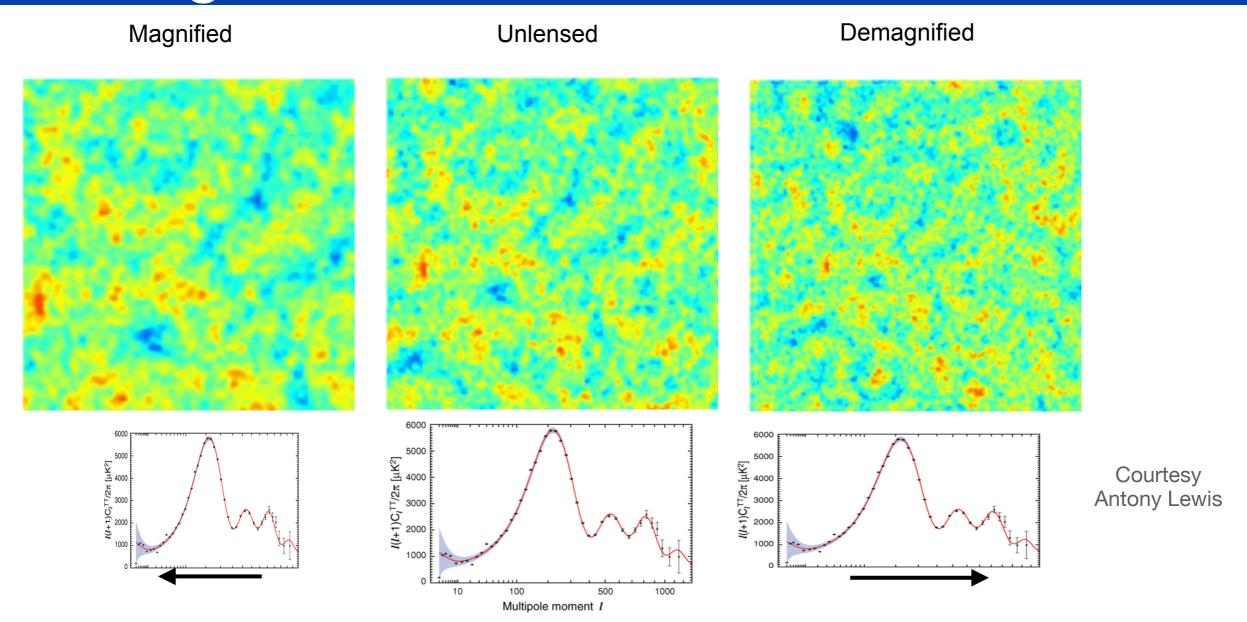
Smoothing = power redistribution. More accurate formulas available...



Visualizing the lensing convolution



CMB lensing reconstruction fundamentals



 Modulation of the statistical properties as a function of the position of the sky, i.e. a field (CMB) modulated by an intervening one (lensing): break of translational invariance

$$\langle \Theta(\mathbf{l})\Theta^*(\mathbf{L} - \mathbf{l}) \rangle = 0 \qquad \longrightarrow \qquad \langle \tilde{\Theta}(\mathbf{l})\tilde{\Theta}^*(\mathbf{L} - \mathbf{l}) \rangle \sim \phi(\mathbf{L})$$

• Similar techniques for other quantities in CMB: $\tau(\hat{\mathbf{n}})$, $\alpha(\hat{\mathbf{n}})$

More in details...

• A general quadratic estimator uses a combination of 2 Fourier modes of the data

$$\hat{\phi}(\mathbf{L}) = A_L \int_{\mathbf{I}} f(\mathbf{I}, \mathbf{L}) \tilde{\Theta}_{expt}(\mathbf{I}) \tilde{\Theta}_{expt}(\mathbf{L} - \mathbf{I})$$
Hu & Okamoto (2001)
Lewis (2011)
Fabbian, Lewis, Beck (2019)

• One has to pick the g and A to make the estimator unbiased and optimal

$$\phi(\mathbf{L}) = \left\langle \hat{\phi}(\mathbf{L}) \right\rangle_{\text{CMB}} \longrightarrow \left\langle \tilde{\Theta}(\mathbf{l}) \tilde{\Theta}(\mathbf{L} - \mathbf{l}) \right\rangle_{\text{CMB}} = \left[(\mathbf{L} - \mathbf{l}) \cdot \mathbf{L} \ \tilde{C}_{\mathbf{l} - \mathbf{L}} + \mathbf{l} \cdot \mathbf{L} \ \tilde{C}_{l} \right] \phi(\mathbf{L}) \equiv K(\mathbf{l}, \mathbf{L}) \phi(\mathbf{L})$$

$$\left\langle \hat{\phi}^*(\mathbf{L})\hat{\phi}(\mathbf{L}') \right\rangle_{\text{CMB}} - \phi^*(\mathbf{L})\phi(\mathbf{L}') = (2\pi)^2 V[f](\mathbf{L}) \delta(\mathbf{L} - \mathbf{L}')$$

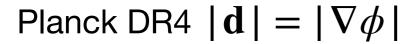
Once you have that you can compute your power spectrum (with some complications)

$$\hat{\phi}(\mathbf{L}) = N(\mathbf{L})\mathbf{L} \cdot \int \frac{d^2l}{(2\pi)^2} \frac{\mathbf{l}C_l}{C_l^{noisy}} \Theta(\mathbf{l}) \frac{C_{|L-l|}}{C_{|L-l|}^{noisy}} \Theta^*(\mathbf{l} - \mathbf{L})$$

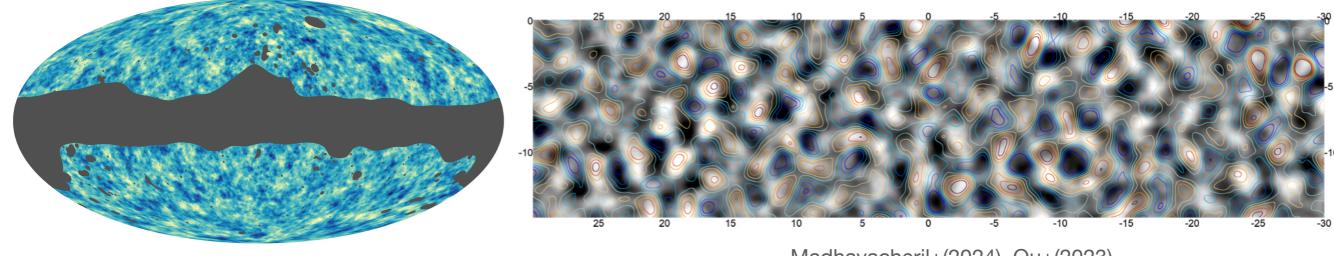
$$C_L^{\hat{\phi}\hat{\phi}} \sim \langle \tilde{\Theta}\tilde{\Theta}\tilde{\Theta}\tilde{\Theta}\rangle \rightarrow \langle \tilde{\Theta}\tilde{\Theta}\tilde{\Theta}\tilde{\Theta}\rangle - \langle \tilde{\Theta}\tilde{\Theta}\rangle\langle \tilde{\Theta}\tilde{\Theta}\rangle + \dots = C_L^{\phi\phi} + N_0 + N_1 \dots$$

- Similar estimators can be derived for polarization or temperature plus polarization.
- Better estimator can be derived to minimize spurious contaminations (e.g. foregrounds...)

CMB lensing state of the art

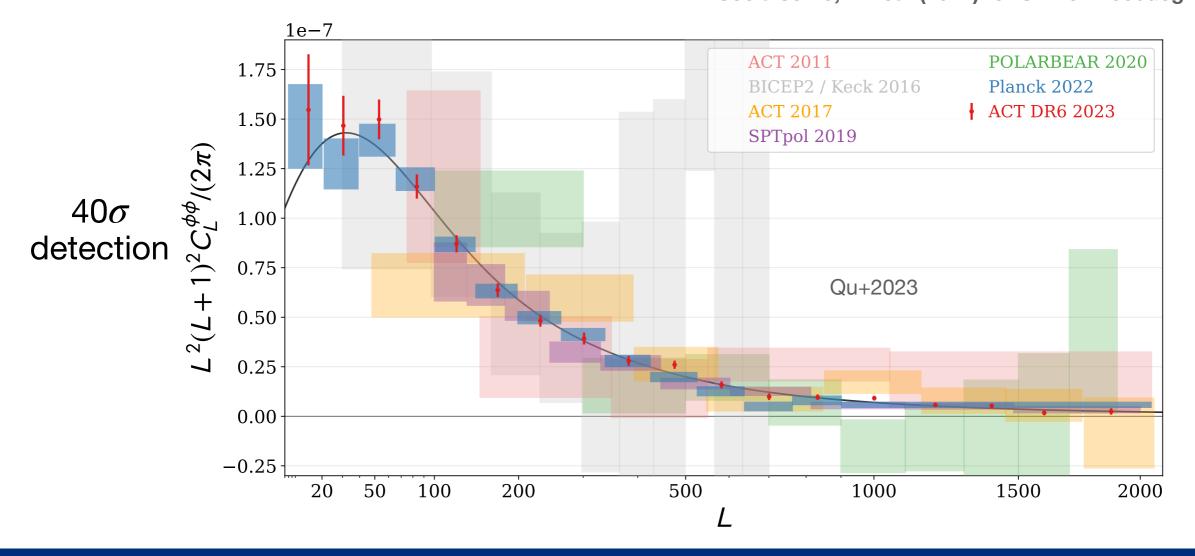


ACT (~40% sky, $\kappa \propto \nabla^2 \phi$)



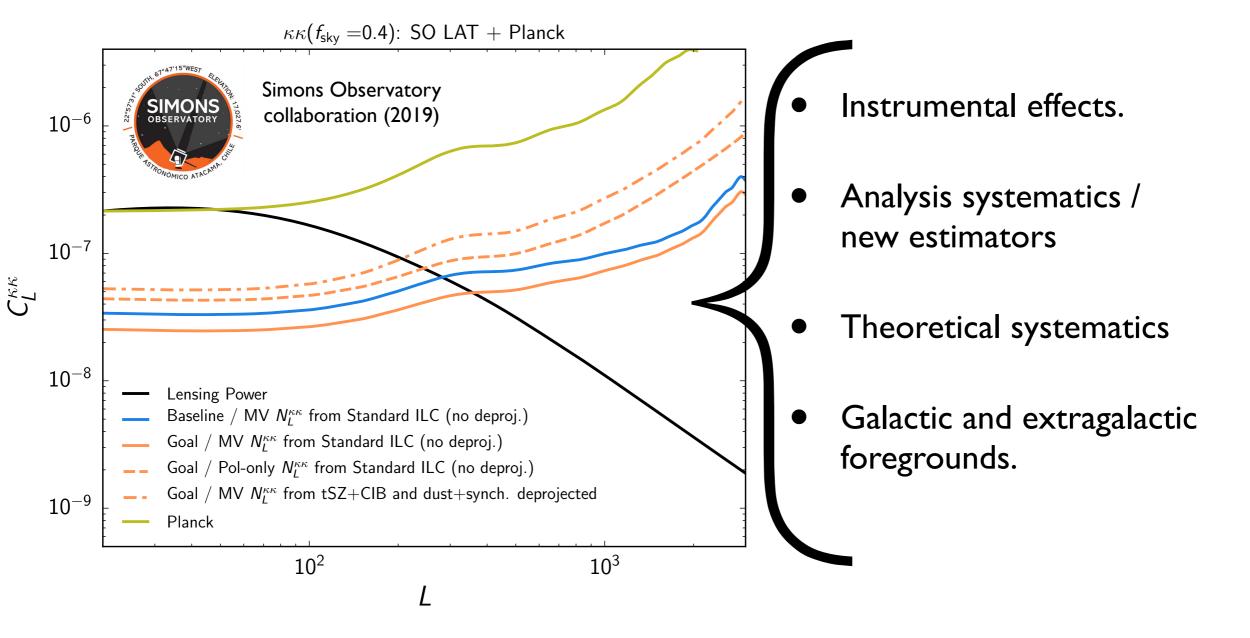
Planck (2018), Carron+(2022)

Madhavacheril+(2024), Qu+(2023). See also Fe, Millea+(2024) for SPT on 1500deg2



What we expect in the coming years

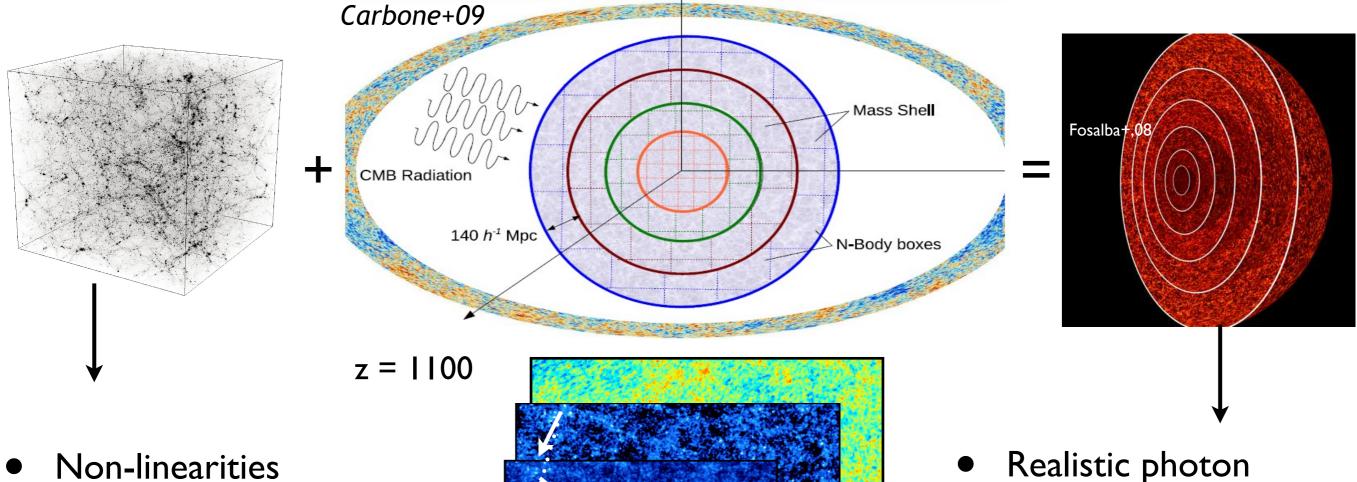
- First detection at 30% precision in ~2011, rapid progress but this is just the beginning.
- SO will measure CMB lensing potential at >100 σ significance, even higher precision for S4.
- CMB lensing will soon start imaging non-linear structures on large sky fractions



Towards a coherent modeling of lensing

z = 0

• Lensing depends on matter and we know matter is not a Gaussian random field...



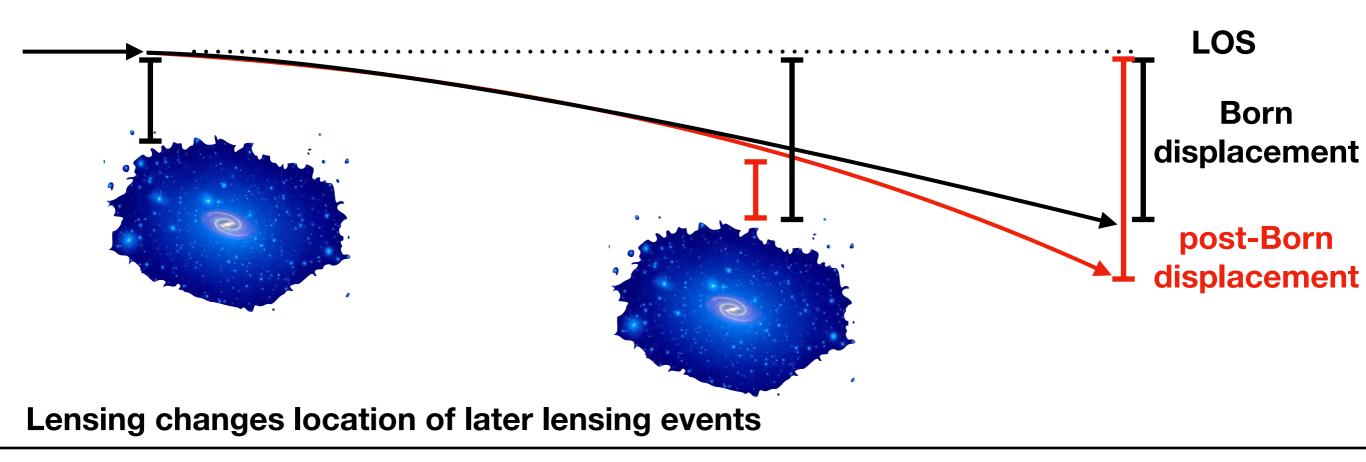
 Non-linearities fully accounted

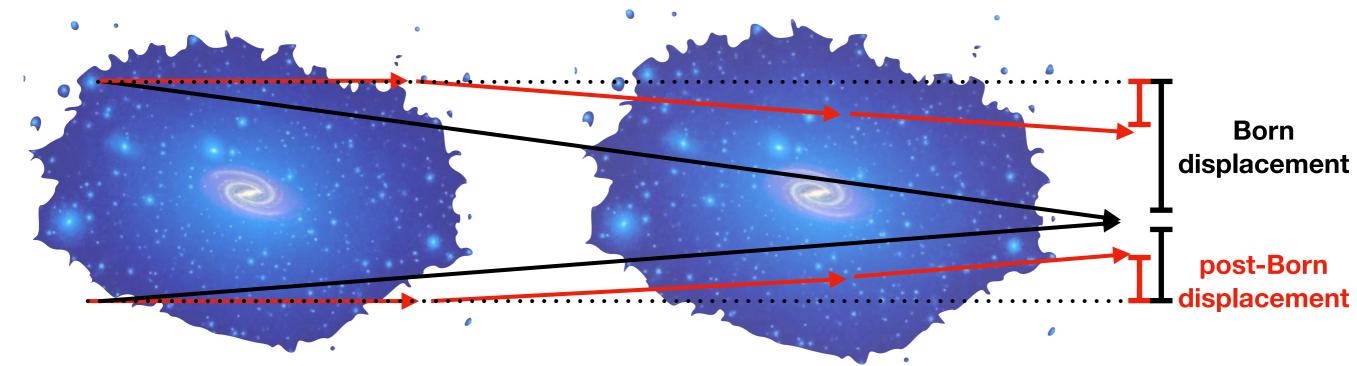
> Carbone+(2009) Calabrese+(2015) Lewis+(2016,2017) Pratten+(2017)

diffusion propagation

Fanizza+(2016) Fabbian+(2018)

Post-Born corrections: what are they?



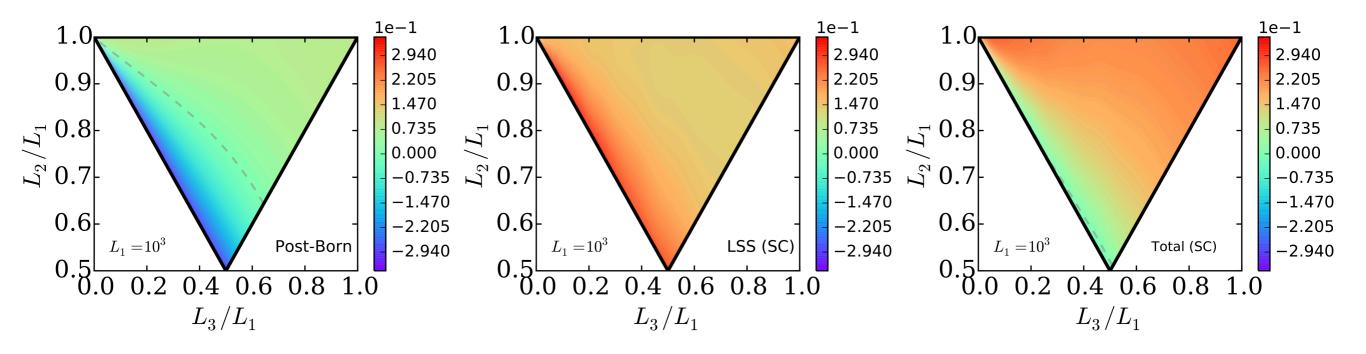


Size and shape of image affected by first lensing event

Higher-order biases in CMB lensing estimation

Pratten & Lewis (2016) Fabbian+(2018)

$$(L_2L_3)^{1/2} b_{L_1L_2L_3}^{\kappa\kappa\kappa} / (C_{L_1}^{\kappa\kappa} C_{L_2}^{\kappa\kappa} C_{L_3}^{\kappa\kappa})^{1/2}$$



$$\hat{\phi}(\mathbf{L}) = A_L \int_{\mathbf{l}} g(\mathbf{l}, \mathbf{L}) \tilde{T}_{\text{expt}}(\mathbf{l}) \tilde{T}_{\text{expt}}(\mathbf{L} - \mathbf{l})$$

$$\tilde{T}(\mathbf{l}) = T(\mathbf{l}) + \delta T(\mathbf{l}) + \delta^2 T(\mathbf{l}) + \mathcal{O}(\phi^3)$$

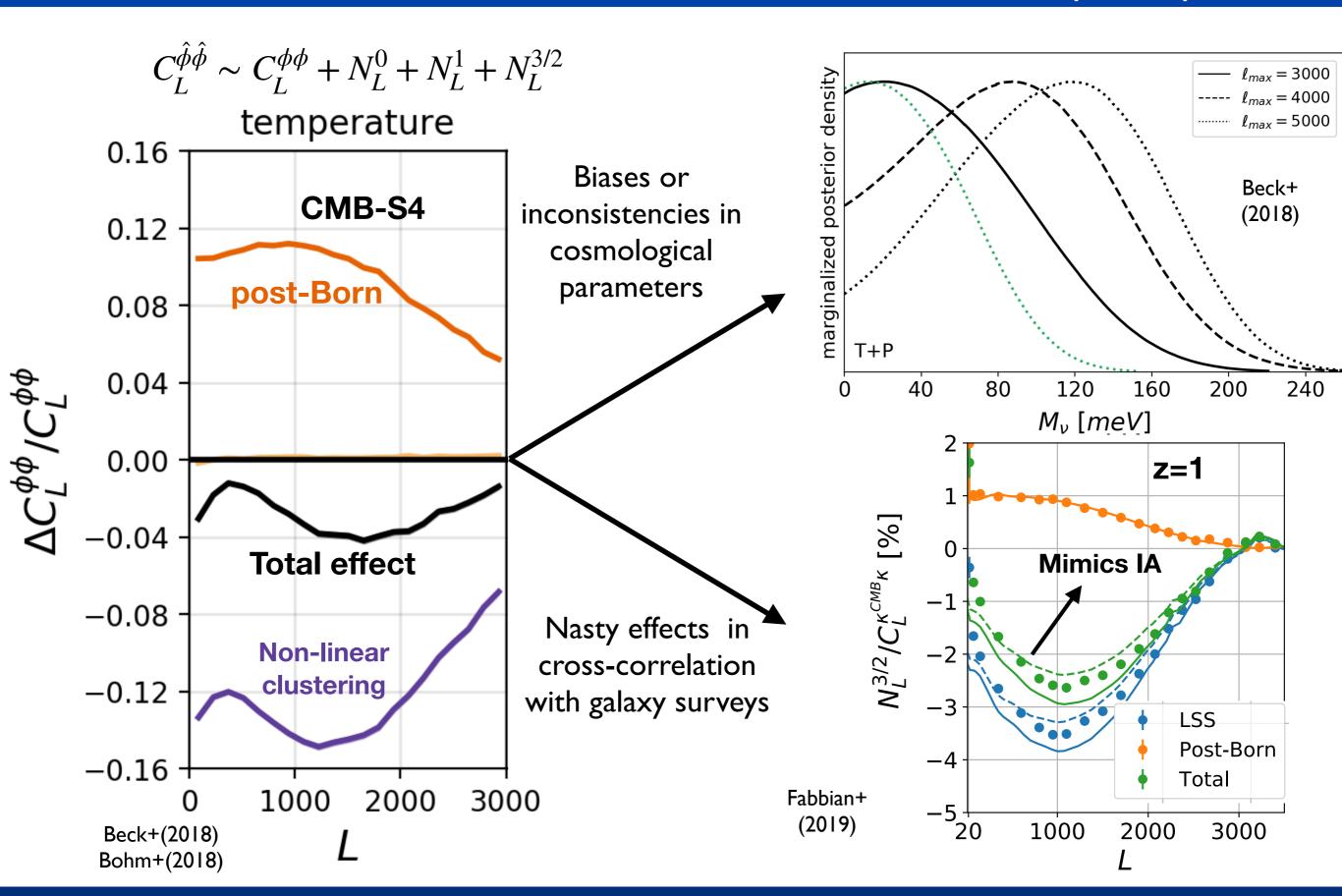
$$\delta T(\mathbf{l}) = -\int_{\mathbf{l}'} \mathbf{l}' \cdot (\mathbf{l} - \mathbf{l}') T(\mathbf{l}') \phi(\mathbf{l} - \mathbf{l}')$$

$$\langle \tilde{T}\tilde{T}\tilde{T}\tilde{T}\tilde{T}\rangle = \langle \delta T\delta T\delta TT\rangle + \cdots = \langle T_{,i}\phi_{,i}T_{,j}\phi_{,j}T_{,k}\phi_{,k}T\rangle + \cdots$$

