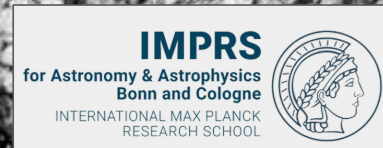


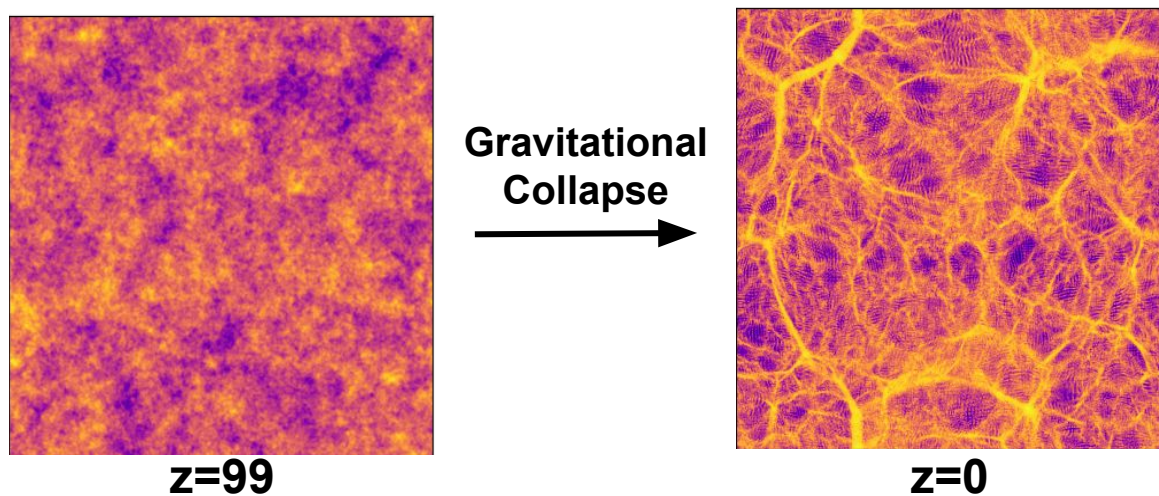
Identification of Protohalos with Deep Learning

Toka Alokda, Cristiano Porciani

Les Houches Dark Universe
24/07/2025

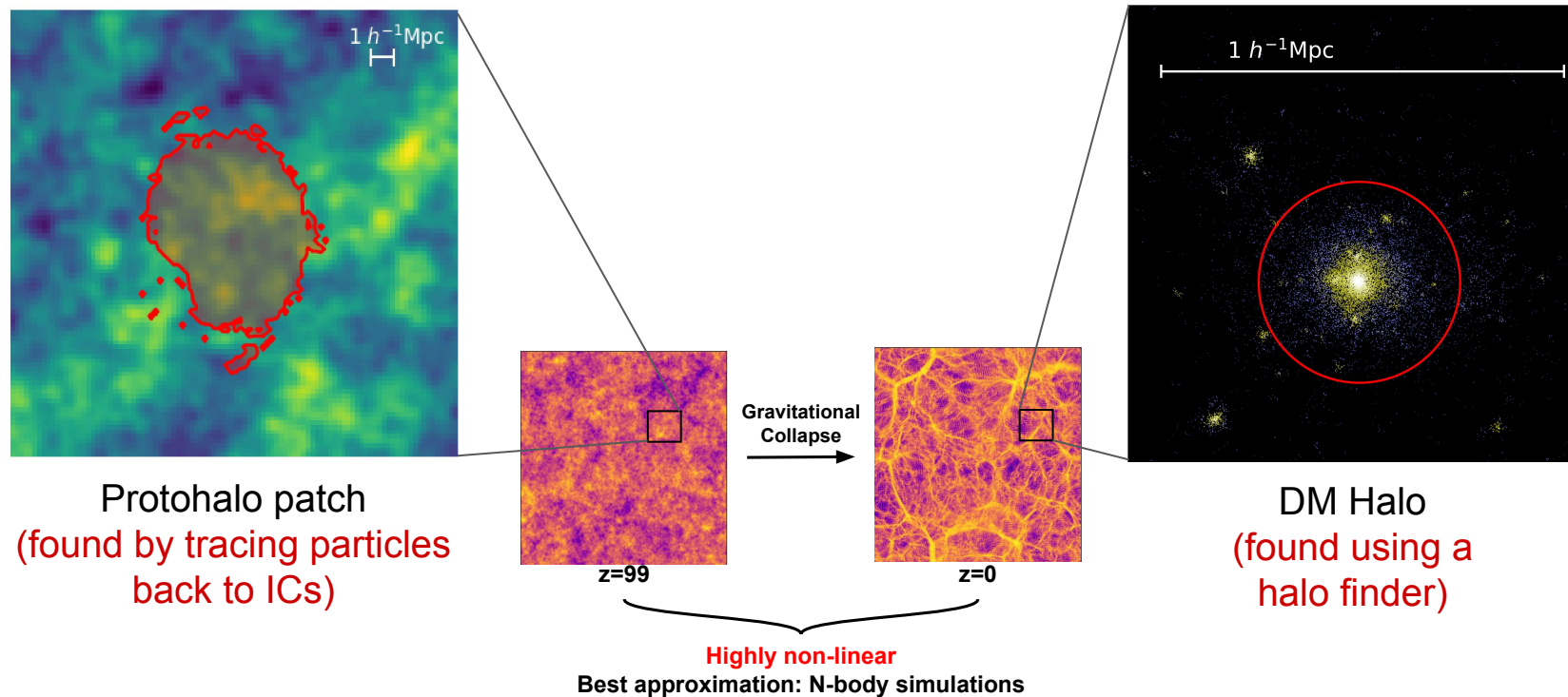


Cosmological Structure Formation

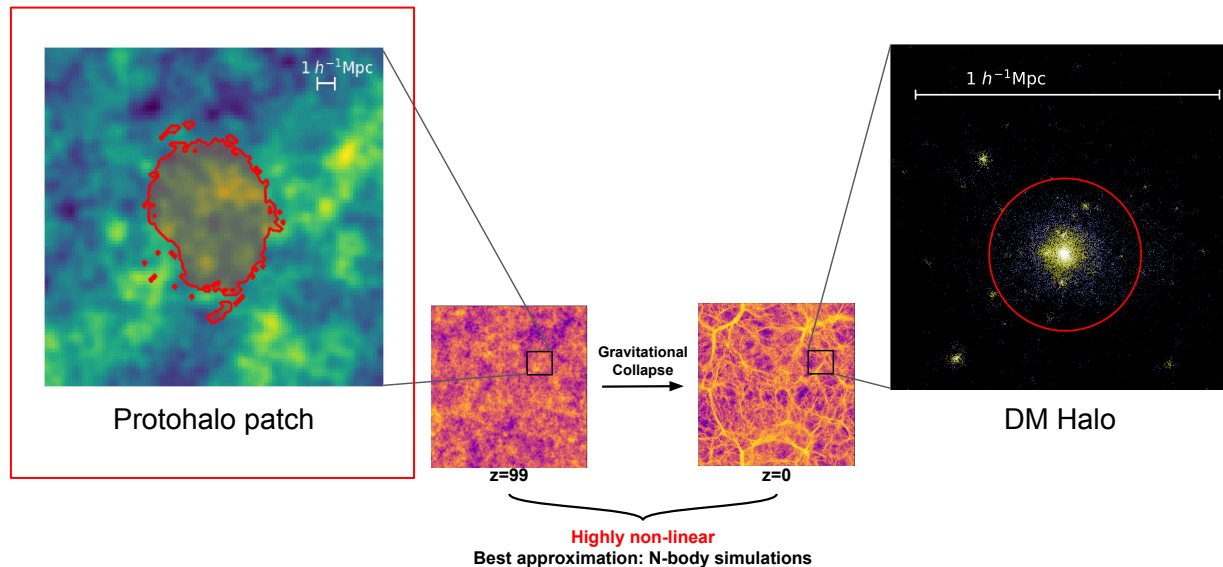


Highly non-linear
Best approximation: N-body simulations

Cosmological Structure Formation



What do we know?



