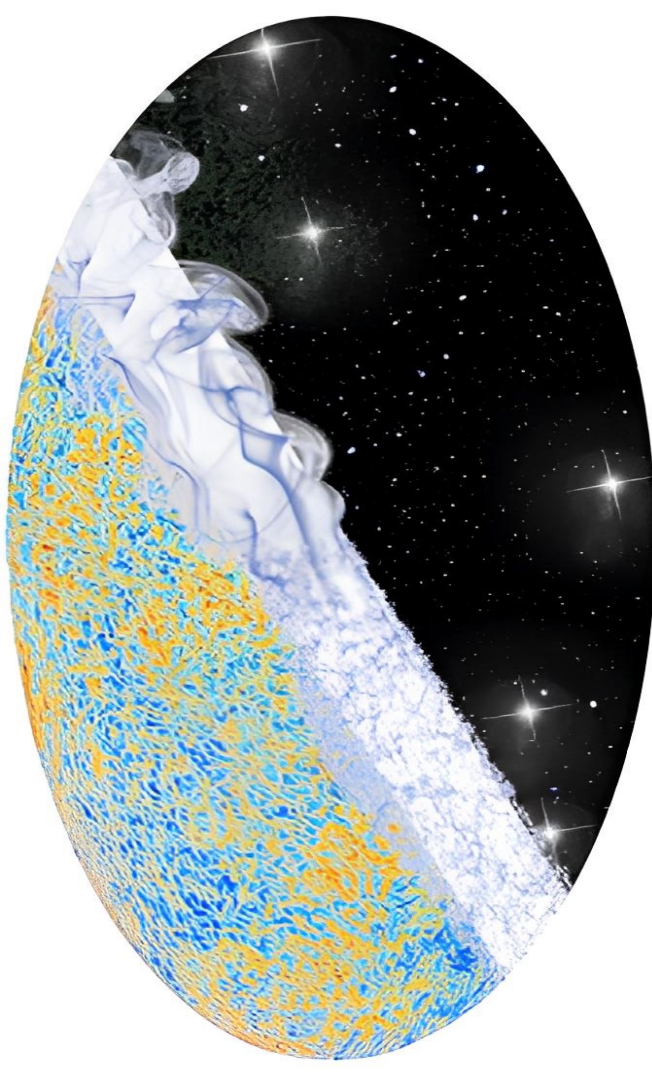




Revisiting the Cosmic Distance **LADDER** with Deep Learning Approaches and Addressing Cosmological Tensions

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Collaborators

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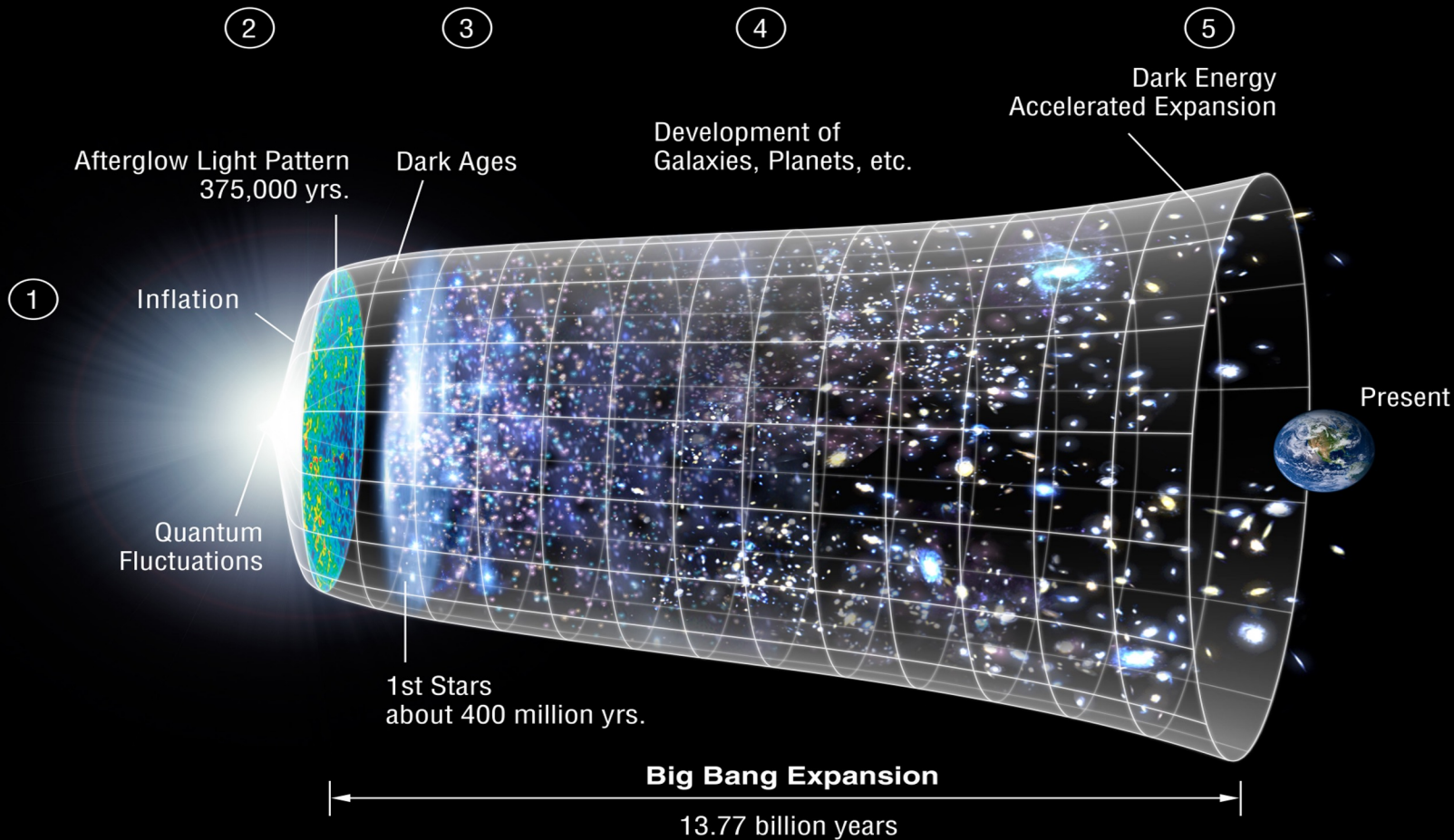
The Astrophysical Journal
Supplement Series
273(2), 27 (2024)
[arXiv:2401.17029]