Böhm+(2016)

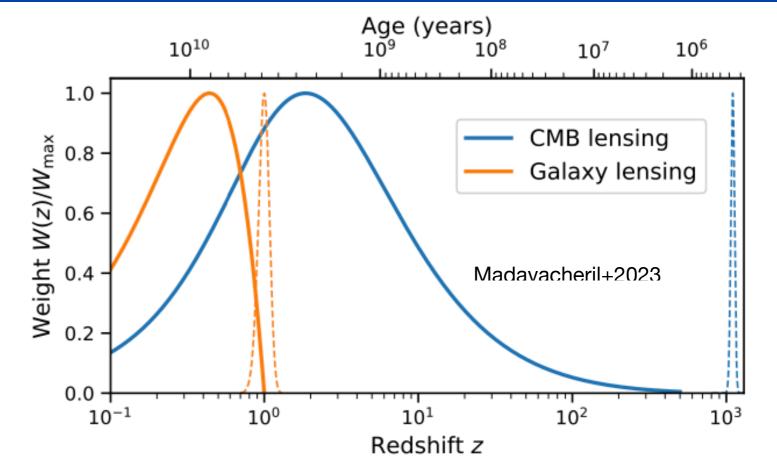
$$C_l^{TT}B_{\phi}(\mathbf{l}_1-\mathbf{l},\mathbf{l}_2+\mathbf{l},-\mathbf{l}_1-\mathbf{l}_2)$$

Non-Gaussian effects in reconstructed $\phi(N^{3/2})$



CMB probes and cross-correlation

- CMB lensing: integrated, 2D projected, unbiased probe of matter.
- Integrated = overlaps with all the matter in the universe.
- Synergies with any other probe of matter e.g. LSS surveys.
- Reduces systematics



$$\kappa_{gal,obs} = \kappa_{gal} + s_{gal} \qquad \kappa_{CMB,obs} = \kappa_{CMB} + s_{CMB}$$

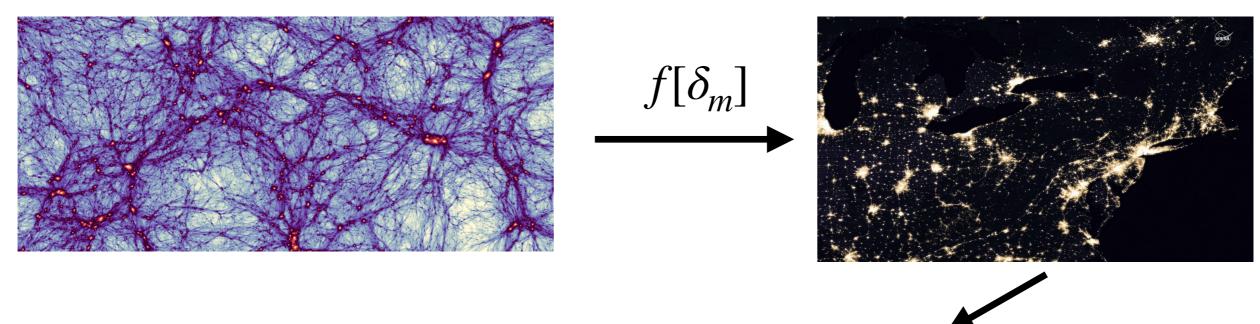
$$\langle \kappa_{gal,obs} \kappa_{gal,obs} \rangle = \langle \kappa_{gal} \kappa_{gal} \rangle + \langle s_{gal} s_{gal} \rangle + \langle \kappa_{gal} s_{gal} \rangle$$

$$\langle \kappa_{CMB,obs} \kappa_{CMB,obs} \rangle = \langle \kappa_{CMB} \kappa_{CMB} \rangle + \langle s_{CMB} s_{CMB} \rangle + \langle \kappa_{CMB} s_{CMB} \rangle$$

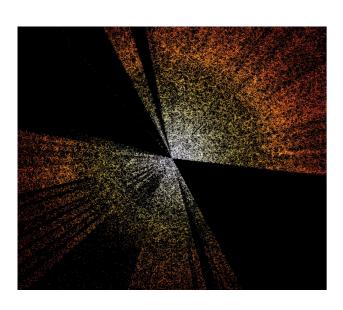
$$\langle \kappa_{CMB,obs} \kappa_{gal,obs} \rangle = \langle \kappa_{CMB} \kappa_{gal} \rangle + \langle s_{CMB} s_{gal} \rangle + \langle \kappa_{CMB} s_{gal} \rangle + \langle \kappa_{gal} s_{CMB} \rangle$$

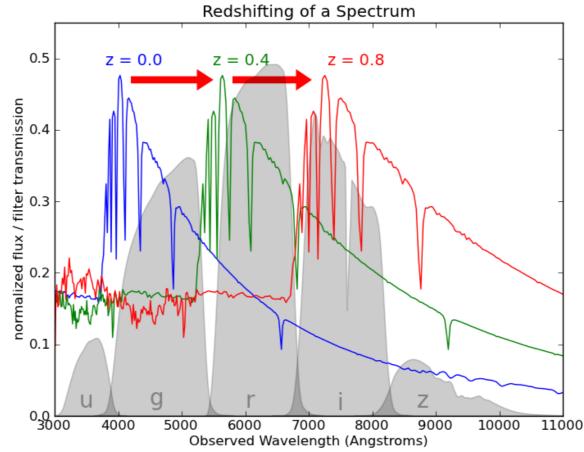
Beyond CMB observations

Observing matter distributions as it grows: we need "tracers"



 Spectroscopic surveys (e.g. DESI, Euclid)



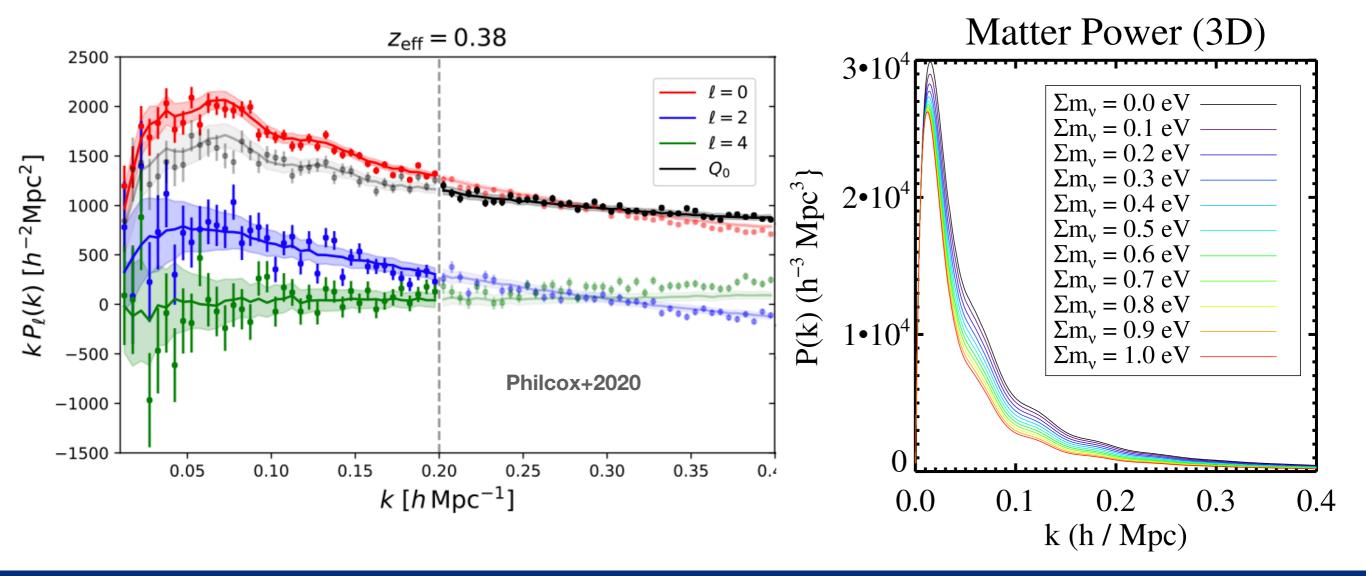


 Photometric surveys (e.g. Rubin, Euclid)



Cosmological probes: galaxy clustering

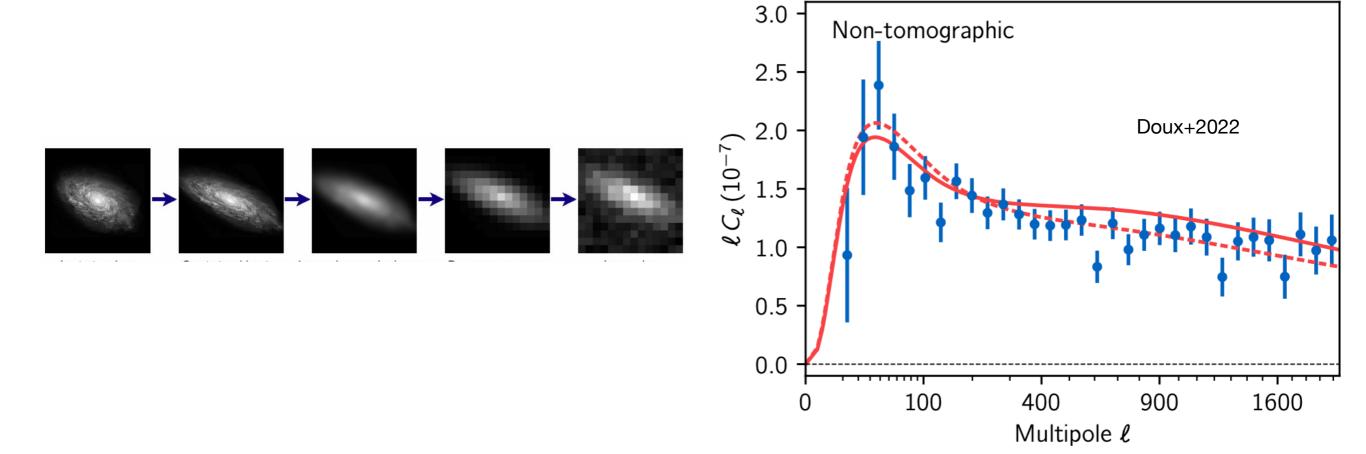
- CMB alone is weakly sensitive to the details of recent growth rate of LSS
- To test LCDM model large scale structures offer invaluable tomographic help!
- Galaxy clustering: P(k), BAO, RSD, voids are more sensitive but are local, biased, non-linear tracers...



Cosmological probes: weak lensing

Galaxy ellipticity: correlated by the presence of dark matter through lensing.

$$\bullet \quad C_{ij}^{\gamma}(\ell) = \frac{2}{\pi} t^2(\ell, 2) \mathcal{A}^2 \int_0^{\infty} \frac{\mathrm{d}\chi}{\chi} \frac{q_i(\chi)}{a(\chi)} \int_0^{\infty} \frac{\mathrm{d}\chi'}{\chi'} \frac{q_j(\chi')}{a(\chi')} \int_0^{\infty} \frac{\mathrm{d}k}{k^2} P_{\mathrm{m}}(k, \chi, \chi') \, \mathrm{j}_{\ell}(k\chi) \, \mathrm{j}_{\ell}(k\chi')$$

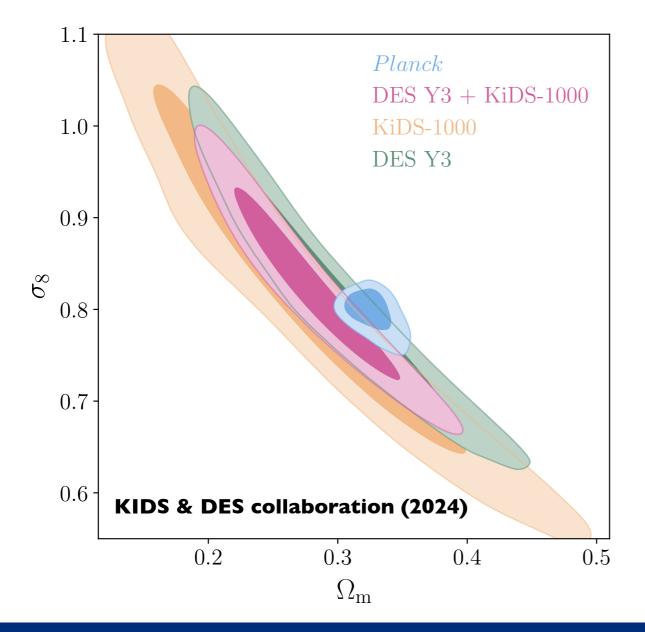


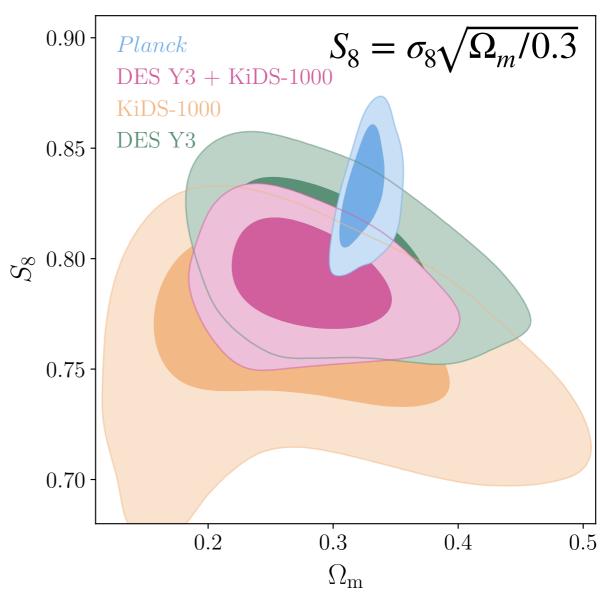
- Galaxy intrinsic alignment: $\langle \hat{\gamma} \hat{\gamma} \rangle = \langle \gamma \gamma \rangle + \langle \epsilon^s \epsilon^s \rangle + \langle \gamma \epsilon^s \rangle$
- PSF, noise and lensed galaxies' distribution: $\hat{\gamma} = (1 + m)\gamma + \mathbf{n}$

Giulio Fabbian 39 Les Houches 2025

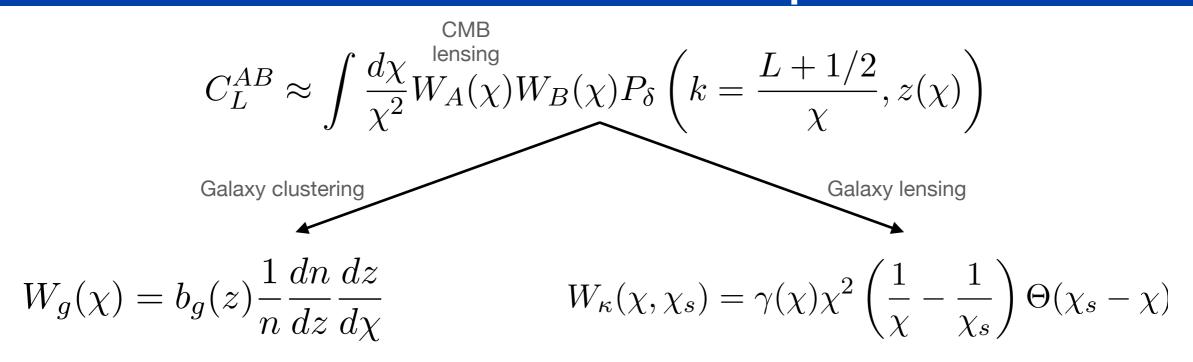
3x2pt in large-scale structure surveys

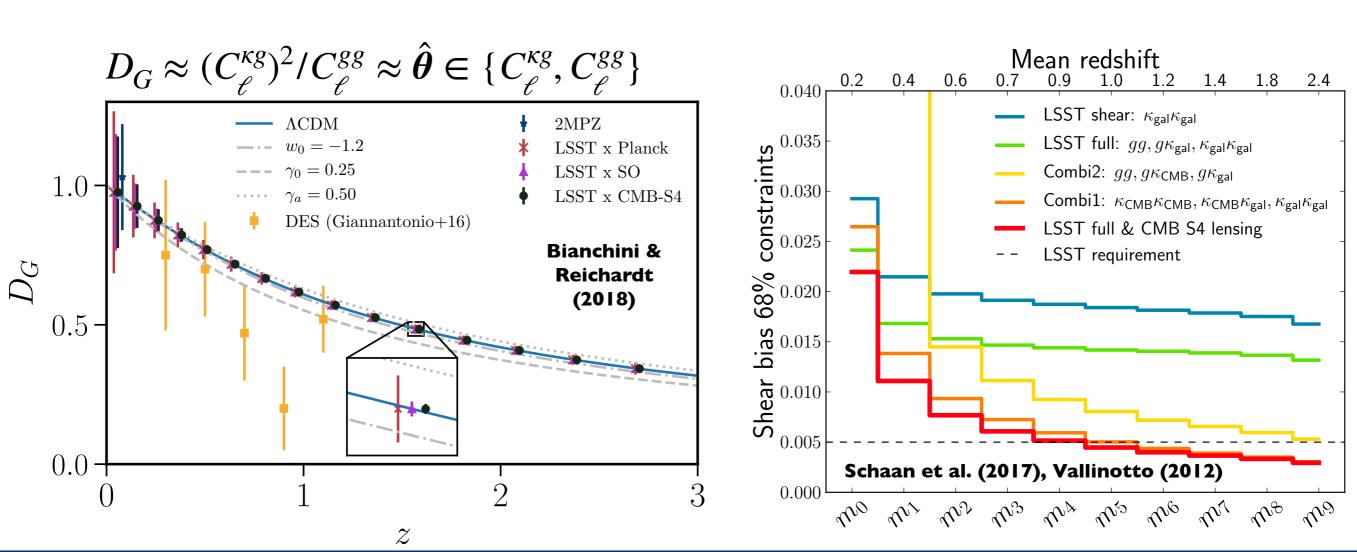
- \bullet Galaxy clustering: local, growth rate $C_\ell^{gg} \propto b_g^2 \sigma_8^2$
- ullet Weak lensing /shear: LOS integrated, sensitive to amplitude of fluctuations S_8 .
- Shear + galaxy-shear: sensitive to $\partial C_\ell/\partial P(k)$, $C_\ell^{g\gamma} \propto b_g \sigma_8^2$





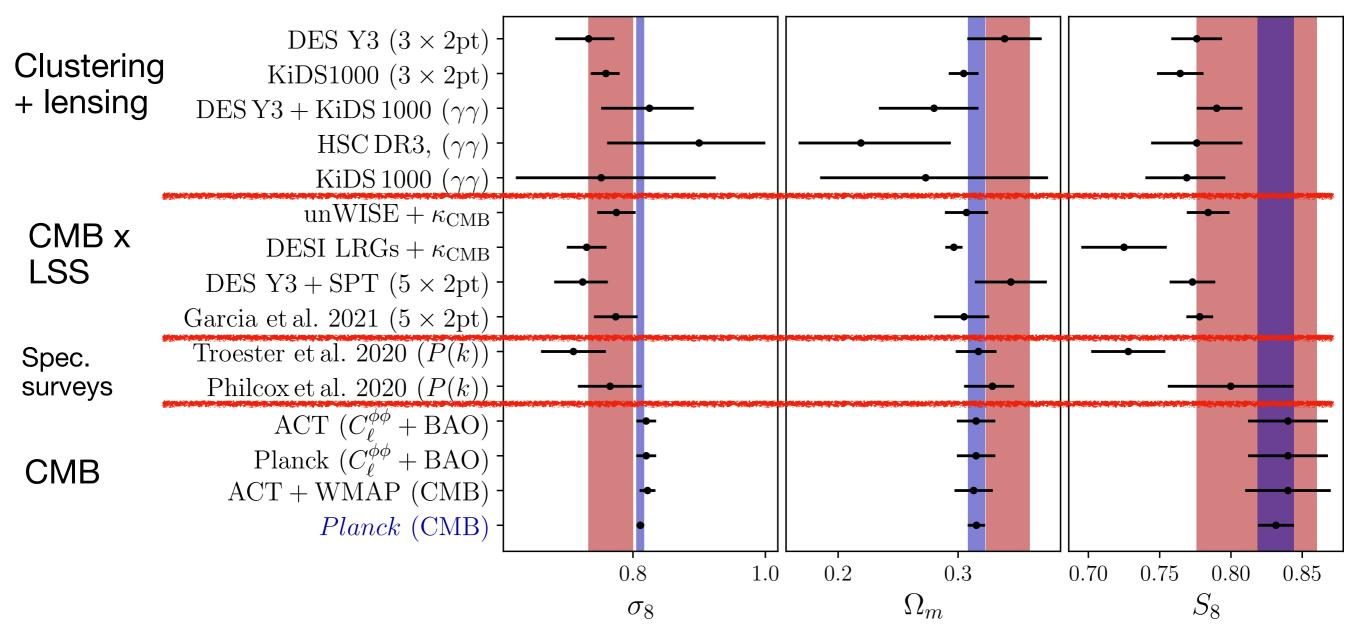
Cross-correlation basis and examples





State of the art on tensions (neglecting H0)

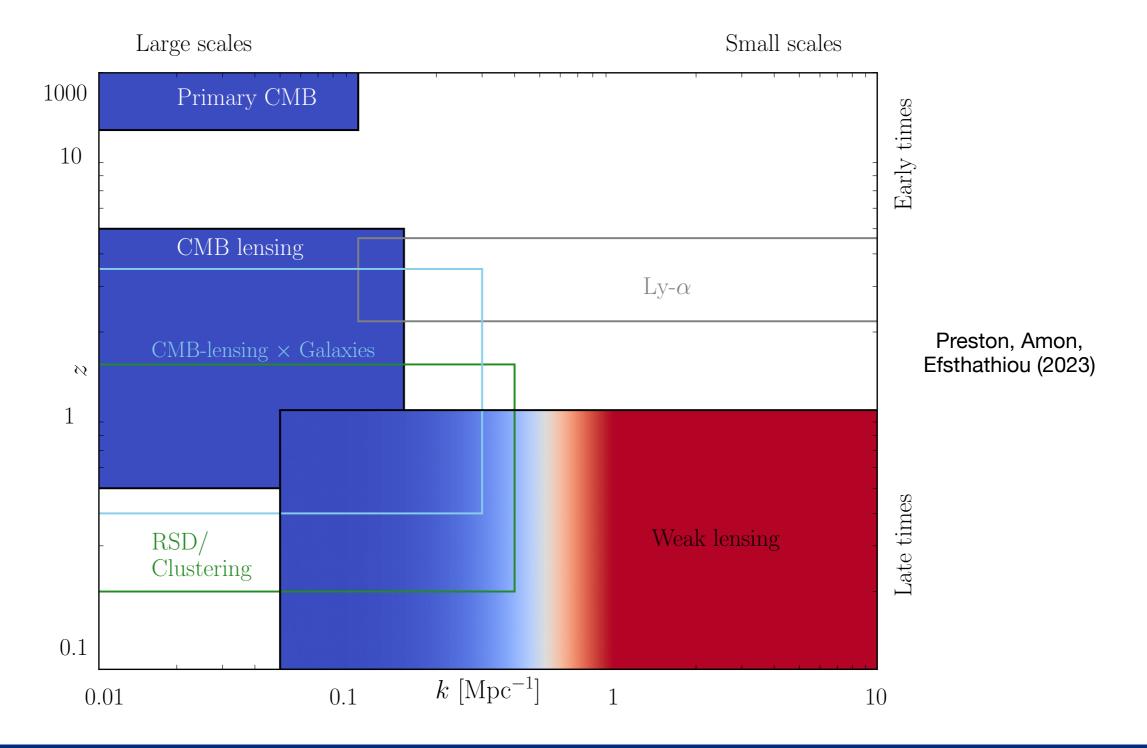
- Lots of inconsistencies and agreement across data sets
- Is inconsistency between probes a consequence of new physics?