- Ellipsoidal regions (lumpy potato-shaped) 🥔
- Shape tends to align with the direction of max. compression of the local tidal field
- Fuzzy boundaries affected by halo definition

Question:

**Can we accurately predict
the formation
of dark-matter halos from the
initial conditions?**

In Theory, one could...

- Use an ellipsoidal collapse model calibrated to simulations
(e.g. Sheth & Tormen '99)

Problem:

**Does very poorly
Predicting final
halo mass for a random
particle (S.D.M. White, 94')**

Question:
**Can we accurately predict
the formation
of dark-matter halos from the
initial conditions?**

In Theory, one could...

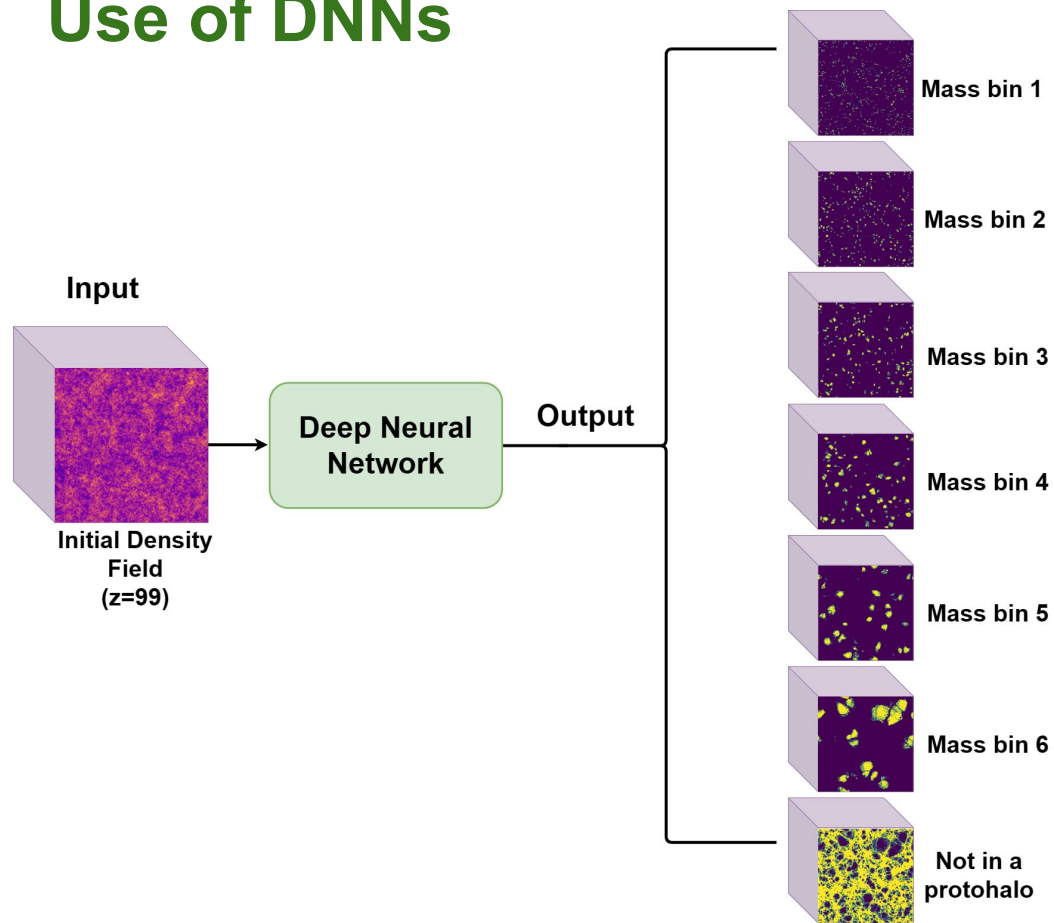
- Find the proto-halos (using e.g. peak-patch; grouping particles perturbatively...)
- Displace with LPT
- Calibrate to simulations a little bit for precision

Wonderful!

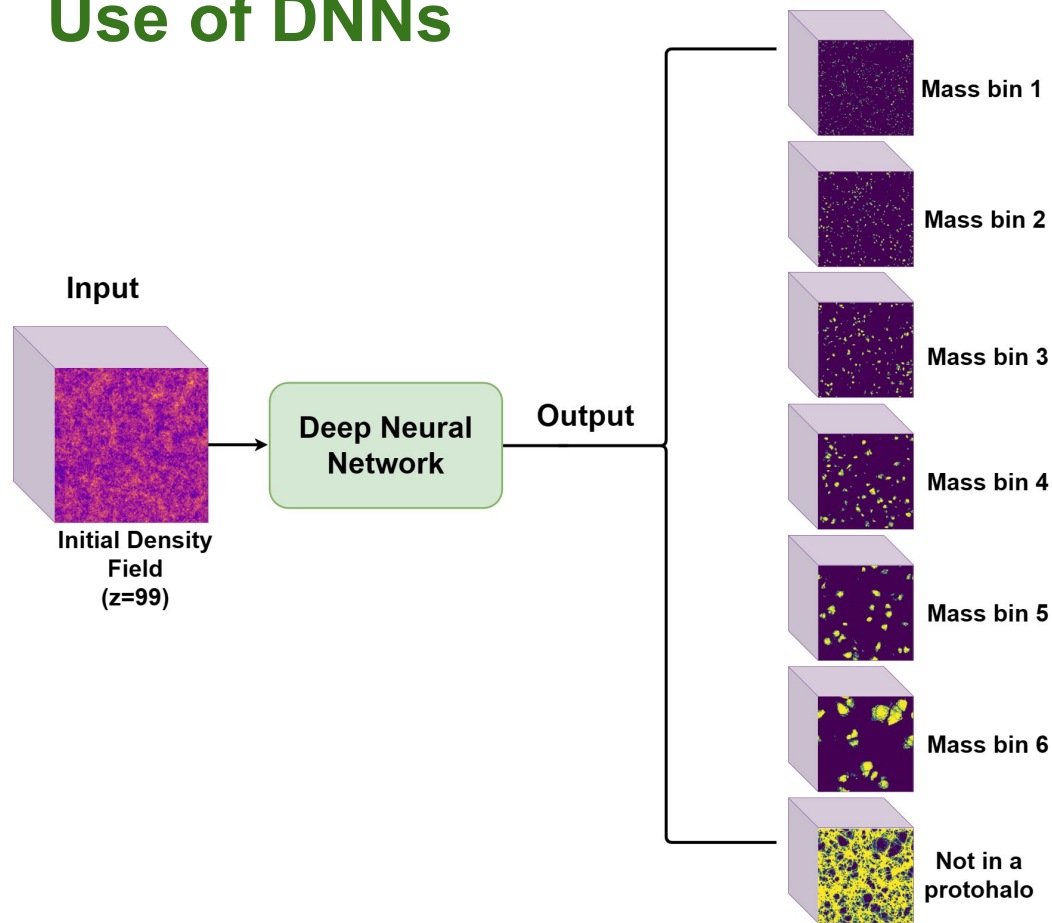
But, can we do more?