arXiv:2412.14750

“In an investigation, assumptions **kill**.”

- Jack Reacher



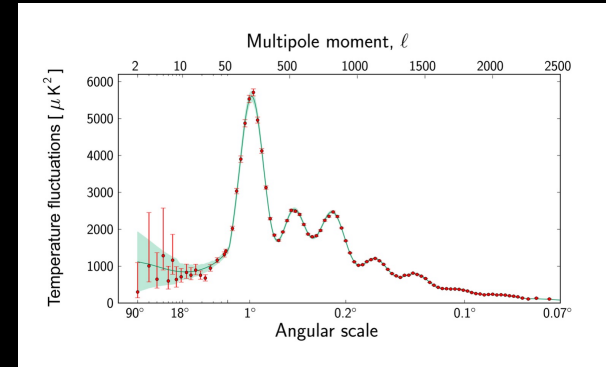
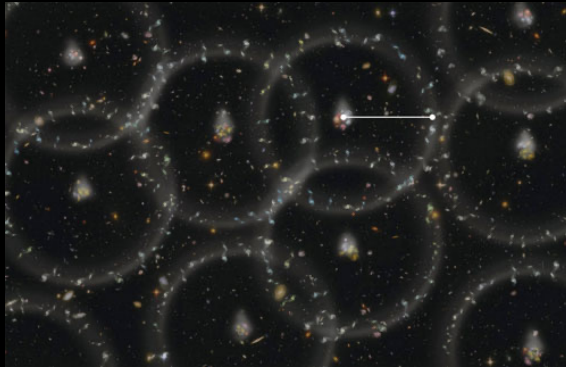
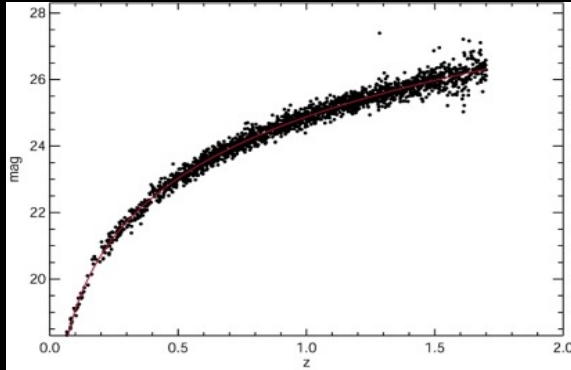


Observing the Cosmological System

Measure distances to look into the past.

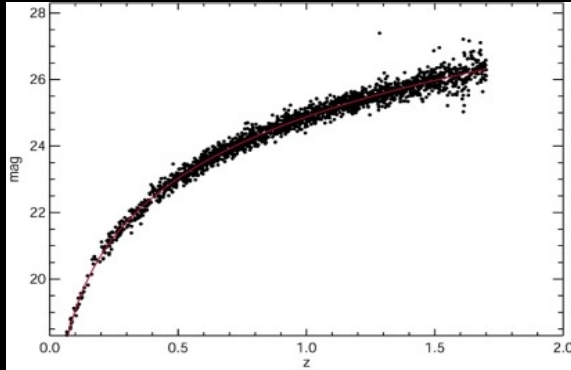
Study patterns in the sky.