Alonso, Fabbian, Storey-Fisher+(2023)

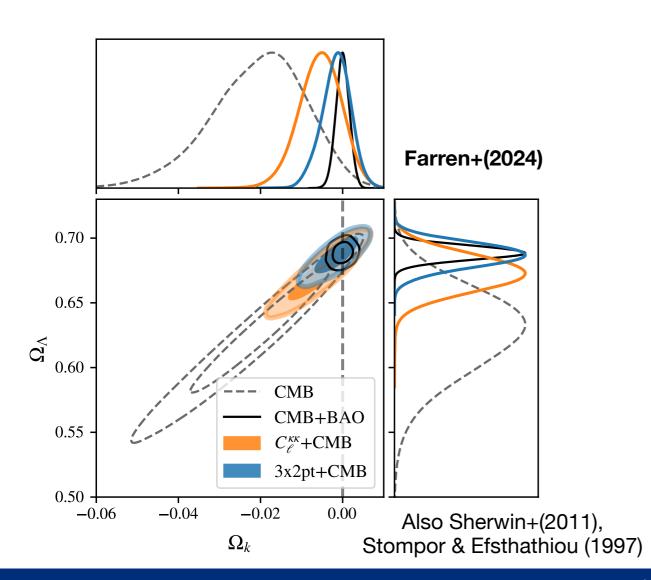
Ways forward

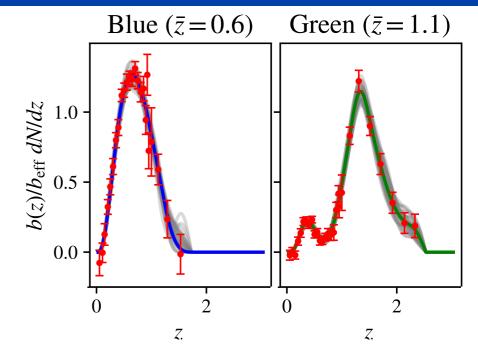
- Different probes means different scales at different redshift...
- Need to assess if this is real or effects of non-linear physics.

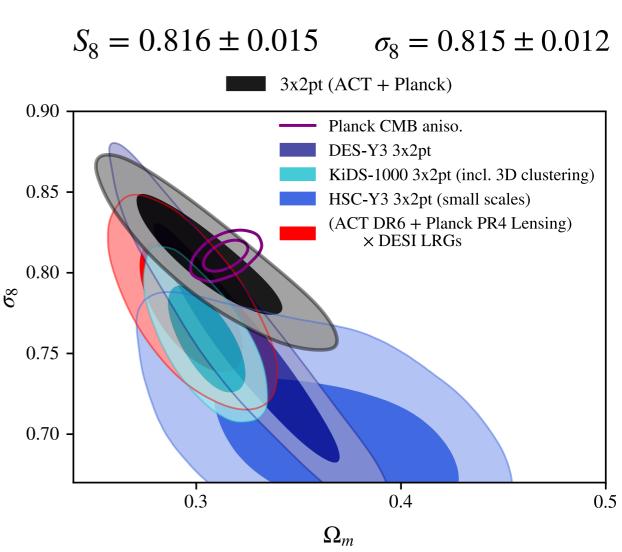


CMB lensing x galaxies: state of the art 1

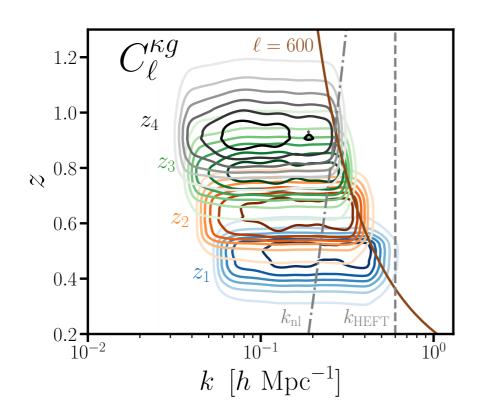
- 6xp2t w/ UNWISE x ACT DR6 & Planck PR4: in agreement with CMB primary
- UNWISe Green / blue galaxies at z~0.6 / 1.1
- Tensions limited to $k \gtrsim 0.3 \ h/\text{Mpc}$ in $0.2 \le z \le 1.6$ (from 2x2pt)

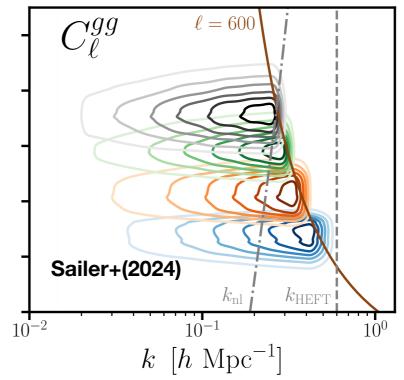




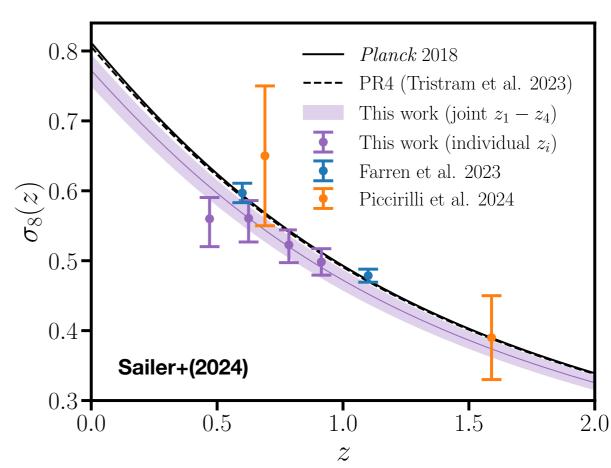


CMB lensing x galaxies: state of the art 2



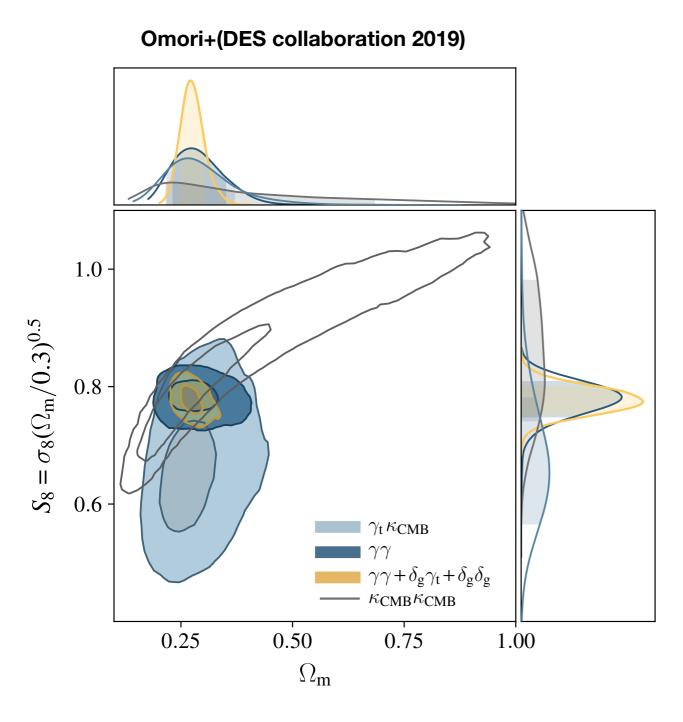


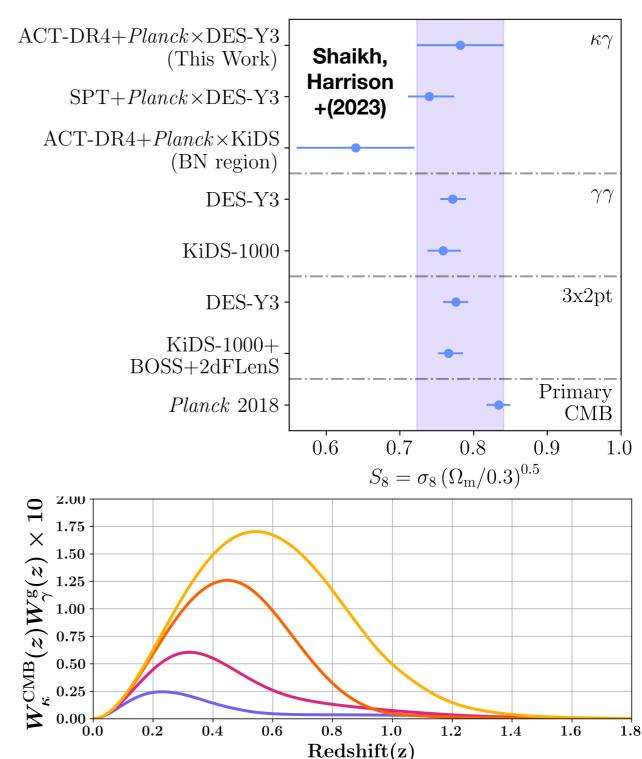
- DESI Legacy LRGs calibrated with spectroscopy data x ACT DR6
- Complementary scales wrt UNWISE.
- Highly tested for bias expansion
- Consistent results with CMB, other analysis ongoing...



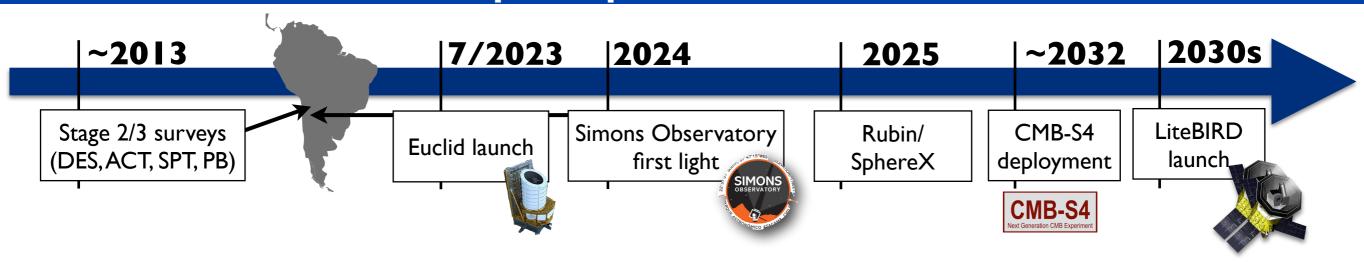
ACT DR4 & SPT X DES cosmic shear

• Tightens systematics but large uncertainties new analyses on the way.

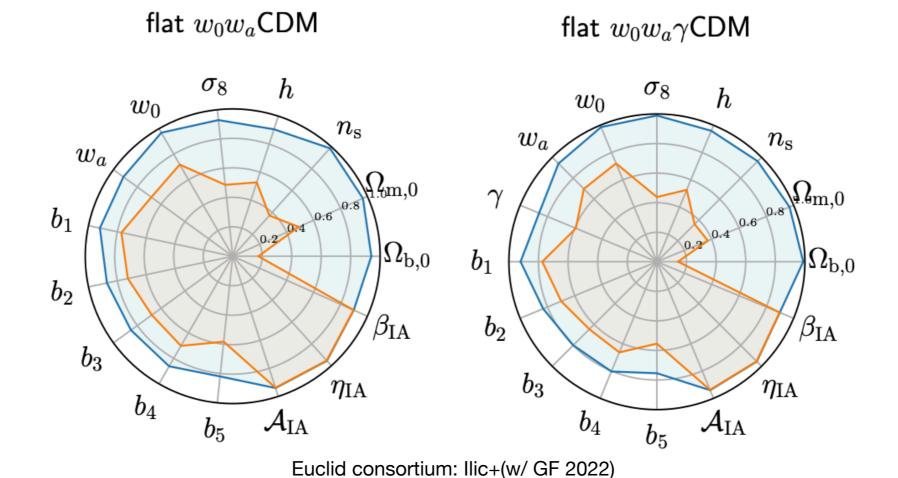




Data combination perspectives...

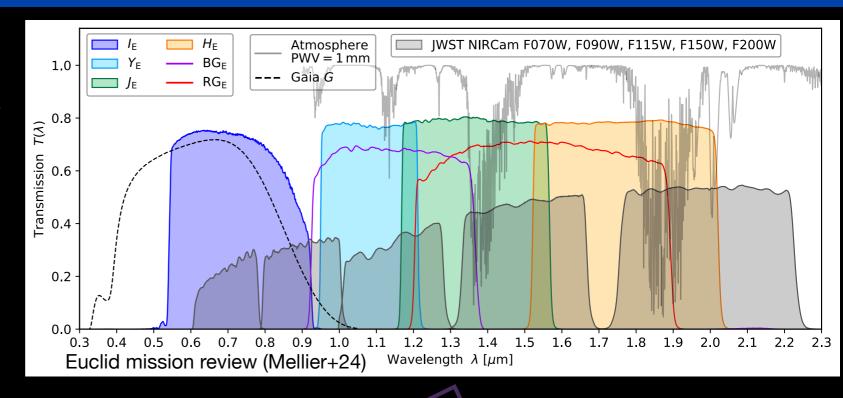


- Current data: marginalizing over systematics at limited cost, no additional power!
- Euclid: ~3x improvement on non-standard /extended models



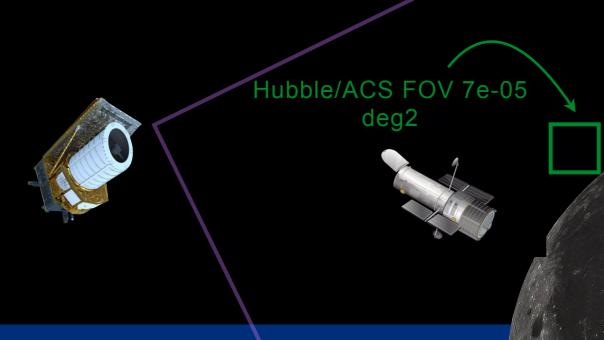
Euclid preview

- Euclid will cover 30 years
 of Hubble operation every
 ~5 days
- Euclid FOV ~ 3x the moon size
- Complements other facilities from space and ground (e.g. DESI).

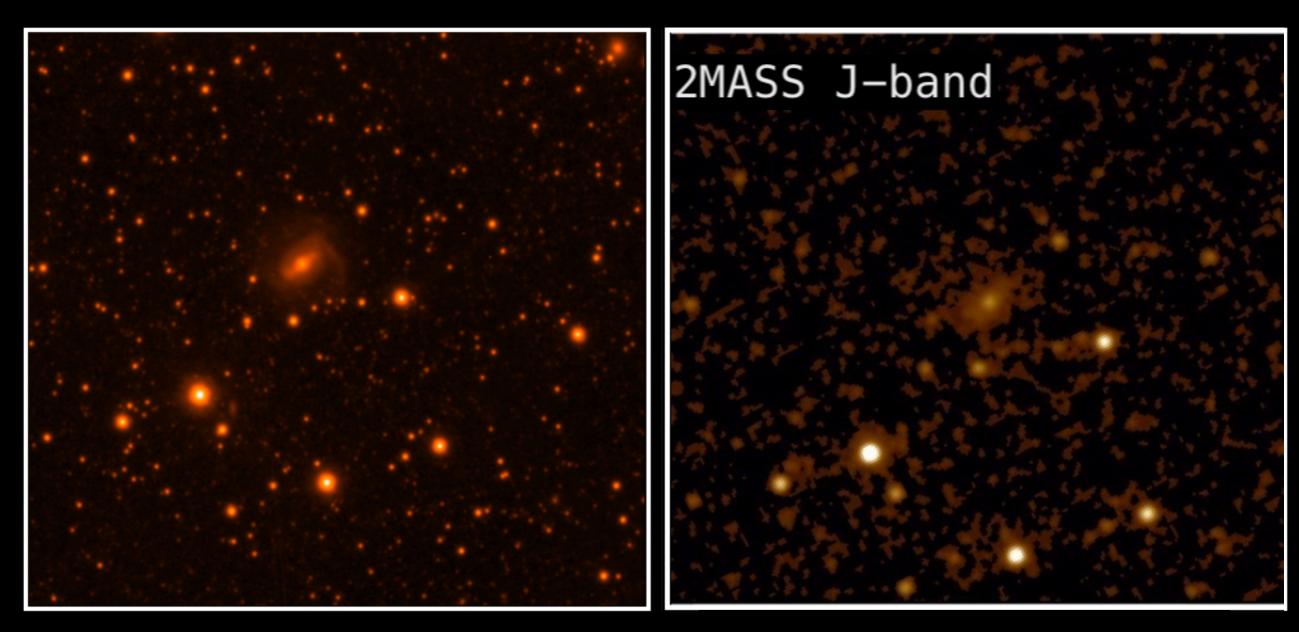


JWST/NIRCam FOV

0.003 deg2



EUCLID RESULTS SO FAR



VISTA VMC J-band

Credit: Ralf Bender & Ross Collins using public data from Euclid and VISTA

EUCLID RESULTS SO FAR



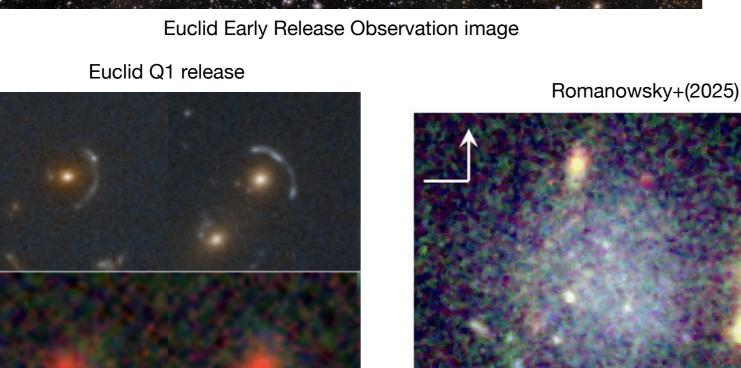
VISTA VMC J-band

Euclid NISP Test Image

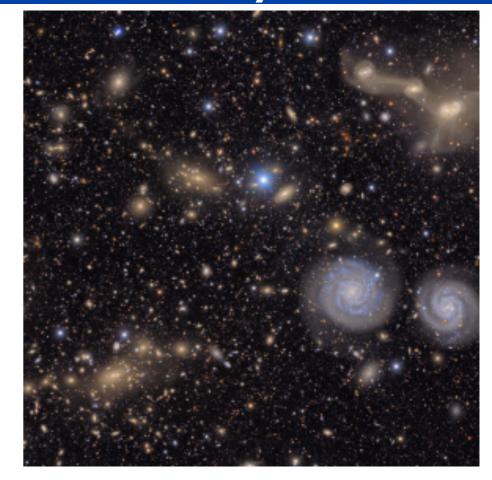
Credit: Ralf Bender & Ross Collins using public data from Euclid and VISTA

What to expect: synergies between surveys.





DESI Legacy Imaging Survey



Rubin 1st wide image

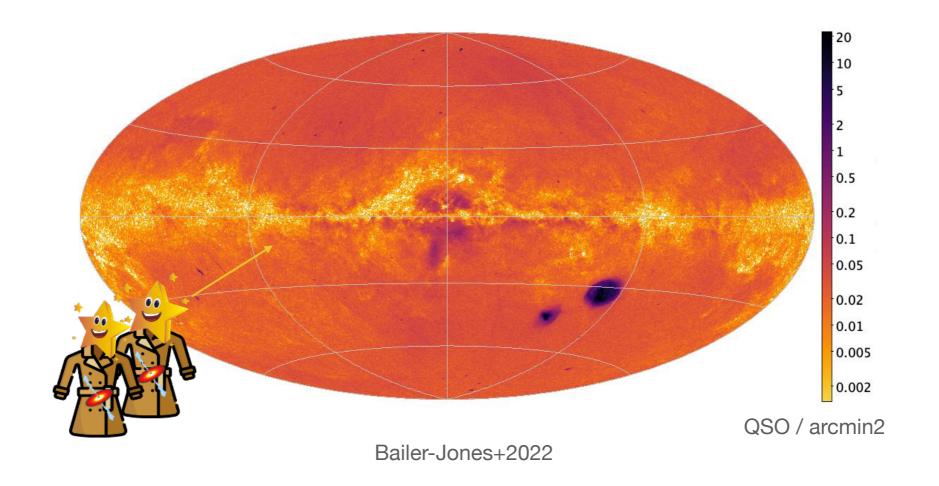


10"

Euclid

In the meantime... Gaia!