**Some unresolved issues still– e.g.
peakless halos (Ludlow & Porciani '11)**

Use of DNNs



Use of DNNs



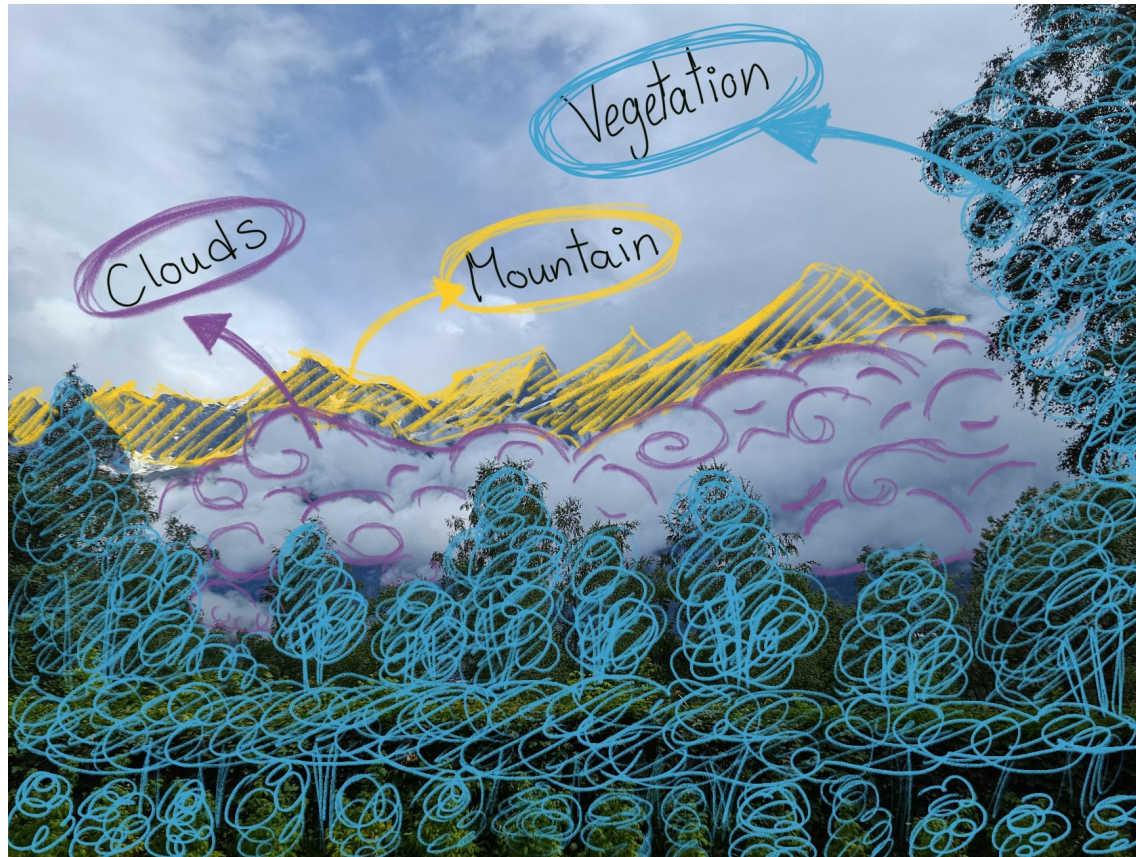
Possible Applications

- **Fast & accurate mock catalogs**
(e.g. Berger & Stein '19)
- **Learning which regions could be interesting to zoom-in simulate**
- **(Informing priors + fast estimation of) Lagrangian bias**
- **Possible to get some insights on structure formation**
(e.g. Lucie-Smith+ '19 '24)

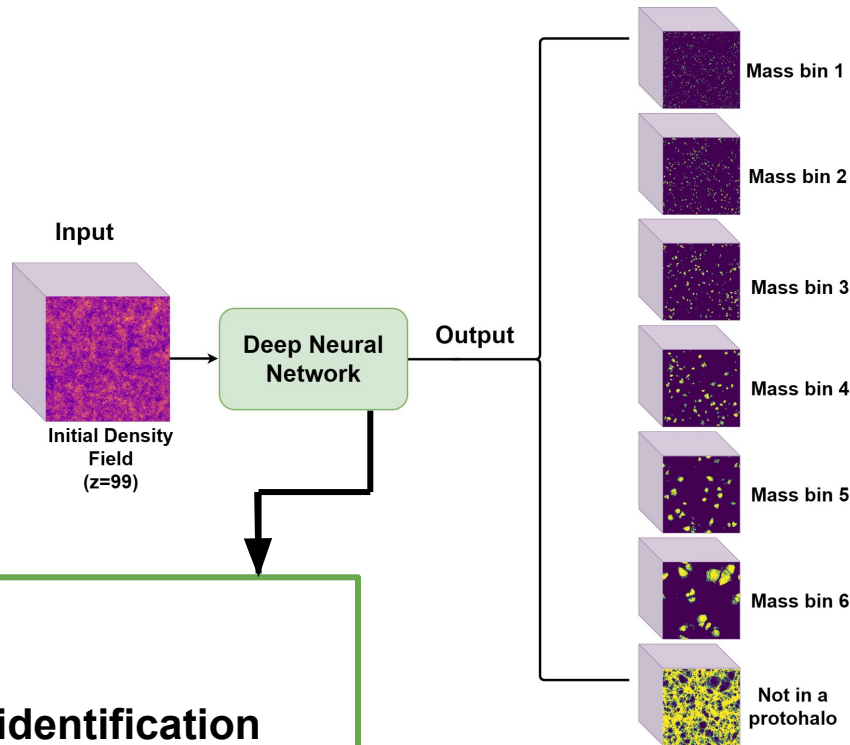
Semantic Segmentation



Semantic Segmentation relies on multi-scale features



Two approaches

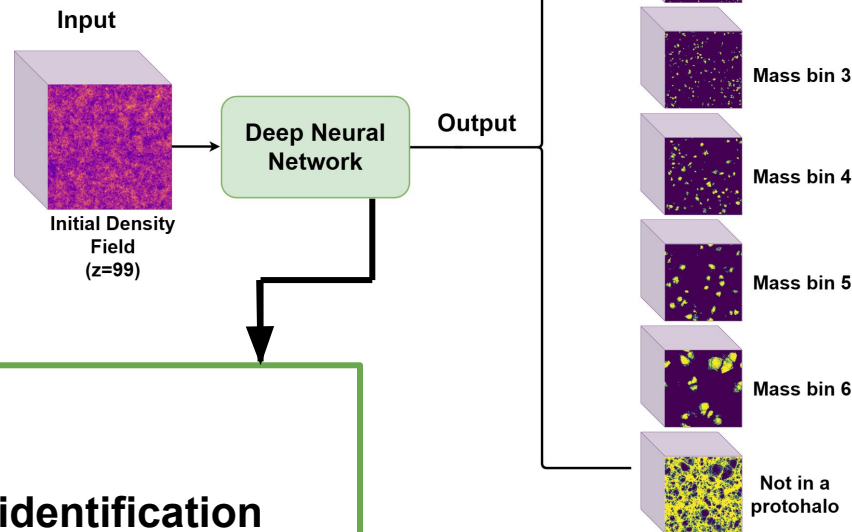


Two models 🦆 (coded up in Python)

1. **COPRA**: COnvolutions for PRoto-hAlo identification based on the V-net (Milletari+ '17)
2. **VIPR**: Vision transformers for PRotohalo identification based on the UNETR (Hatamizadeh+ '21)

Two approaches

“A Lucky Coincidence”
3D Medical images receive a lot of attention from the **computer vision** community.