Measuring Distances

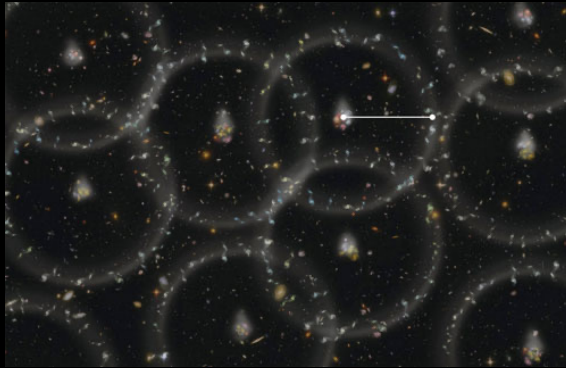


“How far thou art?”

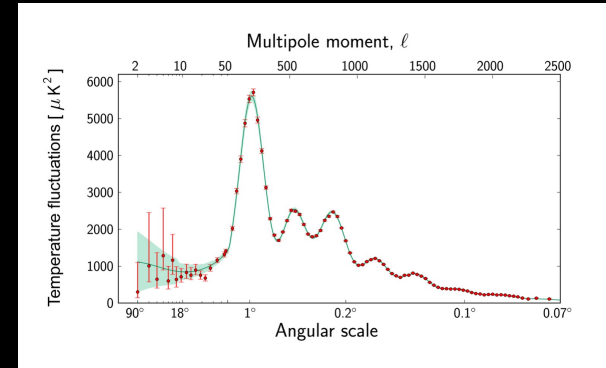
Why Tensions?



Systematics?



Miscalibration?



Λ CDM?

Data Driven Approaches

Cosmography

Parametric

Non-Parametric

Data Driven Approaches



Cosmography

Parametric

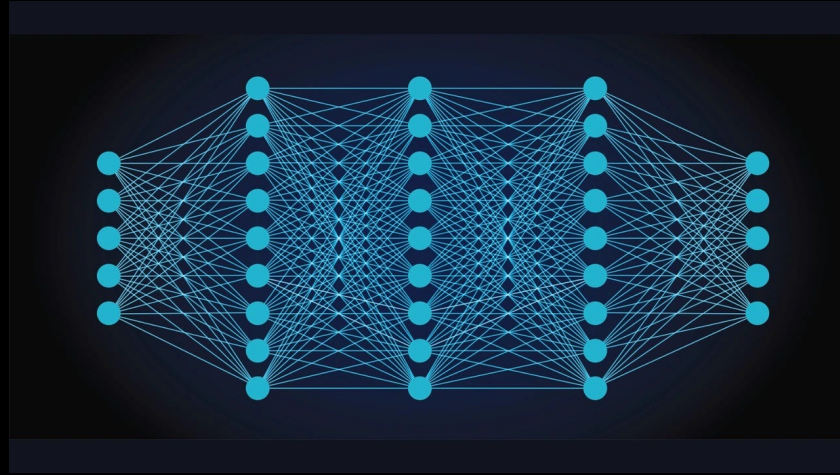
Non-Parametric

Gaussian Processes

Other Methods

Deep Learning

Deep Learning



**Universal
Function
Approximators**

LADDER

Learning Algorithm for Deep Distance Estimation and Reconstruction

Uniqueness of
Reconstruction

Overfitting and
Underfitting Issues

Accurate Predictions
On Precision

Extrapolation Beyond
Training Range



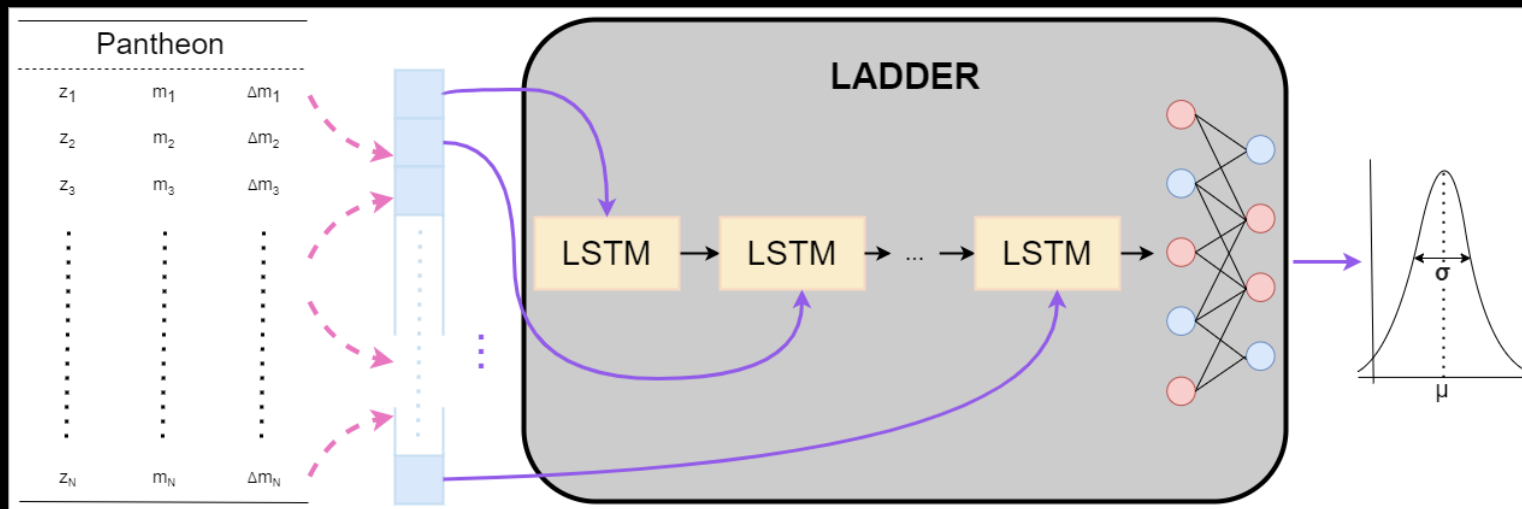
RS, S. Saha, P. Mukherjee, U. Garain, S. Pal
The Astrophysical Journal Supplement Series
273(2), 27 (2024) [arXiv:2401.17029]