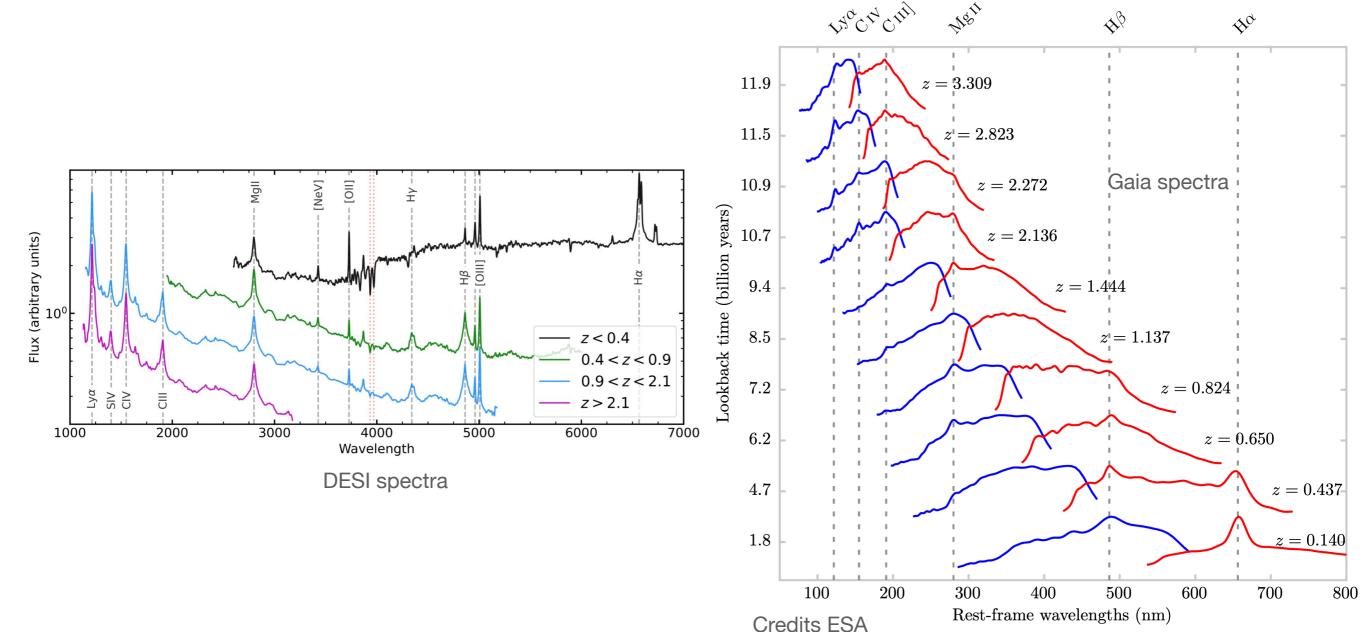
- Photometry, astrometry, slitless spectroscopy with $30 \le \lambda/\Delta\lambda \le 100$ resolution
- DR3 released 6.6 million quasar candidates!



Complete, low purity, as many are stars masquerading as QSO:/ but... we can improve it

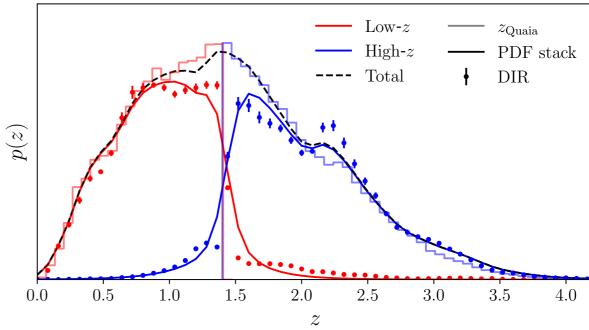
Gaia: more than astrometry

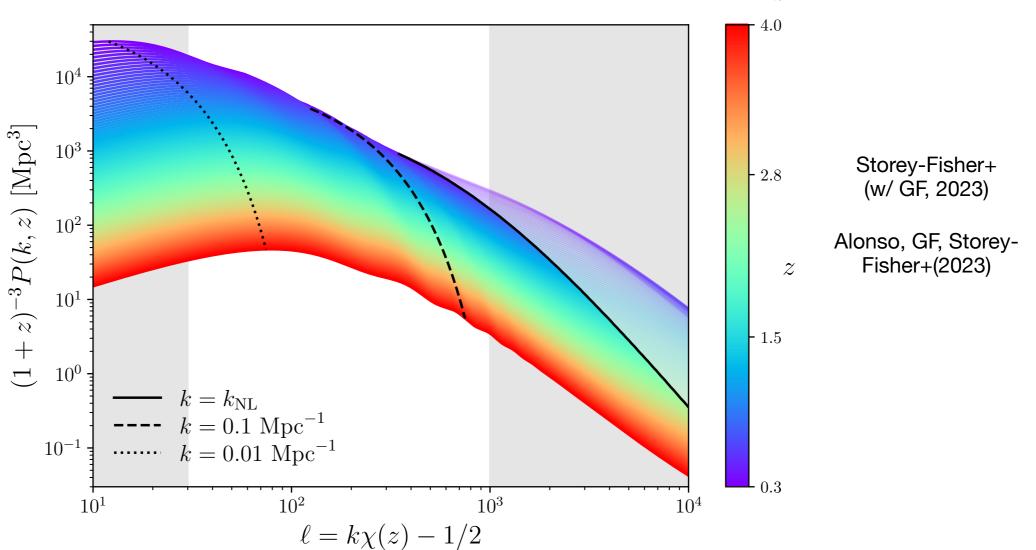
- Space-quality data means e.g. no seeing, airmass, stable observing conditions...
 - larger volume, cleaner selection function than any existing sample (full sky).
 - Synergies with external data allowed to clean this sample further: Quaia



What Quaia can do for cosmology?

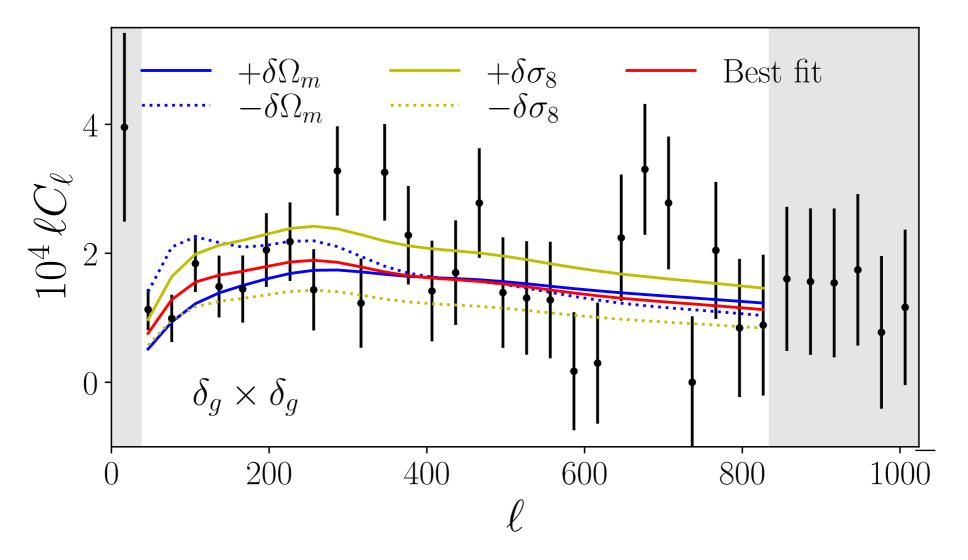
- High redshift
- Linear or quasi-linear scales.





What Quaia can do for cosmology?

- Large sky coverage means capability to measure large angular scales.
- Towards non-degenerate σ_8, Ω_m measurements



Alonso, GF, Storey-Fisher+(2023)

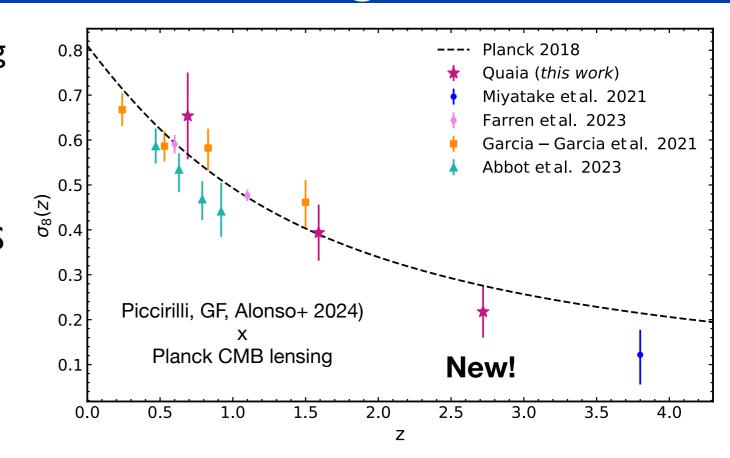
Cosmology from Quaia x CMB lensing

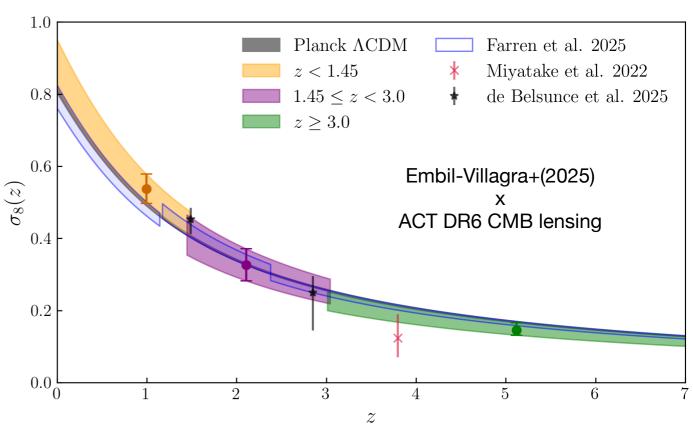
- Tomographic C_ℓ^{gg} , $C_\ell^{\kappa g}$ with Planck lensing
 - New high-z σ_8 constraints
 - Results competitive with current LSS surveys with fewer objects and/or worse redshifts.

- Tomographic 3x2pt C_{ℓ}^{gg} , $C_{\ell}^{\kappa g}$, $C_{\ell}^{\kappa \kappa}$ with ACT CMB lensing
 - Constraints on $\sigma_8(z=5.1)$

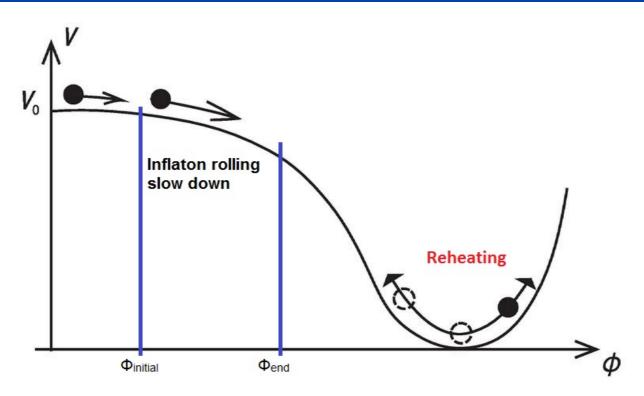
$$P_{\text{lin}}^{\text{new}}(k, z) = P_{\text{lin}}^{\text{input}}(k, z) A(z)$$

$$= P_{\text{lin}}^{\text{input}}(k, z) \begin{cases} A_0 & 0 \le z < z_1 \\ A_1 & z_1 \le z < z_2 \\ A_2 & z_2 \le z \end{cases}$$





(Beyond) Inflation in a nutshell



- Energy density dominated by potential energy of a scalar field that fills the universe
- Small level of acceleration drive the exponential expansion

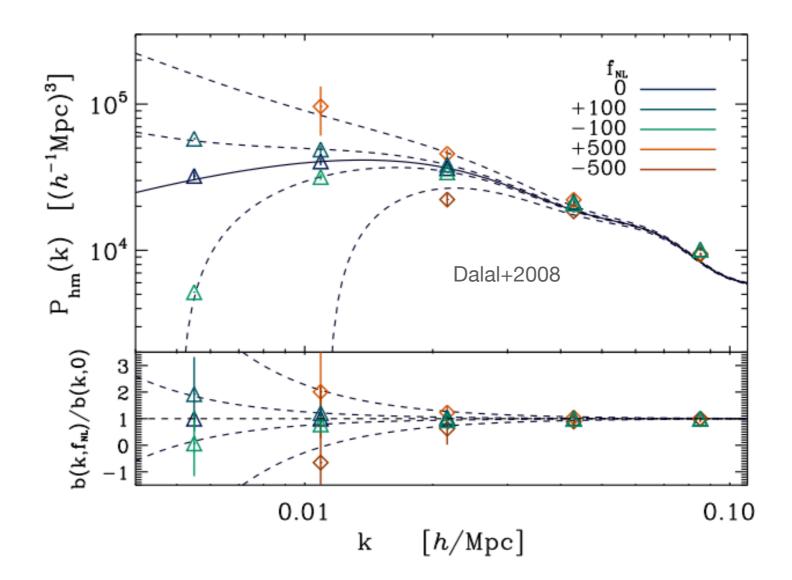
$$n_s, \alpha_s, A_s \longrightarrow dV/d\phi, d^2V/d\phi^2$$

Non-Gaussianity offers a new window beyond slow-roll / single-field models

$$\Phi(\mathbf{x})_{NG} = \Phi(\mathbf{x}) + f_{NL} \left(\Phi^2(\mathbf{x}) - \langle \Phi^2 \rangle \right)$$

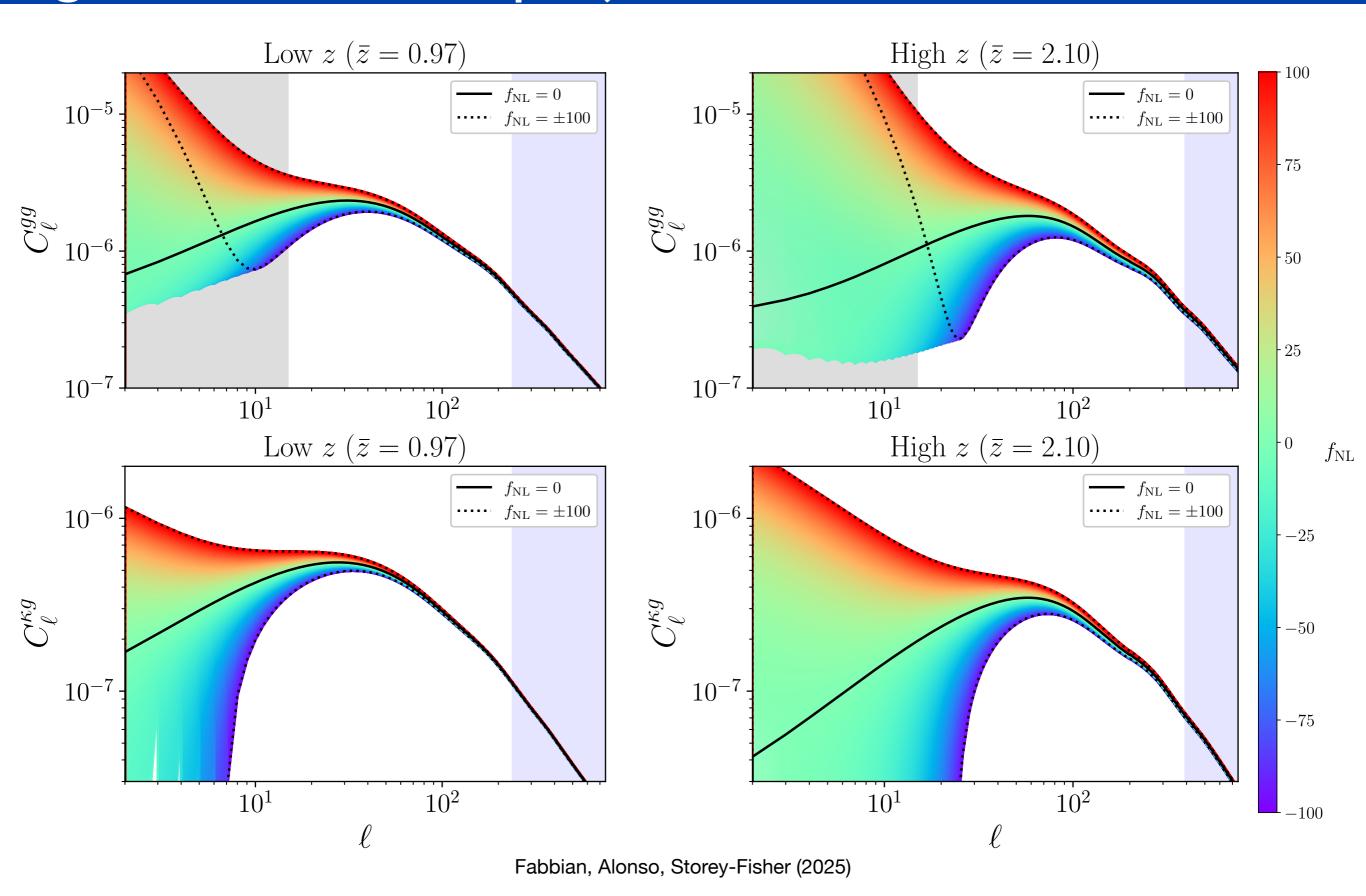
Non-Gaussianities and scale dependent bias

$$\Delta b_1 \propto \frac{f_{\rm NL} b_1 b_\phi}{k^2 T(k)}$$

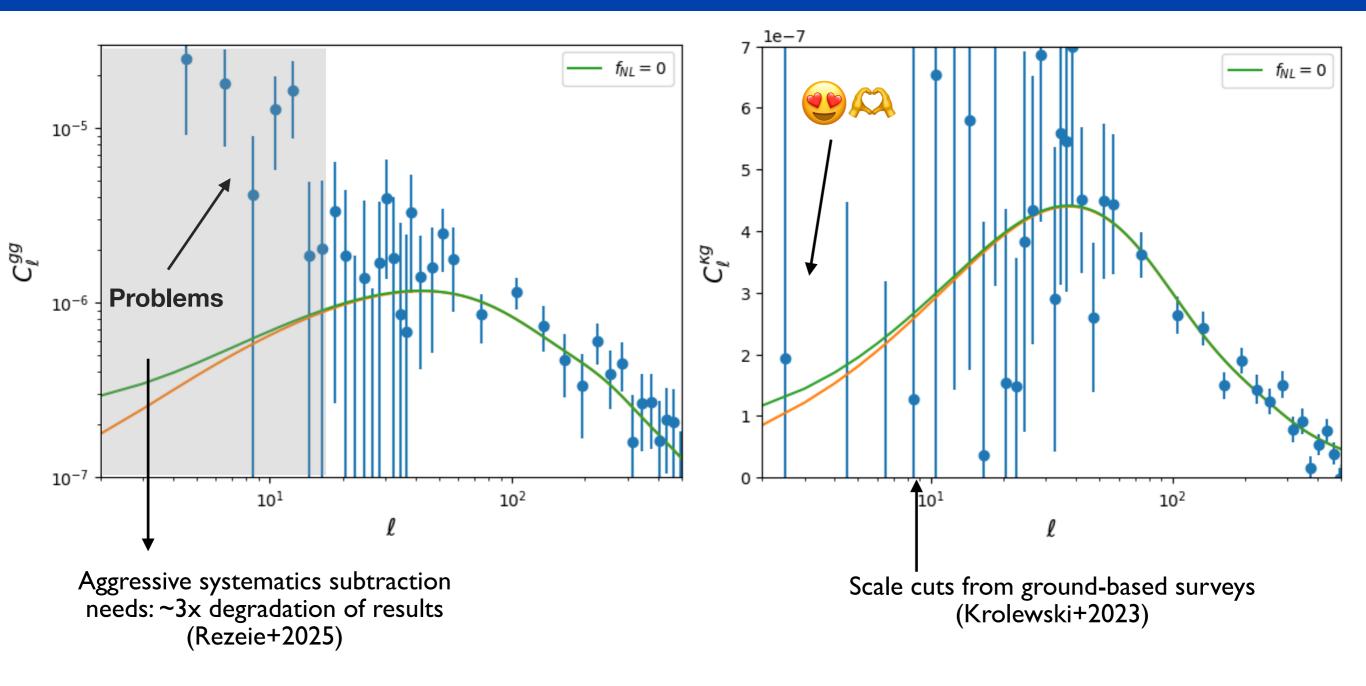


- Huge volume and high bias tracers is required to enhance detection.
- Quasars: detectable at high z thanks to bright AGNs, ~linear scales, ideal for f_{NL} studies.
- Galactic extinction, stellar contamination, seeing, survey depth inhomogeneity cause large scale variations / power excess in clustering measurements...

Signature of f_{NL} for projected statistics

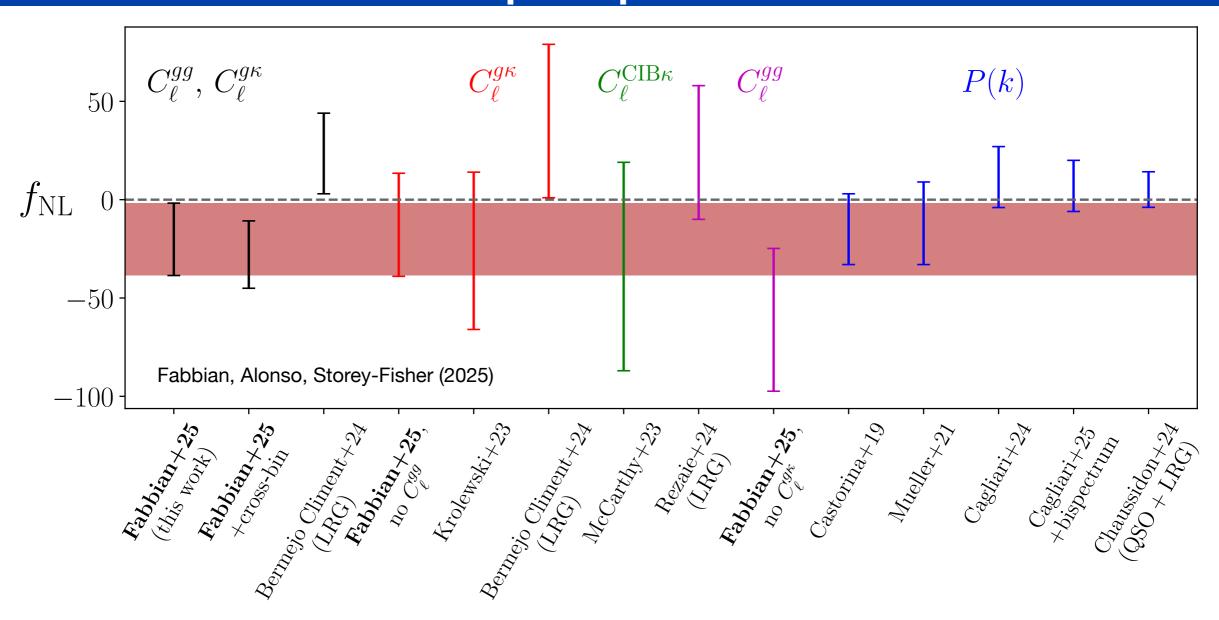


Constraints on f_{NL}



- Cross-correlation can reach the largest scales!
- ullet $\sigma(f_{
 m NL})$: worse than expectations due to residual systematics $\Delta C_\ell^{\kappa g} \propto \sqrt{C_\ell^{\kappa\kappa} C_\ell^{gg}}$

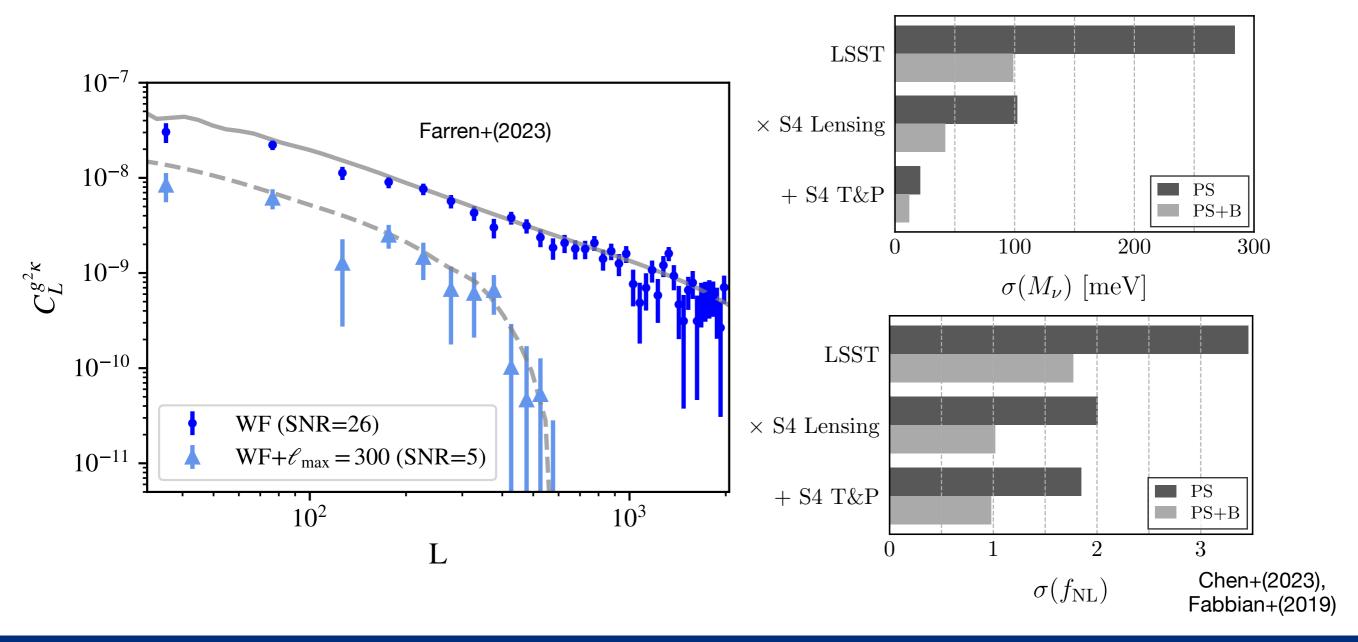
Robustness tests and perspectives



- Sensitivity comparable to spectroscopic galaxy surveys in 3D
- Limited by systematics on auto correlation on large scales but highly robust to systematics.
- Newer data releases from Gaia could improve this results (more sources, different source separation).