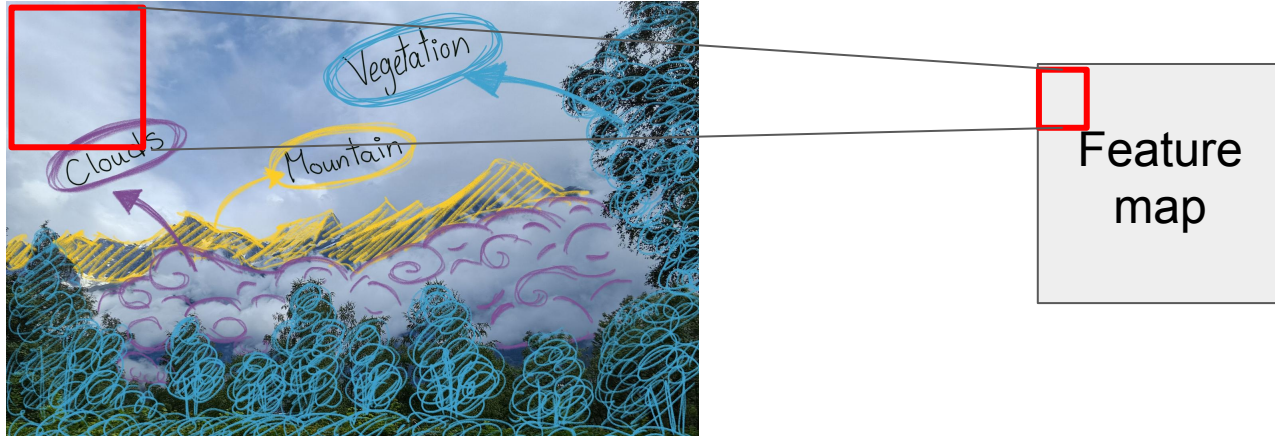


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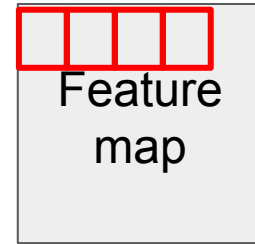
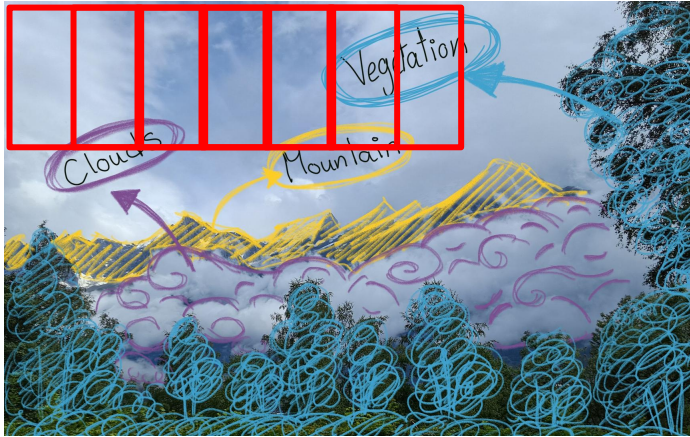
Convolutional Neural Networks (CNNs)

kernel (with learned weights)



Convolutional Neural Networks (CNNs)

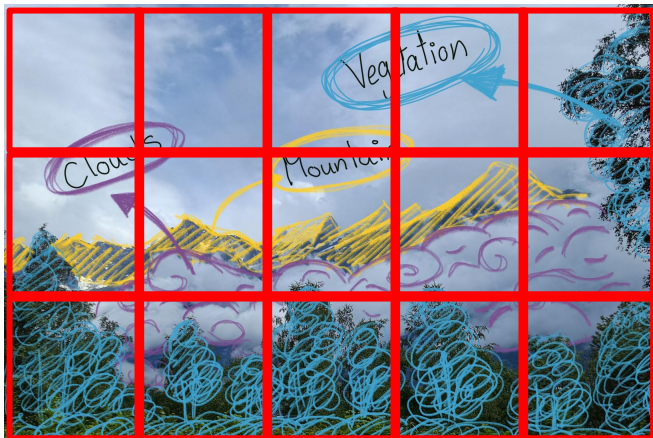
kernel (with learned weights)



Feature map
Built bit by bit

Advantage: very efficient to train + quite accurate

Vision Transformers (ViTs) 🦅



Looks at all the bits at once
in context of each other
+
Assigns “attention” scores to
each one based on its
importance

Advantage: very accurate given enough training data
+ learns large-scale dependencies

Vision Transformers (ViTs) 🦅

Attention Is All You Need

Ashish Vaswani*
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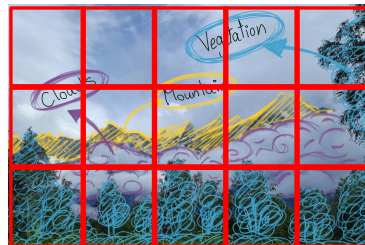
AN IMAGE IS WORTH 16x16 WORDS: TRANSFORMERS FOR IMAGE RECOGNITION AT SCALE

Alexey Dosovitskiy*[†], Lucas Beyer*, Alexander Kolesnikov*, Dirk Weissenborn*,
Xiaohua Zhai*, Thomas Unterthiner, Mostafa Dehghani, Matthias Minderer,
Georg Heigold, Sylvain Gelly, Jakob Uszkoreit, Neil Houlsby*[†]

*equal technical contribution, [†]equal advising

Google Research, Brain Team

{adosovitskiy, neilhoulby}@google.com



Looks at all the bits at once
in context of each other

+

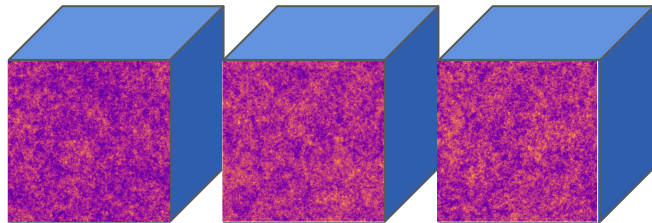
Assigns “attention” scores to
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Training Data

Four **GADGET** simulations

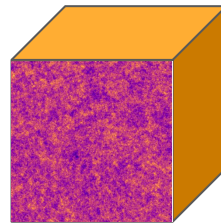
- $N = 512^3$
- $L = 100 \text{ Mpc}/h$
- 2LPT initial conditions
- Run from $z=99$ to $z=0$
- AHF: min. 40 particles in R_{200}



Training

Max. halo mass $\sim 10^{14.4} h^{-1} M_{\odot}$

Min. halo mass $= 10^{10.416} h^{-1} M_{\odot}$



Testing

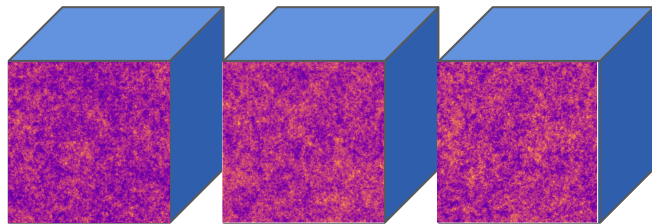
Training Data

Four **GADGET** simulations

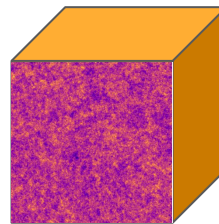
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Created “output”
volumes
with 7 classes
(6 mass bins + “no
halo” class)