<https://github.com/rahulshah1397/LADDER> [publicly available]

LADDER



Learning Algorithm for Deep Distance Estimation and Reconstruction



LADDER

Learning Algorithm for Deep Distance Estimation and Reconstruction



Given $\mathcal{D}$, $\mathbf{C}_{\text{sys}}$ and batch size B .

Initialize θ_0 .

while not StopCondition **do**

$l \leftarrow 0$

for $i = 1, 2, \dots, B$ **do**

 Get K samples from $\mathcal{D}$

$\{(z_1, m_1, \Delta m_1), \dots, (z_K, m_K, \Delta m_K)\}$

$Y_i = (m_{j_1}, \Delta m_{j_1})$

$\hat{m}_{j_2}, \hat{m}_{j_3}, \dots, \hat{m}_{j_K} \sim \mathcal{N}(m_{j_2}, m_{j_3}, \dots, m_{j_K}, \Sigma_m^K) \triangleright$ (Equation (9))

$X_i = (z_{j_1}, z_{j_2}, \hat{m}_{j_2}, \dots, z_{j_K}, \hat{m}_{j_K}) \quad z_{j_2} \leq z_{j_3} \dots$

$\mu, \sigma = f_{\theta_t}(X_i)_1, f_{\theta_t}(X_i)_2 \triangleright$ Forward pass.

$l += D_{\text{KL}}(\mathcal{N}(m_{j_1}, \Delta m_{j_1}), \mathcal{N}(\mu, \sigma))$

end for

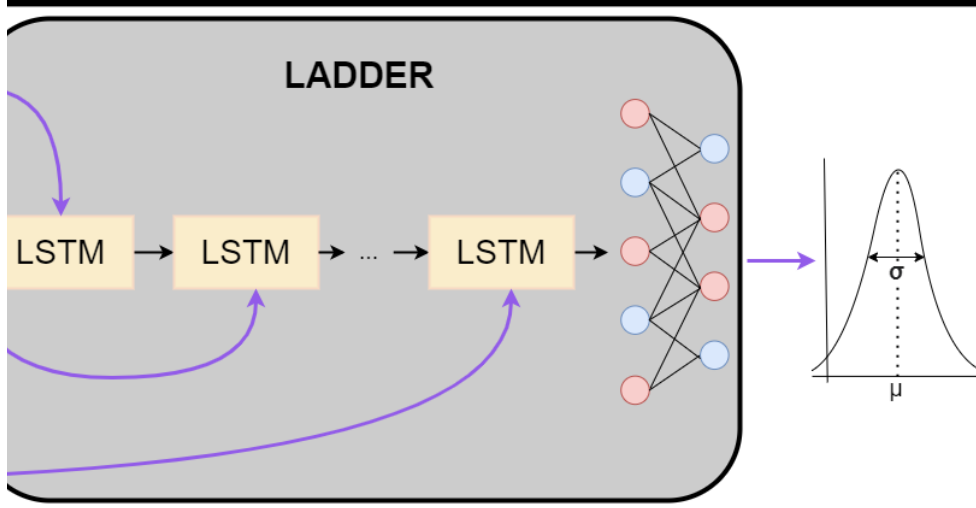
 Compute $\nabla_{\theta_t} l \quad \forall \theta_t$

$\theta_{t+1} = \theta_t + \eta \cdot \nabla_{\theta_t} \triangleright$ Gradient update (illustrative).