Higher-order cross-correlation

- Why limit to 2-point correlation functions....
- $\langle \kappa \kappa g \rangle$, $\langle \kappa g g \rangle$: great tools to reduce errors due to galaxy bias uncertainties.
- High-significant detections appeared very recently, hard to model...



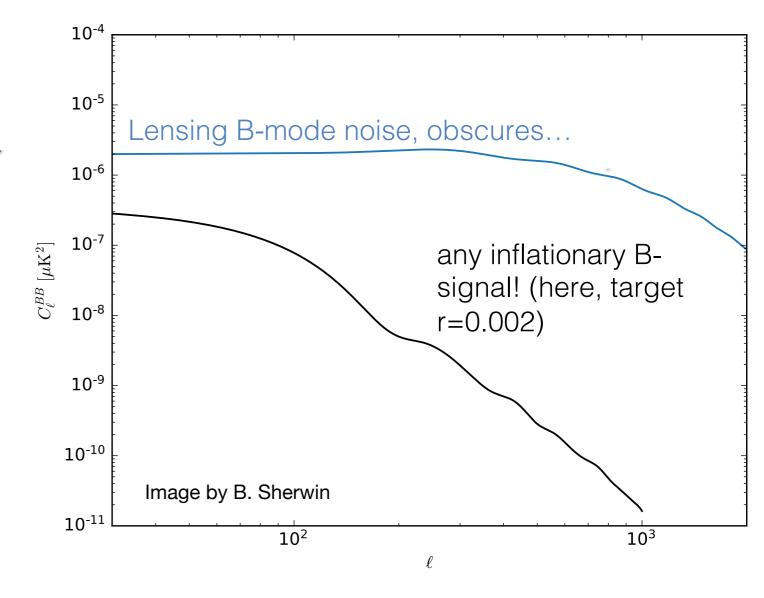
$$B(\hat{n}) \ (\pm 2.5 \mu K)$$

(Small r primordial B-modes)

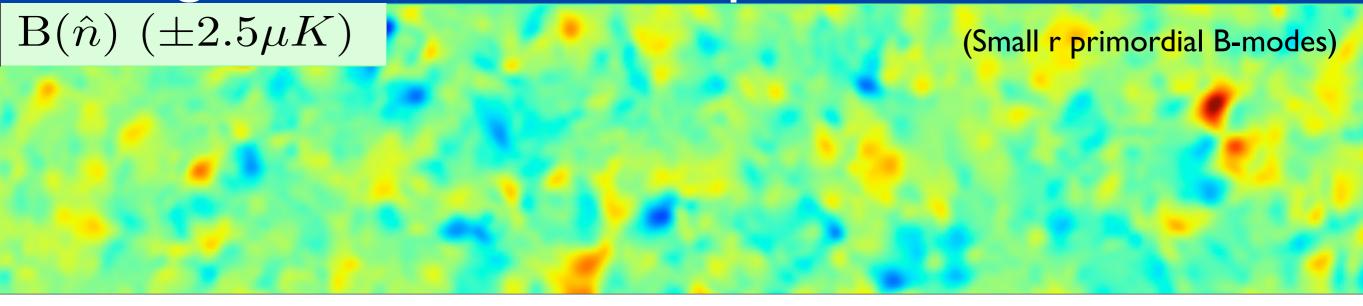
 E to B-modes conversion can hide primordial signal

$$B^{lens}(\mathbf{l}) \sim \int d\mathbf{l'} \ W(\mathbf{l}, \mathbf{l'}) E(\mathbf{l'}) \phi(\mathbf{l} - \mathbf{l'})$$

- $\sigma(r) \propto N_{\ell}^{BB} + C_{\ell}^{BB,lens}$
- Limiting factor to constrain inflation from deep data (10x degradation for CMB-S4)



Lensing and CMB B-modes polarization

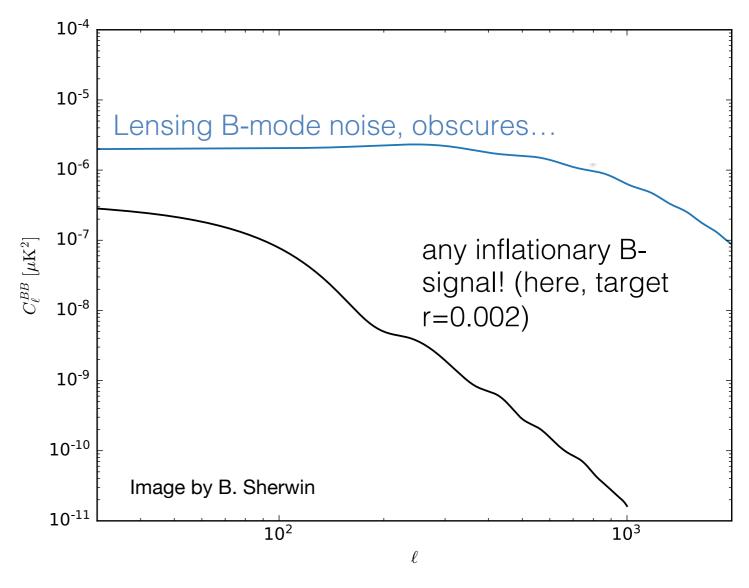


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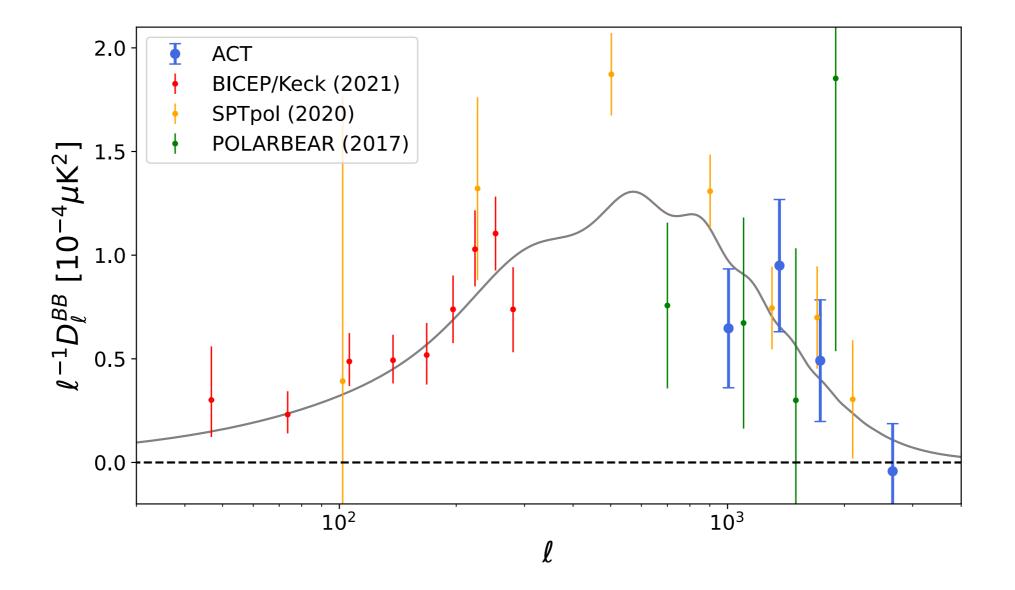
•
$$\sigma(r) \propto N_{\ell}^{BB} + C_{\ell}^{BB,lens}$$

 Limiting factor to constrain inflation from deep data (10x degradation for CMB-S4)



CMB B-modes status

- First direct measurement in 2014 by POLARBEAR ($\sim 3\sigma, f_{sky} < 0.1\,\%$)
- Highest SNR by SPT and BICEP on large sky fractions.
- Inflationary part not detected, signal consistent with lensing only.

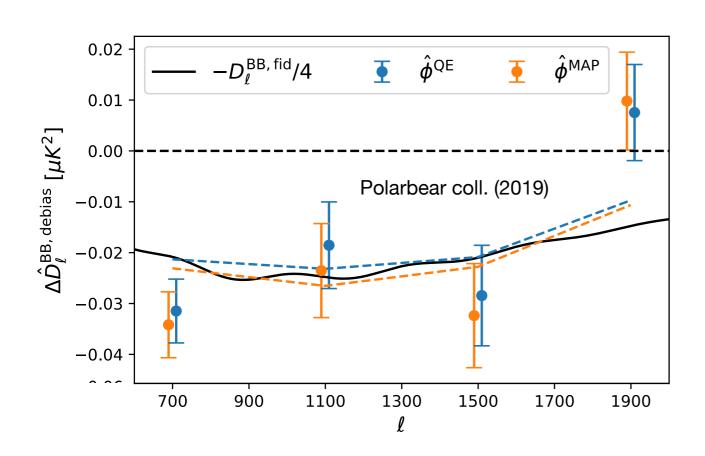


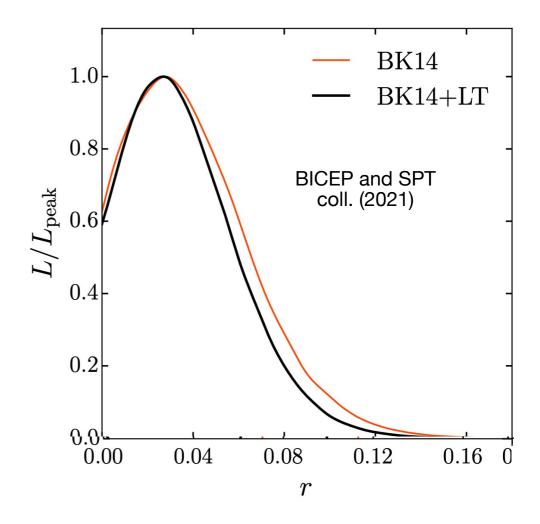
Delensing CMB polarization

Subtract a template of the lensing B-modes to reduce signal and variance

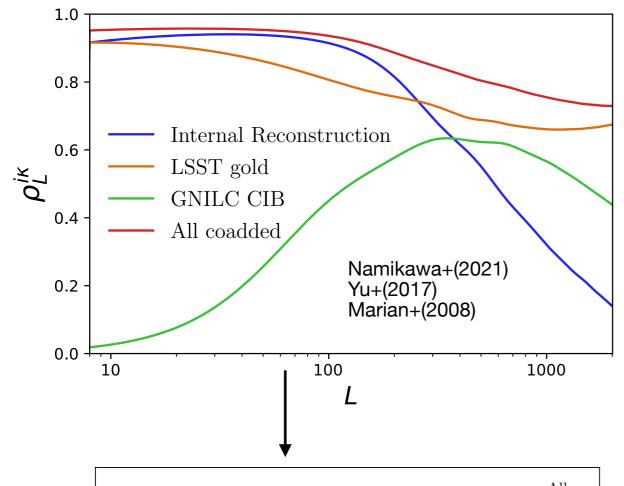
$$B^{data} - \hat{B}^{lens} \sim B^{data} - \int d\mathbf{l}' W(\mathbf{l}, \mathbf{l}') E(\mathbf{l}') \phi(\mathbf{l} - \mathbf{l}')$$

- I need low noise high resolution E-mode polarization (e.g. ACT, SPT...)
- ullet and an estimate of the matter distribution that lensed the CMB, i.e. a good estimate of ϕ

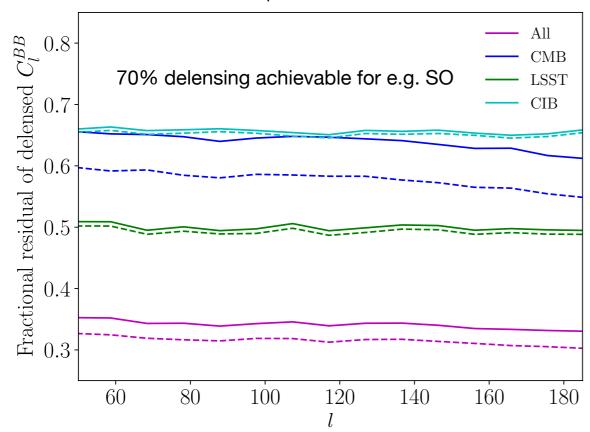


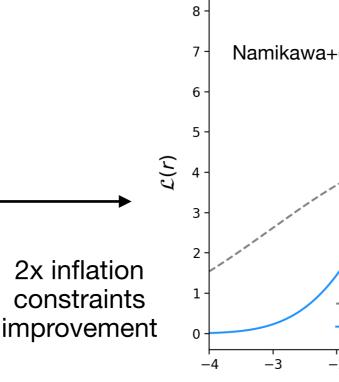


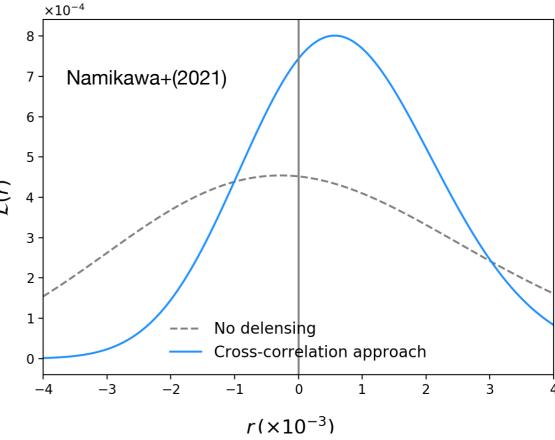
Delensing with galaxy surveys



- Accuracy of CMB lensing reconstruction is limited by noise.
 - Combine external galaxy tracers to improve SNR using cross-correlation.
 - Crucial improvements for lowresolution experiments (Litebird...)

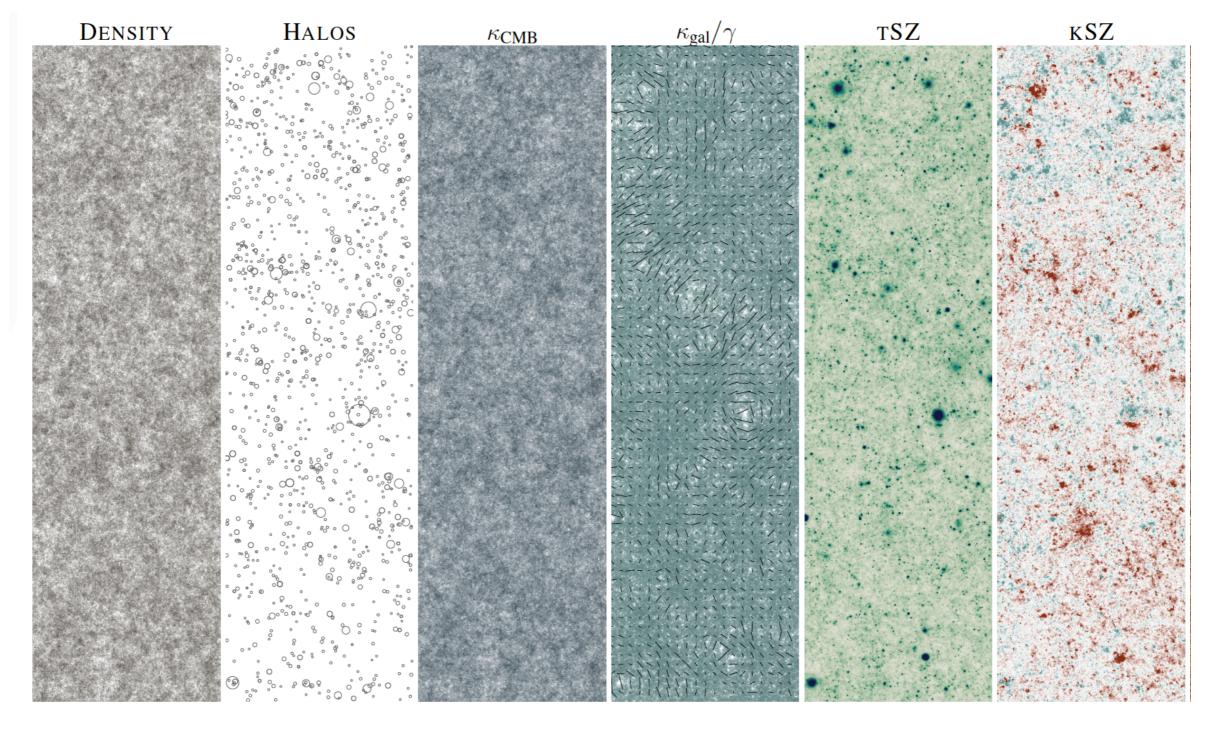






Switching gears to SZ

Questions? Comments? Remarks? Complaints?



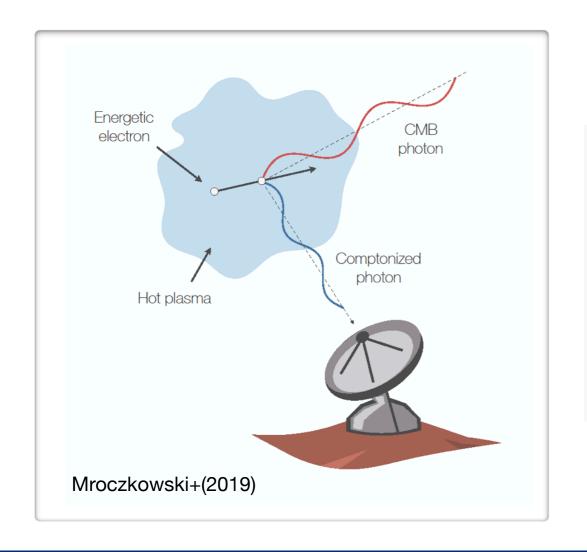
Omori (2023)

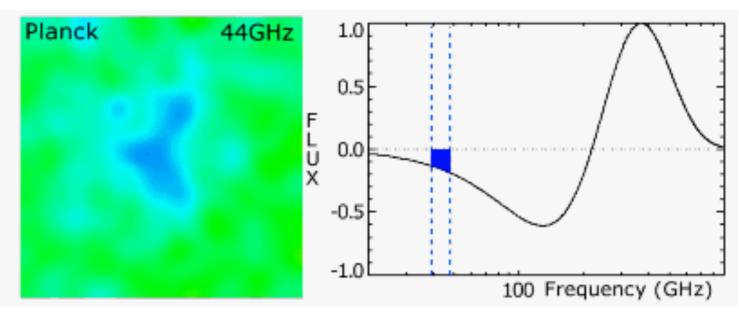
tSZ primer

- Inverse Compton scattering off hot electrons in ICM/CGM changes CMBT locally.
 - Direct probe of gas pressure
 - Interface between astrophysics and cosmology.

$$y(\hat{\mathbf{n}}) = \int n_{\rm e} \frac{k_{\rm B} T_{\rm e}}{m_{\rm e} c^2} \, \sigma_{\rm T} \, ds$$

Can be disentangled through accurate multi-frequency observations.