Generated 3,375
overlapping samples
Of size 64^3
per simulation



Training



Testing

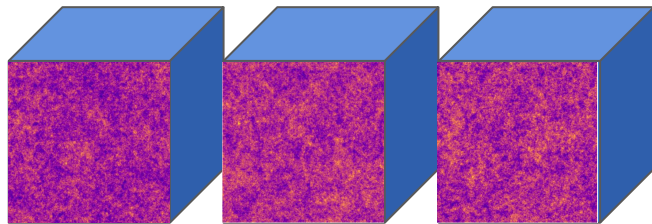
Training Data

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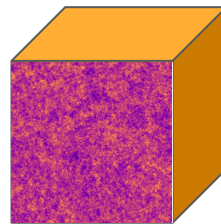
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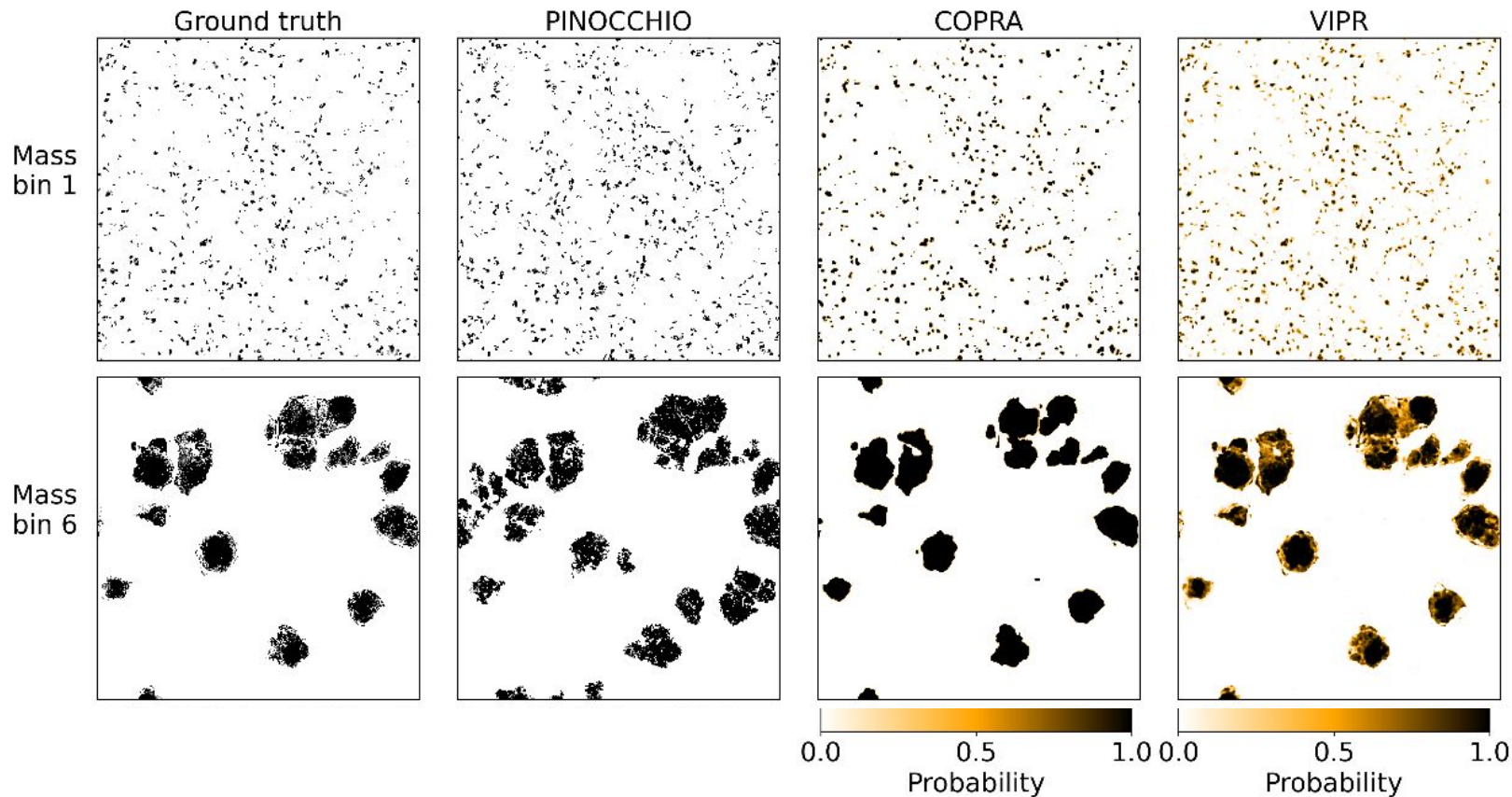
Training



Testing

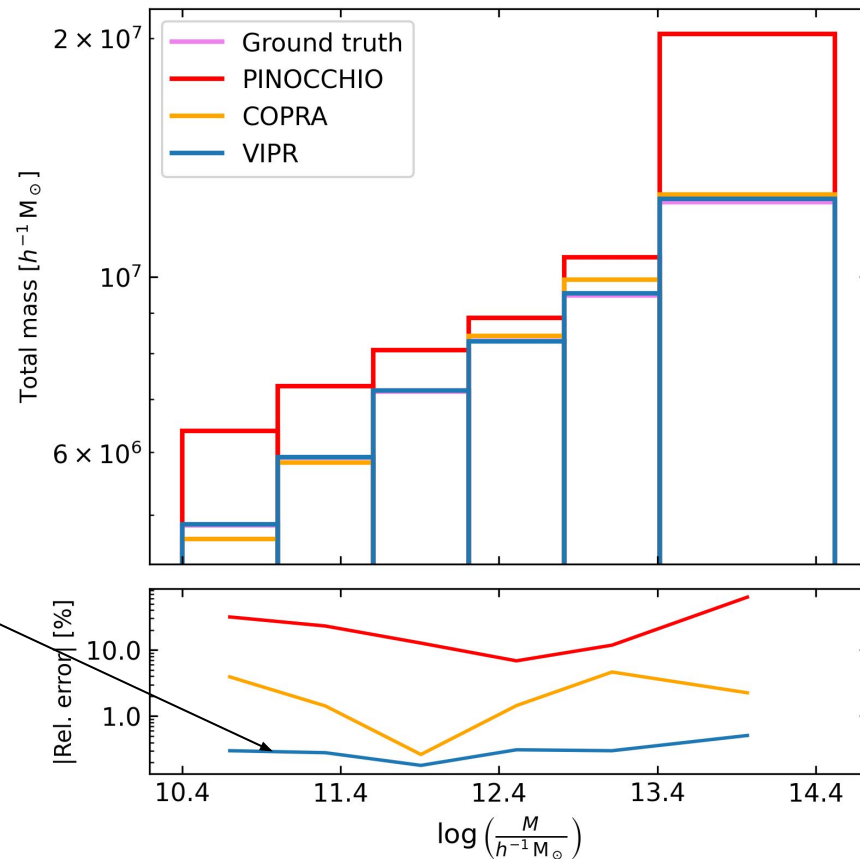
Also generated a catalog with 3LPT-based
code **PINOCCHIO**
(Monaco+ '02)