if ... **then** $\triangleright$ Check if model converged. StopCondition $\leftarrow$ True

end if

end while



LADDER

Learning Algorithm for Deep Distance Estimation and Reconstruction

```

Given  $\mathcal{D}$ ,  $C_{\text{sys}}$  and batch size  $B$ .
Initialize  $\theta_0$ .
while not StopCondition do
     $l \leftarrow 0$ 
    for  $i = 1, 2, \dots, B$  do
        Get  $K$  samples from  $\mathcal{D}$ 
         $\{(z_1, m_1, \Delta m_1), \dots, (z_K, m_K, \Delta m_K)\}$ 
         $Y_i = (m_{j_1}, \Delta m_{j_1})$ 
         $\hat{m}_{j_2}, \hat{m}_{j_3}, \dots, \hat{m}_{j_K} \sim \mathcal{N}(m_{j_2}, m_{j_3}, \dots, m_{j_K}, \Sigma_m^K) \triangleright$  (Equation (9))
         $X_i = (z_{j_1}, z_{j_2}, \hat{m}_{j_2}, \dots, z_{j_K}, \hat{m}_{j_K}) \quad z_{j_2} \leq z_{j_3} \dots$ 
         $\mu, \sigma = f_{\theta_t}(X_i)_1, f_{\theta_t}(X_i)_2 \triangleright$  Forward pass.
         $l += D_{\text{KL}}(\mathcal{N}(m_{j_1}, \Delta m_{j_1}), \mathcal{N}(\mu, \sigma))$ 
    end for
    Compute  $\nabla_{\theta_t} l \quad \forall \theta_t$ 
     $\theta_{t+1} = \theta_t + \eta \cdot \nabla_{\theta_t} \triangleright$  Gradient update (illustrative).
    if ... then  $\triangleright$  Check if model converged. StopCondition  $\leftarrow$  True
end if
end while
    
```

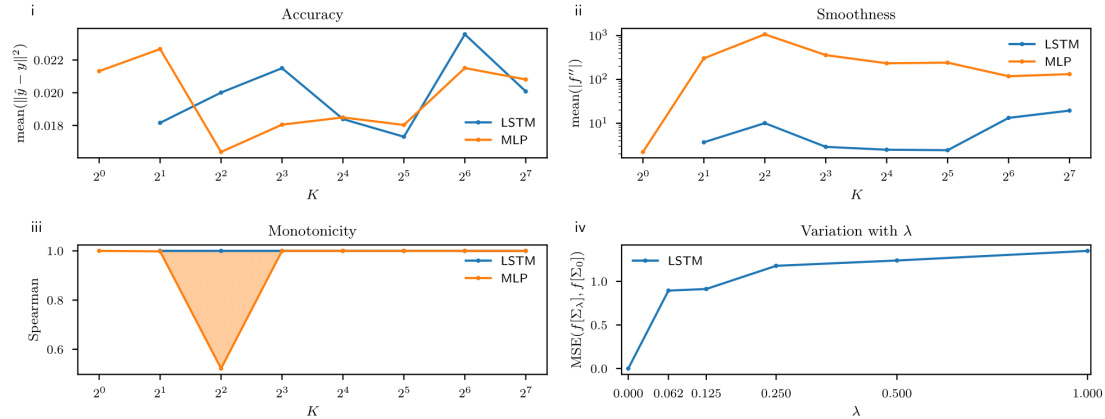
Performance of Various ML Models

Model	MSE ($\downarrow$)	Monotonicity ($\uparrow$)	Smoothness ($\downarrow$)
kNN ($k = 5$)	0.022116	0.99999	90.67500
SVR	0.019358	1.0	3.10633
MLP ($K = 1$)	0.022202	1.0	2.21691
MLP ($K = 32$)	0.020484	0.99997	88.99974
LADDER	0.018495	1.0	2.30022

Notes. ($\downarrow$) indicates lower is better; ($\uparrow$) indicates higher is better. Boldface indicates best performance.



LADDER



THIS IS YOUR MACHINE LEARNING SYSTEM?

YUP! YOU POUR THE DATA INTO THIS BIG
PILE OF LINEAR ALGEBRA, THEN COLLECT
THE ANSWERS ON THE OTHER SIDE.

WHAT IF THE ANSWERS ARE WRONG?

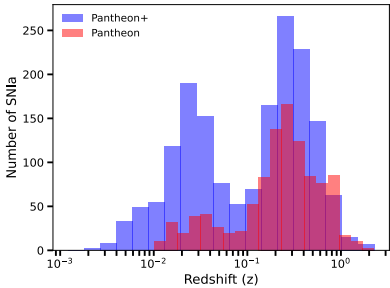
JUST STIR THE PILE UNTIL
THEY START LOOKING RIGHT.



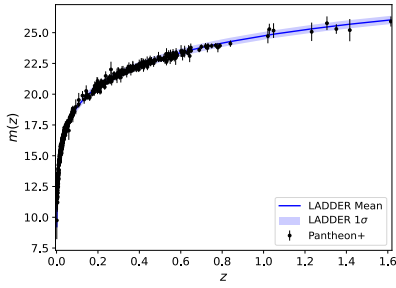
Credit: xkcd comics

Pantheon, LADDER vs Pantheon+

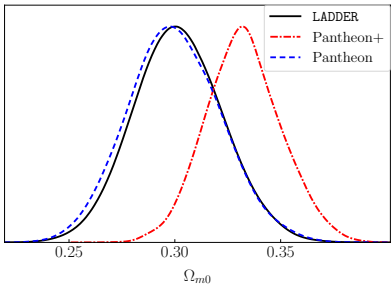
- Why Pantheon+? Range overlaps with Pantheon, high data density at lower z , more precise.
- Concerns regarding the Pantheon+: overestimation of errors, uncorrected systematics¹.