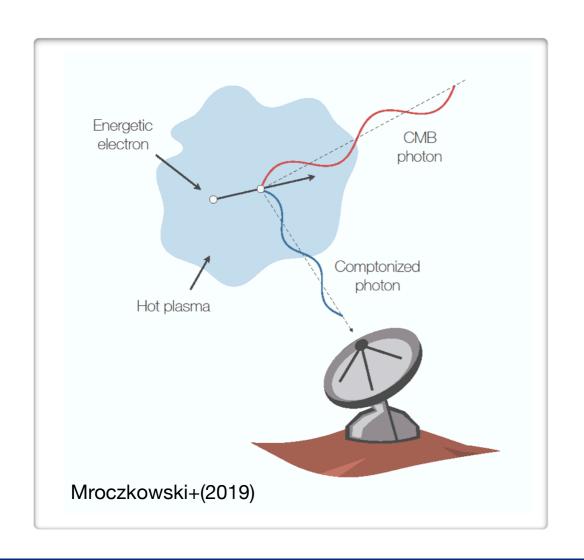


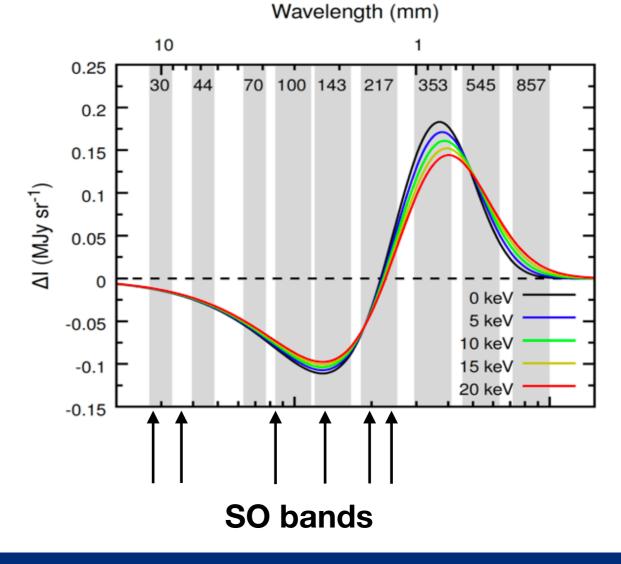
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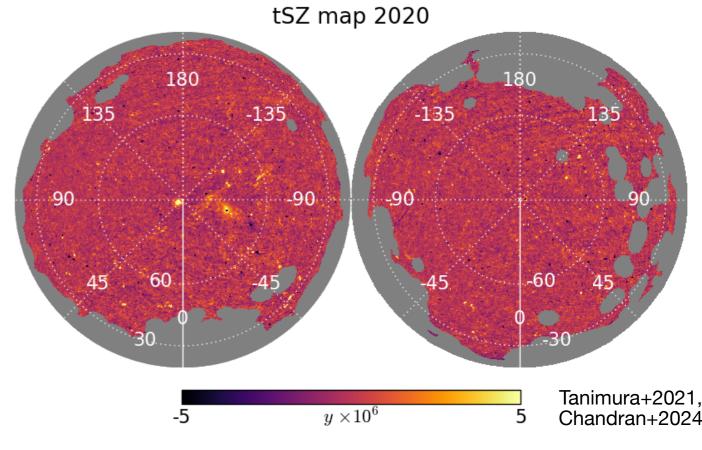
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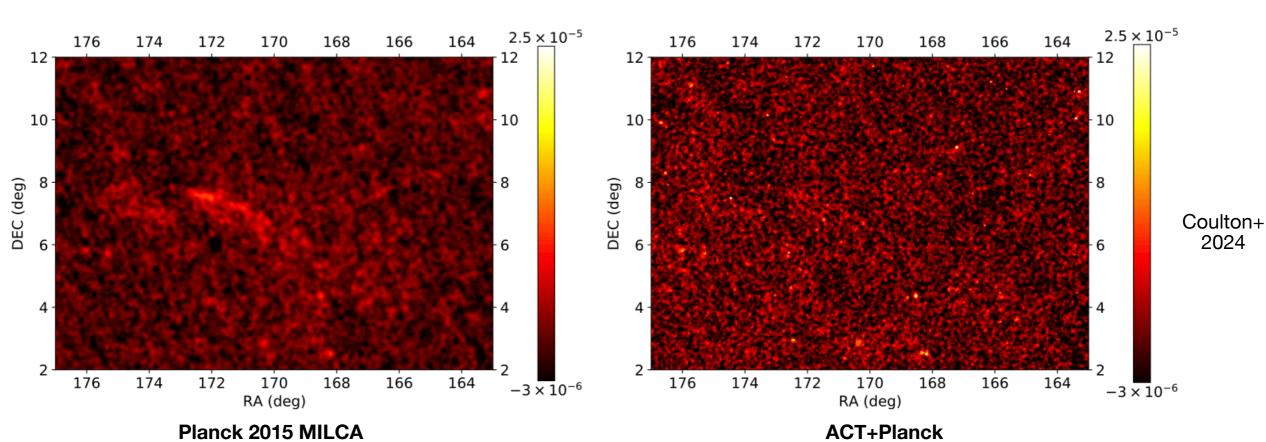




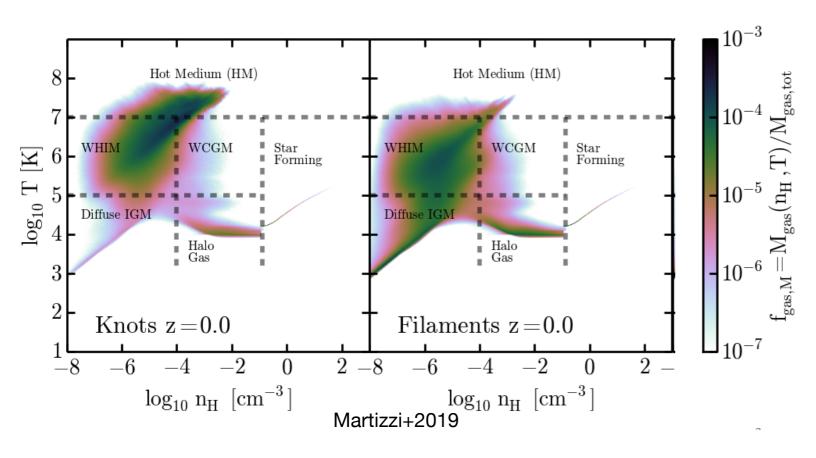
tSZ maps state of the art

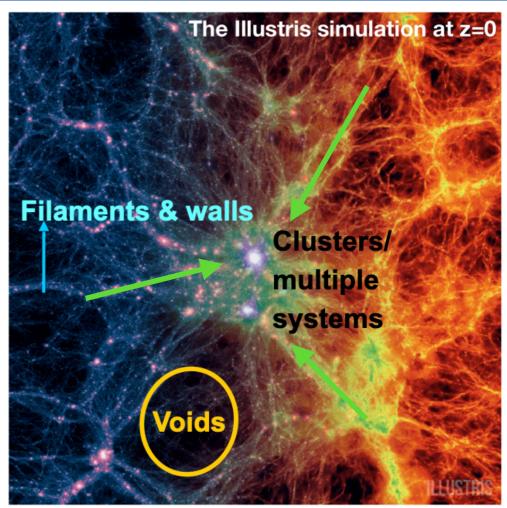
- New analysis on Planck DR4 w/ different foreground cleaning methods.
- ACT DR6 used Planck additional channel and different cleaning method for higherresolution map.





Where is the tSZ?



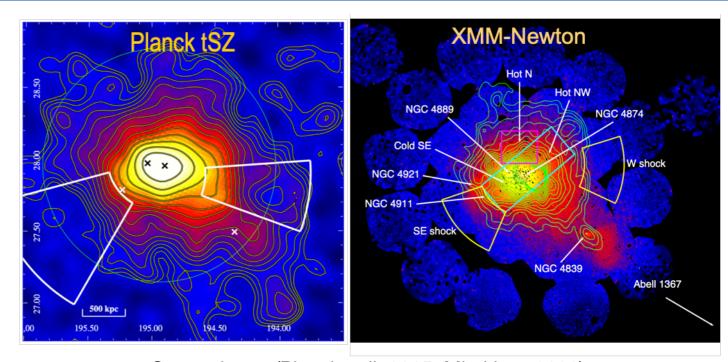


Courtesy N.Battaglia, N. Aghanim

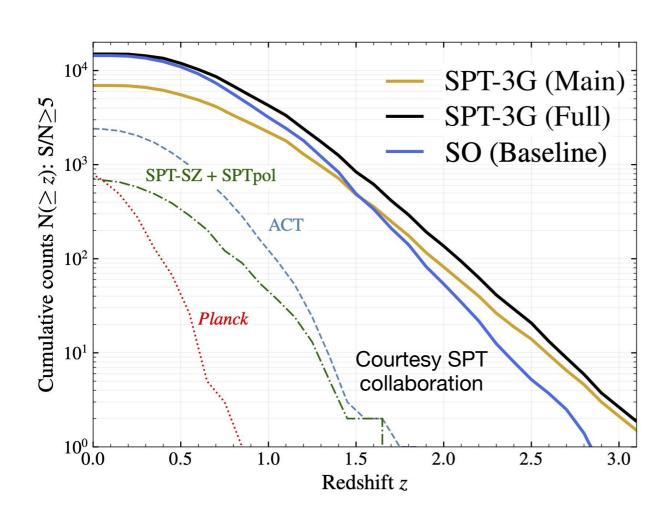
- Ionized hot and warm gas is ubiquitous and can generate tSZ:
 - Direct probe of gas across environments (filaments, voids, clusters)
 - Useful probe of accretion of matter through filaments as well as feedback processes.

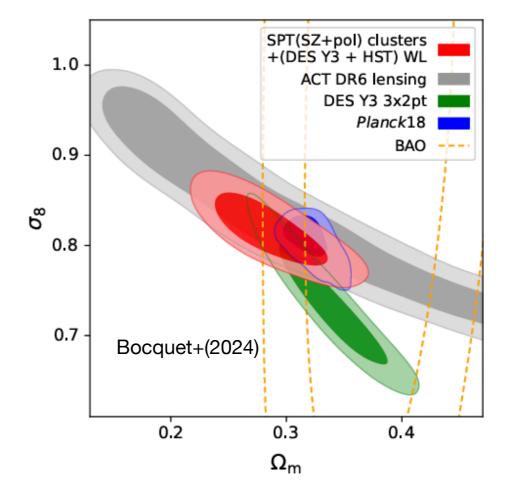
Cluster cosmology

- Number counts sensitive to dark energy (now ~1000s)
 - tSZ flux limit ~ mass limit!
 - Complementarity / synergies
 with X-ray and lensing surveys



Coma cluster (Planck coll. 2015, Mirakhor+2020)





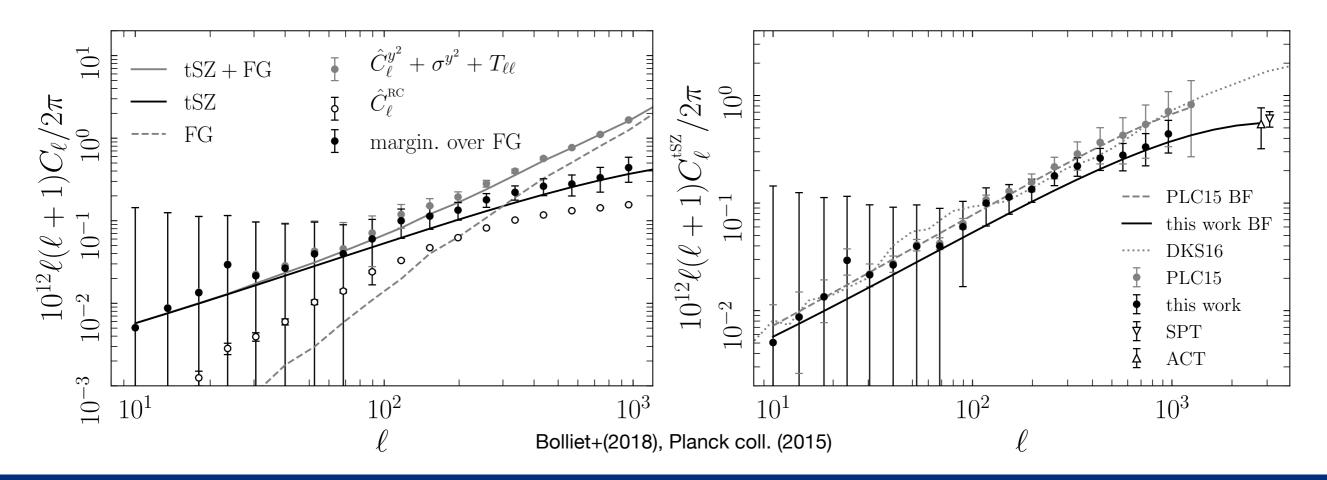
tSZ power spectrum

Strong cosmological dependency on e.g. dark energy and neutrinos...

$$C_{\ell}^{yy} \propto \sigma_8^{8.1} \Omega_m^{3.2} B^{-3.2} h^{-1.7}$$

- Same applies to higher order statistics (e.g. I-p PDF, bispectra...)
- Very sensitive to astrophysical modeling and extragalactic foreground subtraction.
- Work in progress for joint modeling with upcoming lensing surveys

See also Elizabeth's lecture!



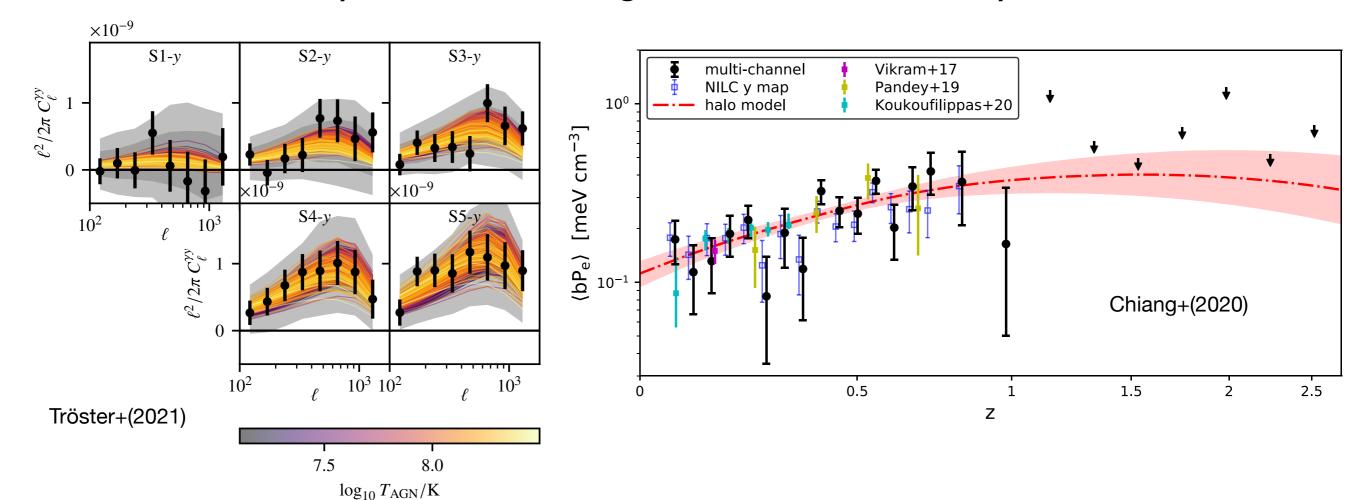
tSZ cross-correlations with LSS surveys

$$C_l^{\text{AB,1h}} = \int_{z_{\text{min}}}^{z_{\text{max}}} \mathrm{d}z \frac{\mathrm{d}V}{\mathrm{d}z \mathrm{d}\Omega} \int_{M_{\text{min}}}^{M_{\text{max}}} \mathrm{d}M \frac{\mathrm{d}n}{\mathrm{d}M} \tilde{u}_l^{\text{A}}(M,z) \tilde{u}_l^{\text{B}}(M,z). \tag{2018}$$

$$\tilde{u}_{l}^{y}(M,z) = \frac{4\pi r_{500c}}{l_{500c}^{2}} \int_{x_{min}}^{x_{max}} dx x^{2} y_{3D}(x) \frac{\sin(lx/l_{500c})}{lx/l_{500c}}$$

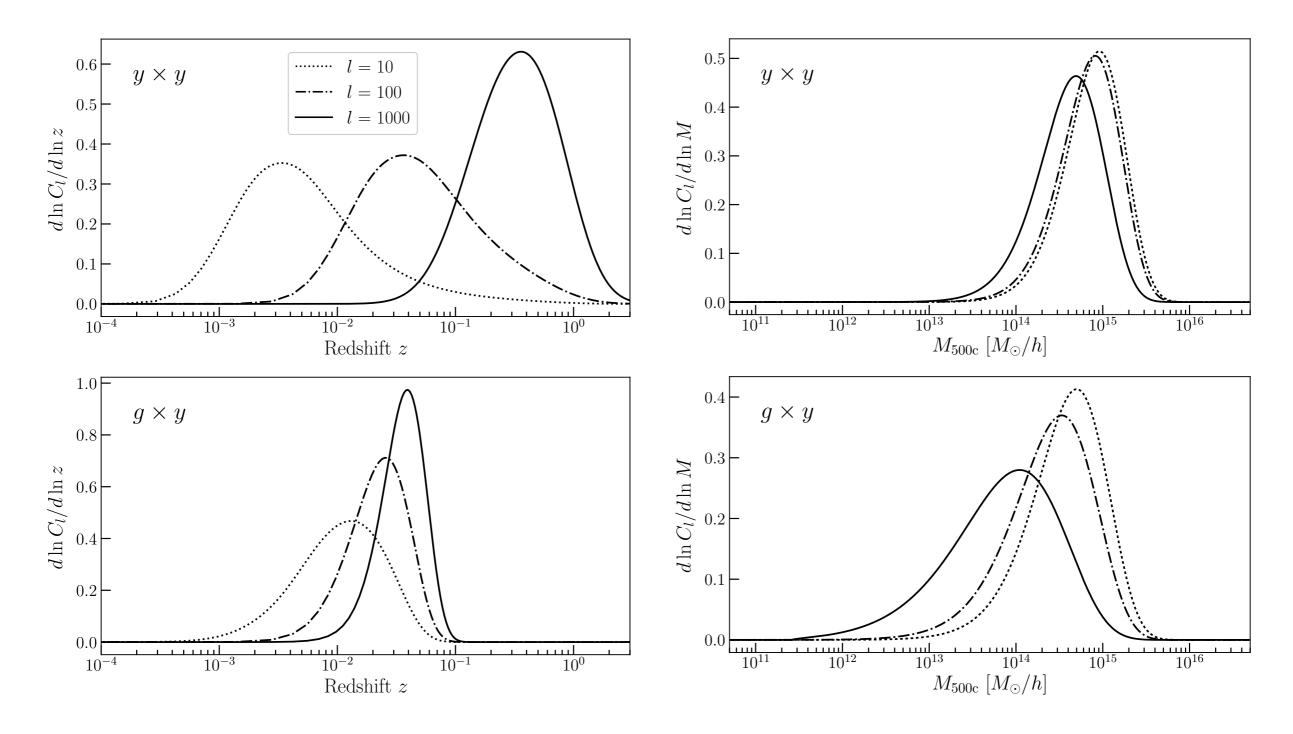
$$\times E^{8/3}(z) \left[\frac{M_{500c}}{3 \times 10^{14}(0.7/h)M_{\odot}} \right]^{2/3 + \alpha_{p}} p(x)$$

- Statistical measurements of pressure in the LSS, probe of thermal history
- Can inform analysis of weak-lensing data to account for baryonic effects.



tSZ cross-correlations with LSS surveys

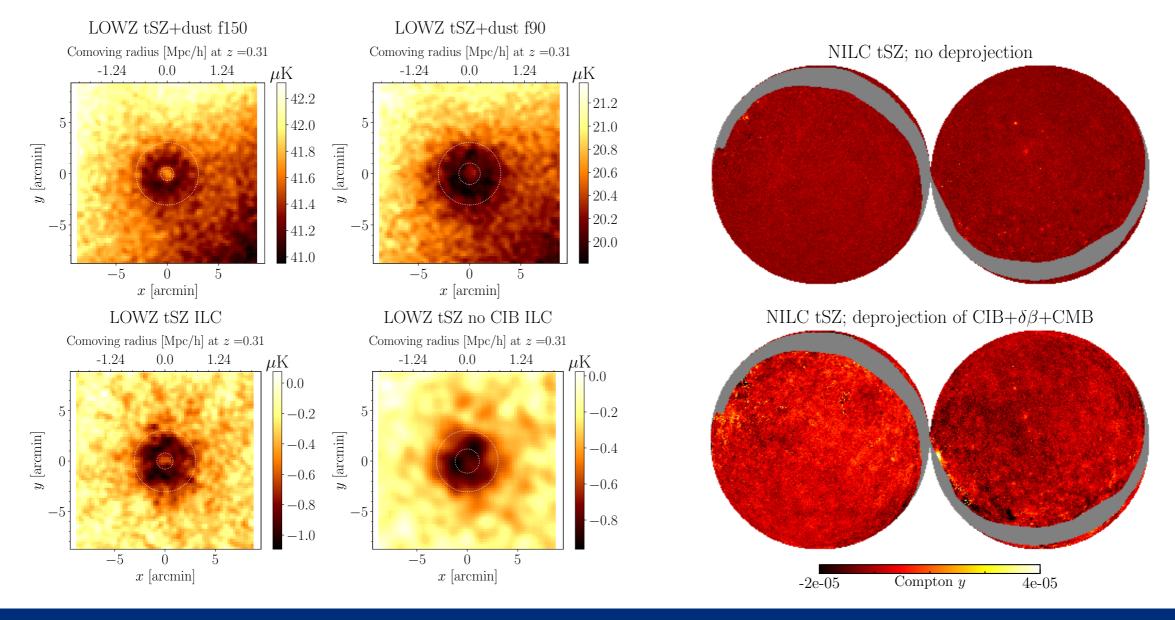
Dissect the physics of the hot gas in baryons tomographically (similar to CMB lensing cross-correlation)



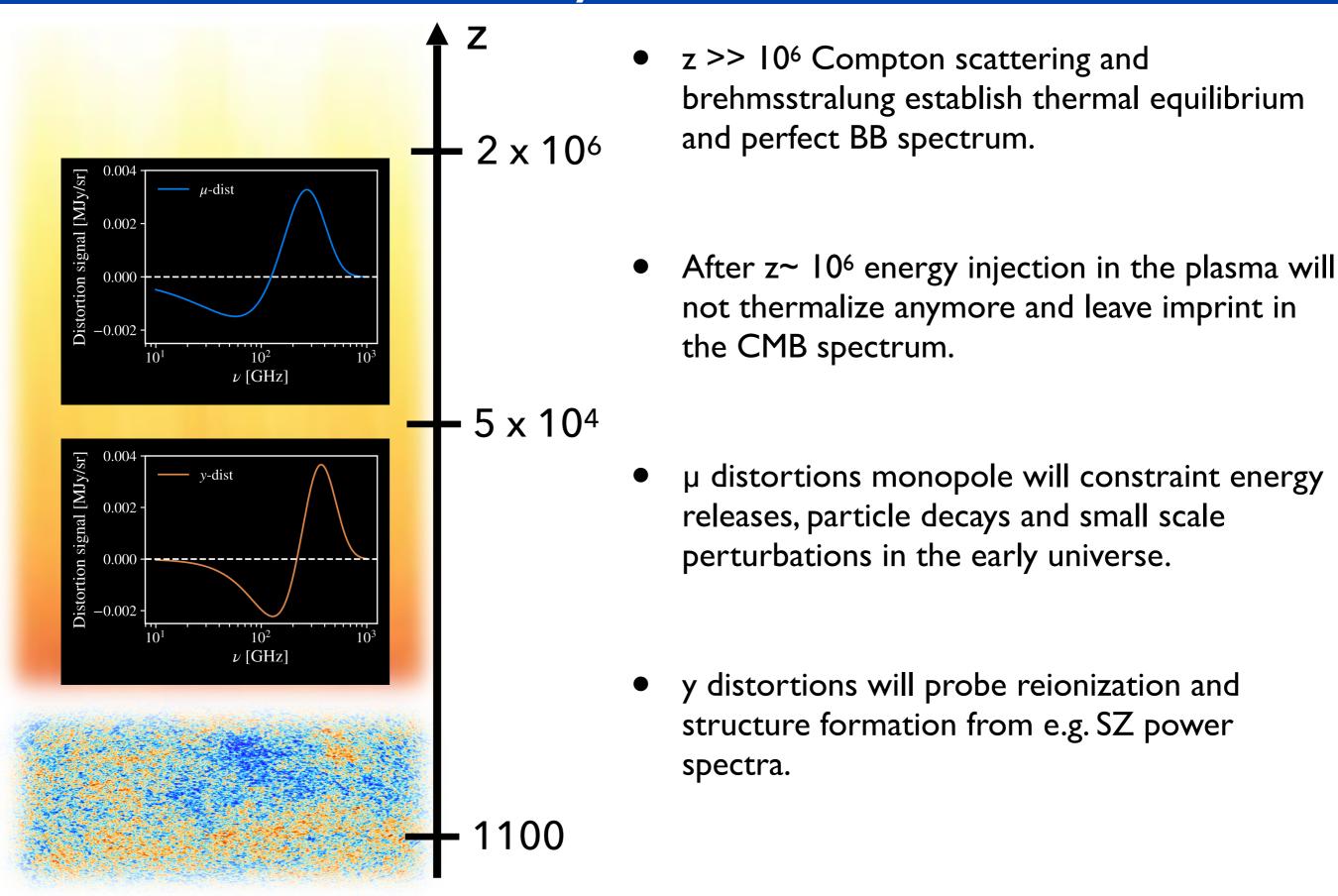
Makyia & Komatsu (2019)

The CIB challenge

- The Cosmic Infrared Background is the most important, critical tSZ contaminant.
 - Highly correlated greybody $\propto v^{\beta}B(\nu,T_{CIB})$ with large SED uncertainties.
 - More important effects as the noise goes down...