Predictions on the test simulation

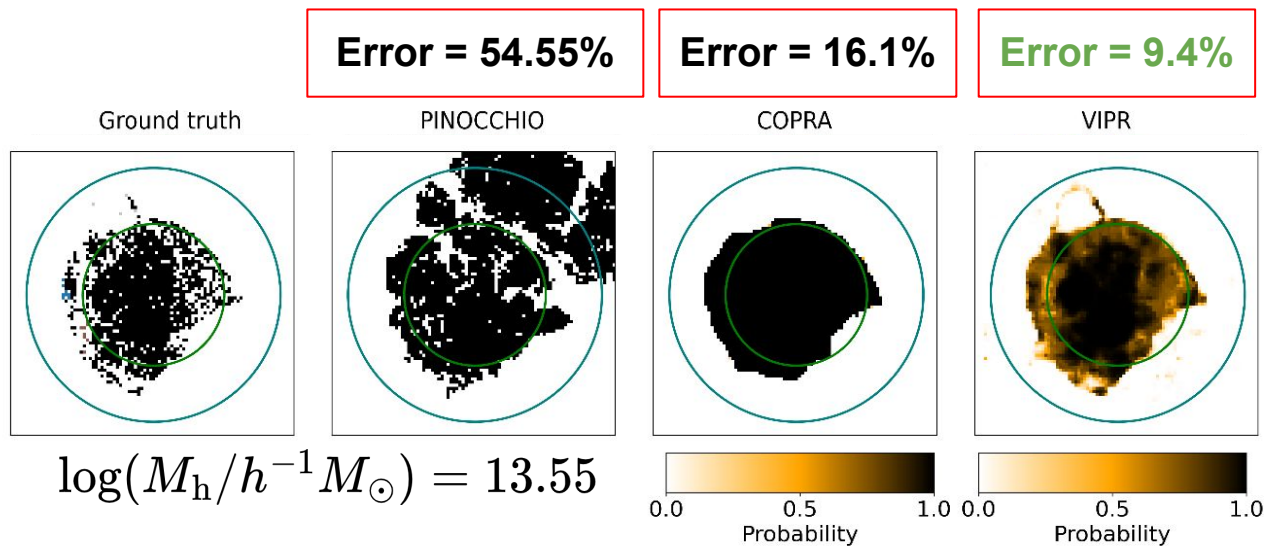


Predictions on the test simulation

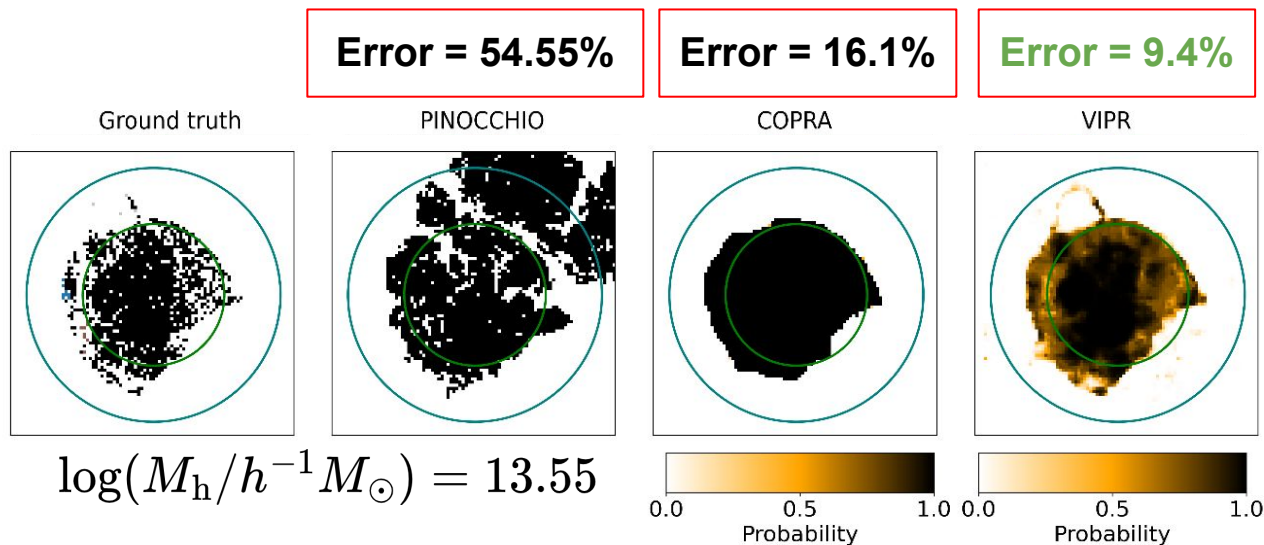
Consistent <1% errors
on box-level



Object-level validation: halo mass

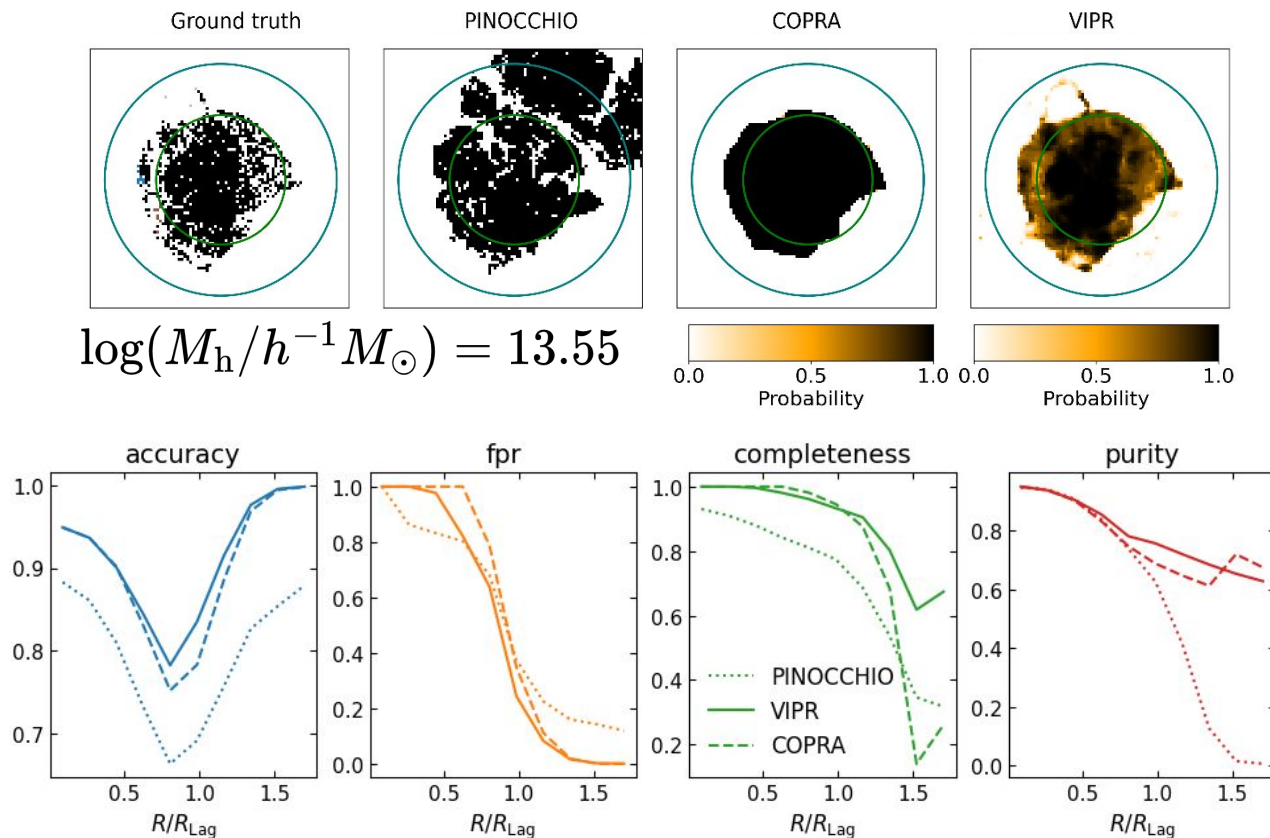


Object-level validation: halo mass

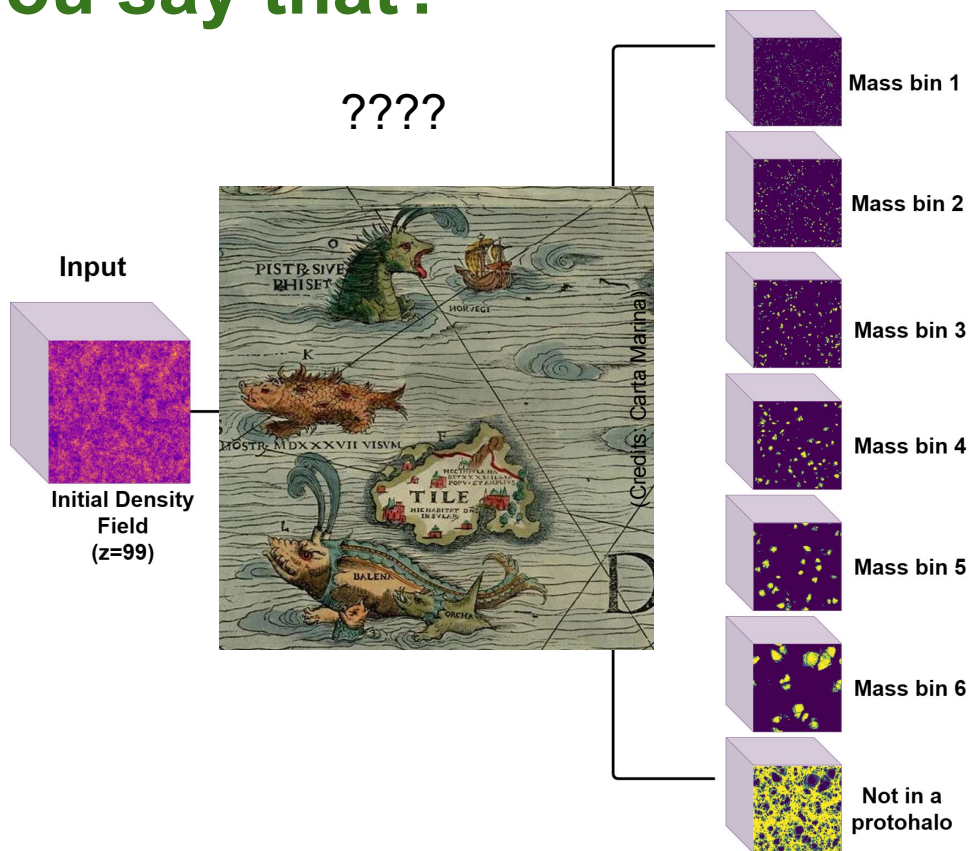


Goes to **<1%** when we average over many small protohalos of the same final mass