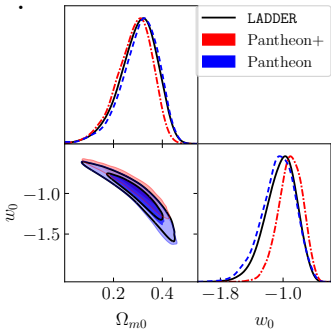
Pantheon vs Pantheon+



LADDER vs Pantheon+



ΛCDM constraints



w CDM constraints

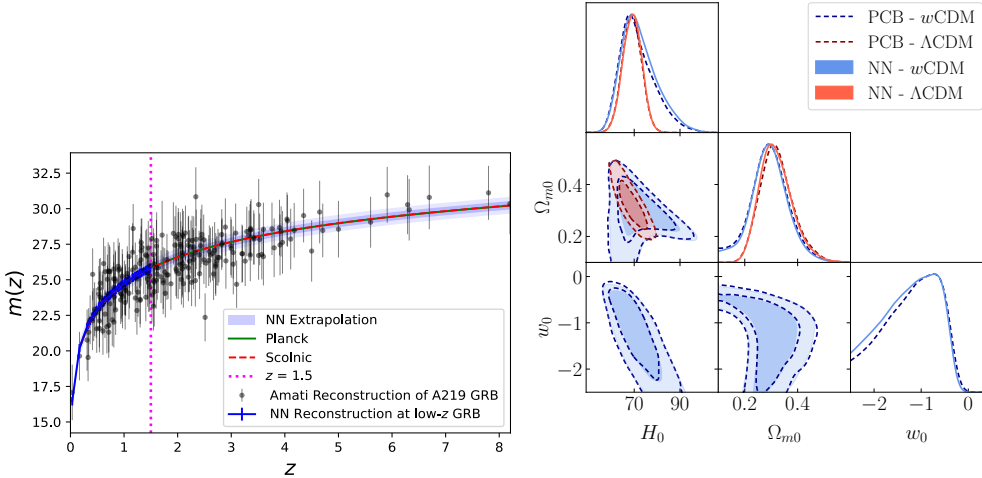
Datasets	ΛCDM	w CDM	
	Ω_{m0}	Ω_{m0}	w_0
Pantheon	$0.299^{+0.023}_{-0.022}$	$0.316^{+0.067}_{-0.083}$	$-1.049^{+0.199}_{-0.228}$
Pantheon+	$0.332^{+0.018}_{-0.017}$	$0.292^{+0.065}_{-0.081}$	$-0.902^{+0.150}_{-0.162}$
LADDER	$0.301^{+0.021}_{-0.021}$	$0.308^{+0.069}_{-0.083}$	$-1.015^{+0.179}_{-0.216}$

- ❑ LADDER traces Pantheon results: good reconstruction.
- ❑ Pantheon, LADDER and Pantheon+ consistent within 1σ .

¹Keeley et al. (2022); Perivolaropoulos & Skara (2023)

Calibration of high-*z* GRBs

- GRB A219 sample [Liang *et al.* (2022)] - redshift range $0.03 < z < 8.2$ - use Amati relation [Amati *et al.* (2002)].
- Split this GRB data into low-*z* < 1.5 and high-*z* > 1.5 samples, consisting of 89 and 130 points respectively.



LADDER calibrated GRB dataset

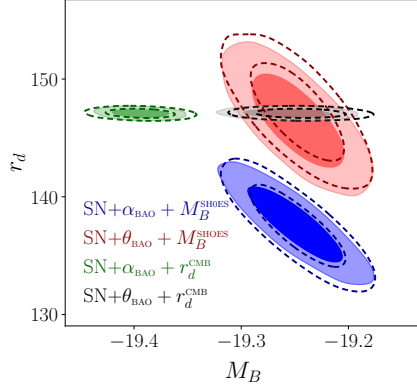
Constraints from CC Hubble + high-*z* GRBs

- Calibration via LADDER: provide a unique high-*z* GRB dataset in a model-independent setting.
- Constraints obtained are consistent, irrespective of the calibration method.
- Marginal widening of errors for the model-independent LADDER calibration.