A brief thermal history of the universe



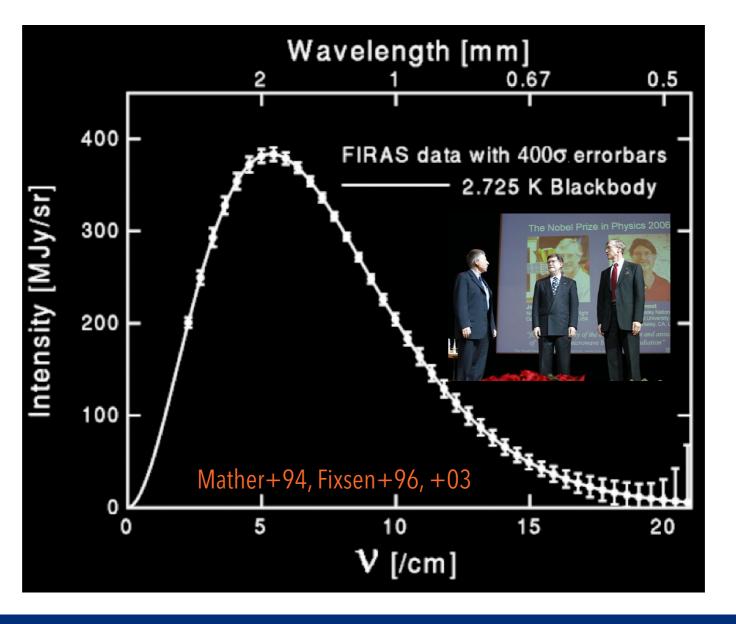
Constraints on spectral distortions

$$|\langle \mu \rangle| \lesssim 90 \times 10^{-6}$$

Limited improvements after FIRAS (~1996)

$$|\langle y \rangle| \lesssim 15 \times 10^{-6} \to (-1 \pm 6 \times 10^{-6} \text{ stat.}) \times 10^{-6}$$

• ARCADE, TRIS: improved at v < 10 GHz, questions on foreground/systematics remain.

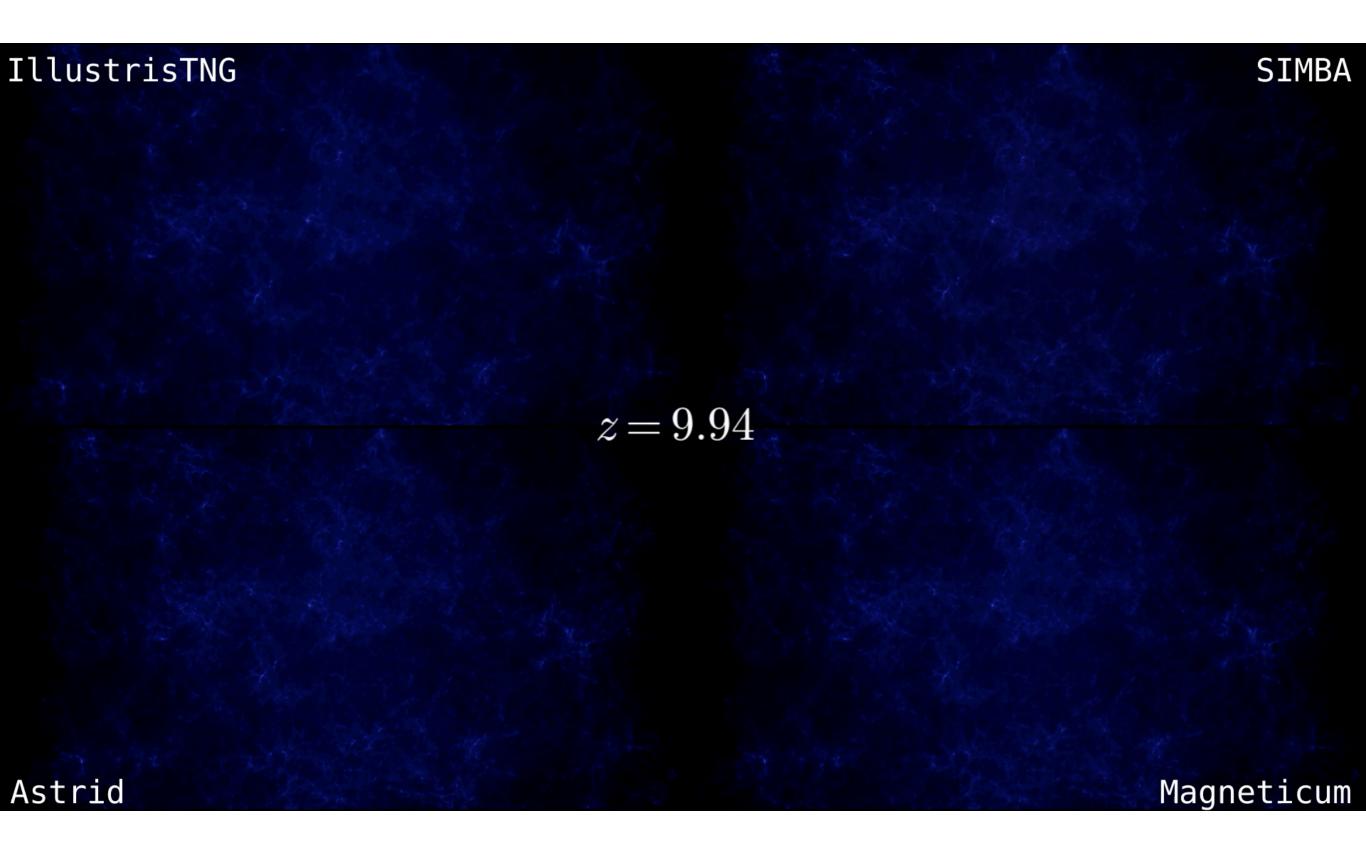


Why do we care?

• y distortions are dominated by late time gas physics: unique probe of feedback.

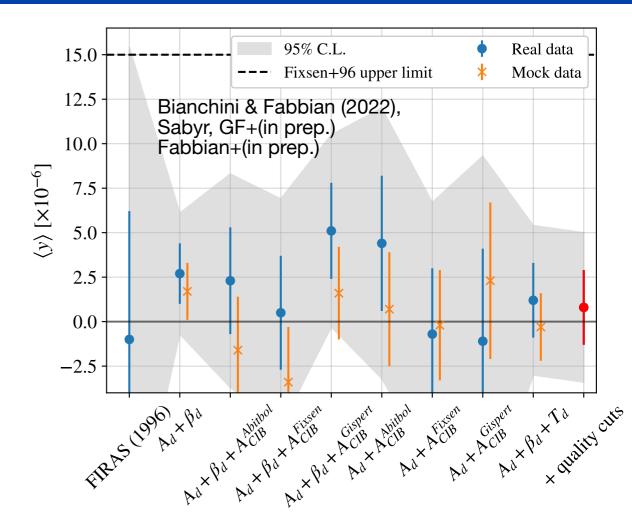
• ... and also reionization (subdominant) or primordial P(k) $k \sim 1-10$ h/Mpc.

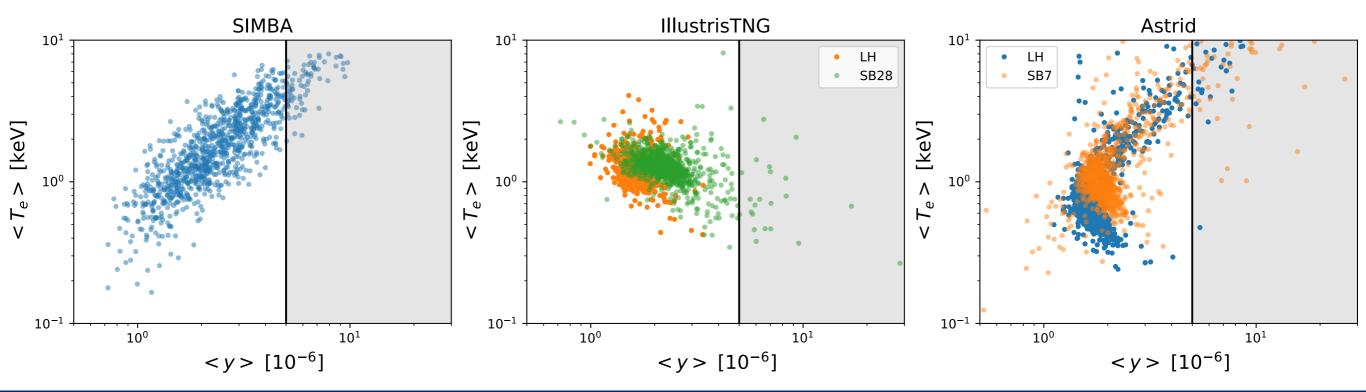
Richness of feedback models



Constraining galaxy formation models

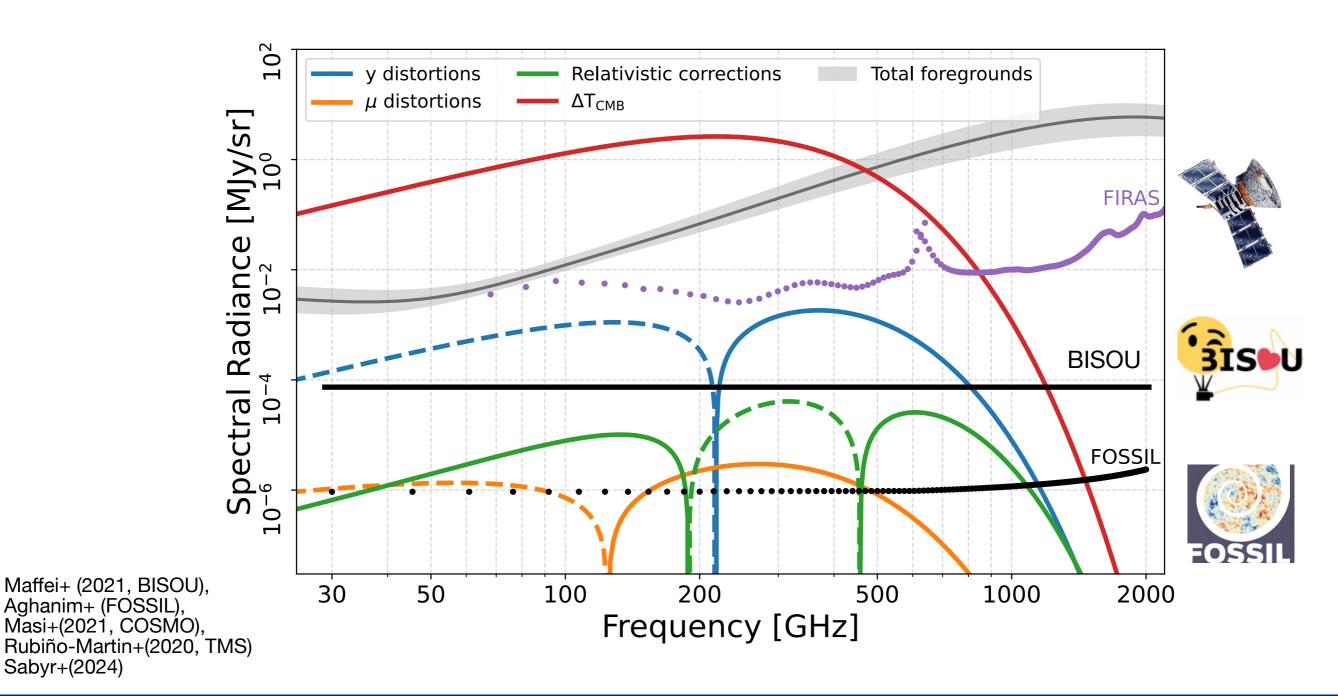
- Reanalysis of archival data with modern component separation techniques brought improvements after ~30 years.
- 2-3x better upper limit
- Feedback models from hydro simulations can be ruled out, too soon for constraints.



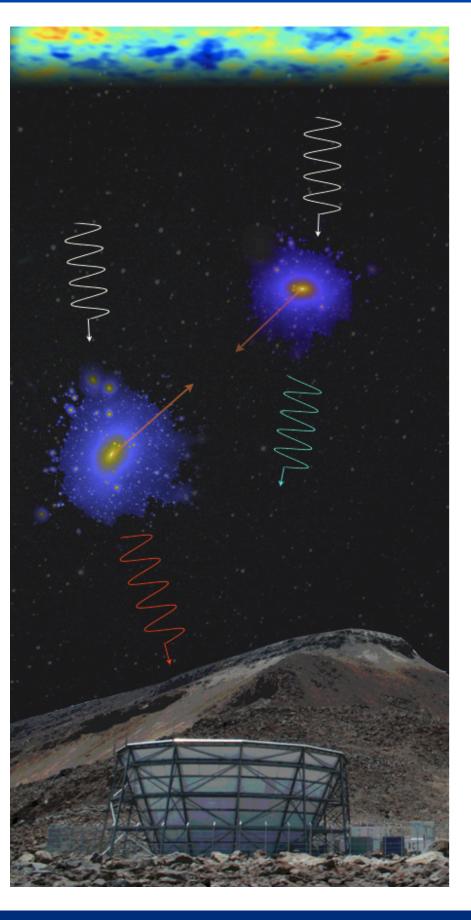


Experimental prospects

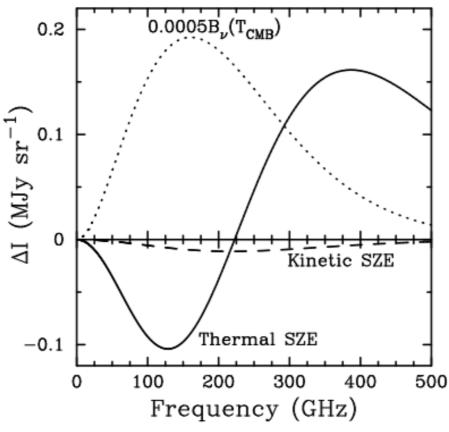
- Several instruments are being built, deployed or in phase A: transformational potential!
- FOSSIL: ESA M8 mission proposal (Pl N. Aghanim, B. Maffei+), get in touch!



What is this



- Compton-scattering of CMB photons off free electrons with non-zero line-of-sight bulk velocity.
- Direct probe of gas momentum and gas abundance!
- Cosmological information through velocity field, gas properties through optical depth.



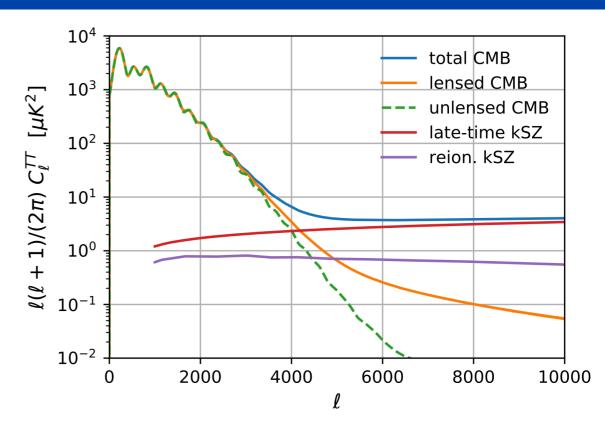
$$\Delta T_{kSZ} \sim -\tau_e \frac{v_{los}}{c}$$

$$\tau_e = \int dl n_e \sigma_T$$

What is kSZ used for and how can we measure it?

- You cannot make a map but you can see it in
 - Internally in CMB data
 - kSZ contribution to CMB

See Marian's lecture



- In combination with LSS catalogues!
 - Direct detection in galaxy clusters (hard, needs very high-resolution data).
 - Pairwise-velocity estimators (hard, needs very good redshift measurements).
 - Projected field estimators.
 - Stacking estimators.
 - kSZ velocity reconstruction.

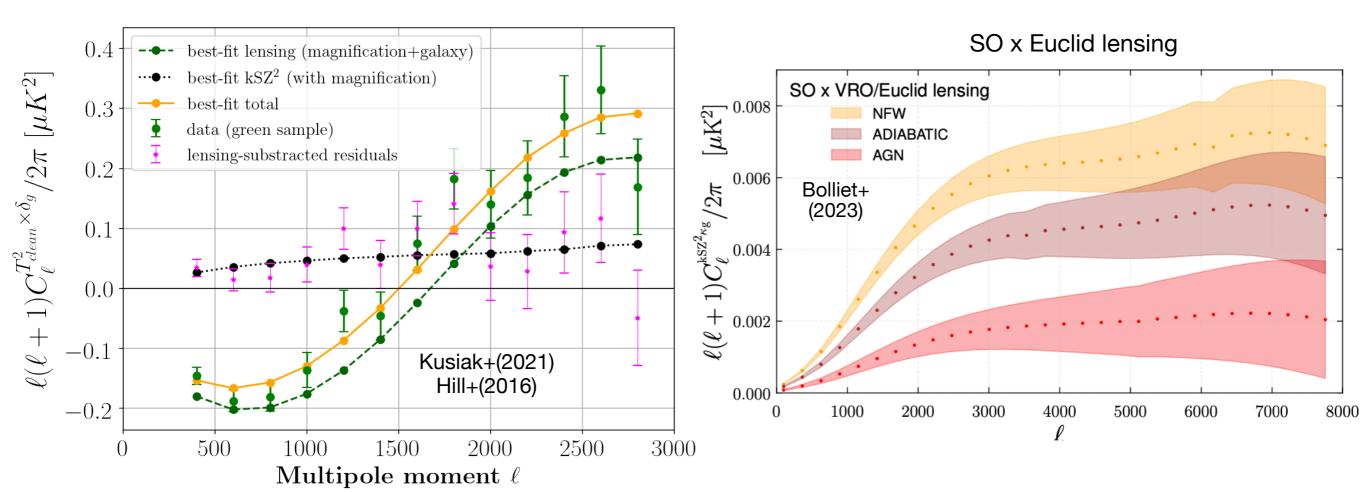
Projected field kSZ

• Doesn't need accurate redshifts, avoids v_{los} cancellation but requires modeling of bispectrum

Doré+(2004)
Ferraro+(2016)

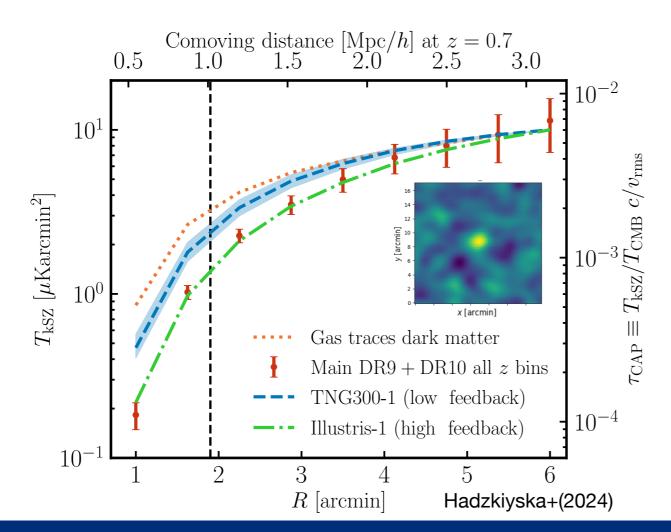
$$C_{\ell}^{\mathrm{kSZ}^2 \times \delta_g} = \int_0^{\eta_{\mathrm{max}}} \frac{d\eta}{\eta^2} W^g(\eta) g^2(\eta) \mathcal{T}\left(j = \frac{\ell}{\eta}, \eta\right) \quad \mathcal{T}(j, \eta) = \int \frac{d^2\mathbf{q}}{(2\pi)^2} f(q\eta) f(|\mathbf{j} + \mathbf{q}|\eta) B_{p_{\mathbf{\hat{n}}}p_{\mathbf{\hat{n}}}\delta}(\mathbf{q}, -\mathbf{j} - \mathbf{q}, \mathbf{j}).$$

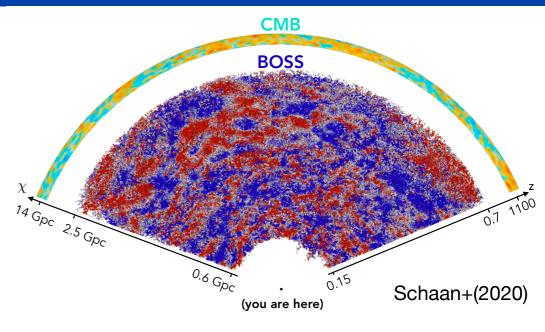
 \bullet ~ 5σ detection, can accurate probe gas with future CMB and LSS measurements.