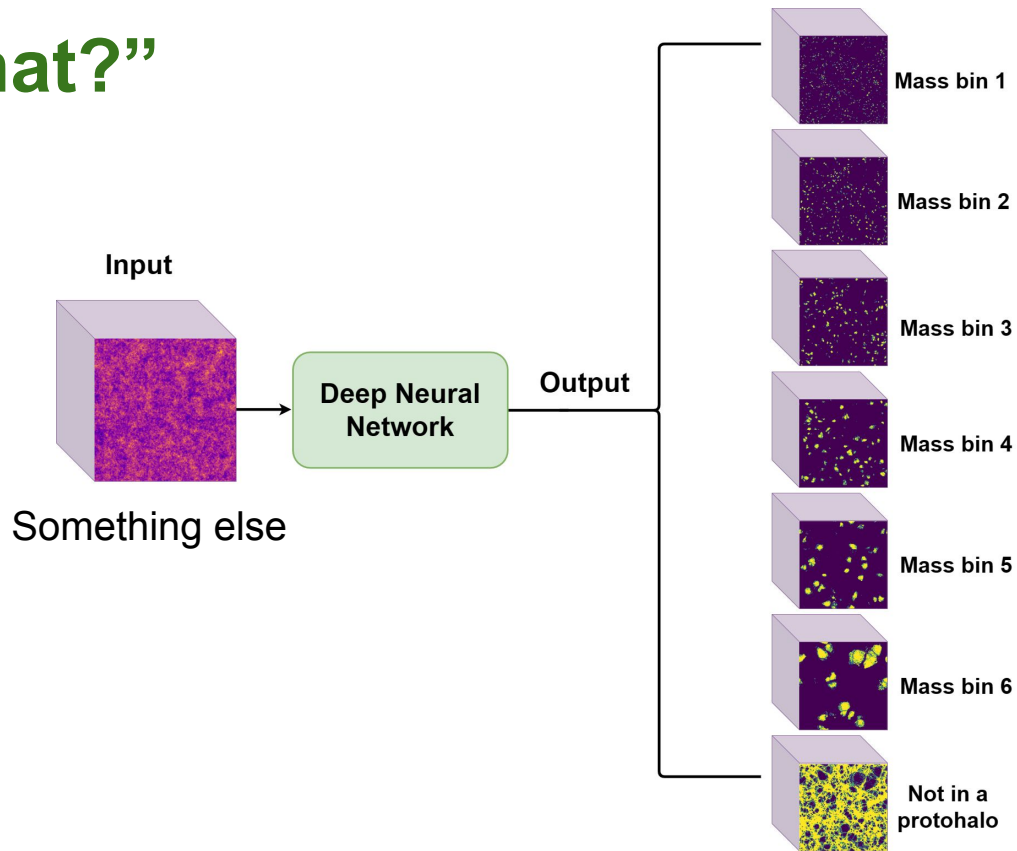
Object-level validation: classification quality



“Why did you say that?”



“Why did you say that?”

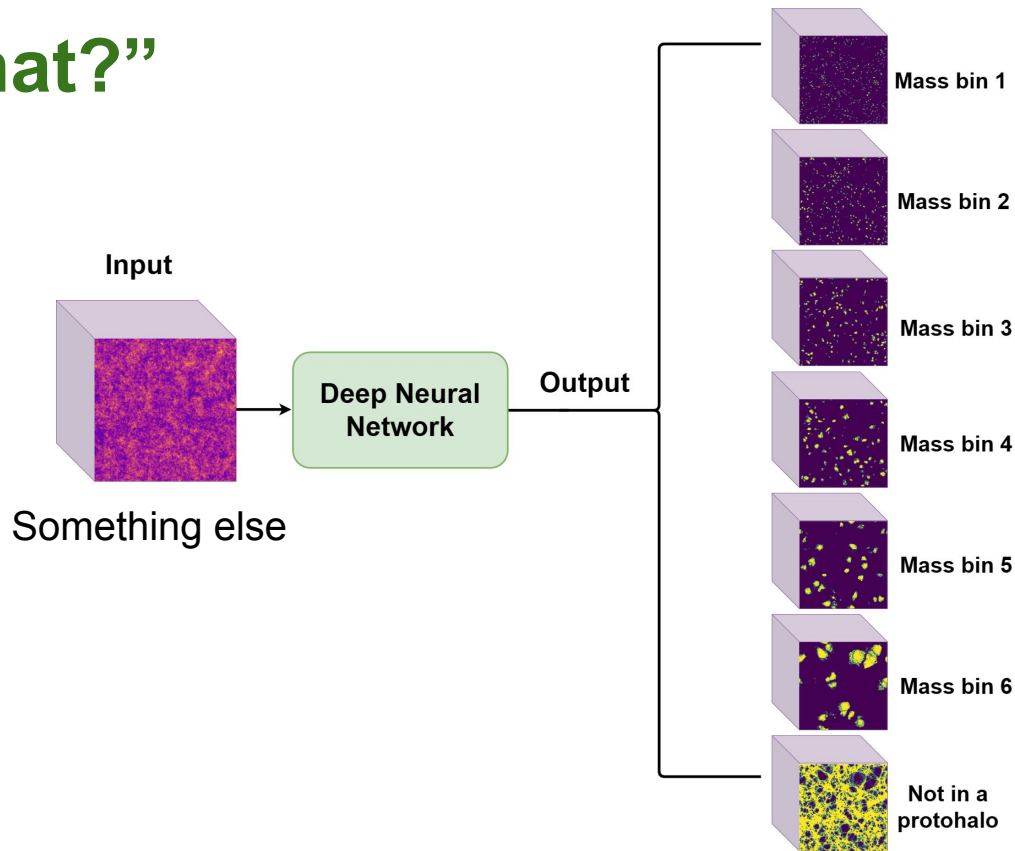


“Why did you say that?”

e.g. magnitude of
the tidal tensor

$$T_{ij} = \frac{\partial^2 \Phi}{\partial x_i \partial x_j} - \frac{1}{3} \nabla^2 \Phi \delta_{ij}$$

$$T = \sqrt{\sum_{i=1}^3 \sum_{j=1}^3 (T_{ij})^2}$$



“Why did you say that?”

e.g. magnitude of
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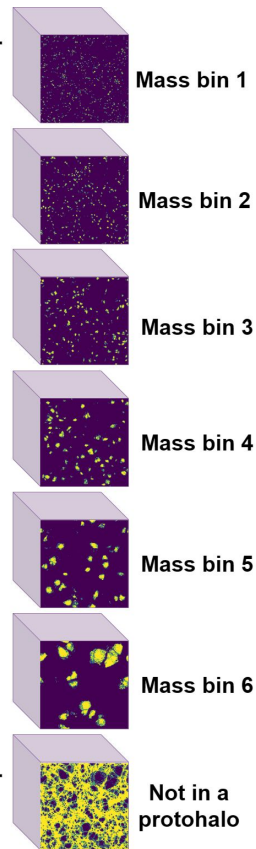
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Input
Something else