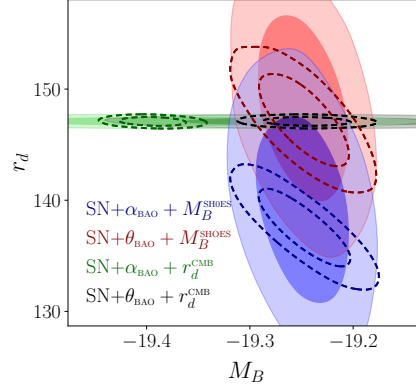
Model Calibrator	Λ CDM		wCDM	
	LADDER	PCB	LADDER	PCB
H_0	$69.203^{+4.050}_{-4.150}$	$68.996^{+4.187}_{-4.095}$	$71.224^{+9.058}_{-6.365}$	$70.265^{+8.989}_{-5.915}$
Ω_{m0}	$0.313^{+0.066}_{-0.055}$	$0.317^{+0.067}_{-0.057}$	$0.289^{+0.068}_{-0.074}$	$0.287^{+0.072}_{-0.085}$
w_0	...	...	$-1.257^{+0.627}_{-0.867}$	$-1.172^{+0.599}_{-0.866}$

Angular vs Anisotropic BAOs

- Transverse Angular BAO (θ_{BAO}): 15 model-independent data in the range $0.11 < z < 2.22$.
- Anisotropic BAO (α_{BAO}): 8 data points in the range $0.38 < z < 2.35$.



LADDER mean vs ΛCDM



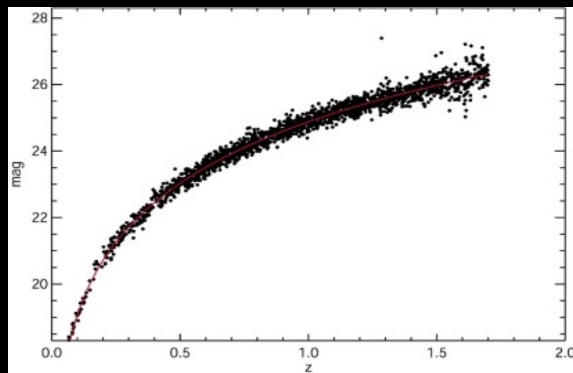
LADDER mean + 1σ vs ΛCDM

- Underlying cosmology close to ΛCDM .
- Existence of internal inconsistency between angular vs anisotropic BAOs [Carter et al. 2020].
- No apparent tension between Pantheon and θ_{BAO} , unlike α_{BAO} .
- Data-driven selection of $M_B - r_d$ parameter space.

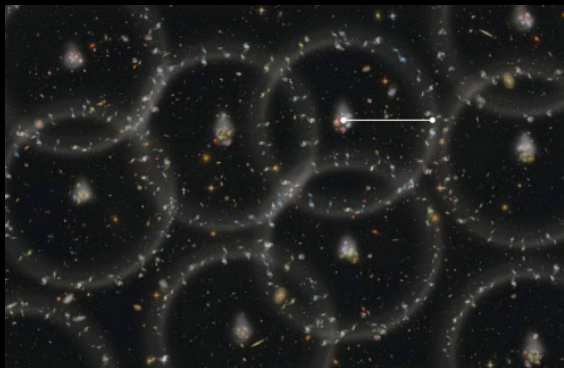
Datasets	LADDER				ΛCDM	
	M_B	r_d	H_0	Ω_{m0}	M_B	r_d
$\text{SN} + \alpha_{\text{BAO}} + M_B^{\text{SHOES}}$	$-19.249^{+0.029}_{-0.029}$	$137.651^{+2.157}_{-2.153}$	$73.195^{+1.054}_{-1.032}$	$0.315^{+0.019}_{-0.019}$	$-19.248^{+0.030}_{-0.029}$	$137.484^{+2.312}_{-2.228}$
$\text{SN} + \theta_{\text{BAO}} + M_B^{\text{SHOES}}$	$-19.248^{+0.028}_{-0.029}$	$146.423^{+2.697}_{-2.569}$	$73.372^{+1.023}_{-1.010}$	$0.302^{+0.022}_{-0.021}$	$-19.248^{+0.028}_{-0.029}$	$147.246^{+2.795}_{-2.712}$
$\text{SN} + \alpha_{\text{BAO}} + r_d^{\text{CMB}}$	$-19.394^{+0.018}_{-0.017}$	$147.090^{+0.250}_{-0.267}$	$68.437^{+0.820}_{-0.826}$	$0.314^{+0.020}_{-0.019}$	$-19.394^{+0.021}_{-0.022}$	$147.087^{+0.258}_{-0.256}$
$\text{SN} + \theta_{\text{BAO}} + r_d^{\text{CMB}}$	$-19.257^{+0.028}_{-0.027}$	$147.085^{+0.261}_{-0.253}$	$73.448^{+1.042}_{-1.025}$	$0.304^{+0.022}_{-0.021}$	$-19.245^{+0.028}_{-0.027}$	$147.088^{+0.259}_{-0.256}$