Velocity-weighted stacking

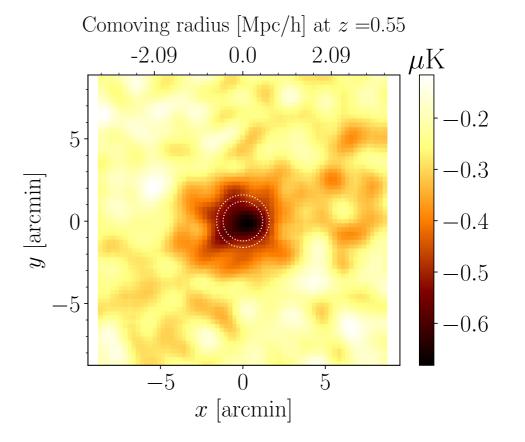
- Stack at position of dark matter halos to accounting for large scale velocity.
- Evidence for feedback pushing the gas out of halos.
- Can be combined with tSZ and CMB lensing stack to solve halo thermodynamics.





$$\mathbf{v}(\mathbf{k}) = i \frac{faH\delta(\mathbf{k})}{k} \hat{\mathbf{k}}$$

CMASS tSZ no CIB ILC

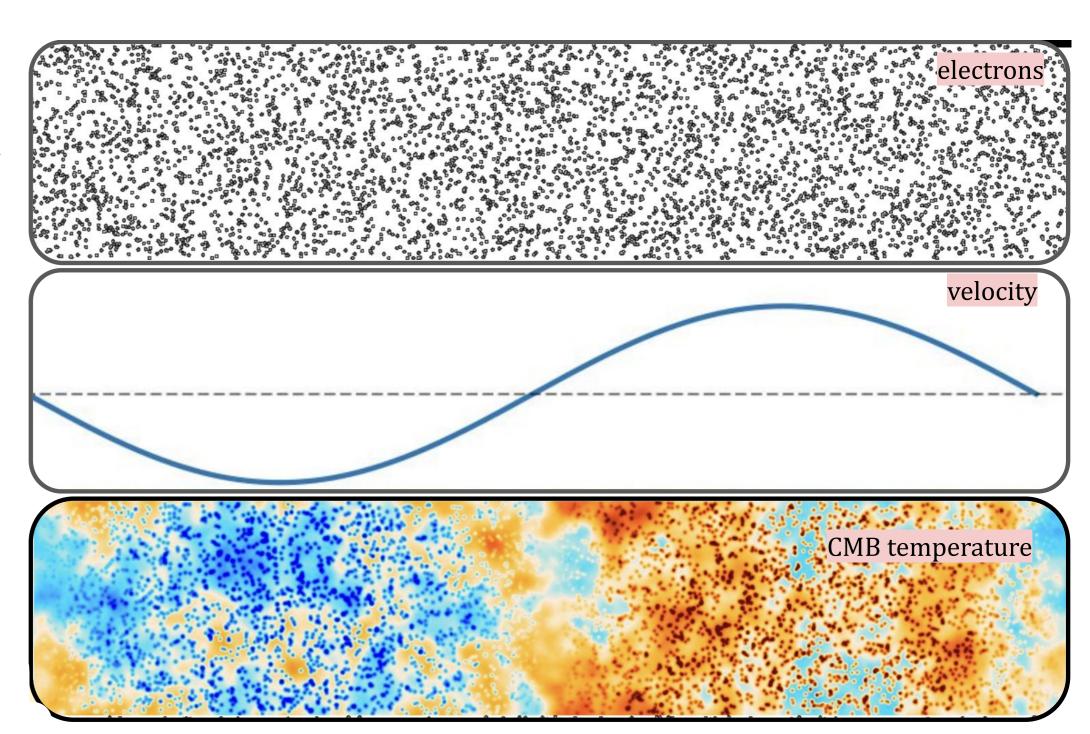


Velocity reconstruction cartoon

Consider distribution of **free electrons**

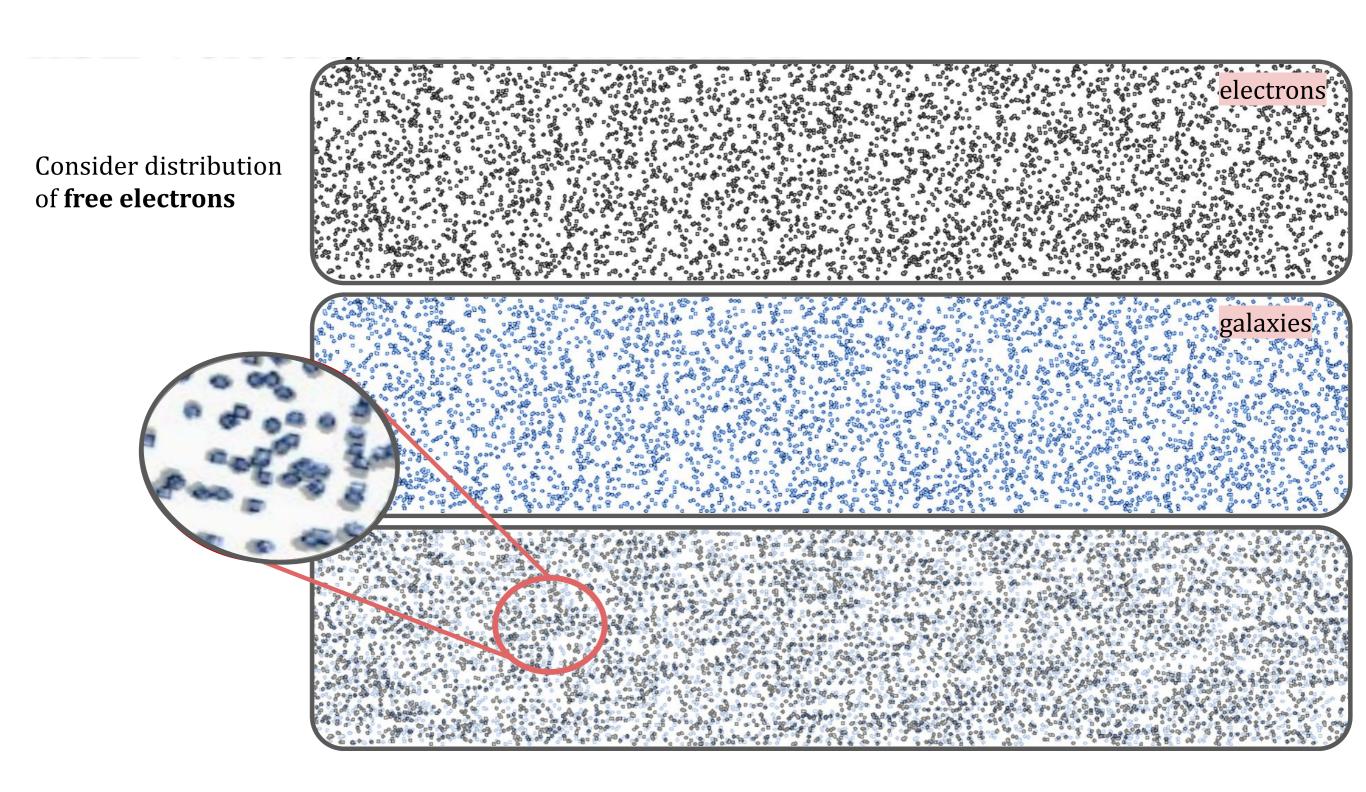
...and a cosmological velocity fluctuation

Primary CMB + kSZ

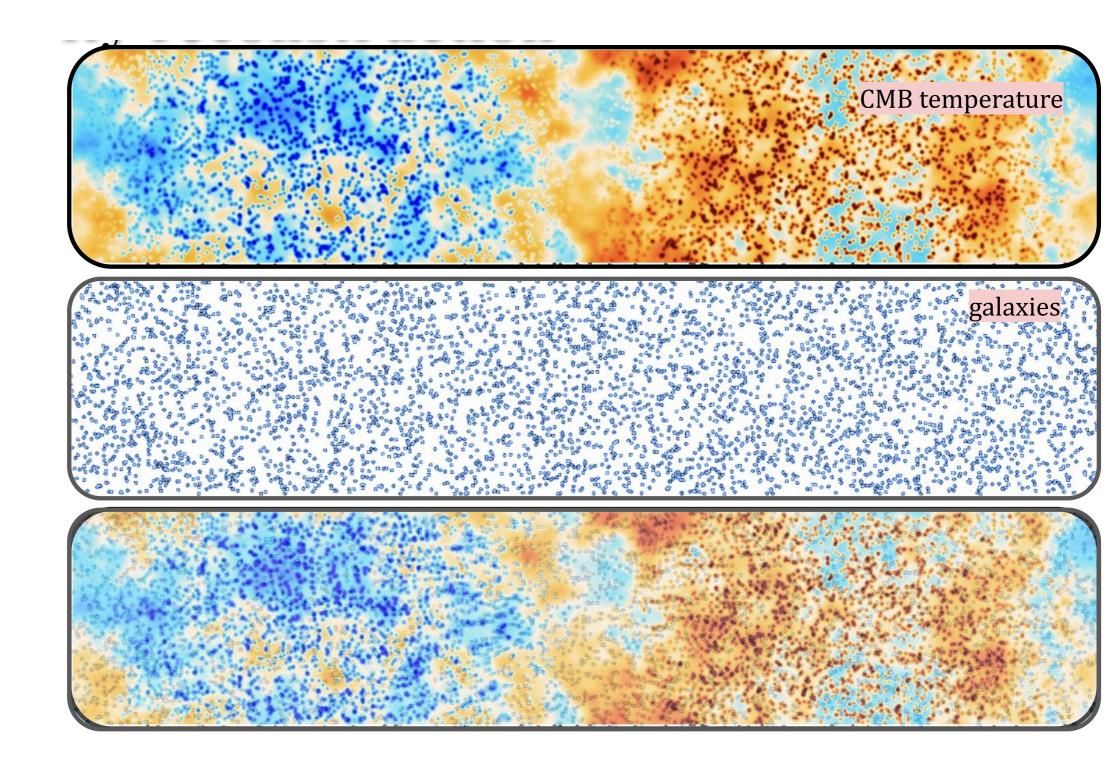


Figures by M. Madhavacheril, A. Lague

Velocity reconstruction



Velocity reconstruction

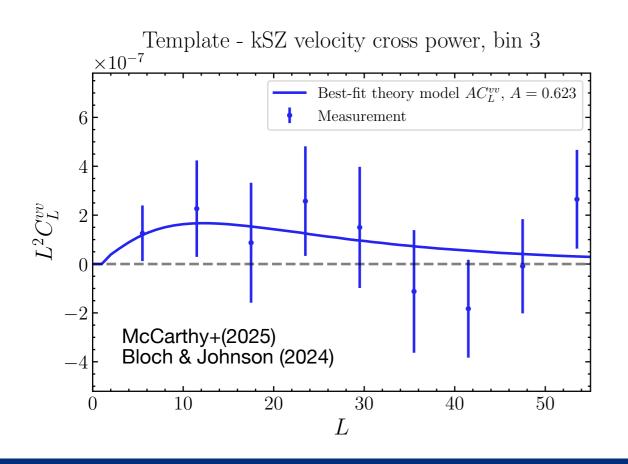


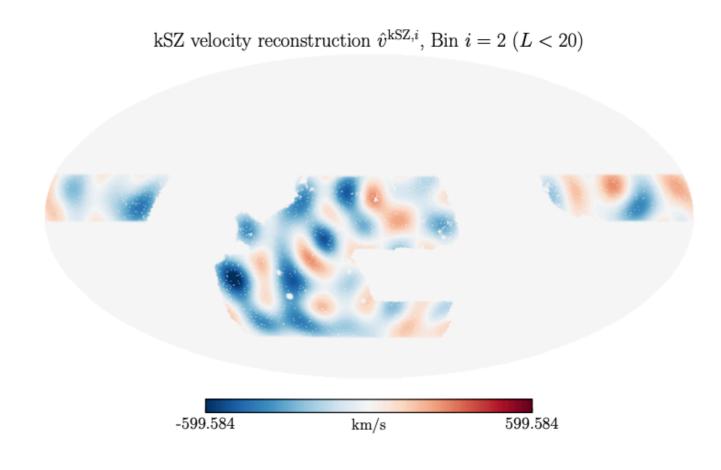
Velocity reconstruction as a quadratic estimator

Cross-correlating CMBT and galaxy surveys as a squeezed bispectrum estimator

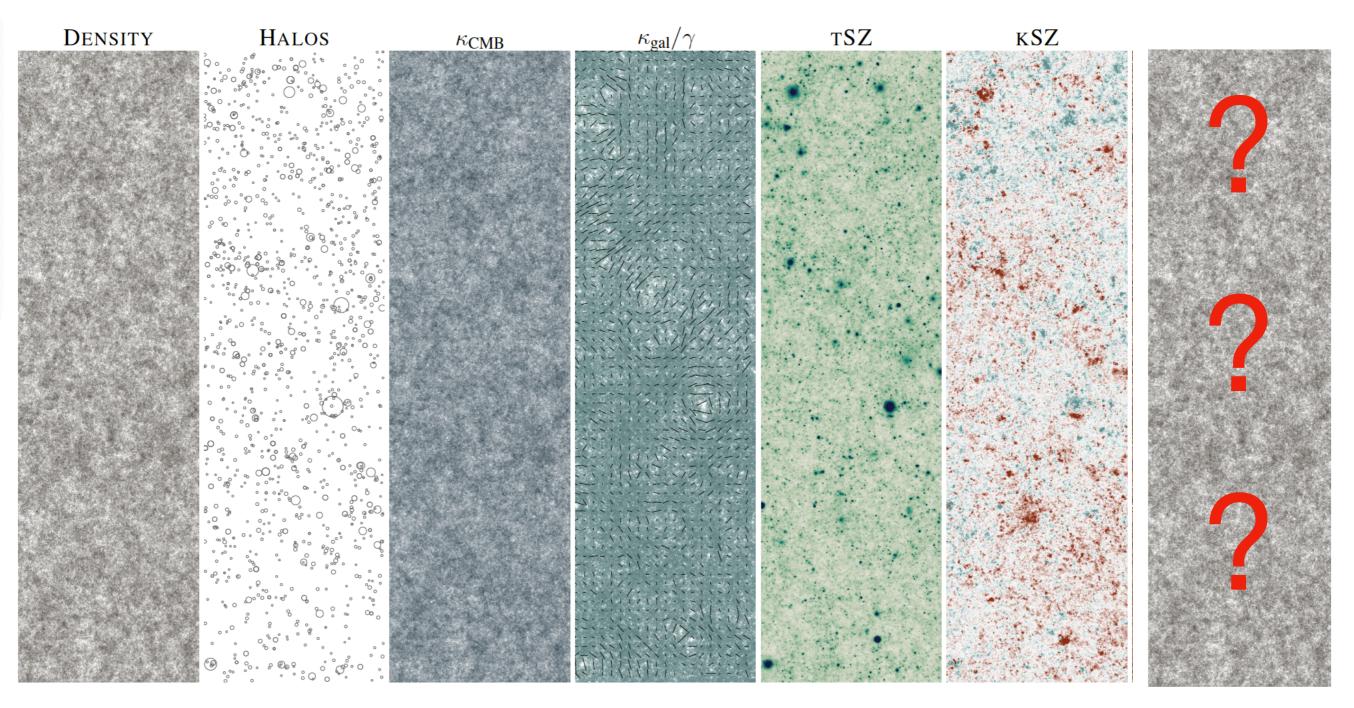
$$\Delta T_{kSZ}(\hat{\mathbf{n}}) = -\int d\chi \dot{\tau}(\hat{\mathbf{n}}, \chi) \frac{v_{los}}{c}(\hat{\mathbf{n}}, \chi) \qquad \langle \delta_g \Delta T_{kSZ} \rangle \sim \int d\chi \langle \delta_g \dot{\tau} v \rangle \sim \int d\chi \langle \delta_g \dot{\tau} \rangle v$$

- If you can model $\langle \delta_g \dot{\tau} \rangle \dots$ $\hat{v} \sim \frac{\delta_g \Delta T_{kSZ}}{\int d\chi \langle \delta_g \dot{\tau} \rangle}$ (also in 3D) Lague+(2025)
- $3\sigma 7\sigma$ detection in auto and cross-correlation, new large-scale cosmology !





Anything else?



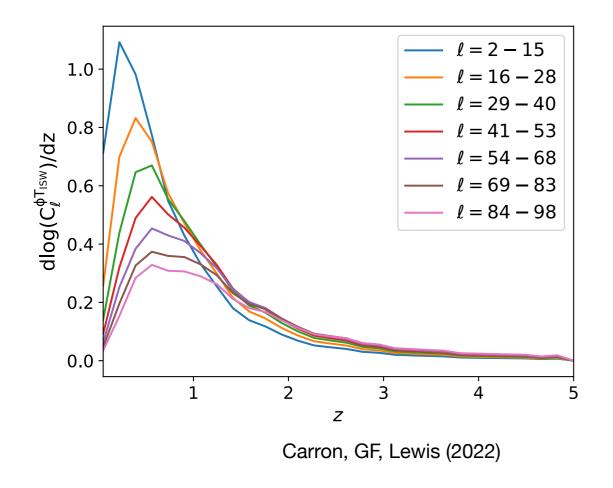
Omori (2023)

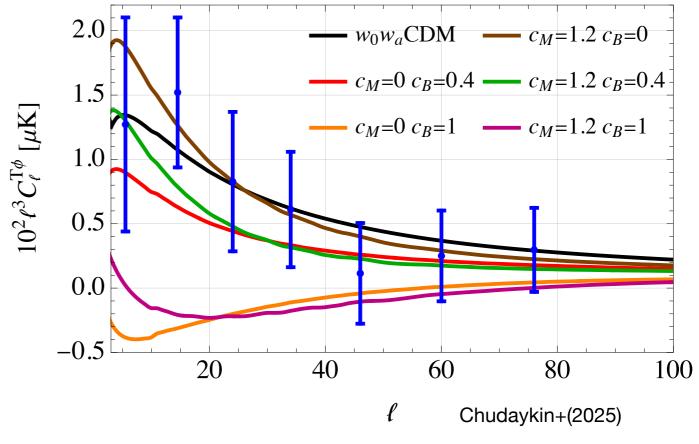
ISW effect

• Photons pick up a net blue or redshift while propagating through time-varying potentials

$$\Delta T(\hat{\boldsymbol{n}})_{\rm ISW} \approx 2 \int_0^{\chi_*} \mathrm{d}\chi \dot{\Psi}(\chi \hat{\boldsymbol{n}}, \eta_0 - \chi)$$

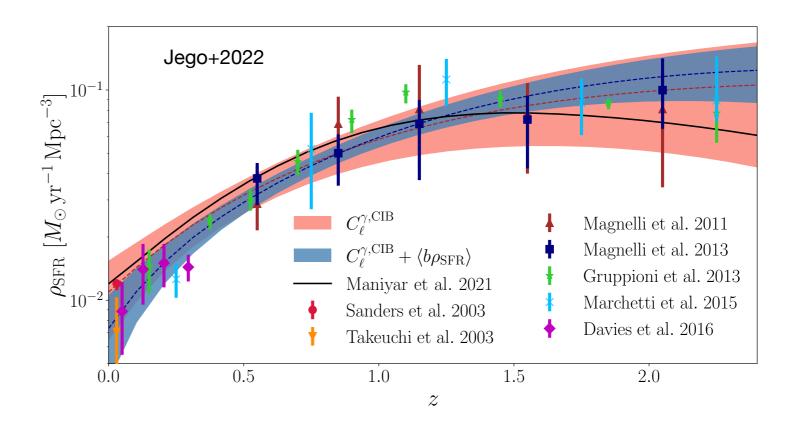
- Effect dominated by onset of dark energy at late time but same potential cause lensing...
 - Limited precision (large scale cosmic variance) but unique constraints on e.g. generalized EFT of dark energy.

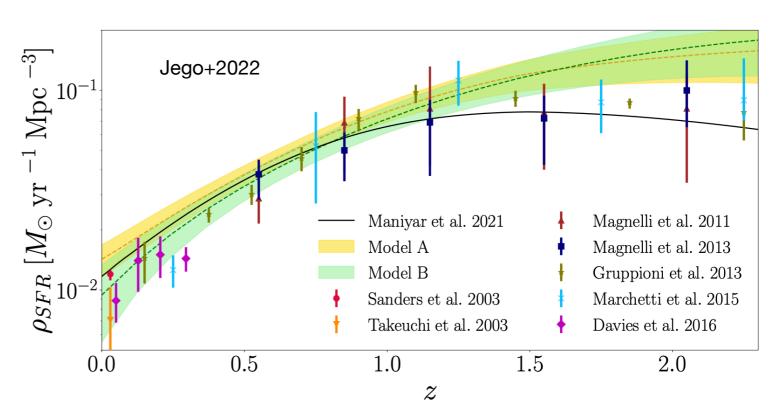




CIB cross-correlations

- CIB: sourced by dusty star-forming galaxies since the epoch of reionisation
- Maps can be extracted from CMB frequencies through component separation
 - also IR bands from e.g. Euclid or others...
- Cross-correlation allows to link SFR and matter distribution





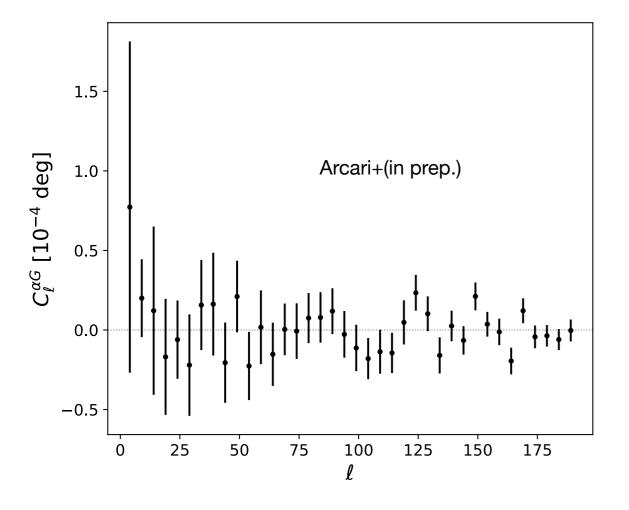
Cross-correlation with cosmic birefringence

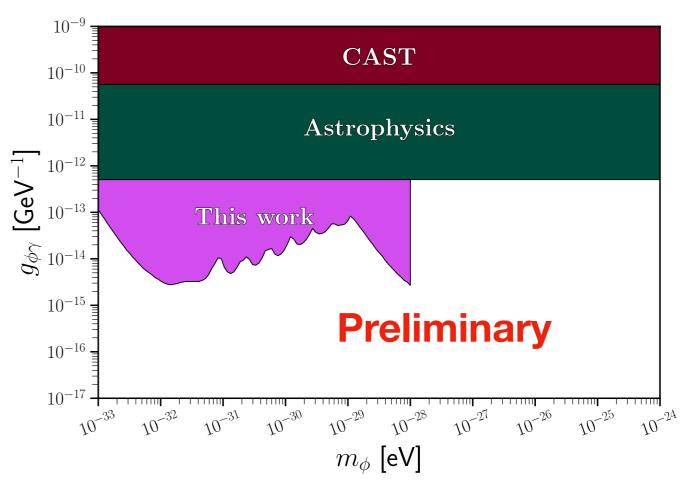
Presence of axion like coupling can generate cosmic birefringence

$$\mathcal{L} \supset -\frac{1}{2} g^{\mu\nu} \partial_{\mu} \phi \, \partial_{\nu} \phi - V(\phi) - \frac{1}{4} g_{\phi\gamma} \phi \, F_{\mu\nu} \tilde{F}^{\mu\nu} \qquad \longrightarrow \qquad Q \pm i U \rightarrow e^{\mp 2i\alpha(\hat{\mathbf{n}})} (Q \pm i U)$$

• $\alpha(\hat{\mathbf{n}})$ can be reconstructed with quadratic estimators and correlated with matter tracers.

$$\delta\phi'' + 2\mathcal{H}\,\delta\phi' + \left(k^2 + a^2\frac{d^2V}{d\bar{\phi}^2}\right)\delta\phi = -\frac{1}{2}h'\bar{\phi}' \quad \Delta_{\ell}^{\alpha}(k) = g_{\phi\gamma}\int_0^{\tau_0} \mathrm{d}\tau \; g(\tau)T_{\delta\phi}(\tau,k)j_{\ell}\left[k(\tau_0 - \tau)\right]$$





Conclusions

- Exciting times ahead with CMB experiments and LSS surveys
 - More than the sum of the two.
- CMB LSS cross-correlations are booming!
 - CMB lensing will be the new high precision/high accuracy cosmological probe.
 - More precise and robust cosmology / fundamental physics and astrophysics.
- Your new ideas and input here...
 - Probe combination / CMB secondaries require cross-disciplinary expertise.
 - Have fun with data!
 - Think about new theory probes and applications out of the box (rotation, bispectra, birefringence, spectral distortions...)