Deep Neural
Network

Output

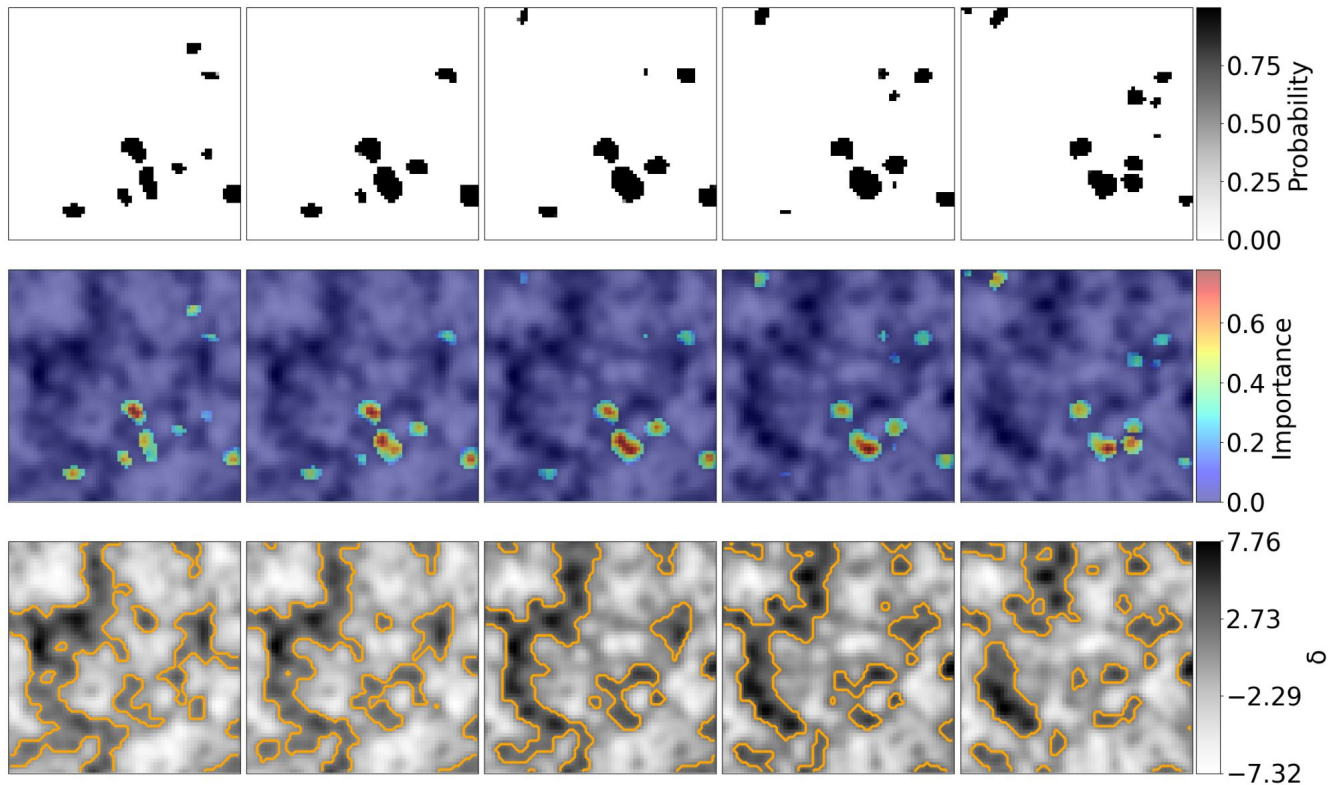


Validation accuracy [%]

Input	COPRA	VIPR
δ	85.2	92.4
T	83.7	92.3
$\delta \wedge T$	85.8	93.1

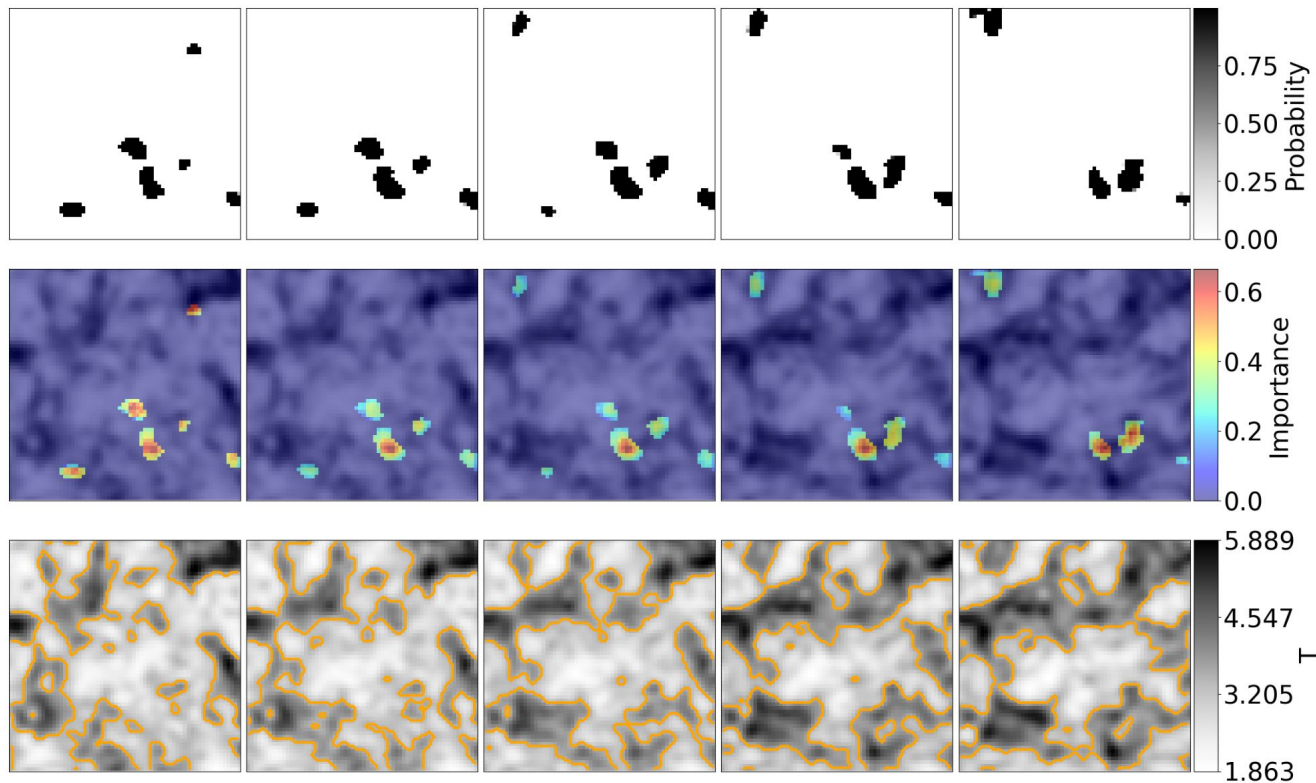
“Why did you say that?”

(Selvaraju+ '17) Grad-CAM



“Why did you say that?”

(Selvaraju+ '17) Grad-CAM



Summary and Conclusions

- **ViTs seem to learn much better than CNNs from Simulation cubes**
 - 1- It may be nice to invest in training them for useful tasks given their scalability.
 - 2- **<1%** error for the total mass, **<10%** error for individual halo masses.
- **Neural Networks seem like a promising alternative to standard tools (PINOCCHIO).**
- **May be possible to get some insights into what the model “looks” at, and which quantities play a bigger role in halo formation.**

The background of the slide is a deep blue space filled with a complex network of golden-yellow filaments and clusters, representing the cosmic web or galaxy distribution. These structures are interconnected, with some denser regions and many smaller, isolated points of light.

Speak to me!

toka@uni-bonn.de

About:

- **This project**
- **(New and higher-order) #Statistics4PnG
+ Inference methods → My PhD work**

Thank You