Cosmological Parameter Estimation

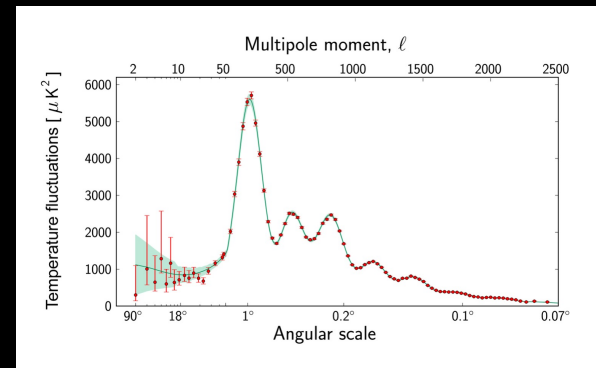
Supernovae



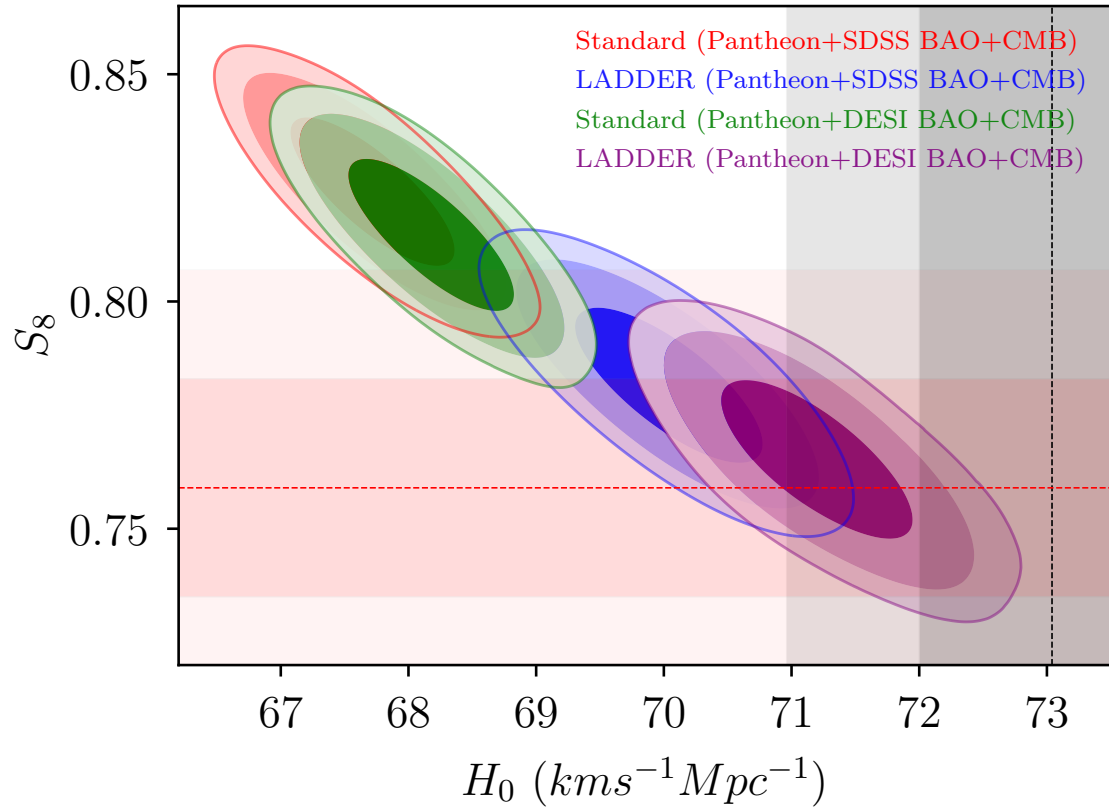
Baryon Acoustic Oscillations



Cosmic Microwave Background



**Recalibrate BAO
with LADDER?**



**In-plane shift in
the H_0 – S_8 plane**

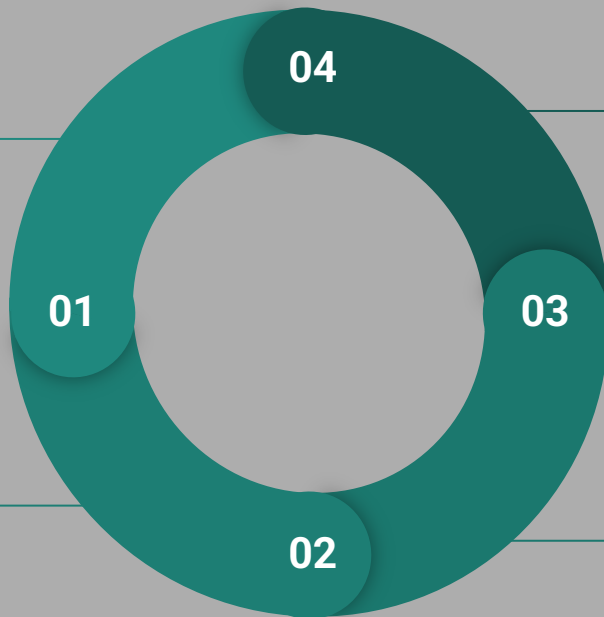
**Alleviates both tensions
simultaneously (!)**

ML Caveats

Overfitting/underfitting issues in deep learning can lead to both inaccurate and imprecise predictions.

Covariance Learning

LADDER thus proposed, learns sequential data, utilizing the full covariance information.



ML in Cosmology

LADDER's potential could usher in new avenues for future exploration.

Extrapolation

LADDER exhibits stability, even in data-sparse regions, gives reliable error + mean predictions beyond the training data range.